

Chapter 3:

Continuous Wave (CW) Modulation

Amplitude and Frequency Modulations

Part A: Amplitude Modulation

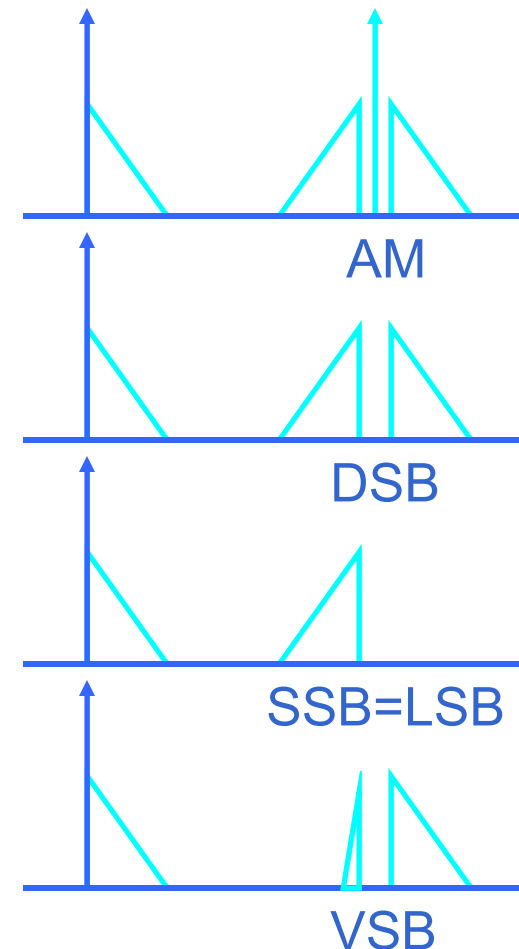
October 2018

Lectured by Prof. Dr. Thuong Le-Tien

Slides with references from HUT Finland; Mc. Graw Hill Co.;
A.B. Carlson's Communication Systems Book;
Simon Haykin - Communication Systems Book.
R.Ziemer&H.Transfer – Principles of Communications Book

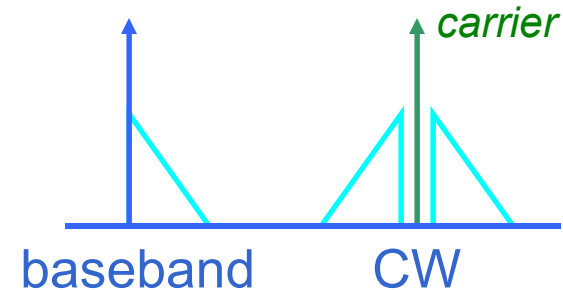
Linear continuous wave (CW) modulation

- Bandpass systems and signals
- Lowpass (LP) equivalents
- Amplitude modulation (AM)
- Double-sideband modulation (DSB)
- Modulator techniques
- Suppressed-sideband
(Single Sideband) amplitude
modulation (LSB, USB)
- Vestigial Sideband modulation (VSB)
- Detection techniques of linear modulation
 - Coherent detection
 - Noncoherent detection

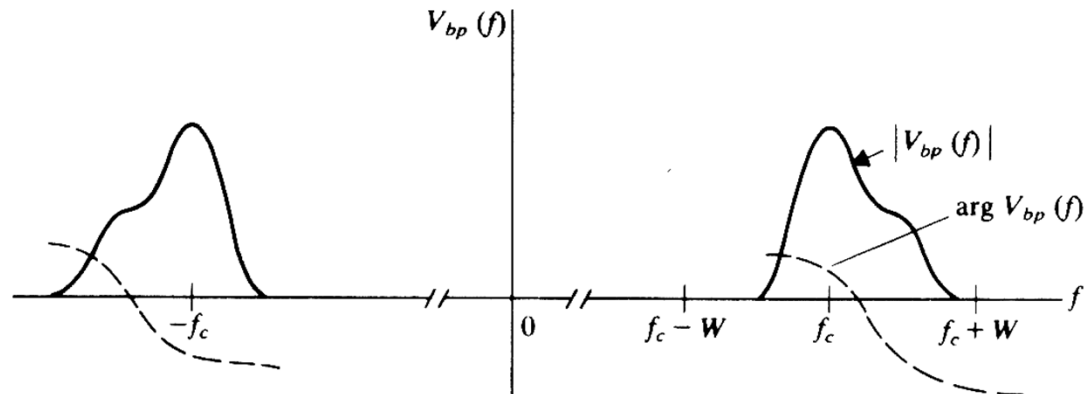


Baseband and CW communications

- Baseband communications is used in
 - PSTN local loop
 - PCM communications for instance between exchanges
 - (fiber-) optical communication
- Using carrier to shape and shift the frequency spectrum (eg CW techniques) enable modulation by which several advantages are obtained
 - different **radio bands** can be used for communications
 - **wireless** communications
 - **multiplexing** techniques become applicable
 - exchanging transmission bandwidth to received SNR



Defining bandpass signals



- The bandpass signal is band limited

$$V_{bp}(f) = 0, |f| < f_c - W \wedge |f| > f_c + W$$

$$V_{bp}(f) \neq 0, \text{otherwise}$$

- We assume also that (why?)
$$W \ll f_c$$
- In telecommunications bandpass signals are used to convey messages over medium
- In practice, transmitted messages are never strictly band limited due to
 - their nature in frequency domain (Fourier series coefficients may extend over very large span of frequencies)
 - non-ideal filtering

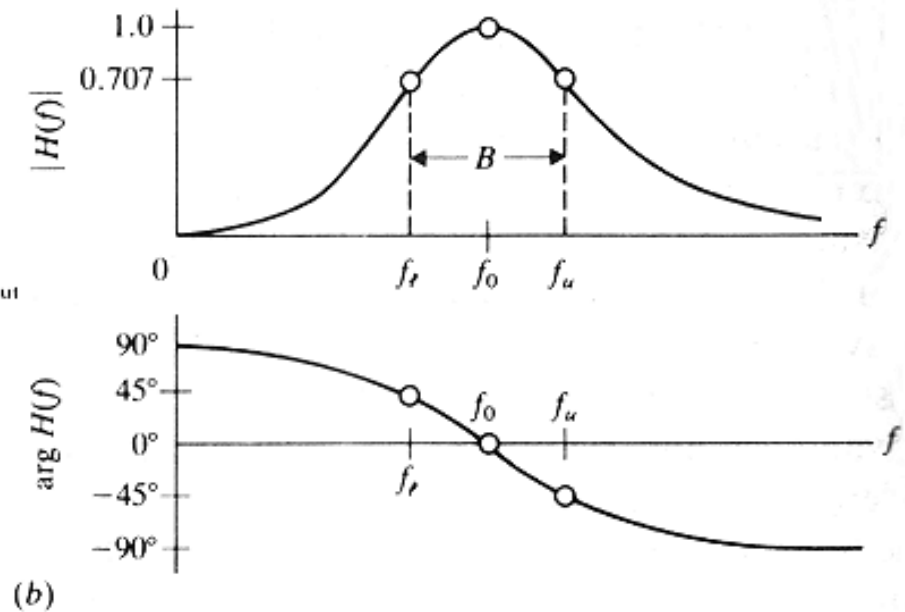
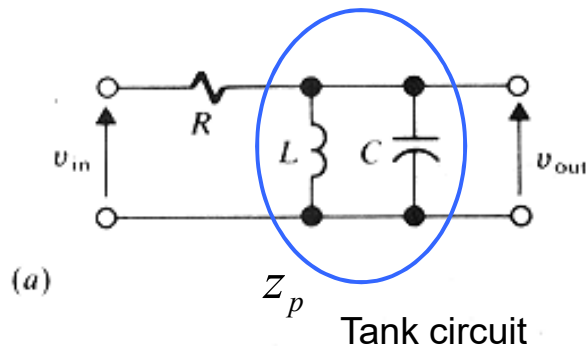
Example of a bandpass system

- Consider a simple bandpass system: a resonant (tank) circuit

$$z_p = \frac{j\omega L / j\omega C}{j\omega L + 1 / j\omega C} \quad z_i = R + z_p \quad V_{in}(\omega)H(\omega) = V_{out}(\omega)$$

$$H(\omega) = V_{out}(\omega) / V_{in}(\omega) = z_p / z_i \Rightarrow H(\omega) = 1 / [1 + jQ(f / f_0 + f_0 / f)]$$

$$\begin{cases} Q = R\sqrt{C/L} \\ f_0 = (2\pi\sqrt{LC})^{-1} \end{cases}$$



Bandwidth and Q-factor

- The bandwidth is inversely proportional to Q-factor:

$$B_{3dB} = f_0 / Q \quad (\text{for the tank circuit: } Q = R\sqrt{C/L})$$

- System design is easier if the fractional bandwidth $1/Q=B/f_0$ is kept relatively small:

$$0.01 < B / f_0 < 0.1$$

- Some practical examples:

Frequency Band	Carrier Frequency	Bandwidth
Longwave radio	100 kHz	2 kHz
Shortwave radio	5 MHz	100 kHz
VHF	100 MHz	2 MHz
Microwave	5 GHz	100 MHz
Millimeterwave	100 GHz	2 GHz
Optical	5×10^{14} Hz	10^{13} Hz

System design is easier for smaller fractional bandwidths (FB).

- Antenna and bandpass amplifier design is difficult for large FB:s:
 - one will have “**difficult to realize**” components or parameters in circuits as
 - too high Q
 - **too small or large values** for capacitors and inductors
- These structures have a bandpass nature because one of their important elements is the resonant circuit. Making them broadband means decreasing **resistive losses** that can be difficult

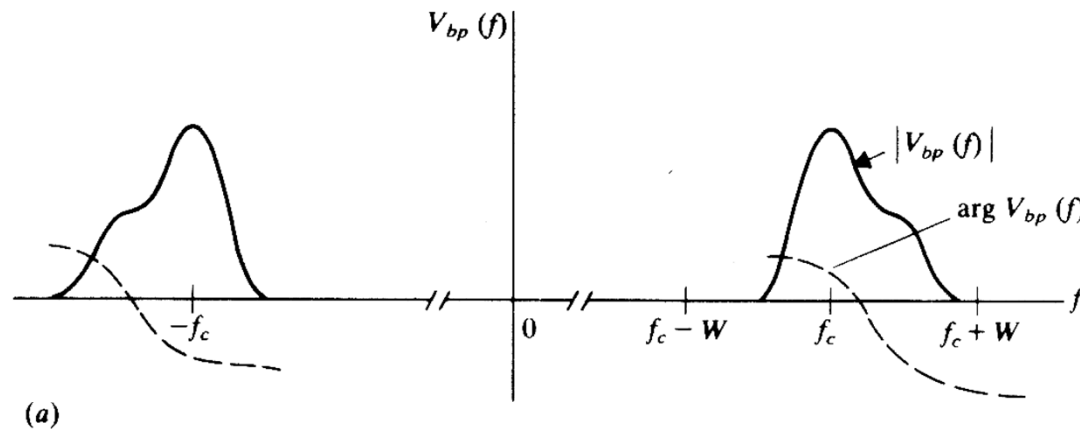
- In I-Q presentation bandpass signal **carrier** and **modulation** parts are separated into different terms

$$v_{bp}(t) = A(t) \cos[\omega_c t + \phi(t)]$$

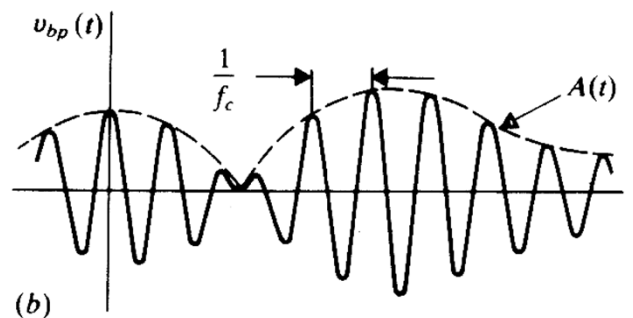
$$v_{bp}(t) = v_i(t) \cos(\omega_c t) - v_q(t) \sin(\omega_c t)$$

$$v_i(t) = A(t) \cos \phi(t), v_q(t) = A(t) \sin \phi(t)$$

Bandpass signal
in frequency
domain



Bandpass signal
in time
domain



$$\cos(\alpha + \beta) = \cos(\alpha) \cos(\beta) - \sin(\alpha) \sin(\beta)$$

dashed line
denotes envelope



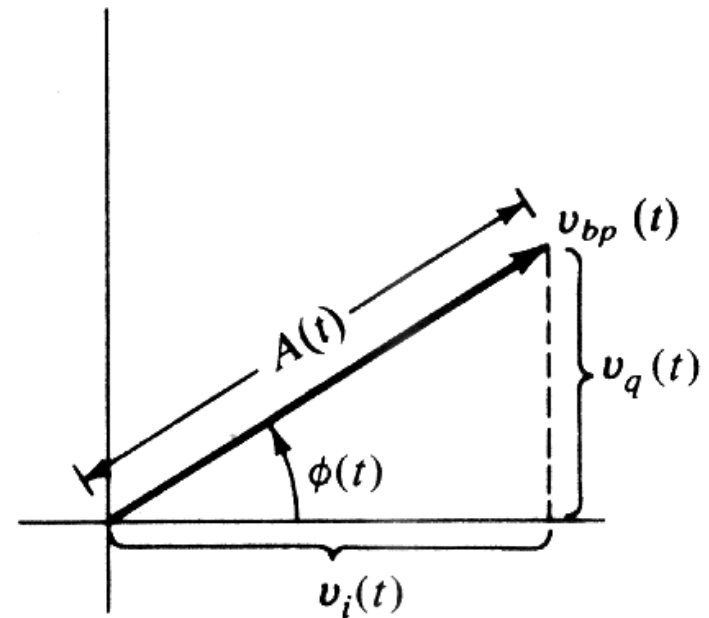
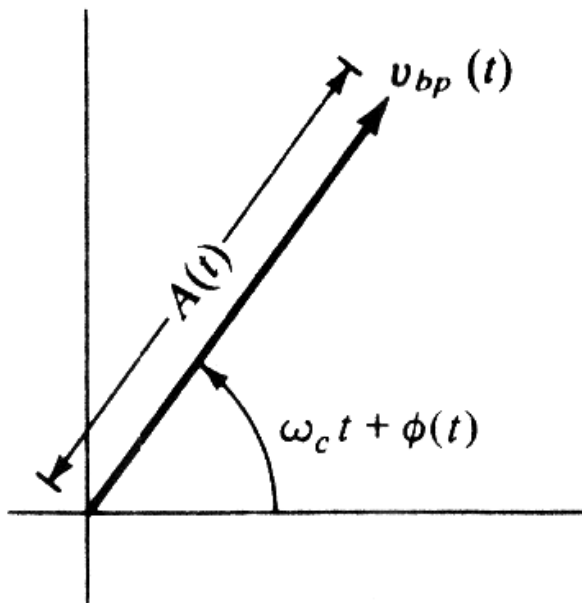
The phasor description of bandpass signal

