

IT-UNIVERSITY OF COPENHAGEN

AUTOMATED SOFTWARE ANALYSIS

Analysis-1

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1:

Prove that the following problem is undecidable - *Is boolean variable 'b' always true in program P?*

Assuming we have a program `bIsTrueInP(P)` that takes another program `P` as an input and decides whether or not the variable `b` is always true, we can construct the program `R` in Listing 1.

Listing 1: R.cs

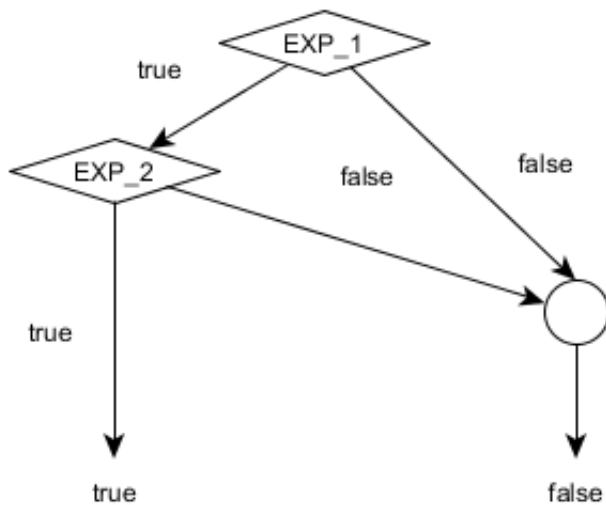
```
bool b = false;  
P // insert the code of P here.  
return b;
```

If we run `bIsTrueInP` with `R` as an input

```
res = bIsTrueInP(R)
```

we can conclude that if `res` is true then the program `R` halts. If not, program `R` loops. This way we have solved the halting problem, which has been proven to be undecidable. We have therefore arrived at a contradiction. We must therefore conclude that the problem - *Is boolean variable 'b' always true in program P?* - is undecidable

2:



3:

