

Friday, May 5

Setup

The following packages are being used.

```
library(dplyr)      # data manipulation
library(tidyr)      # data manipulation
library(lubridate)   # working with dates
library(forcats)     # working with factors
library(wherami)     # find current directory
library(ggplot2)     # graphics
library(mgcv)        # GAMs
library(trtools)     # inference tools
library(emmeans)     # inference tools
options(digits = 4)  # control number of digits displayed
```

Import and Process Tick Count Data

Here I can use `dirname(thisfile())` to find the directory containing this Rmarkdown file, so I do not have to specify the full path to the data file. Note that `thisfile()` is from the **wherami** package. I have the data stored in a sub-directory ("tickdata") of the directory containing this Rmarkdown file.

```
ticks <- read.csv(paste(dirname(thisfile()),
  "/tickdata/tick_data_Robenstein.csv", sep = ""))
names(ticks) <- c("moose", "mortality", "ticks", "size", "date", "gmu", "sex", "note")
head(ticks)
```

| | moose | mortality | ticks | size | date | gmu | sex | note |
|---|----------|-----------|-------|------|------------|-----|------|------|
| 1 | 21005370 | H | 0 | 100 | 9/16/2020 | 1 | MALE | 1 |
| 2 | 21005396 | H | 21 | 100 | 10/14/2020 | 1 | MALE | 1 |
| 3 | 21005452 | H | 0 | 100 | 10/5/2020 | 1 | MALE | 1 |
| 4 | 21005506 | H | 9 | 100 | 11/11/2020 | 1 | MALE | 1 |
| 5 | 21005526 | H | 34 | 100 | 11/22/2020 | 1 | MALE | 1 |
| 6 | 21005538 | H | 1 | 100 | 11/5/2020 | 1 | MALE | 0 |

Here I am going to process the data to get it ready for plotting and modeling.

```
ticks <- ticks %>%
  mutate(note = factor(note, levels = 0:3,
    labels = c("exclude", "include", "deterioration", "nodate")) %>%
  mutate(date = mdy(date)) %>%
  mutate(month = month(date, label = TRUE), year = year(date), day = yday(date)) %>%
  filter(!is.na(date), month %in% c("Aug", "Sep", "Oct", "Nov")) %>%
  mutate(year = factor(year)) %>% mutate(sex = tolower(sex)) %>%
  mutate(day = ifelse(year == "2020", day - 1, day))
head(ticks)
```

| | moose | mortality | ticks | size | date | gmu | sex | note | month | year | day |
|---|----------|-----------|-------|------|------------|-----|------|---------|-------|------|-----|
| 1 | 21005370 | H | 0 | 100 | 2020-09-16 | 1 | male | include | Sep | 2020 | 259 |
| 2 | 21005396 | H | 21 | 100 | 2020-10-14 | 1 | male | include | Oct | 2020 | 287 |

| | | | | | | | | | | | |
|---|----------|---|----|-----|------------|---|------|---------|-----|------|-----|
| 3 | 21005452 | H | 0 | 100 | 2020-10-05 | 1 | male | include | Oct | 2020 | 278 |
| 4 | 21005506 | H | 9 | 100 | 2020-11-11 | 1 | male | include | Nov | 2020 | 315 |
| 5 | 21005526 | H | 34 | 100 | 2020-11-22 | 1 | male | include | Nov | 2020 | 326 |
| 6 | 21005538 | H | 1 | 100 | 2020-11-05 | 1 | male | exclude | Nov | 2020 | 309 |

Import and Process Game Management Unit Data

Here I am going to use `rename` to rename the imported variables.

```
gmu <- read.csv(paste(dirname(thisfile()), "/tickdata/tick_study_areas.csv", sep = "")) %>%
  rename(gmu = GMU, area = study.Area, samples = hh_samples)
head(gmu, 10)
```

| | gmu | area | samples |
|----|------------------|-------|---------|
| 1 | 1 | North | 27 |
| 2 | 2 | North | 36 |
| 3 | 3 | North | 19 |
| 4 | 4 | North | 24 |
| 5 | 4A | North | 6 |
| 6 | 5 North Central | | 18 |
| 7 | 6 North Central | | 22 |
| 8 | 7 North Central | | 7 |
| 9 | 8 North Central | | 9 |
| 10 | 8A North Central | | 8 |

Merging Data Frames and Filtering

```
ticks <- left_join(ticks, gmu) %>%
  mutate(area = factor(area)) %>%
  mutate(area = fct_relevel(area, c("North", "North Central",
    "Central", "Southeast", "Island Park")))
head(ticks)
```

| | moose | mortality | ticks | size | date | gmu | sex | note | month | year | day | area | samples |
|---|----------|-----------|-------|------|------------|-----|------|---------|-------|------|-----|-------|---------|
| 1 | 21005370 | H | 0 | 100 | 2020-09-16 | 1 | male | include | Sep | 2020 | 259 | North | 27 |
| 2 | 21005396 | H | 21 | 100 | 2020-10-14 | 1 | male | include | Oct | 2020 | 287 | North | 27 |
| 3 | 21005452 | H | 0 | 100 | 2020-10-05 | 1 | male | include | Oct | 2020 | 278 | North | 27 |
| 4 | 21005506 | H | 9 | 100 | 2020-11-11 | 1 | male | include | Nov | 2020 | 315 | North | 27 |
| 5 | 21005526 | H | 34 | 100 | 2020-11-22 | 1 | male | include | Nov | 2020 | 326 | North | 27 |
| 6 | 21005538 | H | 1 | 100 | 2020-11-05 | 1 | male | exclude | Nov | 2020 | 309 | North | 27 |

