```
In[2]:= LatticeGraph[k] := GridGraph[{k, k}]
           In[3]:= PC[k_{,} x_{,}] := ChromaticPolynomial[LatticeGraph[k], x];
                                      x = Symbol["x"];
                                      (*Chromatic Polynomial of a 5x5 lattice*)
            ln[6]:= pc5 = PC[5, x]
       Out[6]= 32\ 126\ 211\ x - 290\ 435\ 775\ x^2 + 1\ 292\ 190\ 143\ x^3 - 3\ 767\ 970\ 906\ x^4 + 8\ 082\ 227\ 271\ x^5 -
                                              13\,560\,791\,041\,x^6 + 18\,473\,119\,556\,x^7 - 20\,932\,275\,014\,x^8 + 20\,054\,961\,996\,x^9 -
                                              16\,429\,209\,737\,{\,x^{10}}+11\,594\,826\,096\,{\,x^{11}}-7\,082\,871\,652\,{\,x^{12}}+3\,754\,018\,486\,{\,x^{13}}-
                                              1726958903x^{14} + 688444232x^{15} - 236955938x^{16} + 69997383x^{17} - 17590911x^{18} +
                                              3714180 x^{19} - 647352 x^{20} + 90798 x^{21} - 9864 x^{22} + 780 x^{23} - 40 x^{24} + x^{25}
           In[8]:= (*10 colorings of a 5x5 lattice*)
                                        pc5/. x \rightarrow 10
Out[15]=
                                       151 086 899 096 935 604 867 610
                                      (*k=2*)
           ln[9]:= results2 = Table[{q, PC[2, q]}, {q, 2, 15}]
                                    \{(2, 2), \{3, 18\}, \{4, 84\}, \{5, 260\}, \{6, 630\}, \{7, 1302\}, \{8, 2408\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 4104\}, \{9, 41
                                             \{10, 6570\}, \{11, 10010\}, \{12, 14652\}, \{13, 20748\}, \{14, 28574\}, \{15, 38430\}\}
           ln[2]:= (*k=3*)
      ln[16]:= results3 = Table[{q, PC[3, q]}, {q, 2, 15}]
Out[16]=
                                      \{\{2, 2\}, \{3, 246\}, \{4, 9612\}, \{5, 142820\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{7, 6464682\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\}, \{6, 1166910\},
                                             \{8, 27350456\}, \{9, 95004072\}, \{10, 283982490\}, \{11, 754324670\},
                                             \{12, 1821684612\}, \{13, 4067709516\}, \{14, 8506024982\}, \{15, 16822697010\}\}
           ln[1]:= (*k=4*)
           ln[7]:= results4 = Table[{q, PC[4, q]}, {q, 2, 15}]
       {7, 856 858 754 052}, {8, 11 722 360 851 992}, {9, 111 647 093 496 192},
                                             \{10, 807567269568570\}, \{11, 4707230299664420\}, \{12, 23062698161984052\}, \{13, 23062698161984052\}, \{14, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 23062698161984052\}, \{15, 230626981619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840619840061984061984061984061984061984061984061984061984061984061984061860619840061984061984061984061
                                              \{13, 97963534144477872\}, \{14, 369313246327400102\}, \{15, 1258250118125770980\}\}
```

```
(*k=5*)
                       results5 = Table[\{q, PC[5, q]\}, \{q, 2, 15\}]
Out[10]=
                      \{\{2, 2\}, \{3, 580986\}, \{4, 20442892764\}, \{5, 50820390410180\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869327169310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 219778693100\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 21977869310\}, \{6, 2197786931
                         \{7, 3031776844080257742\}, \{8, 189586772101347563096\}, \{9, 6660747304179593671944\}, \{8, 189586772101347563096\}, \{9, 6660747304179593671944\}, \{9, 6660747304179593671944\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347563096\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 189586772101347696\}, \{1, 1895867721014696\}, \{1, 1895867721014696\}, \{1, 1895867721014696\}, \{1, 1895867721014696\}, \{1, 1895867721014696\}, \{1, 1895867696\}, \{1, 1895867696\}, \{1, 1895867696\}, \{1, 1895867696\}, \{1, 1895867696\}, \{1, 1895867696\}, \{1, 189586676
                          \{10, 151086899096935604867610\}, \{11, 2432514752747773742479970\},
                          {12, 29730874656484222810604532}, {13, 289814278376886365788686156},
                          \{14, 2338706558881006527354278774\}, \{15, 16079941149554432258574500790\}\}
    In[12]:= (*k=6*)
    ln[11]:= results6 = Table[{q, PC[6, q]}, {q, 2, 15}]
Out[11]=
                      \{\{2, 2\}, \{3, 101596896\}, \{4, 380053267505964\}, \}
                          {5, 32 921 147 633 979 091 400}, {6, 223 479 277 713 132 418 833 390},
                          {7, 286 359 202 456 130 400 260 611 752}, {8, 115 702 677 512 781 649 307 005 417 016},
                          {9, 20 172 922 880 766 721 483 554 814 468 464}, {10, 1859 669 891 770 248 856 476 997 904 547 450},
                          {11, 104 094 652 664 259 277 009 814 001 042 264 080},
                          {12, 3902706595258725042220943436744767652},
                          {13, 105 321 232 530 952 648 899 117 870 043 962 825 336},
                          {14, 2 160 076 836 868 464 110 960 157 773 766 060 869 414},
                          {15, 35 111 392 067 312 546 609 182 417 173 618 968 309 400}}
    In[13]:= (*k=7*)
                       results7 = Table[\{q, PC[7, q]\}, \{q, 2, 15\}]
Out[13]=
                      \{2, 2\}, \{3, 41869995708\}, \{4, 38557892676685306572\},
                          {5, 225 313 329 780 157 255 086 187 280}, {6, 40 087 345 104 573 458 097 599 768 622 030},
                          {7, 722 022 905 627 873 731 429 602 000 554 432 412},
                          {8, 2664533696267986042969615868160108207608},
                          {9, 3 101 594 610 276 176 352 440 997 042 418 550 841 885 312},
                          {10, 1505 933 744 255 415 534 793 832 118 356 329 294 462 055 610},
                          {11, 368 879 277 984 660 057 018 944 113 007 596 468 930 552 762 460},
                          {12, 52 165 666 940 966 795 634 555 971 171 590 612 361 421 172 621 572},
                          {13, 4701678278015774960172015306840176414525523362269008},
                          {14, 290 988 136 771 156 891 920 507 578 262 485 806 342 801 661 960 991 302},
                          {15, 13099591719762965565281394772689392638859825972900575740}}
      In[5]:= (*k=8*)
                      results8 = Table[\{q, PC[8, q]\}, \{q, 2, 15\}]
```