- Bandpass signal is conveniently represented by a phasor rotating at the angular carrier rate $\omega_c t + \phi(t)$:

$$v_{bp}(t) = v_i(t) \cos(\omega_c t) - v_q(t) \sin(\omega_c t)$$

$$v_i(t) = A(t) \cos \phi(t), \quad v_q(t) = A(t) \sin \phi(t)$$

$$A(t) = \sqrt{v_i^2(t) + v_q^2(t)} \quad \phi(t) = \begin{cases} v_i(t) \geq 0, \arctan(v_q(t)/v_i(t)) \\ v_i(t) < 0, \pi + \arctan(v_q(t)/v_i(t)) \end{cases}$$



Lowpass (LP) signal $v_{bp}(t) = v_i(t) \cos(\omega_c t) - v_q(t) \sin(\omega_c t)$
 $v_i(t) = A(t) \cos \phi(t), v_q(t) = A(t) \sin \phi(t)$

- Lowpass signal is defined by yielding in time domain $V_{lp}(f) \approx \frac{1}{2} [V_i(f) + jV_q(f)]$

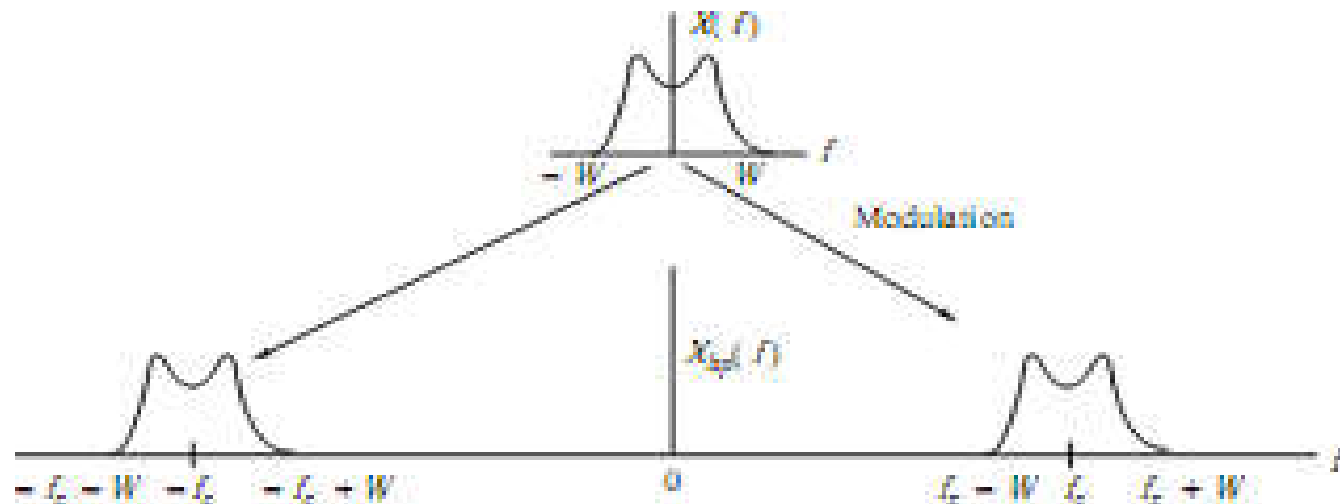
$$v_{lp}(t) = F^{-1} [V_{lp}(f)] = \frac{1}{2} [v_i(t) + jv_q(t)]$$

Taking rectangular-polar conversion yields then

$$v_{lp}(t) = A(t) [\cos \phi(t) + j \sin \phi(t)] / 2 \quad v_{lp}(t) = \frac{1}{2} A(t) \exp j\phi(t)$$

$$|v_{lp}(t)| = A(t) / 2, \arg v_{lp}(t) = \phi(t)$$

\Rightarrow



Transforming lowpass signals and bandpass signals

$$v_{bp}(t) = A(t) \cos[\omega_c t + \phi(t)]$$

$$v_{bp} = \operatorname{Re} \{ A(t) \exp[j\omega_c t + \phi(t)] \}$$

$$v_{bp} = 2 \operatorname{Re} \left\{ \underbrace{\frac{A(t)}{2} \exp[j\phi(t)]}_{v_{lp}(t)} \exp[j\omega_c t] \right\}$$

$$v_{bp} = 2 \operatorname{Re} \{ v_{lp}(t) \exp[j\omega_c t] \}$$

- Physically this means that the lowpass signal is **modulated** to the carrier frequency ω when it is transformed to bandpass signal. Bandpass signal can be transformed into lowpass signal. The physical meaning of this is a spectrum translation.

$$V_{lp}(f) = V_{bp}(f + f_c) u(f + f_c)$$

Amplitude Modulation (AM full)

- Four linear modulation methods: (1) AM (amplitude modulation), (2) DSB (double sideband modulation), (3) SSB (single sideband modulation), (4) VSB (vestigial sideband modulation)

- AM signal:

$$\begin{aligned} x_c(t) &= A_c [1 + \mu x_m(t)] \cos(\omega_c t + \phi(t)) \\ &= \underbrace{A_c \cos(\omega_c t + \phi(t))}_{\text{Carrier}} + \underbrace{A_c \mu x_m(t) \cos(\omega_c t + \phi(t))}_{\text{Information carrying part}} \end{aligned} \quad \left\{ \begin{array}{l} 0 \leq \mu \leq 1 \\ |x_m(t)| \leq 1 \end{array} \right.$$

- $\phi(t)$ is an arbitrary *constant*. Hence we note that no information is transmitted via the phase. Assume for instance that $\phi(t)=0$, then the LP components are

$$v_i(t) = A(t) \cos(\phi(t)) = A(t) = A_c [1 + \mu x_m(t)]$$

$$v_q(t) = A(t) \sin(\phi(t)) = 0$$

- Also, the carrier component contains no information-> Waste of power to transmit the unmodulated carrier, but can still be useful (how?)

AM: waveforms and bandwidth

- AM in frequency domain:

$$x_c(t) = A_c[1 + \mu x_m(t)]\cos(\omega_c t)$$

$$= \underbrace{A_c \cos(\omega_c t)}_{\text{Carrier}} + \mu \underbrace{x_m(t) \cos(\omega_c t)}_{\text{Information carrying part}}$$

$$X_c(f) = \underbrace{A_c \delta(f - f_c)/2}_{\text{Carrier}} + \mu \underbrace{A_c X_m(f - f_c)/2}_{\text{Information carrying part}} \quad f > 0 \text{ (for brief notations)}$$

- AM bandwidth is twice the message bandwidth W :



$$v(t)\cos(\omega_c t + \phi) \leftrightarrow \frac{1}{2}[V(f - f_c)\exp j\phi + V(f + f_c)\exp -j\phi]$$

AM waveforms

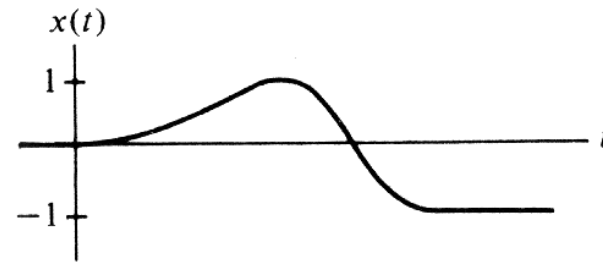
(a): modulation

(b): modulated carrier with $\mu < 1$

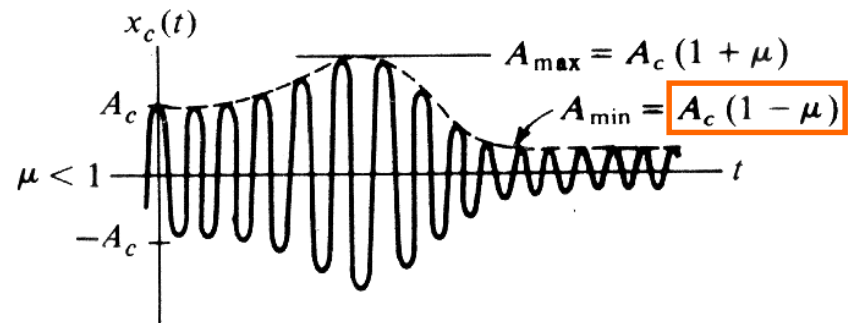
(c): modulated carrier with $\mu > 1$ with distortion

(d) Modulation Index

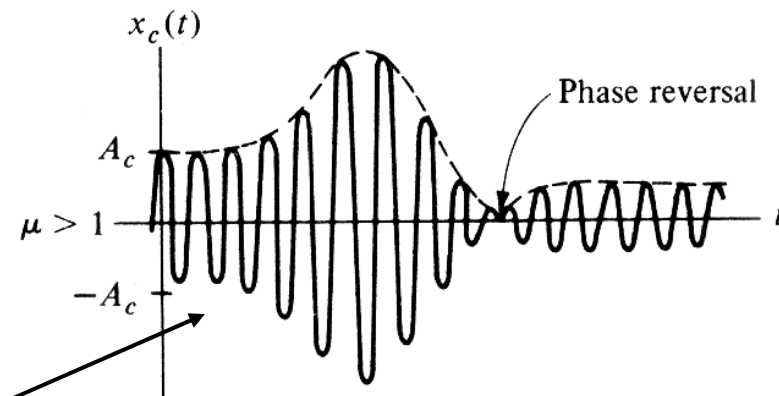
$$\mu = (A_{\max} - A_{\min}) / 2A_c$$



(a)



(b)



(c)

Envelope distortion!

$$(AM \text{ signal: } x_c(t) = A_c[1 + \mu x_m(t)]\cos(\omega_c t))$$



AM power efficiency

- AM wave total power consists of the idle carrier part and the useful signal part: $\langle x_c^2(t) \rangle = \underbrace{\langle A_c^2 \cos^2(\omega_c t) \rangle}_{\text{Carrier}}$

(AM signal: $x_c(t) = A_c[1 + \mu x_m(t)]\cos(\omega_c t)$)

$$+ \underbrace{\langle \mu^2 A_c^2 x_m^2(t) \cos^2(\omega_c t) \rangle}_{\text{Power: } S_X}$$

$$= \underbrace{A_c^2 / 2}_{P_C} + \underbrace{\mu^2 A_c^2 S_X / 2}_{2P_{SB}}$$

- Assume $A_c=1$, $S_X=1$, then for $\mu=1$ (the max value) the total power is

$$P_{T_{\max}} = 1/2 + 1/2 = 50\% + 50\%$$

carrier + modulated power

- Therefore at least half of the total power is wasted on carrier
- Detection of AM is simple by enveloped detector that is a reason why AM is still used. Also, sometimes AM makes system design easier, as in fiber optic communications

$$\frac{A^2}{T} \cdot \int_0^T \cos^2\left(2 \cdot \frac{\pi \cdot t}{T}\right) dt \rightarrow \frac{1}{2} \cdot A^2$$

AM-Double SideBand (DSB)

- In DSB the wasteful carrier is suppressed:

$$x_c(t) = A_c x_m(t) \cos(\omega_c t)$$

- The spectra is otherwise identical to AM and the transmission BW equals again double the message BW

$$X_c(f) = A_c X_m(f - f_c) / 2, f > 0$$

- In time domain **each** modulation signal zero crossing produces *phase reversals* of the carrier. For DSB, the total power S_T and the power/sideband P_{SB} have the relationship

$$S_T = A_c^2 S_X / 2 = 2P_{SB} \Rightarrow P_{SB} = A_c^2 S_X / 4 (DSB)$$

- Therefore AM transmitter requires twice the power of DSB transmitter to produce the same coverage assuming $S_X=1$. However, in practice S_X is usually smaller than 1/2, under which condition at least four times the DSB power is required for the AM transmitter for the same coverage

$$\text{AM: } x_c(t) = A_c [1 + \mu x_m(t)] \cos(\omega_c t)$$

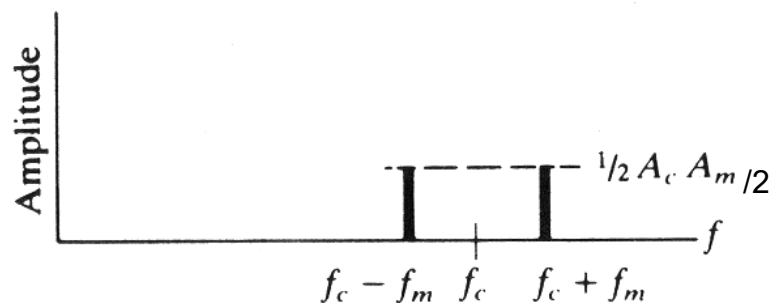
AM-Double SideBand DSB and spectra

- AM in frequency domain with $x_m(t) = A_m \cos(\omega_m t)$

$$X_c(f) = \underbrace{A_c \delta(f - f_c)/2}_{\text{Carrier}} + \underbrace{\mu A_c X_m(f - f_c)/2, f > 0}_{\text{Information carrying part}} \quad (\text{general expression})$$

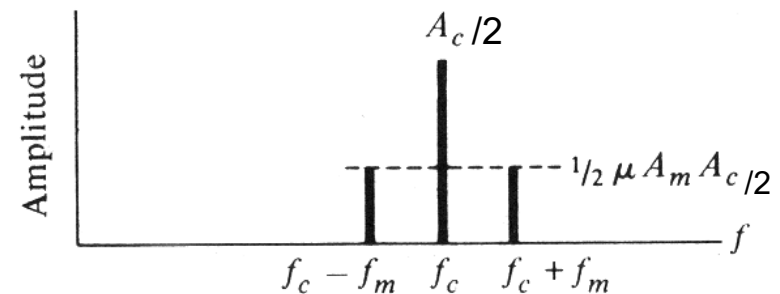
$$X_c(f) = \frac{A_c}{2} \delta(f - f_c) + \frac{\mu A_c A_m}{4} \delta(f - f_c - f_m) + \frac{\mu A_c A_m}{4} \delta(f - f_c + f_m)$$

- In summary, difference of AM and DSB at frequency domain is the missing carrier component. Other differences relate to power efficiency and detection techniques.



