# Friday, Mar 24

This in-class demonstration will feature the estimation of Poisson and logistic regression models, and the interpretation of rate and odds ratios.

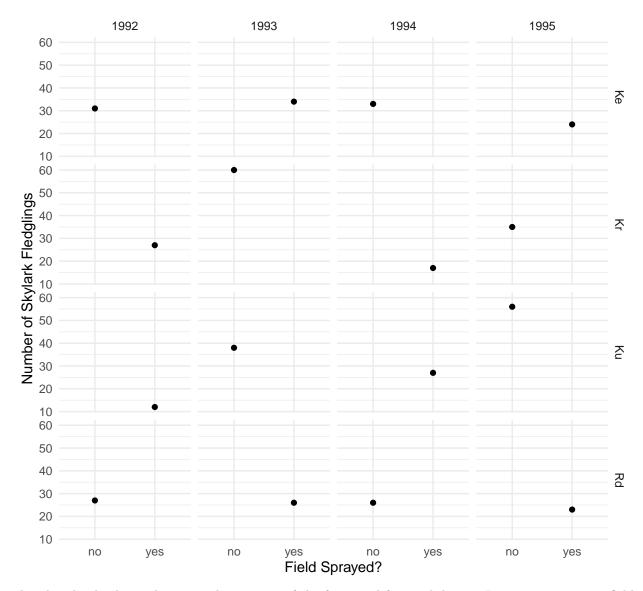
# Impact of Pesticides on Skylark Reproductivity

During the four summers from 1992 to 1995 researchers from the National Environmental Research Institute in the Ministry of Environment and Energy in Denmark conducted a study to examine how pesticide use impacts skylark reproduction in barley fields. The study used a fractional factorial design in which each year two of four fields were sprayed with pesticides while the other two fields were not. Which fields were sprayed was alternated so that a field was sprayed every other year. The number of fledgling skylarks produced in each field each year was recorded. The data are in the skylark data frame from the trtools package. The data are plotted below.

```
library(trtools)
library(ggplot2)
p <- ggplot(skylark, aes(x = spray, y = count)) +
    geom_point() + facet_grid(field ~ year) +
    labs(shape = "Field", x = "Field Sprayed?",
        y = "Number of Skylark Fledglings") + theme_minimal()
plot(p)</pre>
```

<sup>&</sup>lt;sup>1</sup>Odderskær, P., Prang, A., Eknegaard, N., & Andersen, P. N. (1997). Skylark reproduction in pesticide treated fields (Comparative studies of Alauda arvensis breeding performance in sprayed and unsprayed barley fields). Bekæmpelsesmiddelforskning fra Miljøstyrelsennr, 32, National Environmental Research Institute, Ministry of the Environment and Energy, Denmark: Danish Environmental Protection Agency.

<sup>&</sup>lt;sup>2</sup>A fractional factorial design is a design in which observations are made at only a subset of the possible combinations of levels of two or more factors. Such designs are quite economical but can preclude the estimation of interactions. This does not mean that such interactions are not present, but rather that if they are they are confounded with the main effects. For this particular design it is only possible to fully estimate a model with "main effects" for each of the three factors. Ideally factional factorial designs are used when interactions are negligible.



The plot clearly shows the incomplete nature of the fractional factorial design. In any given year, a field either was or was not sprayed. The objective is to investigate the effect of spraying on the number of skylarks while controlling for the effects of year and field.

1. Estimate a Poisson regression model for the number of skylark fledglings as your response variable that will reproduce the following results.

## cbind(summary(m)\$coefficients, confint(m))

	Estimate	Std. Error	z value	Pr(> z )	2.5 %	97.5 %
(Intercept)	3.430943	0.13262	25.86999	1.450e-147	3.16352	3.68367
sprayyes	-0.456126	0.09385	-4.86011	1.173e-06	-0.64141	-0.27324
fieldKr	0.049089	0.12672	0.38738	6.985e-01	-0.19929	0.29806
fieldKu	0.004964	0.12800	0.03879	9.691e-01	-0.24611	0.25625
fieldRd	-0.179048	0.13417	-1.33452	1.820e-01	-0.44342	0.08326
year1993	0.462623	0.13064	3.54108	3.985e-04	0.20868	0.72149
year1994	0.060018	0.14149	0.42420	6.714e-01	-0.21735	0.33816
year1995	0.327281	0.13411	2.44041	1.467e-02	0.06596	0.59240

Note that here m is a model object created using the glm function.

