Department of Electrical and Computer Engineering

University of Victoria

ELEC 300 - Linear Circuits II

Laboratory Report

Experiment No.:	3
Title:	Time Domain Responses
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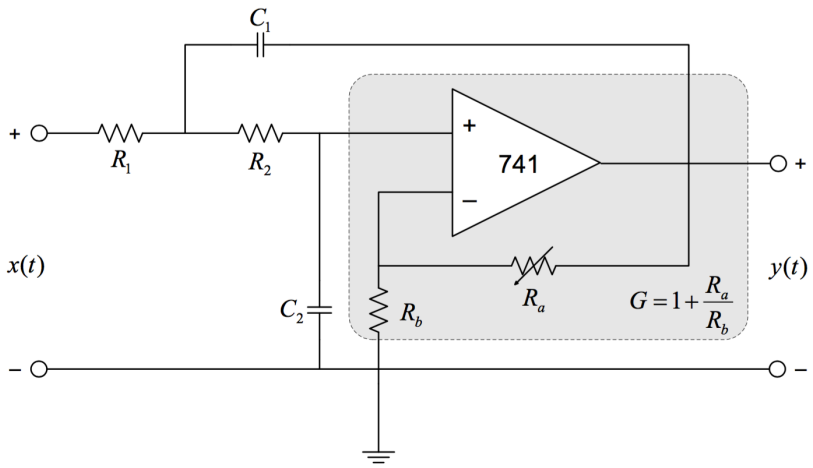
1 Objective

This lab will create an active realization of a second order system. The output of the circuit will be used to verify the system parameters.

2 Introduction

Inductors in second order systems can be replaced by amplifiers and capacitors. Fig. 1 shows an active second order system with a gain of $G = 1 + \frac{R_a}{R_b}$.



$C_1 = C_2 = 16\,\text{nF} = C, \quad R_1 = R_2 = 10\,\text{k}\Omega = R, \quad R_b = 39\,\text{k}\Omega, \quad R_a = 78(1-\zeta)\,\text{k}\Omega$

Figure 1: Active realization of a second order system

The transfer function of this system is:

$$H(s) = \frac{G\omega_0^2}{s^2 + 2\zeta\omega_0 s + \omega_0^2} \tag{1}$$

where

$$\omega_0 = \frac{1}{RC} \tag{2}$$

and

$$\zeta = 1 - \frac{R_a}{2R_b}. \tag{3}$$

When the unit step function is applied to Fig. 1 it will produce an output similar to Fig. 2.

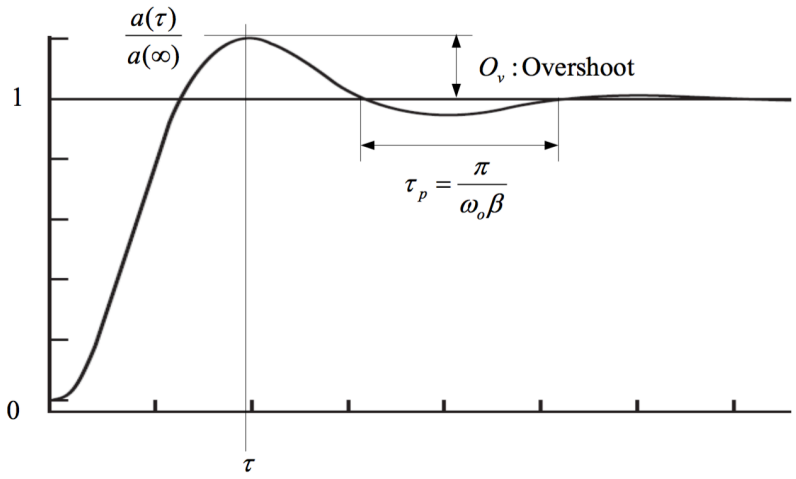


Figure 2: Step response of second order system

The system parameters ζ and ω_0 can be obtained from this graph since:

$$O_v = \exp\left(\frac{-\zeta\pi}{\beta}\right) \tag{4}$$

$$T_p = \frac{\pi}{\omega_0 \beta}. \tag{5}$$

3 Results and Discussion

Fig. 1 was realized with damping factor $\zeta = 0.1$. Using (3), $R_a = 70.2\,\mathrm{k\Omega}$. The opamp supply power was set at $\pm 15\,\mathrm{V}$. An input signal of 1 V_{pp} at 50 Hz square wave was applied to the circuit. One pulse of the square wave will behave locally like a unit step function.

The output of this circuit is shown in Fig. 3. The large overshoot corresponds to significant underdamping, which is consistent with $\zeta = 0.1$.

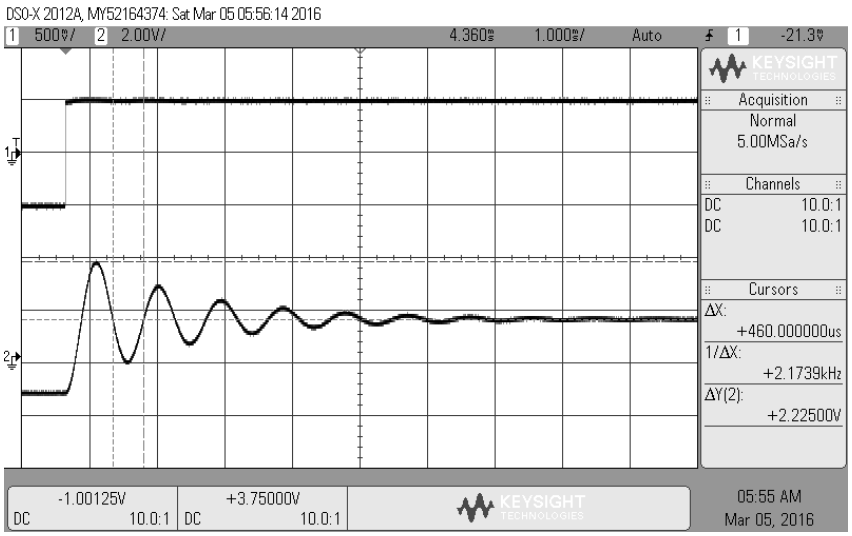


Figure 3: Measured response of second order system

The measured values are $O_v = 2.225\,\mathrm{V}$ and $T_p = 460\,\mu\mathrm{s}$. As the transient response is damped, the value of the output settles to $2.8\,\mathrm{V}$. This is consistent with $G = 1.8$.

4 Conclusion

We realized a second-order voltage amplifier, and found the response of the system using a unit-step input. Our results confirmed our calculated values of ζ and ω, and resembled the general response of a second order system.