Some variables we do not need. Also we are going to discard some questionable observations.

```
ticks <- ticks %>% select(-mortality, -samples, -gmu) %>%
  filter(note == "include")
head(ticks)
```

| | moose | ticks | size | date | sex | note | month | year | day | area |
|---|----------|-------|------|------------|------|---------|-------|------|-----|-------|
| 1 | 21005370 | 0 | 100 | 2020-09-16 | male | include | Sep | 2020 | 259 | North |
| 2 | 21005396 | 21 | 100 | 2020-10-14 | male | include | Oct | 2020 | 287 | North |
| 3 | 21005452 | 0 | 100 | 2020-10-05 | male | include | Oct | 2020 | 278 | North |
| 4 | 21005506 | 9 | 100 | 2020-11-11 | male | include | Nov | 2020 | 315 | North |
| 5 | 21005526 | 34 | 100 | 2020-11-22 | male | include | Nov | 2020 | 326 | North |
| 6 | 21005546 | 1 | 100 | 2020-11-22 | male | include | Nov | 2020 | 326 | North |

Raw Data Visualization

```
d09 <- yday(mdy("09/1/2021"))
d10 <- yday(mdy("10/1/2021"))
d11 <- yday(mdy("11/1/2021"))
d12 <- yday(mdy("12/1/2021"))

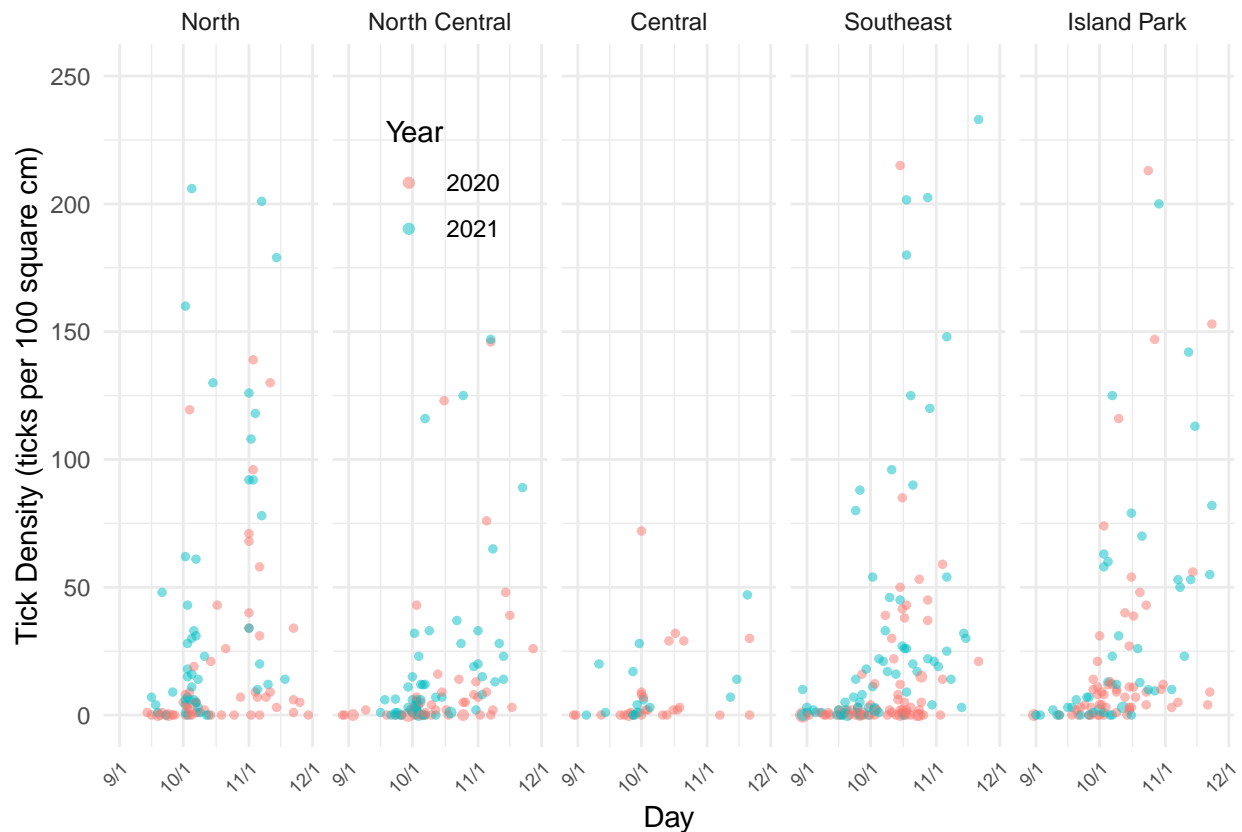
pv <- ggplot(ticks, aes(x = day, y = ticks/size*100, color = year)) +
  geom_count(alpha = 0.5) + scale_size_area(max_size = 2) +
  theme_minimal() + facet_grid(area ~ .) +
  labs(x = "Day", y = "Tick Density (ticks per 100 square cm)", color = "Year") +
  guides(size = "none") +
  scale_x_continuous(breaks = c(d09, d10, d11, d12),
    labels = c("9/1", "10/1", "11/1", "12/1")) + ylim(c(0,250)) +
  theme(legend.position = c(0.15, 0.925))

plot(pv)
```



```
ph <- ggplot(ticks, aes(x = day, y = ticks/size*100, color = year)) +
  geom_count(alpha = 0.5) + scale_size_area(max_size = 2) + theme_minimal() +
  facet_wrap(~ area, ncol = 5) +
  labs(x = "Day", y = "Tick Density (ticks per 100 square cm)", color = "Year") +
  guides(size = "none") +
  scale_x_continuous(breaks = c(d09, d10, d11, d12),
    labels = c("9/1", "10/1", "11/1", "12/1")) + ylim(c(0,250)) +
  theme(legend.position = c(0.3, 0.8),
    axis.text.x = element_text(angle = 45, size = 7, hjust = 1))

plot(ph)
```