**Solution**: The results can be replicated as follows. Note that the output above indicates that only the "main effects" of spray, field, and year were specified. We can see that there are indicator variables for spray, field, and year, but no interaction terms.

```
m <- glm(count ~ spray + field + year, family = poisson, data = skylark)
cbind(summary(m)$coefficients, confint(m))</pre>
```

```
Estimate Std. Error z value
                                           Pr(>|z|)
                                                       2.5 %
                                                               97.5 %
                        0.13262 25.86999 1.450e-147 3.16352 3.68367
(Intercept) 3.430943
           -0.456126
                        0.09385 -4.86011 1.173e-06 -0.64141 -0.27324
sprayyes
fieldKr
            0.049089
                        0.12672   0.38738   6.985e-01 -0.19929   0.29806
fieldKu
            0.004964
                        0.12800 0.03879 9.691e-01 -0.24611 0.25625
fieldRd
           -0.179048
                        0.13417 -1.33452 1.820e-01 -0.44342
            0.462623
                        0.13064
                                 3.54108 3.985e-04 0.20868
                                                              0.72149
year1993
year1994
            0.060018
                        0.14149
                                 0.42420
                                          6.714e-01 -0.21735
                                                              0.33816
                        0.13411 2.44041 1.467e-02 0.06596 0.59240
year1995
            0.327281
```

2. What is the estimated rate ratio for the effect of spraying? How can this be interpreted?

**Solution**: We can estimate this rate ratio several ways. Note that since there is no interaction involving spray the field and year does not matter.

```
trtools::contrast(m, tf = exp,
 a = list(spray = "yes", field = "Ke", year = "1992"),
b = list(spray = "no", field = "Ke", year = "1992"))
 estimate lower upper
   0.6337 0.5273 0.7617
library(emmeans)
pairs(emmeans(m, ~spray|field*year, type = "response"), infer = TRUE)
field = Ke, year = 1992:
                   SE df asymp.LCL asymp.UCL null z.ratio p.value
contrast ratio
no / yes 1.58 0.148 Inf
                               1.31
                                          1.9
                                                 1
                                                     4.860 < .0001
field = Kr, year = 1992:
 contrast ratio
                   SE df asymp.LCL asymp.UCL null z.ratio p.value
no / yes 1.58 0.148 Inf
                               1.31
                                          1.9
                                                 1
                                                     4.860 < .0001
field = Ku, year = 1992:
                   SE df asymp.LCL asymp.UCL null z.ratio p.value
 contrast ratio
no / yes 1.58 0.148 Inf
                               1.31
                                          1.9
                                                 1
                                                     4.860 < .0001
field = Rd, year = 1992:
                   SE df asymp.LCL asymp.UCL null z.ratio p.value
 contrast ratio
no / yes 1.58 0.148 Inf
                               1.31
                                          1.9
                                                     4.860 < .0001
                                                 1
field = Ke, year = 1993:
 contrast ratio
                   SE df asymp.LCL asymp.UCL null z.ratio p.value
                               1.31
                                          1.9
                                                     4.860 < .0001
no / yes 1.58 0.148 Inf
                                                 1
field = Kr, year = 1993:
 contrast ratio
                   SE df asymp.LCL asymp.UCL null z.ratio p.value
no / yes 1.58 0.148 Inf
                               1.31
                                          1.9
                                                     4.860 < .0001
field = Ku, year = 1993:
```

```
contrast ratio
               SE df asymp.LCL asymp.UCL null z.ratio p.value
no / yes 1.58 0.148 Inf 1.31
                                    1.9 1 4.860 <.0001
field = Rd, year = 1993:
contrast ratio
                 SE df asymp.LCL asymp.UCL null z.ratio p.value
no / yes 1.58 0.148 Inf
                           1.31
                                       1.9
                                              1 4.860 <.0001
field = Ke, year = 1994:
contrast ratio SE df asymp.LCL asymp.UCL null z.ratio p.value
no / yes 1.58 0.148 Inf
                             1.31
                                       1.9 1 4.860 <.0001
field = Kr, year = 1994:
contrast ratio
               SE df asymp.LCL asymp.UCL null z.ratio p.value
no / yes 1.58 0.148 Inf
                                       1.9
                                             1 4.860 <.0001
                            1.31
field = Ku, year = 1994:
                 SE df asymp.LCL asymp.UCL null z.ratio p.value
contrast ratio
no / yes 1.58 0.148 Inf
                          1.31
                                       1.9
                                            1 4.860 <.0001
field = Rd, year = 1994:
                 SE df asymp.LCL asymp.UCL null z.ratio p.value
contrast ratio
no / yes 1.58 0.148 Inf
                             1.31
                                       1.9
                                            1 4.860 <.0001
field = Ke, year = 1995:
contrast ratio
                 SE df asymp.LCL asymp.UCL null z.ratio p.value
no / yes 1.58 0.148 Inf
                            1.31
                                       1.9
                                            1
                                                 4.860 <.0001
field = Kr, year = 1995:
contrast ratio
                 SE df asymp.LCL asymp.UCL null z.ratio p.value
                                       1.9
no / yes 1.58 0.148 Inf
                          1.31
                                             1 4.860 <.0001
field = Ku, year = 1995:
               SE df asymp.LCL asymp.UCL null z.ratio p.value
contrast ratio
no / yes 1.58 0.148 Inf
                           1.31
                                       1.9
                                             1 4.860 <.0001
field = Rd, year = 1995:
contrast ratio
                 SE df asymp.LCL asymp.UCL null z.ratio p.value
no / yes 1.58 0.148 Inf
                             1.31
                                       1.9
                                            1 4.860 <.0001
Confidence level used: 0.95
Intervals are back-transformed from the log scale
Tests are performed on the log scale
pairs(emmeans(m, ~spray, type = "response"), reverse = TRUE, infer = TRUE)
                  SE df asymp.LCL asymp.UCL null z.ratio p.value
contrast ratio
yes / no 0.634 0.0595 Inf
                             0.527
                                     0.762
                                               1 -4.860 <.0001
Results are averaged over the levels of: field, year
Confidence level used: 0.95
Intervals are back-transformed from the log scale
Tests are performed on the log scale
```

