

Systems

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1 Properties

1.1 Linearity

$$f(ax + by) = af(x) + bf(y) \quad (1)$$

1.2 Time-Invariance

System is not directly dependent on time:

$$y(t) = F(x(t), t) = F(x(t)) \quad (2)$$

This also means that any shift to time in input translates to the same shift in the output.

$$x(t + \delta) \xrightarrow{F} y(t + \delta) \quad (3)$$

2 Convolution

$$(f * g)(t) = \int_{-\infty}^{\infty} f(\tau)g(t - \tau) d\tau \quad (4)$$

Properties:

- Commutative