Modeling

I used a generalized additive model with a log link function estimated using (penalized) quasi-likelihood to deal with considerable over-dispersion.

```
m <- gam(ticks ~ offset(log(size)) + s(day) + year + area,
  family = quasipoisson(link = log), data = ticks)
summary(m)
```

Family: quasipoisson
Link function: log

Formula:
ticks ~ offset(log(size)) + s(day) + year + area

Parametric coefficients:

| | Estimate | Std. Error | t value | Pr(> t) |
|-------------------|----------|------------|---------|-------------|
| (Intercept) | -2.0218 | 0.1855 | -10.90 | < 2e-16 *** |
| year2021 | 0.6547 | 0.1488 | 4.40 | 1.3e-05 *** |
| areaNorth Central | -0.6532 | 0.2330 | -2.80 | 0.0053 ** |
| areaCentral | -0.7678 | 0.4119 | -1.86 | 0.0629 . |
| areaSoutheast | -0.0852 | 0.1937 | -0.44 | 0.6603 |
| areaIsland Park | 0.0143 | 0.2002 | 0.07 | 0.9431 |

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Approximate significance of smooth terms:

| | edf | Ref.df | F | p-value |
|--------|------|--------|------|------------|
| s(day) | 2.94 | 3.71 | 19.6 | <2e-16 *** |

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

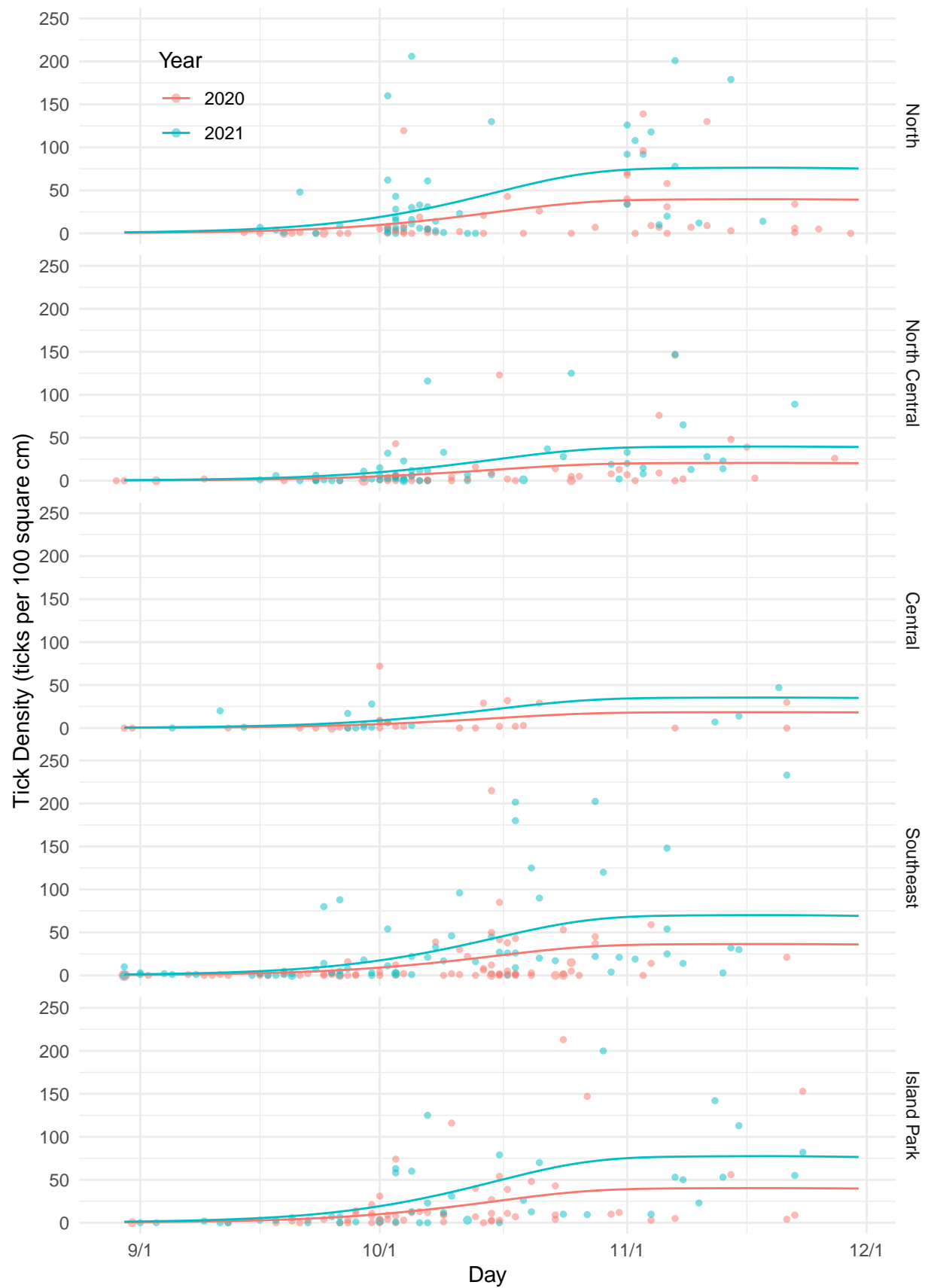
R-sq.(adj) = 0.189 Deviance explained = 32.4%