(a)

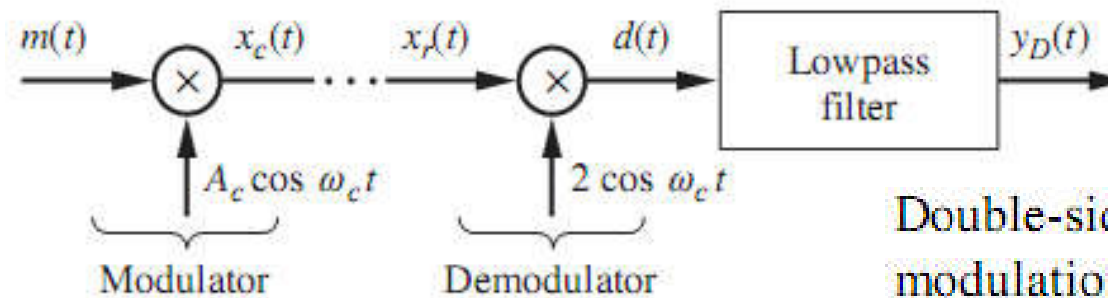
(a) DSB spectra,



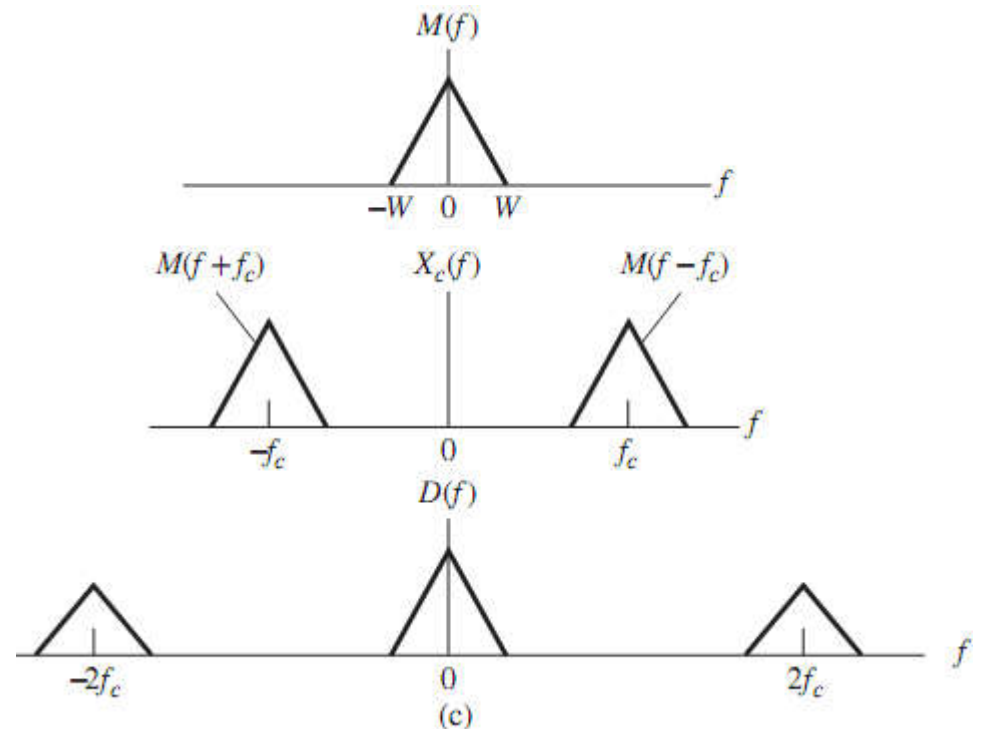
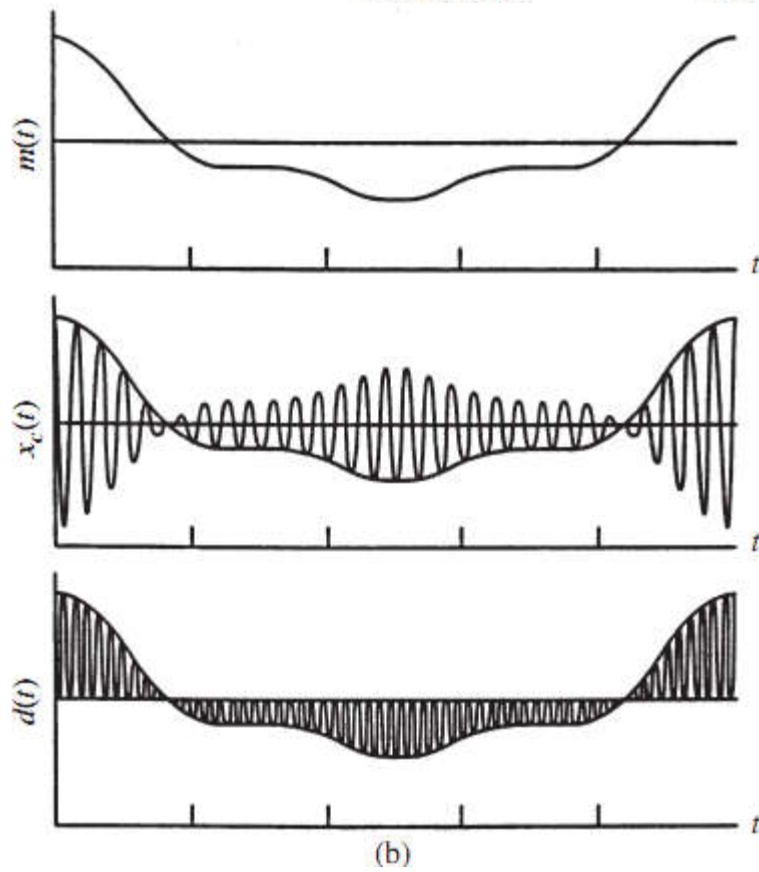
(b)

b) AM spectra

■ Example of DSB Modulator



Double-sideband modulation. (a) System. (b) Example waveforms. (c) Spectra.

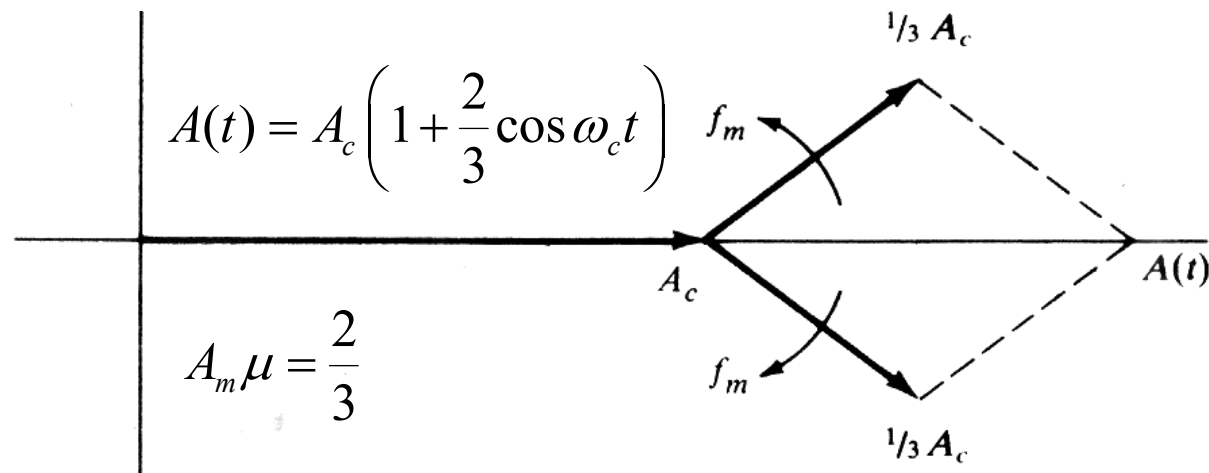


AM phasor analysis, tone modulation

- AM and DSB can be inspected also by trigonometric expansion yielding for instance for AM

$$\begin{aligned} x_c(t) &= A_c A_m \mu \cos(\omega_m t) \cos(\omega_c t) + A_c \cos(\omega_c t) \\ &= \frac{A_c A_m \mu}{2} \cos(\omega_c - \omega_m)t + \frac{A_c A_m \mu}{2} \cos(\omega_c + \omega_m)t \\ &\quad + A_c \cos(\omega_c t) \end{aligned}$$

- This has a nice phasor interpretation; take for instance $\mu=2/3$, $A_m=1$:



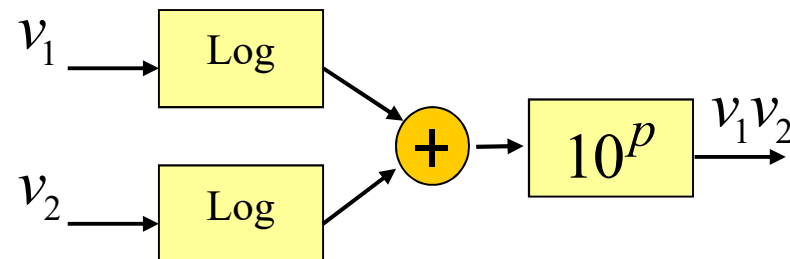
$$\text{AM signal: } x_c(t) = \underbrace{A_c [1 + \mu x_m(t)]}_{A(t)} \cos(\omega_c t)$$

Examples of modulators

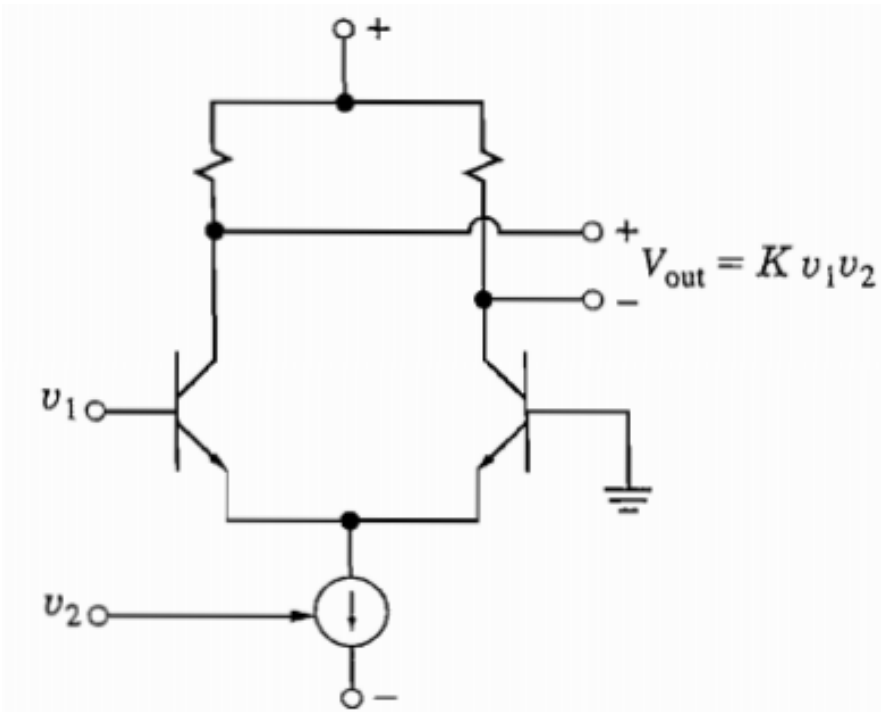
- Both AM and DSB can be generated by
 - Analog or digital multipliers
 - Special nonlinear circuits
 - based on semiconductor junctions (as diodes, FETs etc.)
 - based on analog or digital nonlinear amplifiers as
 - log-antilog amplifiers:

$$p = \log v_1 + \log v_2$$

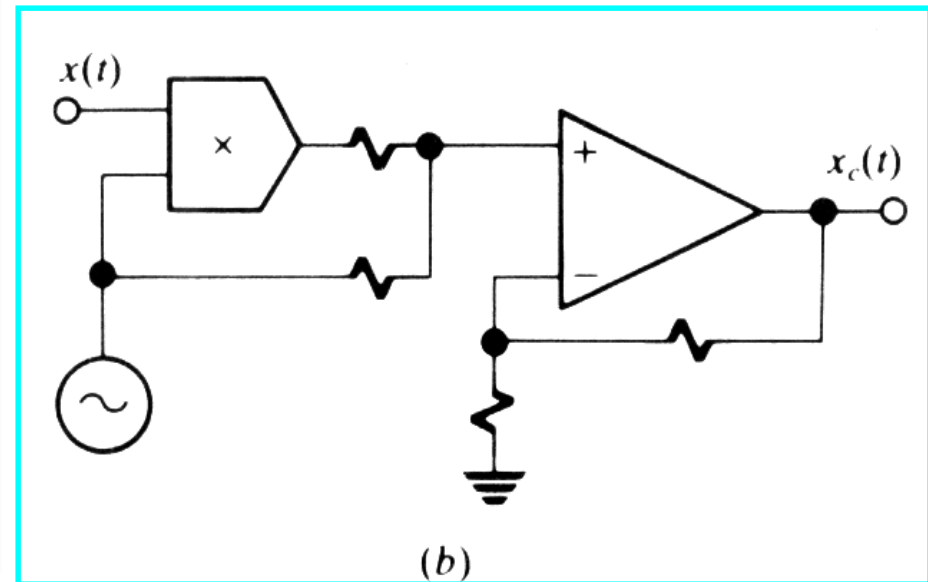
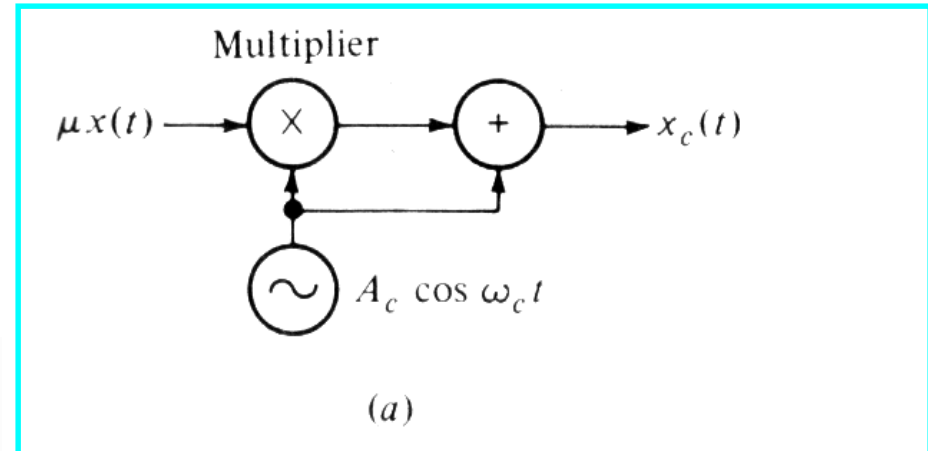
$$10^p = v_1 v_2$$