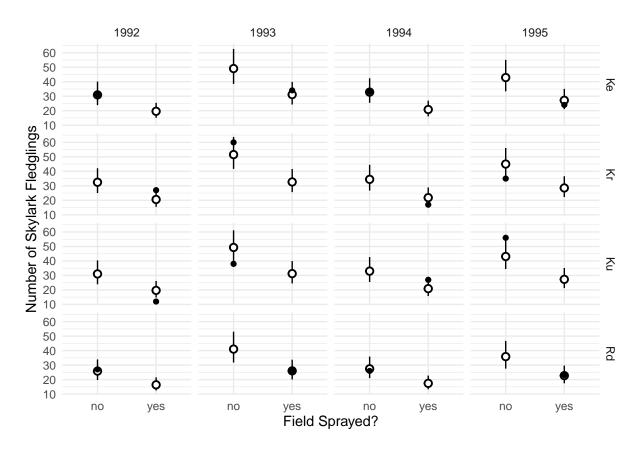
```
exp(cbind(coef(m), confint(m)))
                        2.5 % 97.5 %
  (Intercept) 30.9058 23.6537 39.7921
  sprayyes
               0.6337 0.5265 0.7609
  fieldKr
               1.0503 0.8193 1.3472
               1.0050 0.7818 1.2921
  fieldKu
  fieldRd
               0.8361 0.6418 1.0868
  year1993
               1.5882 1.2321 2.0575
               1.0619 0.8046 1.4024
  year1994
  year1995
               1.3872 1.0682 1.8083
3. What is the estimated expected number of fledglings for each condition?
  Solution: We can estimate this a couple of ways.
  trtools::contrast(m, tf = exp,
   a = list(spray = c("no", "yes"), field = "Ke", year = "1992"),
  cnames = c("no spray", "spray"))
           estimate lower upper
              30.91 23.83 40.08
  no spray
              19.59 15.07 25.45
  spray
  emmeans(m, ~spray|field*year, type = "response")
  field = Ke, year = 1992:
   spray rate SE df asymp.LCL asymp.UCL
         30.9 4.10 Inf
                            23.8
                                      40.1
   no
         19.6 2.62 Inf
                            15.1
                                      25.4
   yes
  field = Kr, year = 1992:
   spray rate SE df asymp.LCL asymp.UCL
         32.5 4.31 Inf
   no
                            25.0
                                      42.1
                                      27.3
         20.6 2.97 Inf
                            15.5
   yes
  field = Ku, year = 1992:
   spray rate SE df asymp.LCL asymp.UCL
   no
         31.1 4.16 Inf
                            23.9
                                      40.4
         19.7 2.87 Inf
                            14.8
                                      26.2
   yes
  field = Rd, year = 1992:
   spray rate SE df asymp.LCL asymp.UCL
         25.8 3.58 Inf
                            19.7
                                      33.9
   no
         16.4 2.28 Inf
                            12.5
                                      21.5
   yes
  field = Ke, year = 1993:
   spray rate SE df asymp.LCL asymp.UCL
   no
         49.1 6.11 Inf
                            38.5
                                      62.6
         31.1 3.94 Inf
                            24.3
                                      39.9
   yes
  field = Kr, year = 1993:
   spray rate SE df asymp.LCL asymp.UCL
   no
         51.6 5.59 Inf
                           41.7
                                      63.8
   yes 32.7 4.04 Inf
                            25.6
                                      41.6
```