GCV = 34.323 Scale est. = 55.985 n = 497

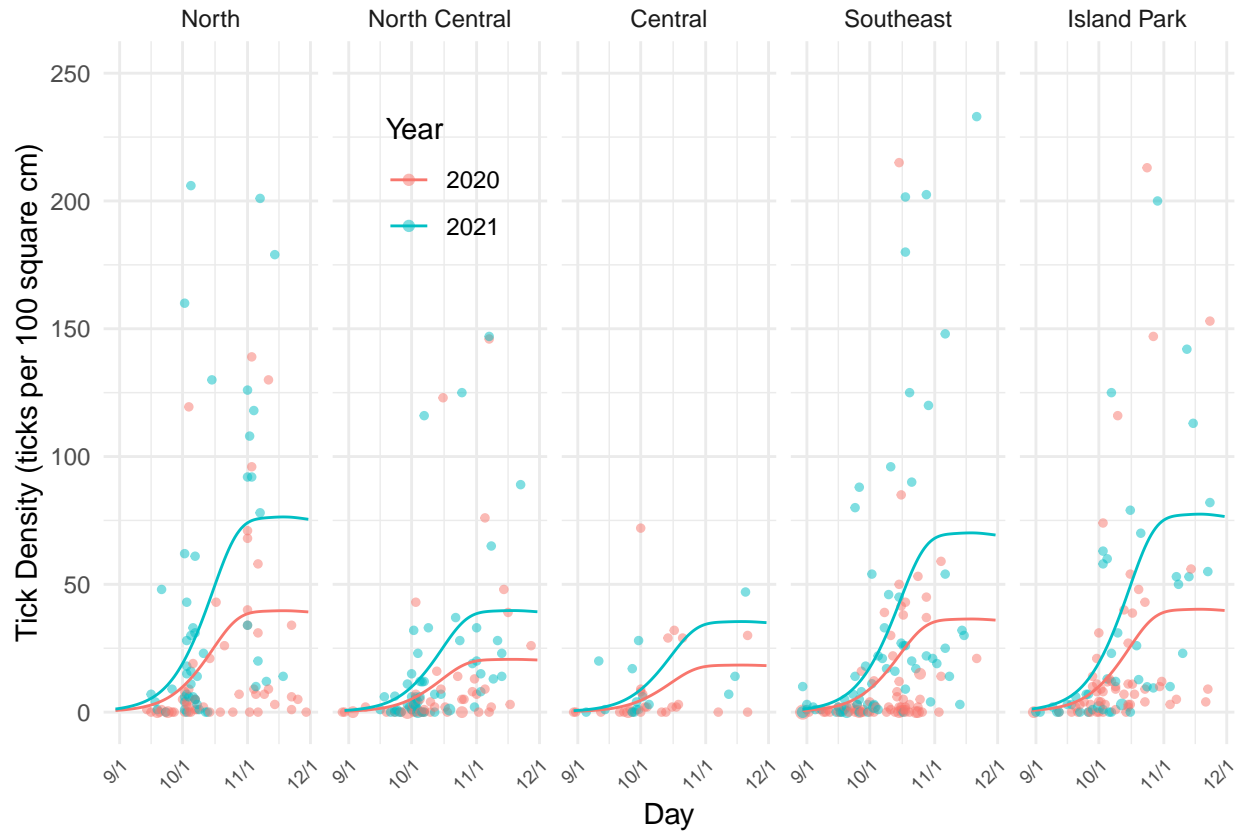
Here we can visualize this model.

```
d <- expand.grid(year = c("2020", "2021"), day = 242:334,
  area = unique(ticks$area), size = 100)
d$yhat <- predict(m, newdata = d, type = "response")

pv <- pv + geom_line(aes(y = yhat), data = d)
plot(pv)
```



```
ph <- ph + geom_line(aes(y = yhat), data = d)
plot(ph)
```



Model-Based Inferences

How much higher is the expected tick density in 2021 than in 2020?

```
emmeans(m, ~year | area, at = list(day = d10),
  type = "response", offset = log(100), data = ticks)
```

area = North:

| year | rate | SE | df | lower.CL | upper.CL |
|------|-------|------|-----|----------|----------|
| 2020 | 9.88 | 2.05 | 488 | 6.57 | 14.86 |
| 2021 | 19.02 | 3.69 | 488 | 12.99 | 27.85 |

area = North Central:

| year | rate | SE | df | lower.CL | upper.CL |
|------|------|------|-----|----------|----------|
| 2020 | 5.14 | 1.28 | 488 | 3.15 | 8.38 |
| 2021 | 9.90 | 2.27 | 488 | 6.31 | 15.52 |

area = Central:

| year | rate | SE | df | lower.CL | upper.CL |
|------|------|------|-----|----------|----------|
| 2020 | 4.59 | 1.87 | 488 | 2.06 | 10.21 |
| 2021 | 8.82 | 3.59 | 488 | 3.97 | 19.63 |

area = Southeast:

| year | rate | SE | df | lower.CL | upper.CL |
|------|------|------|-----|----------|----------|
| 2020 | 9.07 | 1.92 | 488 | 5.99 | 13.74 |


```
2021 17.47 3.36 488    11.97    25.49
```

```
area = Island Park:
```

```
year rate SE df lower.CL upper.CL
2020 10.02 2.13 488    6.60    15.22
2021 19.29 3.81 488    13.09    28.43
```

```
Confidence level used: 0.95
```

```
Intervals are back-transformed from the log scale
```

```
pairs(emmeans(m, ~year | area, at = list(day = d10),
  type = "response", offset = log(100), data = ticks), reverse = TRUE, infer = TRUE)
```

```
area = North:
```

```
contrast          ratio SE df lower.CL upper.CL null t.ratio p.value
year2021 / year2020  1.92 0.286 488    1.44    2.58    1  4.401 <.0001
```

```
area = North Central:
```

```
contrast          ratio SE df lower.CL upper.CL null t.ratio p.value
year2021 / year2020  1.92 0.286 488    1.44    2.58    1  4.401 <.0001
```

```
area = Central:
```

```
contrast          ratio SE df lower.CL upper.CL null t.ratio p.value
year2021 / year2020  1.92 0.286 488    1.44    2.58    1  4.401 <.0001
```

```
area = Southeast:
```

```
contrast          ratio SE df lower.CL upper.CL null t.ratio p.value
year2021 / year2020  1.92 0.286 488    1.44    2.58    1  4.401 <.0001
```

```
area = Island Park:
```

```
contrast          ratio SE df lower.CL upper.CL null t.ratio p.value
year2021 / year2020  1.92 0.286 488    1.44    2.58    1  4.401 <.0001
```

```
Confidence level used: 0.95
```

```
Intervals are back-transformed from the log scale
```

```
Tests are performed on the log scale
```