- (a) Product modulator
(b) respective schematic diagram
=multiplier+adder



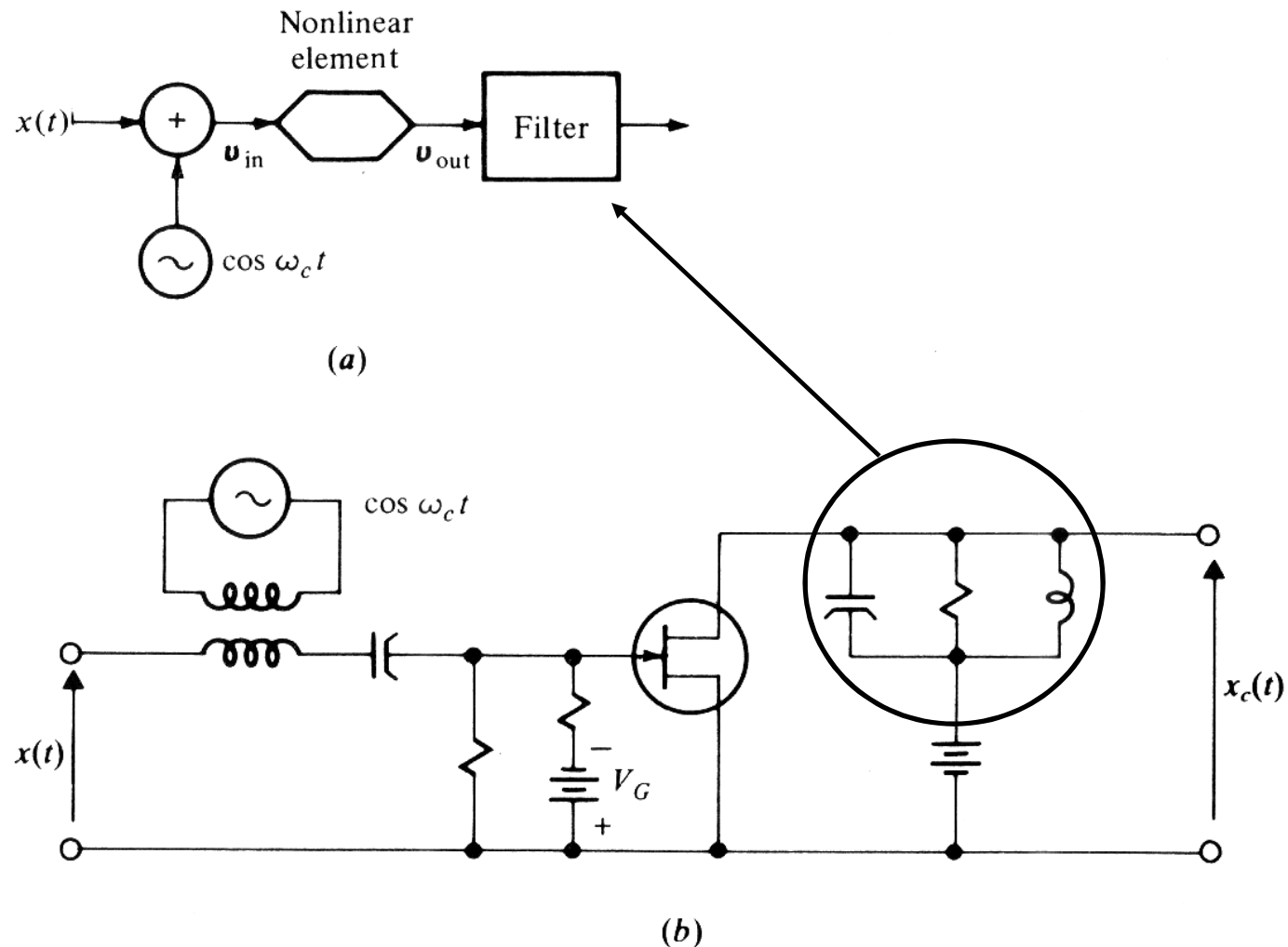
- Circuit for Variable transconductance multiplier



(AM signal: $x_c(t) = A_c[1 + \mu x_m(t)]\cos(\omega_c t)$) 21

Square-law modulator (for AM)

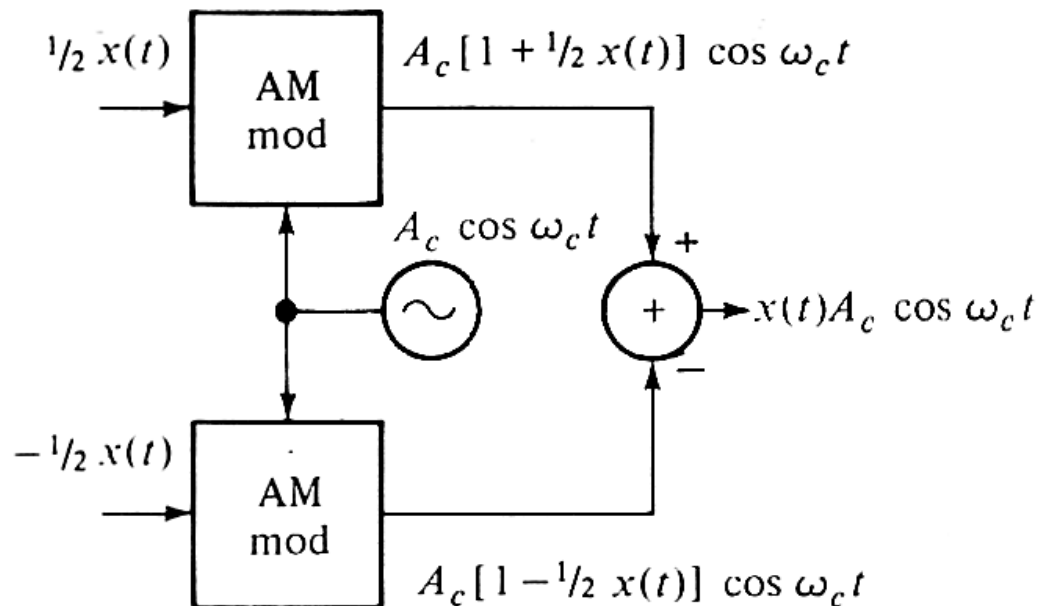
- Square-law modulators are based on nonlinear elements:



(a) functional block diagram, (b) circuit realization

Balanced modulator (for DSB)

- By using balanced configuration non-idealities on square-law characteristics can be compensated resulting a high degree of carrier suppression:



- Note that if the modulating signal has a DC-component, it is not cancelled out and will appear at the carrier frequency of the modulator output

Synchronous detection

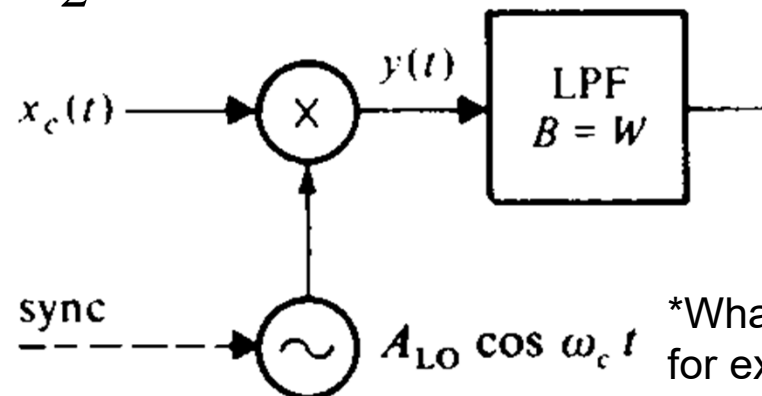
- All **linear modulations** can be detected by synchronous detector
- Regenerated, **in-phase carrier replica** required for signal regeneration that is used to multiple the received signal
- Consider an universal*, linearly modulated signal:

$$x_c(t) = [K_c + K_\mu x(t)] \cos(\omega_c t) + K_\mu x_q(t) \sin(\omega_c t)$$

- The multiplied signal $y(t)$ is:

$$\begin{aligned} x_c(t) A_{LO} \cos(\omega_c t) &= \frac{A_{LO}}{2} \left\{ [K_c + K_\mu x(t)] [1 + \cancel{\cos(2\omega_c t)}] - \cancel{K_\mu x_q(t) \sin(2\omega_c t)} \right\} \\ &= \frac{A_{LO}}{2} [K_c + K_\mu x(t)] \end{aligned}$$

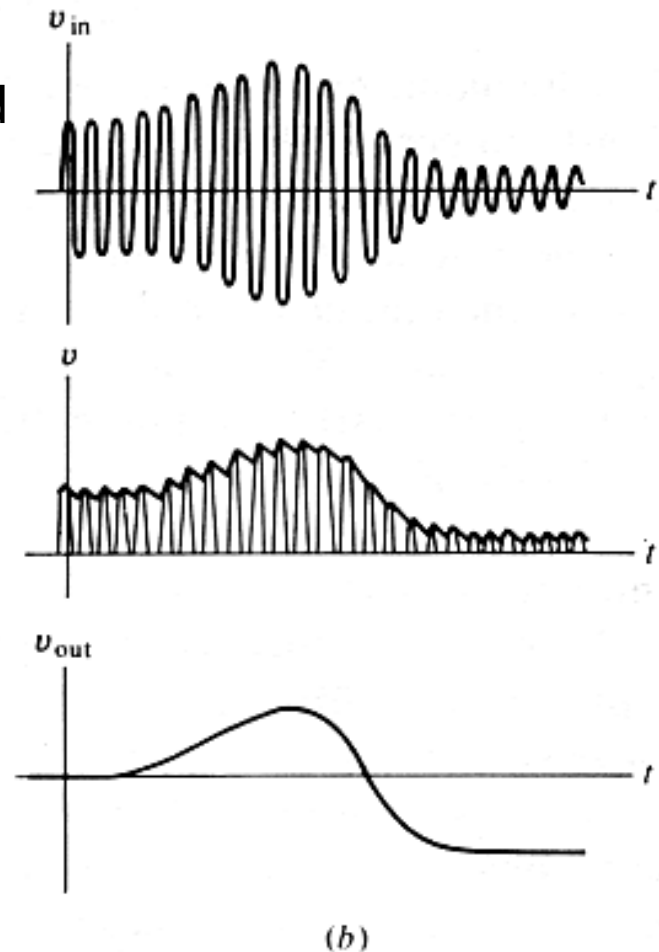
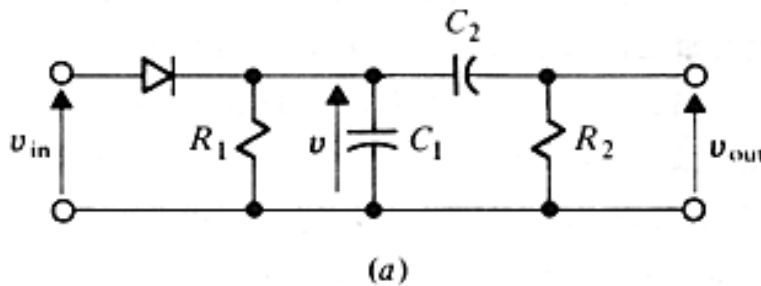
Synchronous
detector



*What are the parameters
for example for AM or DSB?

The envelope detector

- Important motivation for using AM is the possibility to use the envelope detector that
 - has a simple structure (also cheap)
 - needs no synchronization (e.g. no auxiliary, unmodulated carrier input in receiver)
 - no threshold effect (SNR can be very small and receiver still works)



Envelope detector analyzed

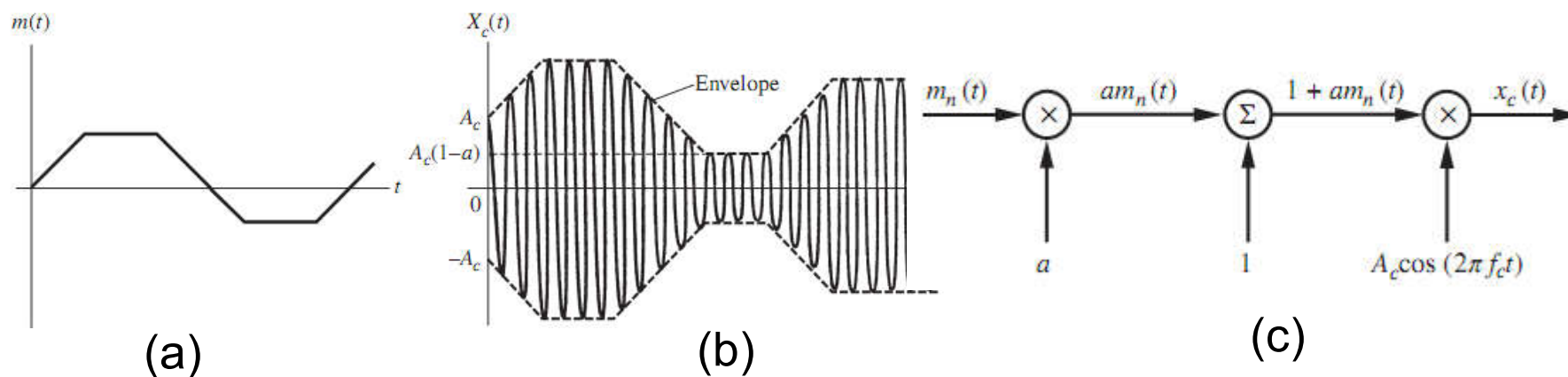
- Assume diode half-wave rectifier used to rectify AM-signal. Therefore after the diode AM modulation is in effect multiplied with the half-wave rectified sinusoidal signal $w(t)$

$$v_R = [A + m(t)] \cos \omega_c t \underbrace{\left[\frac{1}{2} + \frac{2}{\pi} \left(\cos \omega_c t - \frac{1}{3} \cos 3\omega_c t + \dots \right) \right]}_{w(t)}$$
$$v_R = \frac{1}{\pi} [A + m(t)] + \text{other higher order terms}$$

