

ALA BLATTNR. **ABGABEDATUM**

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1. **TODO**

2. **TODO**

3. a)

Umformen:

$$f(x) = (x + 1)^{x+2} = e^{\ln(x+1)^{x+2}} = e^{\ln(x+1)(x+2)}$$

Differenzieren:

$$\begin{aligned} f'(x) &= \left(e^{\ln(x+1)(x+2)} \right)' \\ &= e^{\ln(x+1)(x+2)} \cdot ((x+2) \cdot \ln(x+1))' \\ &= e^{\ln(x+1)(x+2)} \cdot \left(x \cdot \ln(x+1) + (x+2) \cdot \frac{1}{(x+1)} \right) \\ &= (x+1)^{x+2} \cdot \left(x \cdot \ln(x+1) + \frac{x+2}{(x+1)} \right) \end{aligned}$$

b) (i)

Umformen:

$$g(x) = (x^2 + 5)^{x^4+3} = e^{\ln(x^2+5)^{x^4+3}} = e^{(x^4+3) \cdot \ln(x^2+5)}$$

Differenzieren:

$$\begin{aligned} g'(x) &= \left(e^{(x^4+3) \cdot \ln(x^2+5)} \right)' \\ &= e^{(x^4+3) \cdot \ln(x^2+5)} \cdot \left((x^4+3) \cdot \ln(x^2+5) \right)' \\ &= e^{(x^4+3) \cdot \ln(x^2+5)} \cdot \left(4x^3 \cdot \ln(x^2+5) + (x^4+3) \cdot \frac{2x}{x^2+5} \right) \\ &= (x^2+5)^{x^4+3} \cdot \left(4x^3 \cdot \ln(x^2+5) + \frac{2x^5+6x}{x^2+5} \right) \end{aligned}$$

(ii)

Umformen:

$$h(x) = (x^4 + 3)^{\sqrt{3x+1}} = e^{\ln(x^4+3)^{\sqrt{3x+1}}} = e^{\sqrt{3x+1} \cdot \ln(x^4+3)}$$

Differenzieren:

$$\begin{aligned} h'(x) &= e^{\sqrt{3x+1} \cdot \ln(x^4+3)} \cdot \left(\sqrt{3x+1} \cdot \ln(x^4+3) \right)' \\ &= e^{\sqrt{3x+1} \cdot \ln(x^4+3)} \cdot \left((\sqrt{3x+1})' \cdot \ln(x^4+3) + \sqrt{3x+1} \cdot \frac{4x^3}{x^4+3} \right) \\ &= (x^4+3)^{\sqrt{3x+1}} \cdot \left((\sqrt{3x+1})' \cdot \ln(x^4+3) + \frac{4x^3 \sqrt{3x+1}}{x^4+3} \right) \end{aligned}$$

c) **TODO****4. TODO****5. TODO****6. TODO**