Note: Here `emmeans` needs a bit more information that is not contained in the model object, so we pass it the data with `data = ticks`. The `contrast` function will also work here, but it needs to be told the degrees of freedom by including the argument `df = m$df.residual`.

```
trtools::contrast(m, tf = exp, df = m$df.residual,
  a = list(year = "2021", area = unique(ticks$area), day = d10, size = 100),
  b = list(year = "2020", area = unique(ticks$area), day = d10, size = 100),
  cnames = unique(ticks$area))
```

```
          estimate lower upper
North          1.925 1.437 2.578
North Central  1.925 1.437 2.578
Central        1.925 1.437 2.578
Southeast      1.925 1.437 2.578
Island Park    1.925 1.437 2.578
```

How about the *difference* in the expected density for each area and the first of October? This is a *discrete marginal effect*, and both area and day matter.

```
margeff(m,
  a = list(year = "2021", area = unique(ticks$area), day = d10, size = 100),
  b = list(year = "2020", area = unique(ticks$area), day = d10, size = 100),
  cnames = unique(ticks$area), df = m$df.residual)
```

| | estimate | se | lower | upper | tvalue | df | pvalue |
|---------------|----------|-------|--------|--------|--------|-------|-----------|
| North | 9.137 | 2.610 | 4.0093 | 14.265 | 3.501 | 488.1 | 0.0005058 |
| North Central | 4.755 | 1.442 | 1.9210 | 7.589 | 3.297 | 488.1 | 0.0010493 |
| Central | 4.240 | 1.964 | 0.3801 | 8.100 | 2.158 | 488.1 | 0.0313905 |
| Southeast | 8.391 | 2.352 | 3.7705 | 13.012 | 3.568 | 488.1 | 0.0003950 |
| Island Park | 9.269 | 2.655 | 4.0512 | 14.486 | 3.490 | 488.1 | 0.0005259 |

Interestingly this can also be done using the **emmeans** package through use of the `regrid` function.

```
tmp <- emmeans(m, ~year | area, at = list(day = d10),
  type = "response", offset = log(100), data = ticks)
pairs(regrid(tmp, type = "response"), reverse = TRUE, infer = TRUE)
```

```
area = North:
  contrast      estimate    SE  df lower.CL upper.CL t.ratio p.value
year2021 - year2020      9.14 2.61 488      4.01    14.27   3.501 0.0005
```

```
area = North Central:
  contrast      estimate    SE  df lower.CL upper.CL t.ratio p.value
year2021 - year2020      4.75 1.44 488      1.92      7.59   3.297 0.0010
```

```
area = Central:
  contrast      estimate    SE  df lower.CL upper.CL t.ratio p.value
year2021 - year2020      4.24 1.96 488      0.38      8.10   2.158 0.0314
```

```
area = Southeast:
  contrast      estimate    SE  df lower.CL upper.CL t.ratio p.value
year2021 - year2020      8.39 2.35 488      3.77    13.01   3.568 0.0004
```

```
area = Island Park:
  contrast      estimate    SE  df lower.CL upper.CL t.ratio p.value
year2021 - year2020      9.27 2.66 488      4.05    14.49   3.490 0.0005
```

Confidence level used: 0.95

How about inferences for the *average* difference across areas?

```
emmeans(regrid(pairs(regrid(tmp, type = "response"), reverse = TRUE)), ~1)
```

| 1 | estimate | SE | df | lower.CL | upper.CL |
|---------|----------|------|-----|----------|----------|
| overall | 7.16 | 1.86 | 488 | 3.51 | 10.8 |

Results are averaged over the levels of: area

Confidence level used: 0.95

Tricky!

How much does the expected tick density increase between, say, the first day of October and November?

```
emmeans(m, ~ day | year * area, at = list(day = c(d11,d10)),
  data = ticks, type = "response")
```

```
year = 2020, area = North:
```

| day | rate | SE | df | lower.CL | upper.CL |
|-----|-------|------|-----|----------|----------|
| 305 | 36.34 | 6.56 | 488 | 25.49 | 51.82 |
| 274 | 9.33 | 1.94 | 488 | 6.20 | 14.04 |

year = 2021, area = North:

| day | rate | SE | df | lower.CL | upper.CL |
|-----|-------|-------|-----|----------|----------|
| 305 | 69.95 | 11.98 | 488 | 49.95 | 97.95 |
| 274 | 17.96 | 3.49 | 488 | 12.26 | 26.30 |

year = 2020, area = North Central:

| day | rate | SE | df | lower.CL | upper.CL |
|-----|-------|------|-----|----------|----------|
| 305 | 18.91 | 4.30 | 488 | 12.10 | 29.56 |
| 274 | 4.86 | 1.21 | 488 | 2.98 | 7.92 |

year = 2021, area = North Central:

| day | rate | SE | df | lower.CL | upper.CL |
|-----|-------|------|-----|----------|----------|
| 305 | 36.40 | 7.67 | 488 | 24.06 | 55.07 |
| 274 | 9.34 | 2.14 | 488 | 5.96 | 14.65 |

