

# MMS

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1. a)  $f(t) = \sin(t)$

$$\alpha_k = \frac{1}{\pi} \int_{-\pi}^{\pi} (\sin(t) \cos(kt)) dt$$

Für  $k \neq 1$  gilt  $\alpha = 0$ , da sie orthogonal zu einander sind. Für  $k = 1$  sind gilt auch  $\alpha = 0$

$$\begin{aligned} \beta_k &= \frac{1}{\pi} \int_{-\pi}^{\pi} (\sin(t) \sin(kt)) dt \\ &= \frac{1}{\pi} \left( \int_{-\pi}^{\pi} (\cos(t) \cos(kt)) dt - \int_{-\pi}^{\pi} (\cos(t + kt)) dt \right) \\ &= \frac{1}{\pi} \left( \frac{1}{2} \int_{-\pi}^{\pi} (\cos(t - kt)) dt + \frac{1}{2} \int_{-\pi}^{\pi} (\cos(t + kt)) dt - \int_{-\pi}^{\pi} (\cos(t + kt)) dt \right) \\ &= \frac{1}{\pi} \left( \frac{1}{2} \int_{-\pi}^{\pi} (\cos(t - kt)) dt - \frac{1}{2} \int_{-\pi}^{\pi} (\cos(t + kt)) dt \right) \\ &= \int_{-\pi}^{\pi} (\cos(t - kt)) dt = \begin{cases} 0 & k \neq 1 \\ 2\pi & k = 1 \end{cases} \\ &= \int_{-\pi}^{\pi} (\cos(t - kt)) dt = 0 \\ \beta_1 &= \frac{1}{\pi} \cdot \frac{1}{2} \cdot 2\pi = 1 \\ \beta_k &= 0 \text{ für } k > 1 \end{aligned}$$