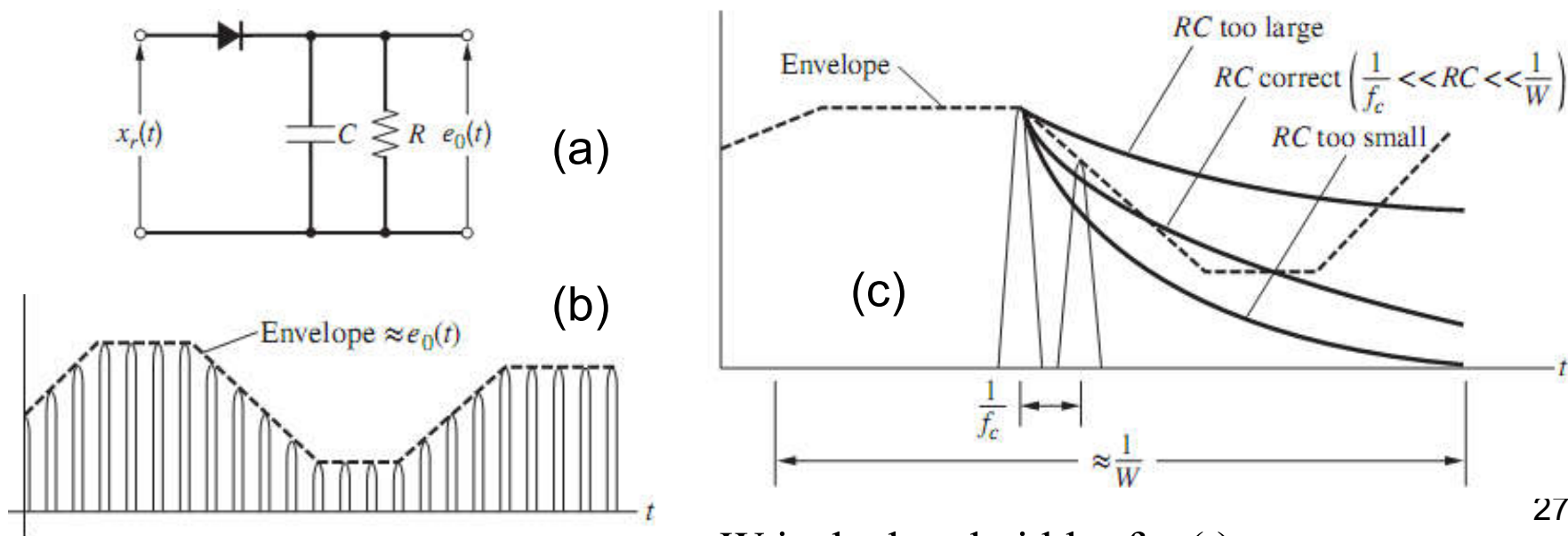
- The diode detector is then followed by a lowpass circuit to remove the higher order terms
- The resulting DC-term may also be blocked by a capacitor
- Note the close resembles of this principle to the synchronous-detector.

$$\cos^2(x) = \frac{1}{2} [1 + \cos(2x)]$$

Amplitude modulation. (a) Message signal. (b) Modulator output for $a < 1$. (c) Modulator

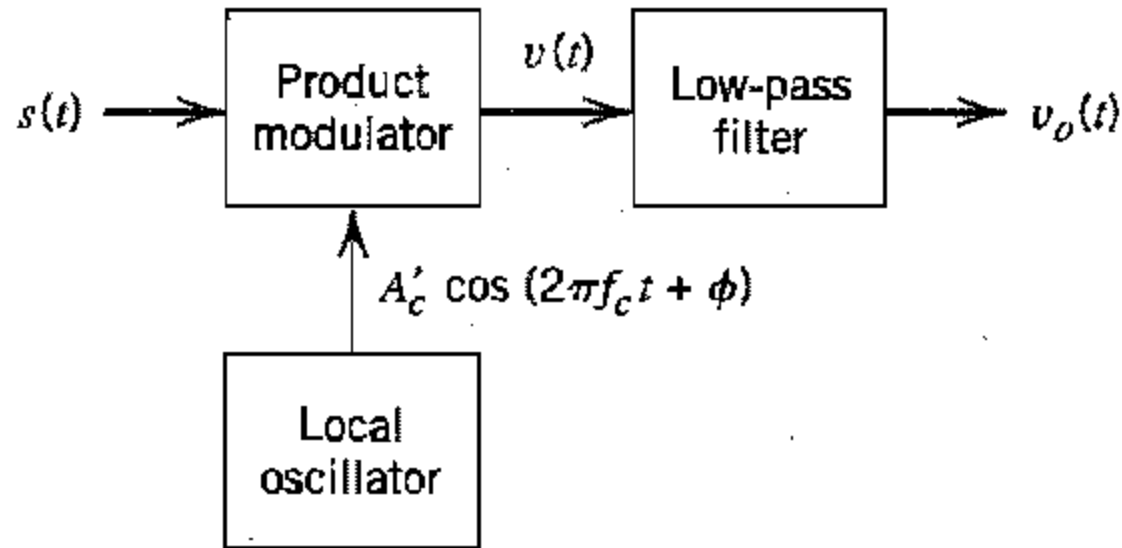


Envelope detection. (a) Circuit. (b) Waveform. (c) Effect of RC time constant.



W is the bandwidth of $m(t)$

■ COHERENT DETECTION FOR DSB SIGNALS

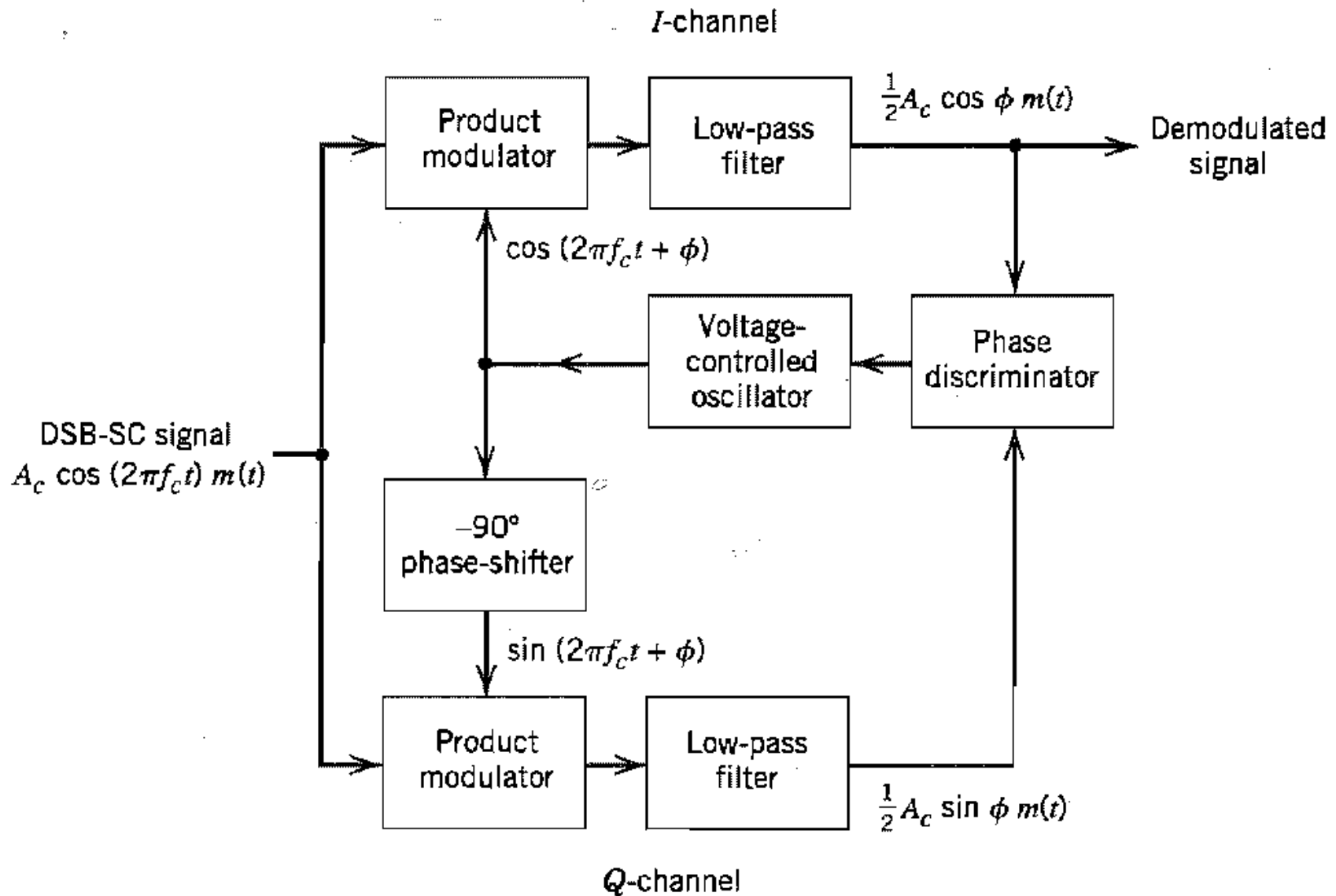


$$\begin{aligned} v(t) &= A'_c \cos(2\pi f_c t + \phi) s(t) \\ &= A_c A'_c \cos(2\pi f_c t) \cos(2\pi f_c t + \phi) m(t) \\ &= \frac{1}{2} A_c A'_c \cos(4\pi f_c t + \phi) m(t) + \frac{1}{2} A_c A'_c \cos \phi m(t) \end{aligned}$$

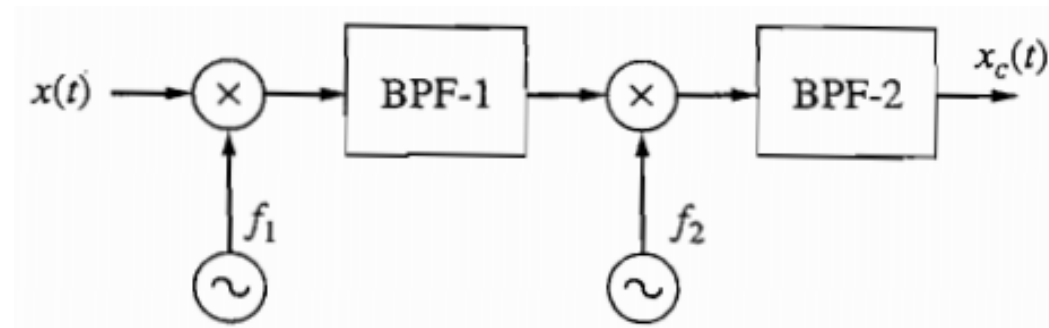
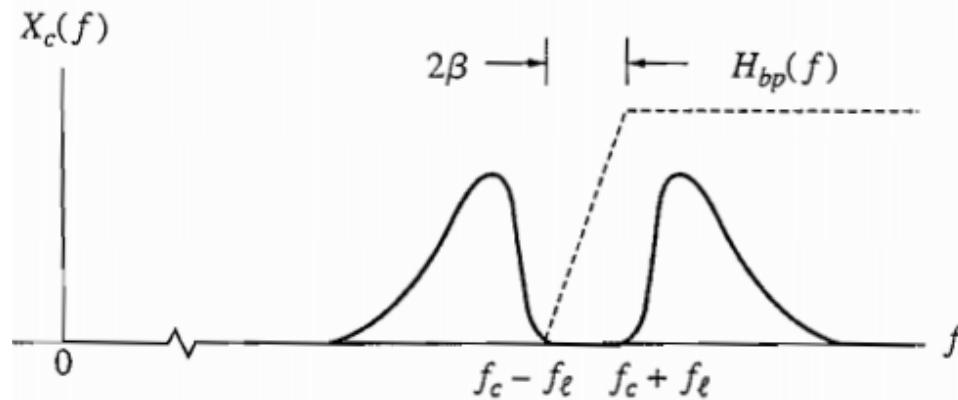
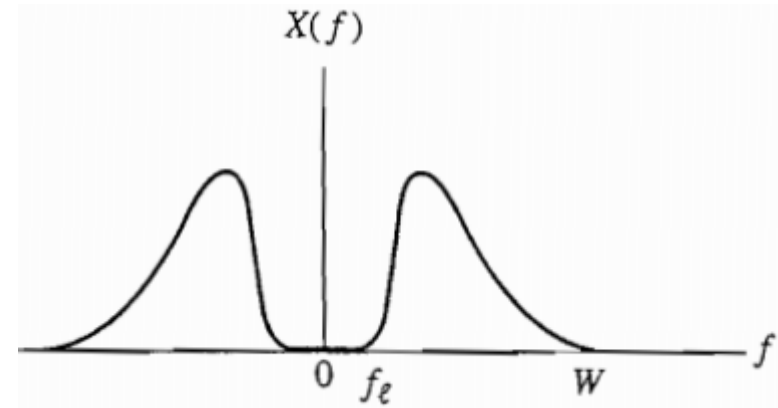
- Pass the signal through a filter we get the output with
- $\cos \phi$ is a constant phase error