field = Ku, year = 1993: spray rate SE df asymp.LCL asymp.UCL 49.3 5.42 Inf 61.2 39.8 31.3 3.90 Inf 24.5 39.9 yes field = Rd, year = 1993: spray rate SE df asymp.LCL asymp.UCL 41.0 5.37 Inf 31.8 no 53.0 yes 26.0 3.45 Inf 20.1 33.7 field = Ke, year = 1994: spray rate SE df asymp.LCL asymp.UCL 25.4 no 32.8 4.28 Inf 42.4 26.9 yes 20.8 2.73 Inf 16.1 field = Kr, year = 1994: spray rate SE df asymp.LCL asymp.UCL 34.5 4.50 Inf 26.7 21.8 3.11 Inf 16.5 28.9 yes field = Ku, year = 1994: spray rate SE df asymp.LCL asymp.UCL 33.0 4.34 Inf 25.5 42.7 nο 20.9 3.00 Inf 15.8 27.7 yes field = Rd, year = 1994: spray rate SE df asymp.LCL asymp.UCL 27.4 3.74 Inf 21.0 35.8 no 17.4 2.39 Inf 13.3 22.8 yes field = Ke, year = 1995: spray rate SE df asymp.LCL asymp.UCL 55.1 42.9 5.49 Inf 33.4 27.2 3.54 Inf 21.1 35.1 yes field = Kr, year = 1995: spray rate SE df asymp.LCL asymp.UCL no 45.0 5.07 Inf 36.1 56.1 22.2 yes 28.5 3.63 Inf 36.6 field = Ku, year = 1995: spray rate SE df asymp.LCL asymp.UCL 43.1 4.91 Inf 34.5 53.9 no 27.3 3.51 Inf 21.2 35.1 yes field = Rd, year = 1995: spray rate SE df asymp.LCL asymp.UCL 35.8 4.81 Inf 27.6 46.6 yes 22.7 3.09 Inf 17.4 29.7