year = 2020, area = Central:

| day | rate | SE | df | lower.CL | upper.CL |
|-----|-------|------|-----|----------|----------|
| 305 | 16.86 | 6.94 | 488 | 7.51 | 37.87 |
| 274 | 4.33 | 1.76 | 488 | 1.94 | 9.65 |

year = 2021, area = Central:

| day | rate | SE | df | lower.CL | upper.CL |
|-----|-------|-------|-----|----------|----------|
| 305 | 32.46 | 13.43 | 488 | 14.40 | 73.16 |
| 274 | 8.33 | 3.39 | 488 | 3.75 | 18.53 |

year = 2020, area = Southeast:

| day | rate | SE | df | lower.CL | upper.CL |
|-----|-------|------|-----|----------|----------|
| 305 | 33.38 | 6.06 | 488 | 23.36 | 47.70 |
| 274 | 8.57 | 1.81 | 488 | 5.66 | 12.98 |

year = 2021, area = Southeast:

| day | rate | SE | df | lower.CL | upper.CL |
|-----|-------|-------|-----|----------|----------|
| 305 | 64.24 | 10.67 | 488 | 46.35 | 89.03 |
| 274 | 16.49 | 3.17 | 488 | 11.30 | 24.07 |

year = 2020, area = Island Park:

| day | rate | SE | df | lower.CL | upper.CL |
|-----|-------|------|-----|----------|----------|
| 305 | 36.87 | 7.21 | 488 | 25.11 | 54.13 |
| 274 | 9.47 | 2.01 | 488 | 6.23 | 14.37 |

year = 2021, area = Island Park:

| day | rate | SE | df | lower.CL | upper.CL |
|-----|-------|-------|-----|----------|----------|
| 305 | 70.95 | 13.13 | 488 | 49.33 | 102.06 |
| 274 | 18.22 | 3.60 | 488 | 12.36 | 26.85 |

Confidence level used: 0.95
Intervals are back-transformed from the log scale

```

pairs(emmeans(m, ~ day | year * area, at = list(day = c(d11,d10)),
  data = ticks, type = "response"), infer = TRUE)

```

```
year = 2020, area = North:
  contrast      ratio    SE  df lower.CL upper.CL null t.ratio p.value
day305 / day274  3.9 0.735 488   2.69    5.64    1   7.211 <.0001
```

```
year = 2021, area = North:
  contrast      ratio    SE  df lower.CL upper.CL null t.ratio p.value
day305 / day274  3.9 0.735 488   2.69    5.64    1   7.211 <.0001
```

```
year = 2020, area = North Central:
  contrast      ratio    SE  df lower.CL upper.CL null t.ratio p.value
day305 / day274  3.9 0.735 488   2.69    5.64    1   7.211 <.0001
```

```
year = 2021, area = North Central:
  contrast      ratio    SE  df lower.CL upper.CL null t.ratio p.value
day305 / day274  3.9 0.735 488   2.69    5.64    1   7.211 <.0001
```

```
year = 2020, area = Central:
  contrast      ratio    SE  df lower.CL upper.CL null t.ratio p.value
day305 / day274  3.9 0.735 488   2.69    5.64    1   7.211 <.0001
```

```
year = 2021, area = Central:
  contrast      ratio    SE  df lower.CL upper.CL null t.ratio p.value
day305 / day274  3.9 0.735 488   2.69    5.64    1   7.211 <.0001
```

```
year = 2020, area = Southeast:
  contrast      ratio    SE  df lower.CL upper.CL null t.ratio p.value
day305 / day274  3.9 0.735 488   2.69    5.64    1   7.211 <.0001
```

```
year = 2021, area = Southeast:
  contrast      ratio    SE  df lower.CL upper.CL null t.ratio p.value
day305 / day274  3.9 0.735 488   2.69    5.64    1   7.211 <.0001
```

```
year = 2020, area = Island Park:
  contrast      ratio    SE  df lower.CL upper.CL null t.ratio p.value
day305 / day274  3.9 0.735 488   2.69    5.64    1   7.211 <.0001
```

```
year = 2021, area = Island Park:
  contrast      ratio    SE  df lower.CL upper.CL null t.ratio p.value
day305 / day274  3.9 0.735 488   2.69    5.64    1   7.211 <.0001
```

Confidence level used: 0.95

Intervals are back-transformed from the log scale

Tests are performed on the log scale

What about the *difference* in the expected densities (i.e., marginal effects)?

```
tmp <- emmeans(m, ~ day | year * area, at = list(day = c(d11,d10)),
  data = ticks, type = "response")
pairs(regrid(tmp, type = "response"), infer = TRUE)
```

```
year = 2020, area = North:
  contrast      estimate    SE  df lower.CL upper.CL t.ratio p.value
day305 - day274   27.0  5.76 488   15.69    38.3   4.689 <.0001
```

```
year = 2021, area = North:
```