$$v_o(t) = \frac{1}{2} A_c A'_c \cos \phi m(t)$$

■ COSTAS RECEIVER FOR DSB SIGNALS

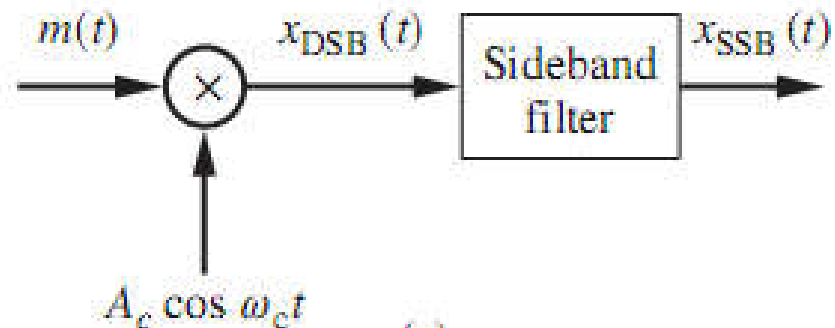


AM Single SideBand (SSB) GENERATION



■SSB Generation

$m(t)$ is the message
and its Fourier Transform $M(f)$



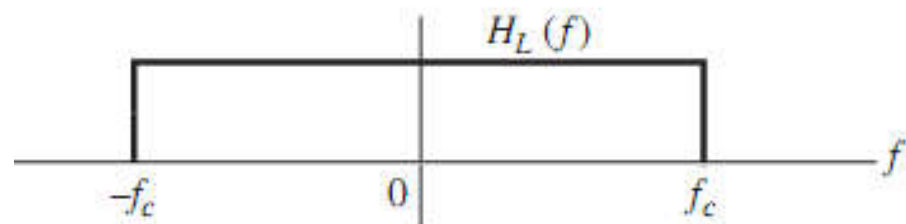
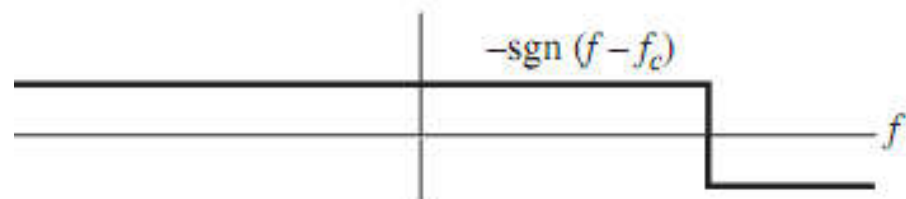
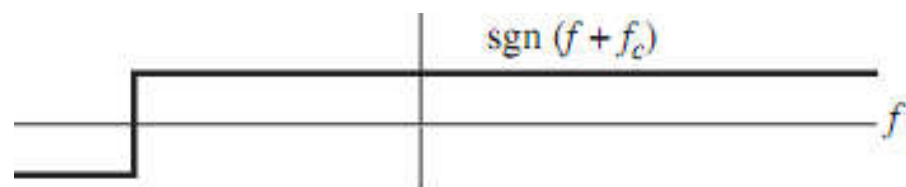
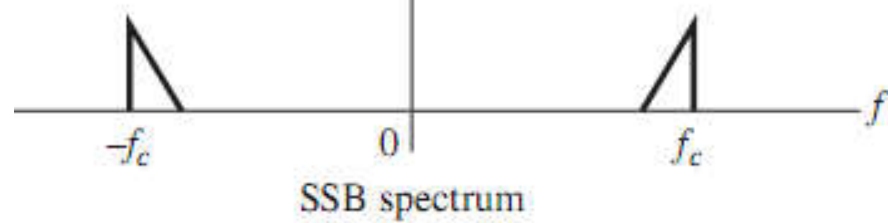
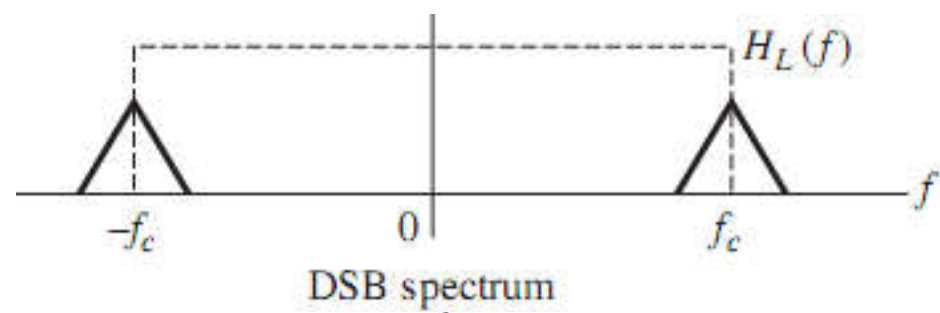
■Response of the LP filter

$$H_L(f) = \frac{1}{2}[\text{sgn}(f + f_c) - \text{sgn}(f - f_c)]$$

$$X_{\text{DSB}}(f) = \frac{1}{2}A_c M(f + f_c) + \frac{1}{2}A_c M(f - f_c)$$

■Lower Sideband signal

$$\begin{aligned}
 X_c(f) &= \frac{1}{4}A_c[M(f + f_c)\text{sgn}(f + f_c) + M(f - f_c)\text{sgn}(f + f_c)] \\
 &\quad - \frac{1}{4}A_c[M(f + f_c)\text{sgn}(f - f_c) + M(f - f_c)\text{sgn}(f - f_c)] \\
 X_c(f) &= \frac{1}{4}A_c[M(f + f_c) + M(f - f_c)] \\
 &\quad + \frac{1}{4}A_c[M(f + f_c)\text{sgn}(f + f_c) - M(f - f_c)\text{sgn}(f - f_c)]
 \end{aligned}$$



■ DSB signal

$$\frac{1}{2}A_c m(t) \cos(2\pi f_c t) \leftrightarrow \frac{1}{4}A_c [M(f + f_c) + M(f - f_c)] \quad (*)$$

■ Hilbert Transform

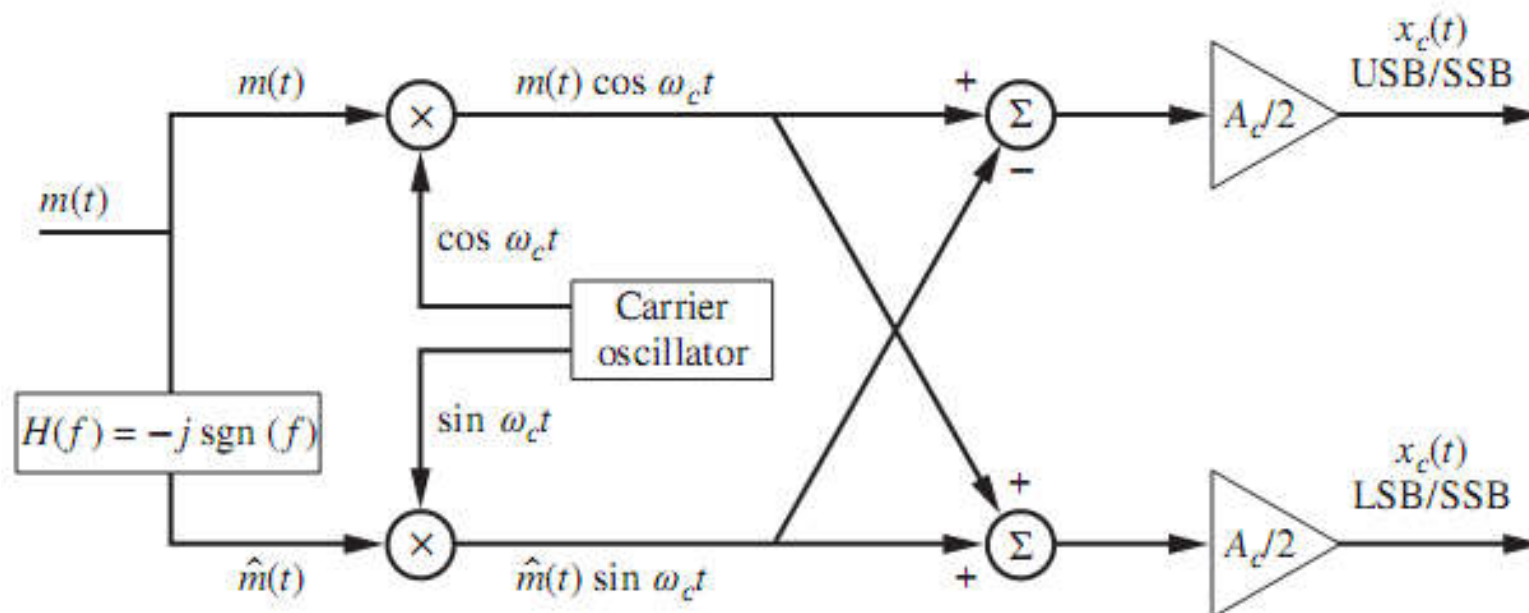
$$\hat{m}(t) \leftrightarrow -j(\text{sgn } f)M(f)$$

$$m(t)e^{\pm j2\pi f_c t} \leftrightarrow M(f \mp f_c)$$

$$\hat{m}(t)e^{\pm j2\pi f_c t} \leftrightarrow -jM(f \mp f_c)\text{sgn}(f \mp f_c)$$

$$\mathfrak{F}^{-1} \left\{ \frac{1}{4}A_c [M(f + f_c)\text{sgn}(f + f_c) - M(f - f_c)\text{sgn}(f - f_c)] \right\} \quad (**)$$

$$= -A_c \frac{1}{4j} \hat{m}(t)e^{-j2\pi f_c t} + A_c \frac{1}{4j} \hat{m}(t)e^{+j2\pi f_c t} = \frac{1}{2}A_c \hat{m}(t) \sin(2\pi f_c t)$$



- Combining (*) and (**), we get the lower-Sideband SSB

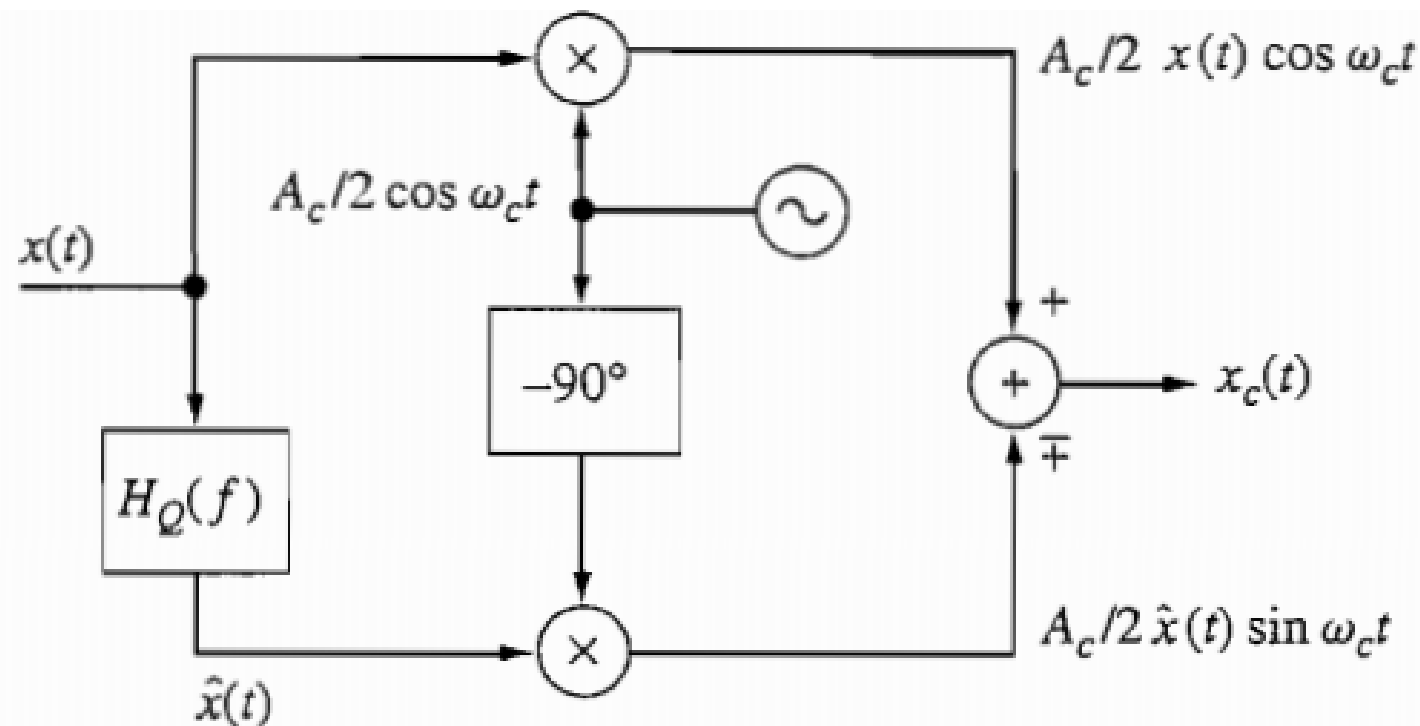
$$x_c(t) = \frac{1}{2} A_c m(t) \cos(2\pi f_c t) + \frac{1}{2} A_c \hat{m}(t) \sin(2\pi f_c t)$$

- Or similar for the Upper-sideband SSB

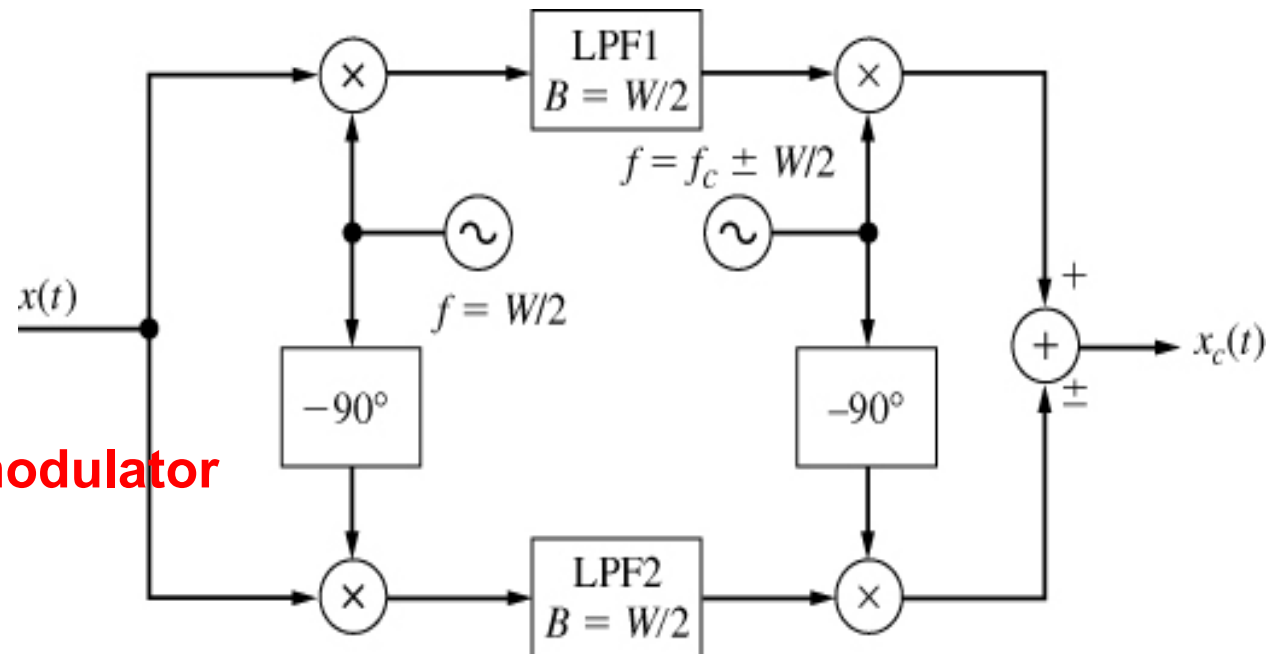
$$x_c(t) = \frac{1}{2} A_c m(t) \cos(2\pi f_c t) - \frac{1}{2} A_c \hat{m}(t) \sin(2\pi f_c t)$$