Confidence level used: 0.95

Intervals are back-transformed from the log scale

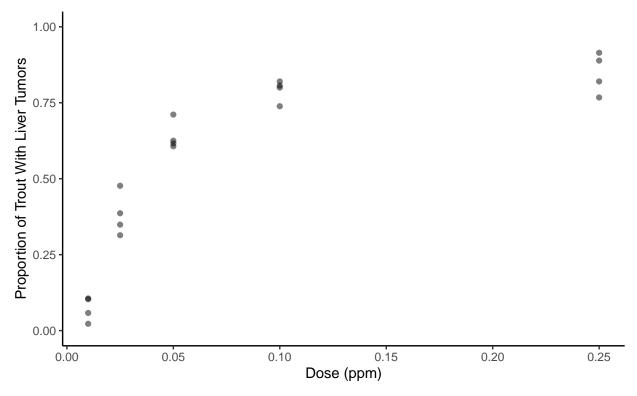
```
d <- expand.grid(spray = c("yes", "no"), field = c("Ke", "Kr", "Ku", "Rd"),</pre>
 year = c("1992","1993","1994","1995"))
cbind(d, trtools::glmint(m, newdata = d))
   spray field year
                       fit
                             low
1
     yes
            Ke 1992 19.59 15.07 25.45
2
            Ke 1992 30.91 23.83 40.08
      no
3
            Kr 1992 20.57 15.50 27.31
     yes
4
            Kr 1992 32.46 25.02 42.11
     no
5
     yes
            Ku 1992 19.68 14.80 26.18
6
      no
            Ku 1992 31.06 23.88 40.39
7
            Rd 1992 16.38 12.46 21.52
     yes
8
            Rd 1992 25.84 19.69 33.90
     no
9
            Ke 1993 31.11 24.27 39.87
     yes
10
            Ke 1993 49.09 38.46 62.65
     no
11
     yes
            Kr 1993 32.67 25.64 41.63
12
            Kr 1993 51.56 41.68 63.76
      no
13
            Ku 1993 31.26 24.47 39.93
     yes
            Ku 1993 49.33 39.77 61.19
14
      no
            Rd 1993 26.01 20.05 33.74
15
     yes
            Rd 1993 41.04 31.76 53.03
16
17
     yes
            Ke 1994 20.80 16.08 26.90
18
            Ke 1994 32.82 25.42 42.37
     no
            Kr 1994 21.84 16.52 28.88
19
     yes
20
            Kr 1994 34.47 26.69 44.52
      no
21
            Ku 1994 20.90 15.78 27.69
     yes
22
     no
            Ku 1994 32.98 25.47 42.70
23
            Rd 1994 17.39 13.29 22.76
     yes
24
            Rd 1994 27.44 21.00 35.84
     no
25
            Ke 1995 27.17 21.05 35.07
     yes
26
            Ke 1995 42.87 33.35 55.11
     no
27
            Kr 1995 28.54 22.24 36.62
     yes
28
            Kr 1995 45.03 36.11 56.15
      no
29
            Ku 1995 27.30 21.22 35.13
     yes
30
            Ku 1995 43.09 34.46 53.88
     no
31
            Rd 1995 22.72 17.39 29.67
     yes
32
            Rd 1995 35.84 27.55 46.63
d <- cbind(d, glmint(m, newdata = d))</pre>
p <- p + geom_pointrange(aes(y = fit, ymin = low, ymax = upp),
  shape = 21, fill = "white", data = d) + geom_point()
plot(p)
```



#### Aflatoxicol and Liver Tumors in Trout

The data in the data frame ex2116 in the Sleuth3 package are from an experiment that investigated the relationship between aflatoxicol and liver tumors in trout. The figure below shows the proportion of trout in each tank that developed liver tumors as well as the dose of aflatoxicol to which the trout were exposed. Aflatoxicol is a metabolite of Aflatoxin B1, a toxic by-product produced by a mold that infects some nuts and grains. Twenty tanks of rainbow trout embryos were exposed to one of five doses of aflatoxicol for one hour. The number of fish in each tank that developed liver tumors one year later was then observed. The plot below shows the data.

```
library(Sleuth3)
library(ggplot2)
p <- ggplot(ex2116, aes(x = Dose, y = Tumor/Total)) +
    geom_point(alpha = 0.5) + theme_classic() + ylim(0, 1) +
    labs(x = "Dose (ppm)", y = "Proportion of Trout With Liver Tumors")
plot(p)</pre>
```



The goal here is to estimate the effect of aflatoxicol on the risk of liver tumors in trout. Here we will consider three different logistic regression models.

## 1. Consider the logistic regression model

$$\log \left[ \frac{E(Y_i)}{1 - E(Y_i)} \right] = \beta_0 + \beta_1 d_i,$$

where  $Y_i$  is the *i*-th observation of the proportion of trout from a tank that developed liver tumors and  $d_i$  is the corresponding dose of aflatoxicol to which those trout were exposed. This model can also be written as

$$E(Y_i) = \frac{e^{\eta_i}}{1 + e^{\eta_i}},$$

where  $\eta_i = \beta_0 + \beta_1 d_i$ . Note that by definition  $E(Y_i)$  is also the *probability* that a trout from a given tank will develop liver tumors, and  $E(Y_i)/[1-E(Y_i)]$  is the *odds* that a trout from a given tank will develop liver tumors. Estimate this model using glm. You should be able to replicate the following results.