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|-------|-----|----------|----------|---------|---------|
| day305 - day274 | 52.0 | 10.78 | 488 | 30.80 | 73.2 | 4.822 | <.0001 |

year = 2020, area = North Central:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|------|-----|----------|----------|---------|---------|
| day305 - day274 | 14.1 | 3.57 | 488 | 7.04 | 21.1 | 3.934 | 0.0001 |

year = 2021, area = North Central:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|------|-----|----------|----------|---------|---------|
| day305 - day274 | 27.1 | 6.53 | 488 | 14.23 | 39.9 | 4.146 | <.0001 |

year = 2020, area = Central:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|------|-----|----------|----------|---------|---------|
| day305 - day274 | 12.5 | 5.42 | 488 | 1.88 | 23.2 | 2.311 | 0.0212 |

year = 2021, area = Central:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|-------|-----|----------|----------|---------|---------|
| day305 - day274 | 24.1 | 10.50 | 488 | 3.49 | 44.8 | 2.297 | 0.0221 |

year = 2020, area = Southeast:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|------|-----|----------|----------|---------|---------|
| day305 - day274 | 24.8 | 5.29 | 488 | 14.41 | 35.2 | 4.687 | <.0001 |

year = 2021, area = Southeast:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|------|-----|----------|----------|---------|---------|
| day305 - day274 | 47.7 | 9.65 | 488 | 28.78 | 66.7 | 4.946 | <.0001 |

year = 2020, area = Island Park:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|------|-----|----------|----------|---------|---------|
| day305 - day274 | 27.4 | 6.27 | 488 | 15.09 | 39.7 | 4.372 | <.0001 |

year = 2021, area = Island Park:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|-------|-----|----------|----------|---------|---------|
| day305 - day274 | 52.7 | 11.69 | 488 | 29.77 | 75.7 | 4.511 | <.0001 |

Confidence level used: 0.95

Here is the average marginal effect for each year (i.e., averaging across areas).

```
emmeans(regrid(pairs(regrid(tmp, type = "response"))), ~year)
```

| year | estimate | SE | df | lower.CL | upper.CL |
|------|----------|------|-----|----------|----------|
| 2020 | 21.2 | 4.00 | 488 | 13.3 | 29.0 |
| 2021 | 40.7 | 7.36 | 488 | 26.3 | 55.2 |

Results are averaged over the levels of: area

Confidence level used: 0.95

How fast was the expected tick density increasing on the first day of October? This is an *instantaneous* marginal effect.

```
margeff(m, delta = 0.001, df = m$df.residual,
  a = list(day = d10 + 0.001, area = unique(ticks$area), year = "2020", size = 100),
  b = list(day = d10, area = unique(ticks$area), year = "2020", size = 100),
  cnames = unique(ticks$area))
```

| | estimate | se | lower | upper | tvalue | df | pvalue |
|---------------|----------|--------|---------|--------|--------|-------|-----------|
| North | 0.7546 | 0.1900 | 0.38121 | 1.1280 | 3.971 | 488.1 | 8.238e-05 |
| North Central | 0.3927 | 0.1123 | 0.17203 | 0.6133 | 3.497 | 488.1 | 5.140e-04 |
| Central | 0.3501 | 0.1549 | 0.04583 | 0.6545 | 2.261 | 488.1 | 2.422e-02 |
| Southeast | 0.6930 | 0.1735 | 0.35209 | 1.0339 | 3.994 | 488.1 | 7.490e-05 |
| Island Park | 0.7655 | 0.1942 | 0.38391 | 1.1470 | 3.942 | 488.1 | 9.267e-05 |

We can approximate this fairly well with the change in the expected tick density between the first and second days of October.

```
tmp <- emmeans(m, ~ day | year * area, at = list(day = c(d10 + 1, d10), year = "2020"),
  data = ticks, type = "response")
pairs(regrid(tmp, type = "response"), infer = TRUE)
```

year = 2020, area = North:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|-------|-----|----------|----------|---------|---------|
| day275 - day274 | 0.732 | 0.185 | 488 | 0.3682 | 1.096 | 3.953 | 0.0001 |

year = 2020, area = North Central:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|-------|-----|----------|----------|---------|---------|
| day275 - day274 | 0.381 | 0.109 | 488 | 0.1663 | 0.596 | 3.487 | 0.0005 |

year = 2020, area = Central:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|-------|-----|----------|----------|---------|---------|
| day275 - day274 | 0.340 | 0.151 | 488 | 0.0437 | 0.636 | 2.255 | 0.0246 |

year = 2020, area = Southeast:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|-------|-----|----------|----------|---------|---------|
| day275 - day274 | 0.672 | 0.168 | 488 | 0.3416 | 1.003 | 3.995 | 0.0001 |

year = 2020, area = Island Park:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------|----------|-------|-----|----------|----------|---------|---------|
| day275 - day274 | 0.743 | 0.189 | 488 | 0.3714 | 1.114 | 3.931 | 0.0001 |

Confidence level used: 0.95

Finally consider a comparison of areas.

```
pairs(emmeans(m, ~area | year, at = list(day = d10), type = "response",
  data = ticks), adjust = "none")
```

year = 2020:

| contrast | ratio | SE | df | null | t.ratio | p.value |
|-----------------------------|-------|-------|-----|------|---------|---------|
| North / North Central | 1.922 | 0.448 | 488 | 1 | 2.804 | 0.0053 |
| North / Central | 2.155 | 0.888 | 488 | 1 | 1.864 | 0.0629 |
| North / Southeast | 1.089 | 0.211 | 488 | 1 | 0.440 | 0.6603 |
| North / Island Park | 0.986 | 0.197 | 488 | 1 | -0.071 | 0.9431 |
| North Central / Central | 1.121 | 0.485 | 488 | 1 | 0.265 | 0.7913 |
| North Central / Southeast | 0.567 | 0.131 | 488 | 1 | -2.461 | 0.0142 |
| North Central / Island Park | 0.513 | 0.122 | 488 | 1 | -2.801 | 0.0053 |
| Central / Southeast | 0.505 | 0.209 | 488 | 1 | -1.653 | 0.0990 |
| Central / Island Park | 0.457 | 0.189 | 488 | 1 | -1.890 | 0.0594 |
| Southeast / Island Park | 0.905 | 0.179 | 488 | 1 | -0.503 | 0.6151 |

year = 2021:

| contrast | ratio | SE | df | null | t.ratio | p.value |
|----------|-------|----|----|------|---------|---------|
|----------|-------|----|----|------|---------|---------|

