

$$\begin{aligned}
& \int \cos(x) \cos(2x) \sin(4x) \, dx \\
&= \int 1/2 \cos(x) (\sin(6x) + \sin(2x)) \, dx \text{ (viết lại, } \cos(x) \cos(2x) \sin(4x) = 1/2 \cos(x) (\sin(6x) + \sin(2x)) \text{)} \\
&= \int 1/2 \cos(x) \sin(6x) + 1/2 \cos(x) \sin(2x) \, dx \text{ (viết lại, } 1/2 \cos(x) (\sin(6x) + \sin(2x)) \text{)} \\
&= \int 1/2 \cos(x) \sin(6x) \, dx + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (công thức tổng)} \\
&= 1/2 \int \cos(x) \sin(6x) \, dx + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (nhân hằng số)} \\
&= 1/2 \int 1/2 \sin(7x) + 1/2 \sin(5x) \, dx + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (viết lại, } \cos(x) \sin(6x) = 1/2 \sin(7x) + 1/2 \sin(5x) \text{)} \\
&= 1/2 \int 1/2 \sin(7x) \, dx + 1/2 \int 1/2 \sin(5x) \, dx + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (công thức tích)} \\
&= 1/4 \int \sin(7x) \, dx + 1/2 \int 1/2 \sin(5x) \, dx + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (nhân hằng số)} \\
&= 1/4 \int 1/7 \sin(u) \, du + 1/2 \int 1/2 \sin(5x) \, dx + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (đặt } u = 7x \text{)}
\end{aligned}$$

$$= 1/28 \int \sin(u) \, du + 1/2 \int 1/2 \sin(5x) \, dx + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (nhân hằng số)}$$

$$= -1/28 \cos(u) + 1/2 \int 1/2 \sin(5x) \, dx + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (công thức sin)}$$

$$= -1/28 \cos(7x) + 1/2 \int 1/2 \sin(5x) \, dx + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (trả lại)}$$

$$= -1/28 \cos(7x) + 1/4 \int \sin(5x) \, dx + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (nhân hằng số)}$$

$$= -1/28 \cos(7x) + 1/4 \int 1/5 \sin(u) \, du + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (đặt biến, } u = 5x \text{)}$$

$$= -1/28 \cos(7x) + 1/20 \int \sin(u) \, du + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (nhân hằng số)}$$

$$= -1/28 \cos(7x) - 1/20 \cos(u) + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (công thức sin)}$$

$$= -1/28 \cos(7x) - 1/20 \cos(5x) + \int 1/2 \cos(x) \sin(2x) \, dx \text{ (trả lại)}$$

$$= -1/28 \cos(7x) - 1/20 \cos(5x) + 1/2 \int \cos(x) \sin(2x) \, dx \text{ (nhân hằng số)}$$

$$\begin{aligned}
&= -1/28 \cos(7x) - 1/20 \cos(5x) + 1/2 \int 1/2 \sin(3x) + 1/2 \sin(x) \, dx \text{ (viết lại, cos)} \\
&= -1/28 \cos(7x) - 1/20 \cos(5x) + 1/2 \int 1/2 \sin(3x) \, dx + 1/2 \int 1/2 \sin(x) \, dx \text{ (c)} \\
&= -1/28 \cos(7x) - 1/20 \cos(5x) + 1/4 \int \sin(3x) \, dx + 1/2 \int 1/2 \sin(x) \, dx \text{ (nhân)} \\
&= -1/28 \cos(7x) - 1/20 \cos(5x) + 1/4 \int 1/3 \sin(u) \, du + 1/2 \int 1/2 \sin(x) \, dx \text{ (đặ)} \\
&= -1/28 \cos(7x) - 1/20 \cos(5x) + 1/12 \int \sin(u) \, du + 1/2 \int 1/2 \sin(x) \, dx \text{ (nhân)} \\
&= -1/28 \cos(7x) - 1/20 \cos(5x) - 1/12 \cos(u) + 1/2 \int 1/2 \sin(x) \, dx \text{ (công thức s)} \\
&= -1/28 \cos(7x) - 1/20 \cos(5x) - 1/12 \cos(3x) + 1/2 \int 1/2 \sin(x) \, dx \text{ (trả lại)} \\
&= -1/28 \cos(7x) - 1/20 \cos(5x) - 1/12 \cos(3x) + 1/4 \int \sin(x) \, dx \text{ (nhân hằng số)} \\
&= -1/28 \cos(7x) - 1/20 \cos(5x) - 1/12 \cos(3x) - 1/4 \cos(x) \text{ (công thức sin)}
\end{aligned}$$