### cbind(summary(m)\$coefficients, confint(m))

	Estimate	Std.	Error	z	value	Pr(> z )	2.5 %	97.5 %
(Intercept)	-0.867	0.	07673		-11.3	1.321e-29	-1.019	-0.7179
Dose	14.334	0.	93695		15.3	7.838e-53	12.558	16.2346

Next estimate the odds ratio for the effect of increasing dose by 0.05 ppm using the contrast function.<sup>3</sup> How is this odds ratio interpreted?

**Solution**: We can estimate the model as follows.

 $<sup>^3</sup>$ Here  $e^{\beta_1}$  would be the odds ratio for the effect of increasing dose by 1 ppm. However that is probably not a realistic effect as it would be a relatively large increase in dose. The study only considered up to 0.25 ppm. Using **contrast** is convenient here to estimate the odds ratio for the effect of an arbitrary change in dose.

```
m <- glm(cbind(Tumor, Total - Tumor) ~ Dose, family = binomial, data = ex2116)
summary(m)$coefficients</pre>
```

```
Estimate Std. Error z value Pr(>|z|)
(Intercept) -0.867 0.07673 -11.3 1.321e-29
Dose 14.334 0.93695 15.3 7.838e-53
```

The odds ratio can be estimated as follows.

```
trtools::contrast(m,
  a = list(Dose = 0.1),
 b = list(Dose = 0.05), tf = exp)
 estimate lower upper
    2.048 1.868 2.245
pairs(emmeans(m, ~Dose, at = list(Dose = c(0.1, 0.05)), type = "response"), infer = TRUE)
                                      df asymp.LCL asymp.UCL null z.ratio p.value
 contrast
                    odds.ratio
                                   SE
 Dose0.1 / Dose0.05
                          2.05 0.0959 Inf
                                               1.87
                                                         2.24
                                                                  1 15.298 <.0001
Confidence level used: 0.95
Intervals are back-transformed from the log odds ratio scale
Tests are performed on the log odds ratio scale
```

2. Now consider a model where we use the base-2 logarithm of dose as the explanatory variable so that

$$\eta_i = \beta_0 + \beta_1 \log_2(d_i).$$

Recall that the function  $\log_2$  is known to R as  $\log 2$ . Estimate this model using glm. You should be able to replicate the following results.

```
cbind(summary(m)$coefficients, confint(m))
```

```
Estimate Std. Error z value Pr(>|z|) 2.5 % 97.5 % (Intercept) 4.1634 0.2085 19.97 9.564e-89 3.7631 4.581 log2(Dose) 0.8997 0.0446 20.17 1.628e-90 0.8141 0.989
```

Here increasing the base-2 logarithm of dose by one unit is the same thing as *doubling* dose, and so the effect on the odds ratio of doubling dose will be the same regardless of what you double (e.g., 0.05 to 1 ppm, 0.1 to 0.2 ppm, etc.).<sup>4</sup> How is this odds ratio interpreted?

**Solution** We can estimate the model as follows.

```
m <- glm(cbind(Tumor, Total-Tumor) ~ log2(Dose), family = binomial, data = ex2116)
cbind(summary(m)$coefficients, confint(m))</pre>
```

```
Estimate Std. Error z value Pr(>|z|) 2.5 % 97.5 % (Intercept) 4.1634 0.2085 19.97 9.564e-89 3.7631 4.581 log2(Dose) 0.8997 0.0446 20.17 1.628e-90 0.8141 0.989
```

The odds ratio can be estimated as follows.

<sup>&</sup>lt;sup>4</sup>We do not have to use the odds ratio for the effect of doubling dose just because we are using the base-2 logarithm of dose as our explanatory variable. We could also estimate the odds ratio for the effect of increasing dose from, say, 0.05 ppm to 0.1 ppm. But we would need to remember that because we are using the base-2 logarithm of dose as an explanatory variable that this would *not* be the same odds ratio as increasing dose the same amount from, say, 0.1 ppm to 0.15 ppm. Similarly for the previous model where we did not use the base-2 logarithm of dose, we could still estimate the odds ratio for the effect of doubling dose. But here we would need to remember that the odds ratio of doubling from, say, 0.05 ppm to 0.1 ppm would *not* be the same as the odds ratio for doubling from 0.1 ppm to 0.2 ppm.

```
trtools::contrast(m,
 a = list(Dose = 0.2),
 b = list(Dose = 0.1), tf = exp)
 estimate lower upper
    2.459 2.253 2.684
pairs(emmeans(m, ~Dose, at = list(Dose = c(0.2, 0.1)), type = "response"), infer = TRUE)
                                SE df asymp.LCL asymp.UCL null z.ratio p.value
 contrast
                   odds.ratio
 Dose0.2 / Dose0.1
                         2.46 0.11 Inf
                                            2.25
                                                               1 20.175 < .0001
Confidence level used: 0.95
Intervals are back-transformed from the log odds ratio scale
Tests are performed on the log odds ratio scale
```