| | | | | | | |
|-----------------------------|-------|-------|-----|---|--------|--------|
| North / North Central | 1.922 | 0.448 | 488 | 1 | 2.804 | 0.0053 |
| North / Central | 2.155 | 0.888 | 488 | 1 | 1.864 | 0.0629 |
| North / Southeast | 1.089 | 0.211 | 488 | 1 | 0.440 | 0.6603 |
| North / Island Park | 0.986 | 0.197 | 488 | 1 | -0.071 | 0.9431 |
| North Central / Central | 1.121 | 0.485 | 488 | 1 | 0.265 | 0.7913 |
| North Central / Southeast | 0.567 | 0.131 | 488 | 1 | -2.461 | 0.0142 |
| North Central / Island Park | 0.513 | 0.122 | 488 | 1 | -2.801 | 0.0053 |
| Central / Southeast | 0.505 | 0.209 | 488 | 1 | -1.653 | 0.0990 |
| Central / Island Park | 0.457 | 0.189 | 488 | 1 | -1.890 | 0.0594 |
| Southeast / Island Park | 0.905 | 0.179 | 488 | 1 | -0.503 | 0.6151 |

Tests are performed on the log scale

Due to an absence of interactions involving area, neither year or day matter.

```
pairs(emmeans(m, ~area, type = "response", data = ticks), adjust = "none")
```

| contrast | ratio | SE | df | null | t.ratio | p.value |
|-----------------------------|-------|-------|-----|------|---------|---------|
| North / North Central | 1.922 | 0.448 | 488 | 1 | 2.804 | 0.0053 |
| North / Central | 2.155 | 0.888 | 488 | 1 | 1.864 | 0.0629 |
| North / Southeast | 1.089 | 0.211 | 488 | 1 | 0.440 | 0.6603 |
| North / Island Park | 0.986 | 0.197 | 488 | 1 | -0.071 | 0.9431 |
| North Central / Central | 1.121 | 0.485 | 488 | 1 | 0.265 | 0.7913 |
| North Central / Southeast | 0.567 | 0.131 | 488 | 1 | -2.461 | 0.0142 |
| North Central / Island Park | 0.513 | 0.122 | 488 | 1 | -2.801 | 0.0053 |
| Central / Southeast | 0.505 | 0.209 | 488 | 1 | -1.653 | 0.0990 |
| Central / Island Park | 0.457 | 0.189 | 488 | 1 | -1.890 | 0.0594 |
| Southeast / Island Park | 0.905 | 0.179 | 488 | 1 | -0.503 | 0.6151 |

Results are averaged over the levels of: year

Tests are performed on the log scale

How about *differences* in the expected density (here day and year matter)?

```
tmp <- emmeans(m, ~area | year, at = list(day = d10), type = "response", data = ticks)
pairs(regrid(tmp, type = "response"), infer = TRUE, adjust = "none")
```

year = 2020:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------------------|----------|------|-----|----------|----------|---------|---------|
| North - North Central | 4.475 | 1.71 | 488 | 1.12 | 7.831 | 2.620 | 0.0091 |
| North - Central | 5.001 | 2.30 | 488 | 0.49 | 9.512 | 2.178 | 0.0299 |
| North - Southeast | 0.762 | 1.74 | 488 | -2.65 | 4.173 | 0.439 | 0.6610 |
| North - Island Park | -0.134 | 1.88 | 488 | -3.83 | 3.565 | -0.071 | 0.9431 |
| North Central - Central | 0.526 | 1.93 | 488 | -3.26 | 4.316 | 0.273 | 0.7853 |
| North Central - Southeast | -3.713 | 1.59 | 488 | -6.83 | -0.594 | -2.339 | 0.0198 |
| North Central - Island Park | -4.610 | 1.79 | 488 | -8.12 | -1.097 | -2.578 | 0.0102 |
| Central - Southeast | -4.239 | 2.21 | 488 | -8.59 | 0.110 | -1.915 | 0.0560 |
| Central - Island Park | -5.135 | 2.35 | 488 | -9.75 | -0.519 | -2.186 | 0.0293 |
| Southeast - Island Park | -0.896 | 1.79 | 488 | -4.42 | 2.624 | -0.500 | 0.6172 |

year = 2021:

| contrast | estimate | SE | df | lower.CL | upper.CL | t.ratio | p.value |
|-----------------------|----------|------|-----|----------|----------|---------|---------|
| North - North Central | 8.613 | 3.27 | 488 | 2.18 | 15.046 | 2.631 | 0.0088 |
| North - Central | 9.625 | 4.32 | 488 | 1.15 | 18.105 | 2.230 | 0.0262 |
| North - Southeast | 1.466 | 3.35 | 488 | -5.11 | 8.044 | 0.438 | 0.6616 |
| North - Island Park | -0.259 | 3.62 | 488 | -7.38 | 6.860 | -0.071 | 0.9431 |

| | | | | | | | |
|-----------------------------|--------|------|-----|--------|--------|--------|--------|
| North Central - Central | 1.012 | 3.70 | 488 | -6.26 | 8.283 | 0.274 | 0.7846 |
| North Central - Southeast | -7.147 | 3.01 | 488 | -13.06 | -1.230 | -2.373 | 0.0180 |
| North Central - Island Park | -8.872 | 3.41 | 488 | -15.57 | -2.174 | -2.602 | 0.0095 |
| Central - Southeast | -8.159 | 4.14 | 488 | -16.30 | -0.019 | -1.969 | 0.0495 |
| Central - Island Park | -9.884 | 4.40 | 488 | -18.53 | -1.234 | -2.245 | 0.0252 |
| Southeast - Island Park | -1.725 | 3.45 | 488 | -8.51 | 5.057 | -0.500 | 0.6175 |

Confidence level used: 0.95