■ Phase shift method for SSB generation

$$x_c(t) = \frac{A_c}{2} x(t) \cos \omega_c t \pm \frac{A_c}{2} \hat{x}(t) \cos (\omega_c t - 90^\circ)$$

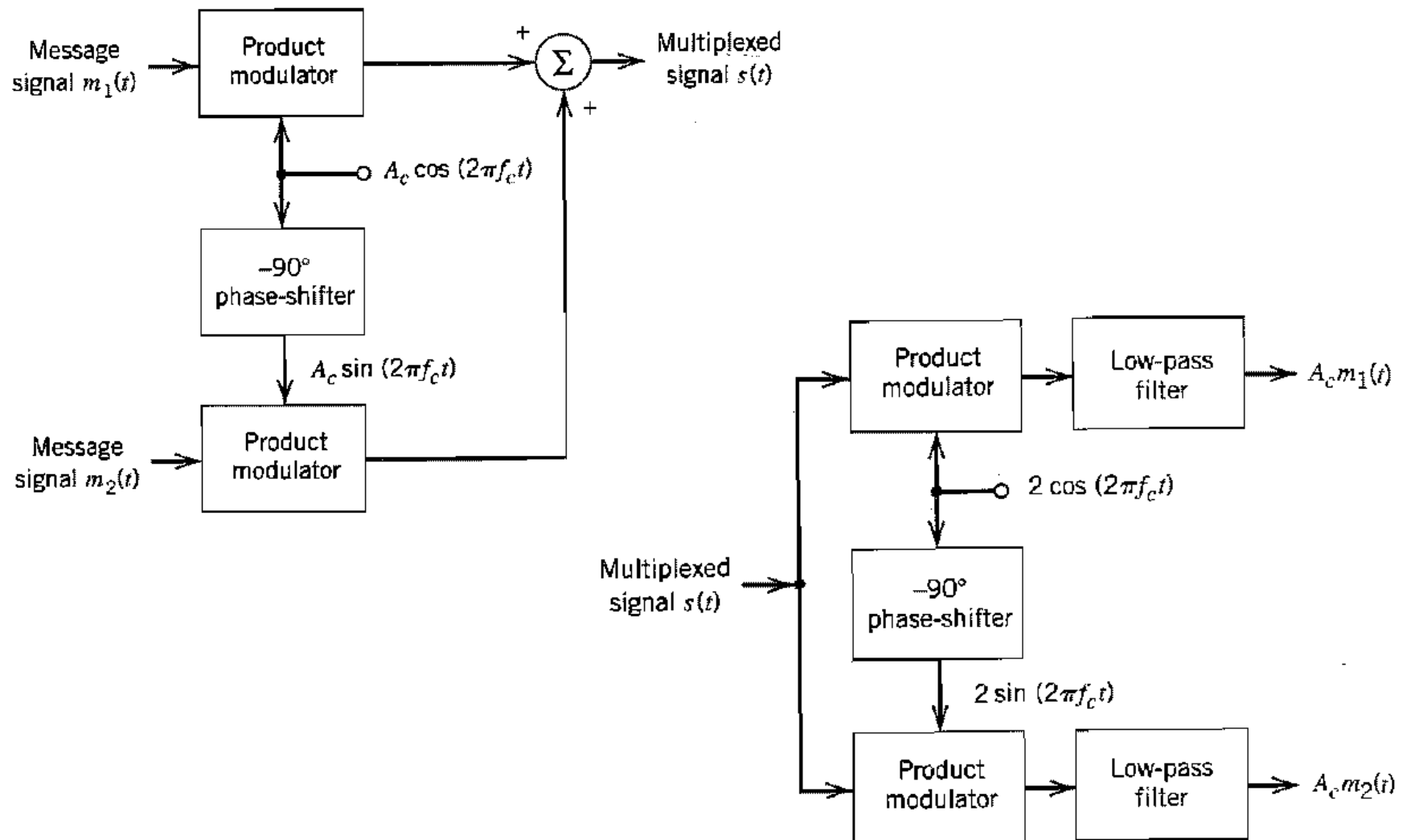


■ Weaver's SSB modulator

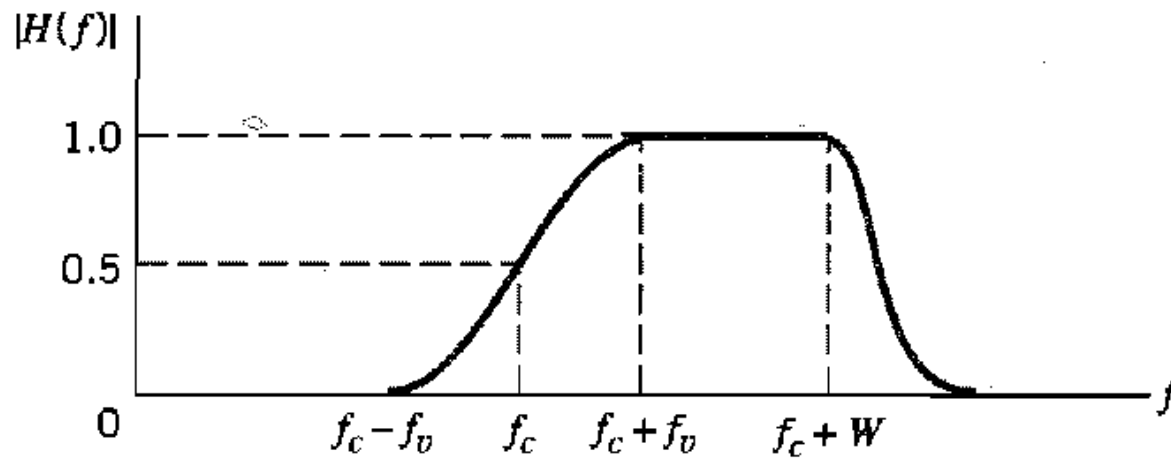
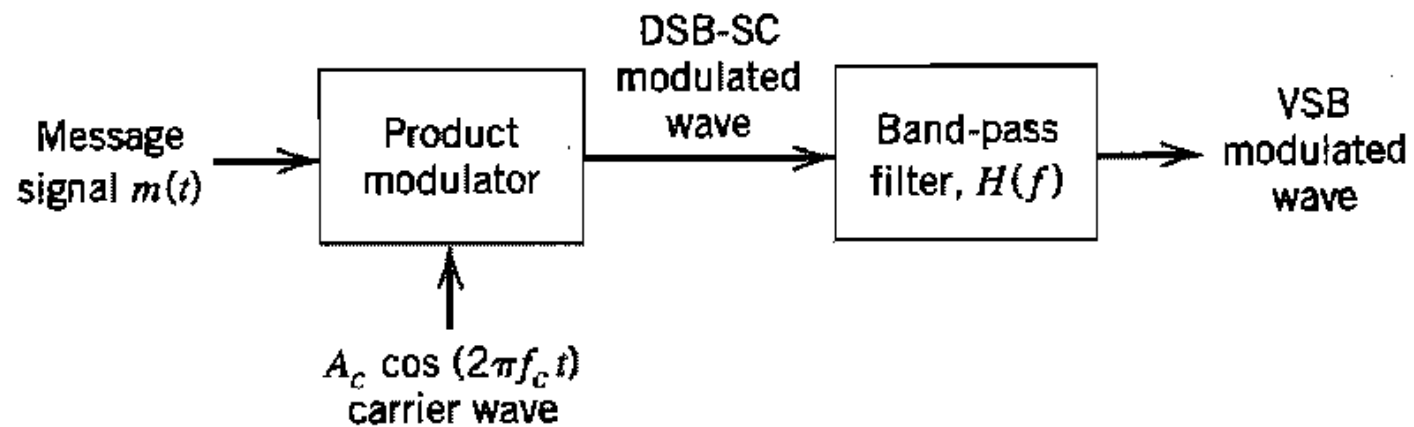


$x_c(t) = v_1 \pm v_2$ where v_1 is the signal from the upper part of the loop and v_2 is from the lower part. Taking these separately, the input to the upper LPF is $\cos 2\pi f_m t \cos 2\pi \frac{W}{2} t$. The output of LPF1 is multiplied by $\cos 2\pi (f_c \pm \frac{W}{2}) t$, resulting in $v_1 = \frac{1}{4} [\cos 2\pi (f_c \pm \frac{W}{2} - \frac{W}{2} + f_m) t + \cos 2\pi (f_c \pm \frac{W}{2} + \frac{W}{2} - f_m) t]$. The input to the lower LPF is $\cos 2\pi f_m t \sin 2\pi \frac{W}{2} t$. The output of LPF2 is multiplied by $\sin 2\pi (f_c \pm \frac{W}{2}) t$, resulting in $v_2 = \frac{1}{4} [\cos 2\pi (f_c \pm \frac{W}{2} - \frac{W}{2} + f_m) t - \cos 2\pi (f_c \pm \frac{W}{2} + \frac{W}{2} - f_m) t]$. Taking the upper signs, $x_c(t) = 2 \times \frac{1}{4} \cos 2\pi (f_c + \frac{W}{2} - \frac{W}{2} + f_m) t = \frac{1}{2} \cos (\omega_c + \omega_m) t$, which corresponds to USSB. Similarly, we achieve LSSB by taking the lower signs, resulting in $x_c(t) = \frac{1}{2} \cos (\omega_c - \omega_m) t$.

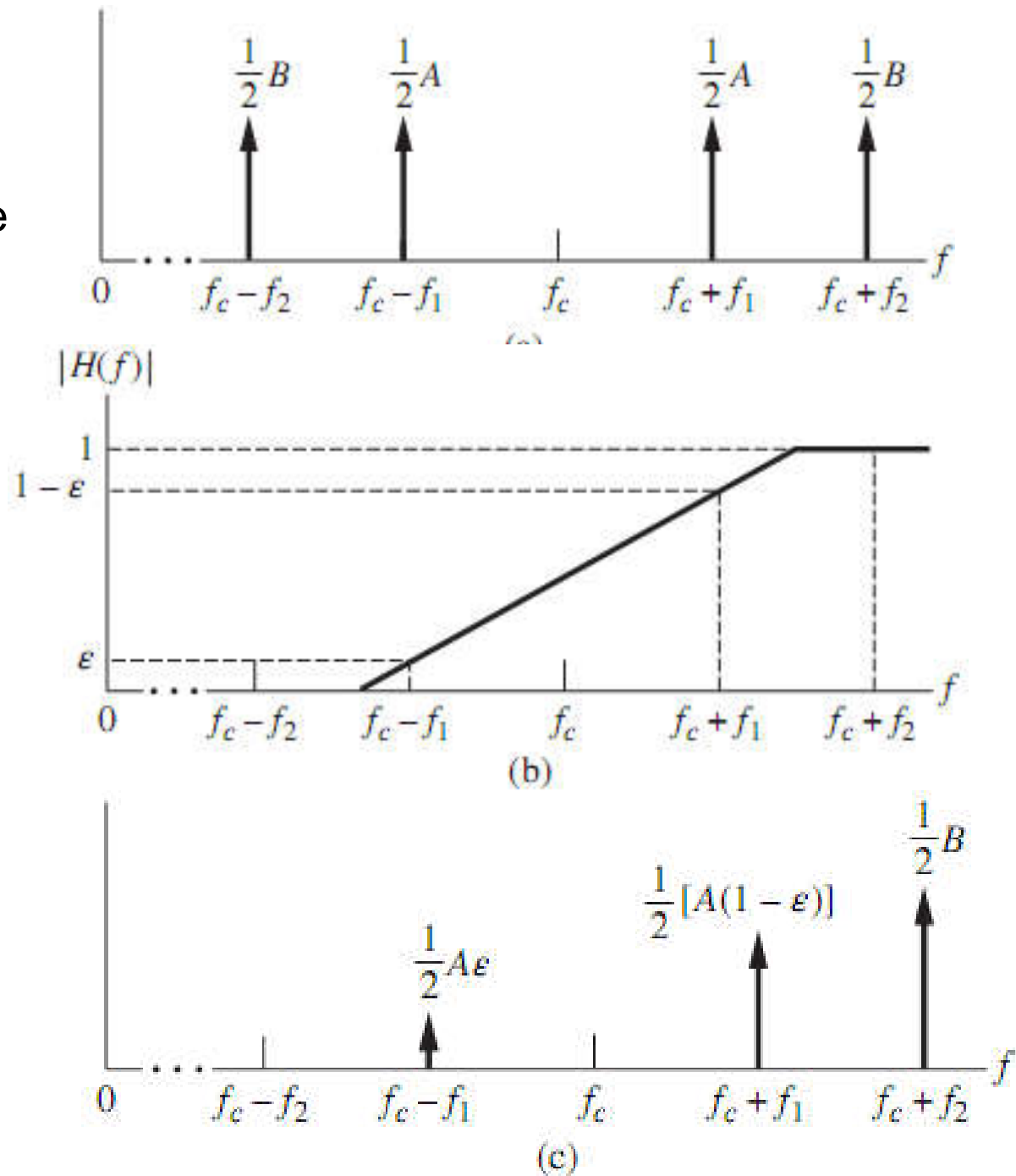
■ Quadrature carrier multiplexing or quadrature amplitude modulation QAM



■ VESTIGIAL SIDEBAND (VSB) MODULATION



- Generation VSB
- a. DSB Magnitude
- b. VSB filter
- c. VSB spectrum



■ Given Modulating Signal $m(t) = A \cos(2\pi f_1 t) + B \cos(2\pi f_2 t)$

■ DSB signal

$$e_{DSB}(t) = \frac{1}{2} A \cos[2\pi(f_c - f_1)t] + \frac{1}{2} A \cos[2\pi(f_c + f_1)t] \\ + \frac{1}{2} B \cos[2\pi(f_c - f_2)t] + \frac{1}{2} B \cos[2\pi(f_c + f_2)t]$$