3. Rather than trying to decide between using dose or some transformation of dose in the model, we can instead define dose as a 5-level factor. There are two ways we could specify dose as a factor. One would be to create a new variable.

```
ex2116$Dosef <- factor(ex2116$Dose)</pre>
```

The levels of Dosef will be the original values of Dose but converted to strings, which we can see if we use the levels function.

```
levels(ex2116$Dosef)
```

```
[1] "0.01" "0.025" "0.05" "0.1" "0.25"
```

Another approach is to replace Dose in the model formula with factor(Dose). Use the contrast function to estimate the odds ratio for the odds of tumor development at 0.025 ppm versus 0.01 ppm, 0.05 ppm versus 0.01 ppm, 0.1 ppm versus 0.01 ppm, and 0.25 ppm versus 0.01 ppm.<sup>5</sup> How are these odds ratios interpreted?

**Solution**: Here is how to estimate this model.

```
m <- glm(cbind(Tumor, Total-Tumor) ~ factor(Dose), family = binomial, data = ex2116)
cbind(summary(m)$coefficients, confint(m))</pre>
```

```
Estimate Std. Error z value Pr(>|z|) 2.5 % 97.5 %
(Intercept)
                   -2.556
                              0.2076 -12.310 8.049e-35 -2.988 -2.171
factor(Dose)0.025
                    2.073
                              0.2353
                                      8.809 1.264e-18 1.628 2.553
factor(Dose)0.05
                    3.132
                              0.2354 13.306 2.130e-40
                                                        2.688 3.614
factor(Dose)0.1
                    3.890
                              0.2453 15.857 1.252e-56 3.427 4.391
factor(Dose)0.25
                    4.260
                              0.2566 16.605 6.436e-62 3.775 4.784
```

The odds ratios can be estimated as follows.

```
trtools::contrast(m, tf = exp,
    a = list(Dose = c(0.025,0.05,0.1,0.25)),
    b = list(Dose = 0.01))

estimate lower upper
    7.945   5.01   12.60
    22.920   14.45   36.36
    48.909   30.24   79.10
    70.840   42.84   117.13
```

<sup>&</sup>lt;sup>5</sup>Note that how you specify the levels of dose will depend on whether you created a new variable like <code>Dosef</code> or converted it to a factor within the model formula with <code>factor(Dose)</code>. For the latter you will need to specify dose as a *number* but if you created it to a new variable you will need to specify it as a *string* by enclosing it in quotes.

```
contrast(emmeans(m, ~Dose, type = "response"), method = "trt.vs.ctrl",
  ref = 1, adjust = "none", infer = TRUE)
```

```
contrast
                    odds.ratio
                                  SE df asymp.LCL asymp.UCL null z.ratio p.value
Dose0.025 / Dose0.01
                          7.94 1.87 Inf
                                                                    8.809 <.0001
                                              5.01
                                                        12.6
                                                                1
Dose0.05 / Dose0.01
                         22.92 5.39 Inf
                                             14.45
                                                        36.4
                                                                1
                                                                   13.306 <.0001
Dose0.1 / Dose0.01
                         48.91 12.00 Inf
                                             30.24
                                                        79.1
                                                                1 15.857 <.0001
Dose0.25 / Dose0.01
                         70.84 18.18 Inf
                                             42.84
                                                       117.1
                                                                1 16.605 <.0001
```

Confidence level used: 0.95

Intervals are back-transformed from the log odds ratio scale Tests are performed on the log odds ratio scale

4. Estimate the odds and probability of tumor development at each value of dose used in the study for any of the three models.