■ VSB filter response

$$H(f_c - f_2) = 0, \quad H(f_c - f_1) = \epsilon e^{-j\theta_a}$$

$$H(f_c + f_1) = (1 - \epsilon)e^{-j\theta_b}, \quad H(f_c + f_2) = 1e^{-j\theta_c}$$

■ DSB signal

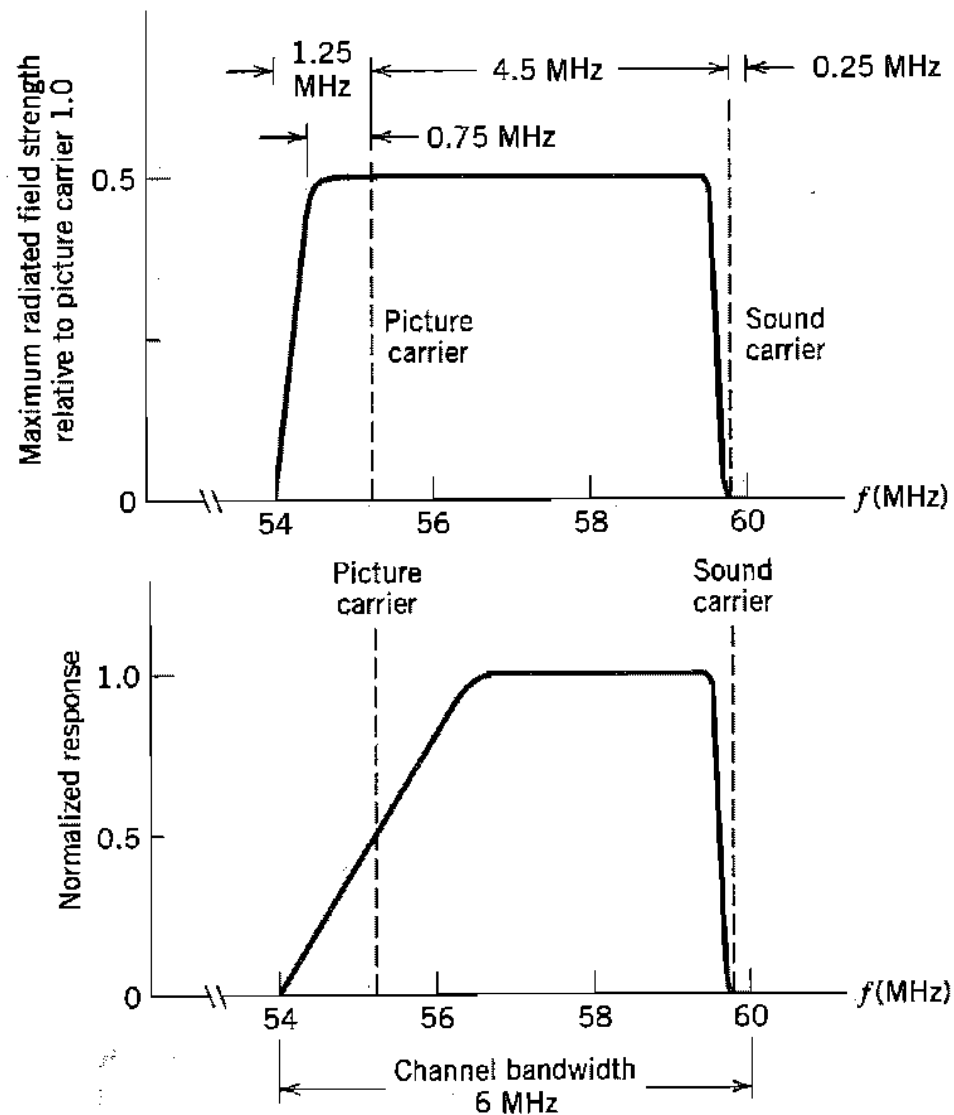
$$x_{DSB}(t) = \text{Re} \left[\left(\frac{A}{2} e^{-j2\pi f_1 t} + \frac{A}{2} e^{j2\pi f_1 t} + \frac{B}{2} e^{-j2\pi f_2 t} + \frac{B}{2} e^{j2\pi f_2 t} \right) e^{j2\pi f_c t} \right]$$

■ VSB signal

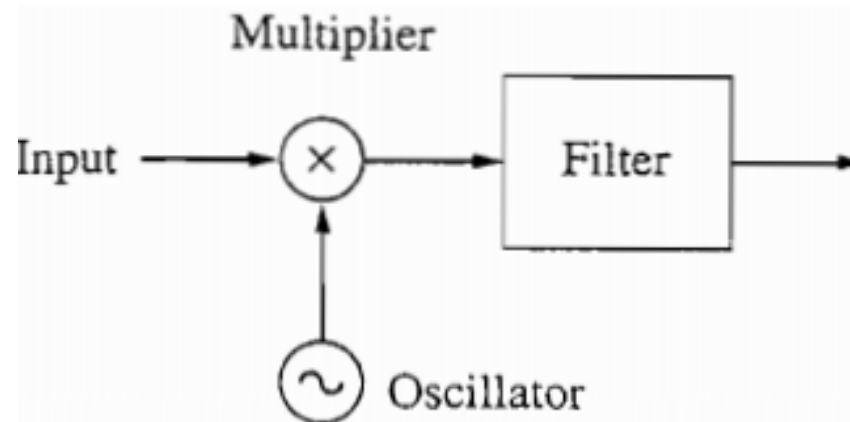
$$x_c(t) = \text{Re} \left\{ \left[\frac{A}{2} \epsilon e^{-j(2\pi f_1 t + \theta_a)} + \frac{A}{2} (1 - \epsilon) e^{j(2\pi f_1 t - \theta_b)} + \frac{B}{2} e^{j(2\pi f_2 t - \theta_c)} \right] e^{j2\pi f_c t} \right\}$$

■ SOME APPLICATIONS OF AMPLITUDE MODULATION

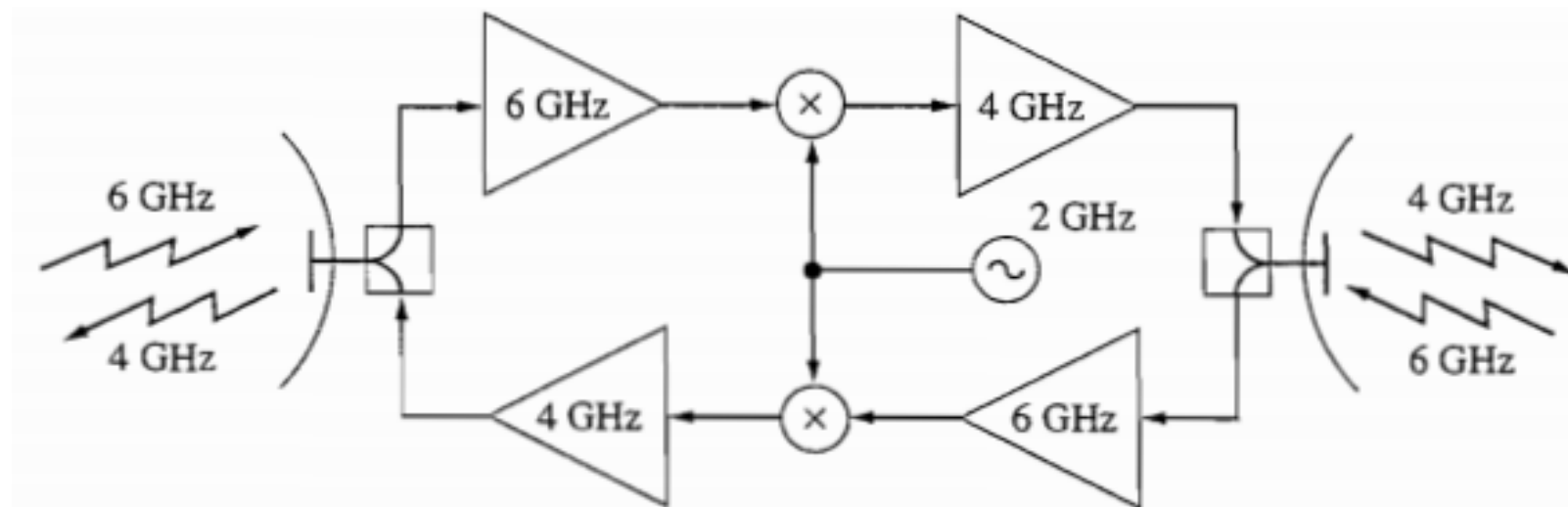
■ TV Signal using VSB modulation



■ Frequency conversion using SSB

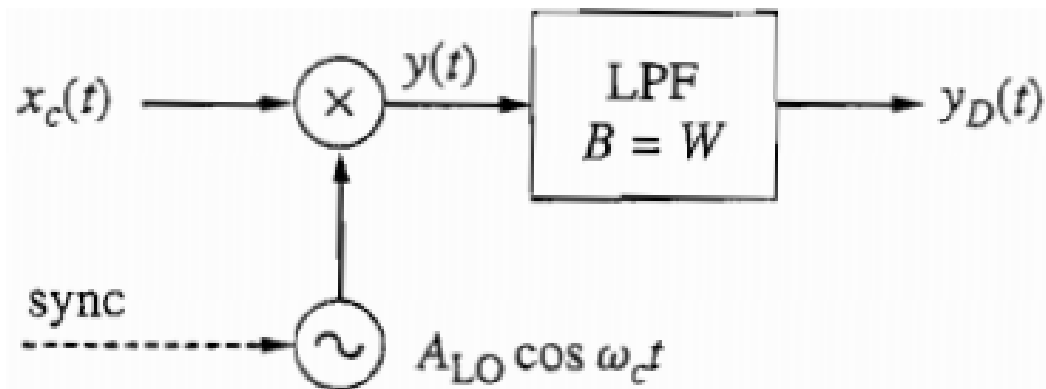


■ Satellite transponder with frequency conversion



■ Synchronous detection

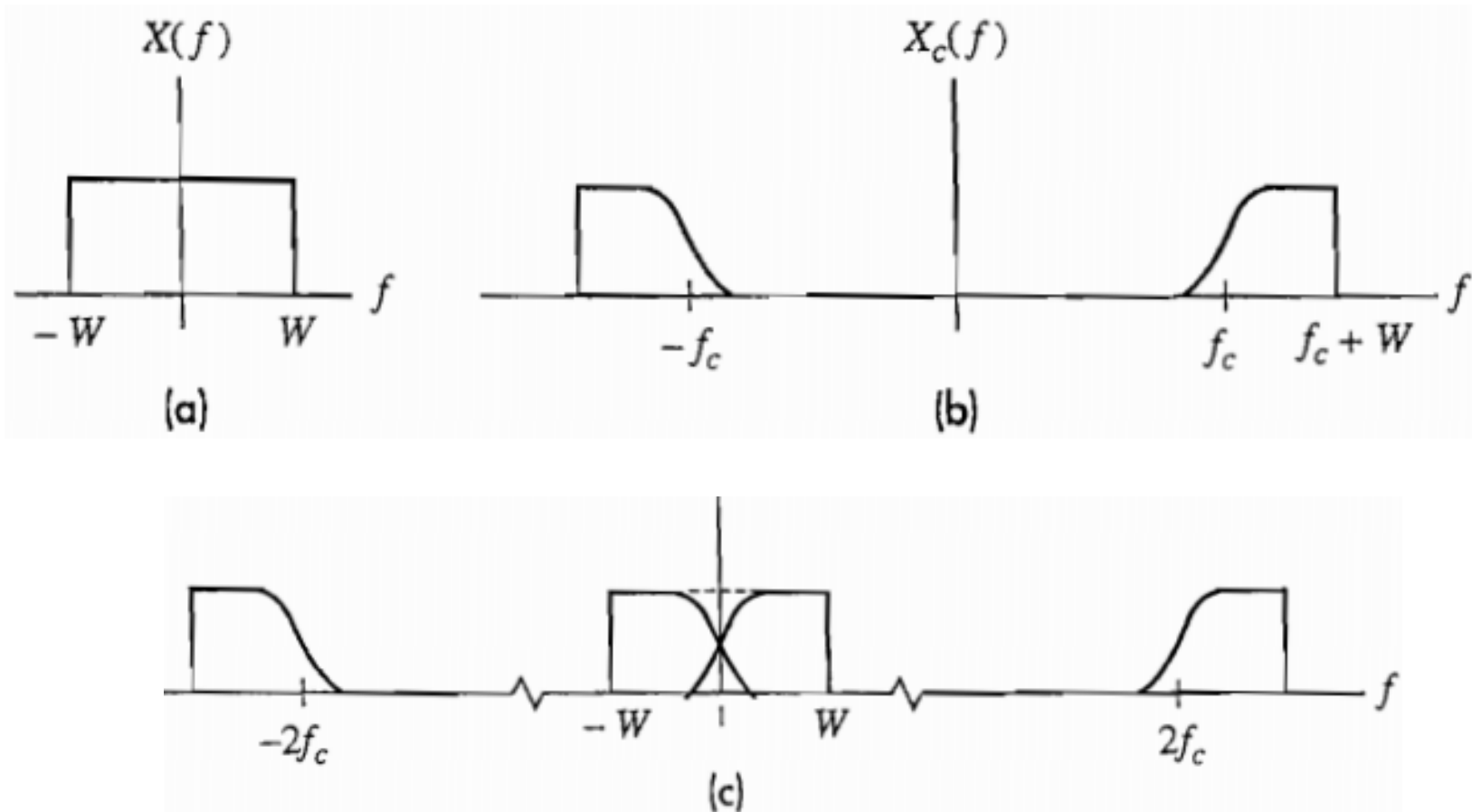
$$x_c(t) = [K_c + K_\mu x(t)] \cos \omega_c t - K_\mu x_q(t) \sin \omega_c t$$



$$x_c(t) A_{LO} \cos \omega_c t$$

$$= \frac{A_{LO}}{2} \{ [K_c + K_\mu x(t)] + [K_c + K_\mu x(t)] \cos 2\omega_c t - K_\mu x_q(t) \sin 2\omega_c t \}$$

$$y_D(t) = K_D [K_c + K_\mu x(t)]$$



- **VSB spectra. a) Message; b) Modulated signal**
- c) Frequency-translated signal before lowpass filtering**