

UNIVERSITY OF VICTORIA

ELEC 340

APPLIED ELECTROMAGNETICS AND PHOTONICS

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## Lab 4 - Oblique Incidence and Waveguides

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# 1 Objective

Purpose of the lab.

# 2 Introduction

Short section on the background and motivation i.e. what the experiment is about and what is being measured [1].

# 3 Procedure

Overview of lab sequence.

# 4 Discussion

## 4.1 Snell's Law

**Task 4** *Compare the angles of incidence, reflection and transmission in an  $\text{air} \rightarrow \epsilon_r = 2$  and  $\epsilon_r = 2 \rightarrow \text{air}$  interface.*

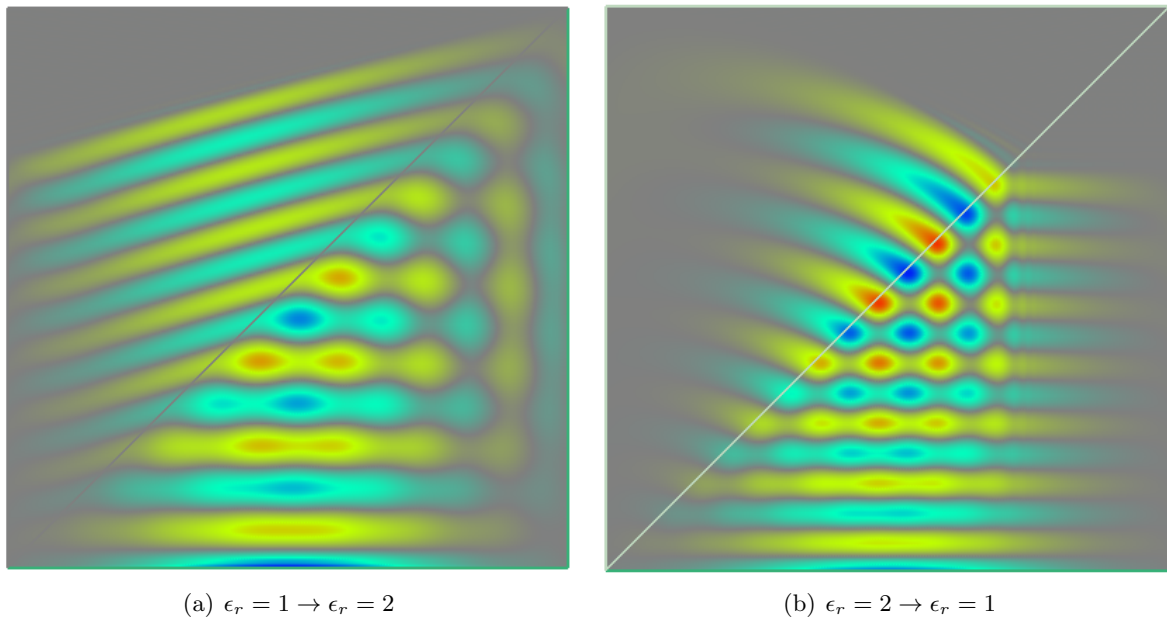


Figure 1: Behavior at 45° incidence

Compute the angles of reflection and transmission

**Task 6** Compare the images for  $\epsilon_r = 2.0, 2.5, 3.0$  in the ABC-bounded region.

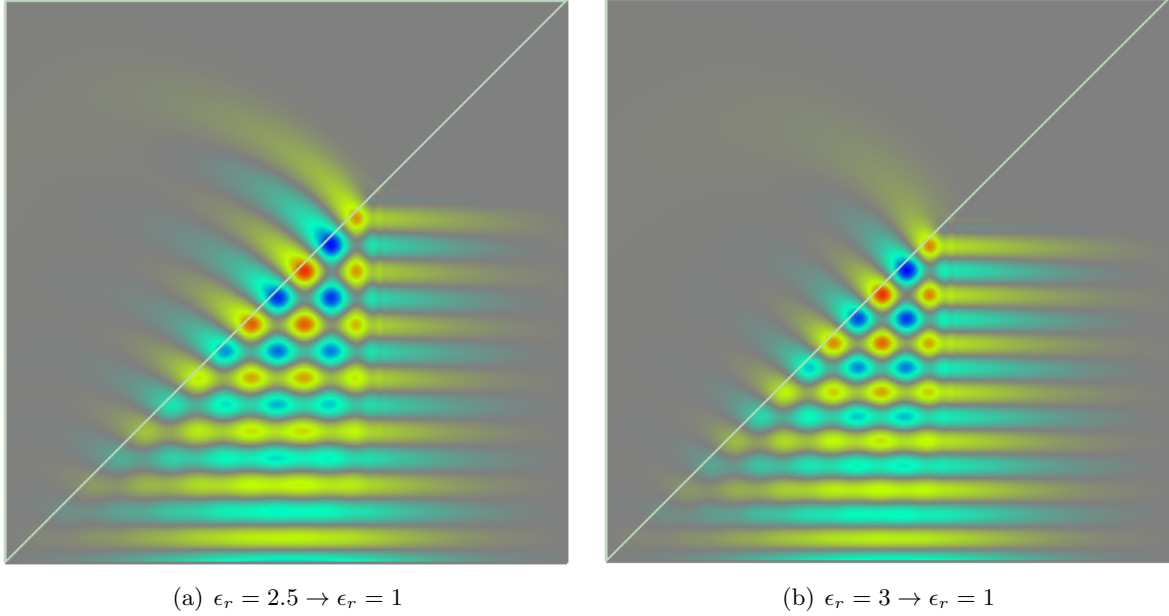


Figure 2: Behavior at  $45^\circ$  incidence

Compute the TIR angles for the 2, 2.5, 3 to 1 interface.

Why does the “spray” into the second medium decrease as  $\epsilon_r$  increases?

**Task 8** Capture an animation of  $\mathbf{H}$  with pointer mode and comment on it.

As  $\mathbf{E}$  is reflected by the boundary it creates a standing wave, perpendicular to the plane of Fig. 3. As per Ampere’s Law,  $\mathbf{H}$  curls around the perpendicular  $\mathbf{E}$  field, creating the “pools” in the image.

Fig. 4 shows that  $\mathbf{H}$  is not altered by the boundary. Since  $\mathbf{E}$  was reflected by the boundary,  $\mathbf{H}$  dissipates because it is not able to generate itself in isolation.

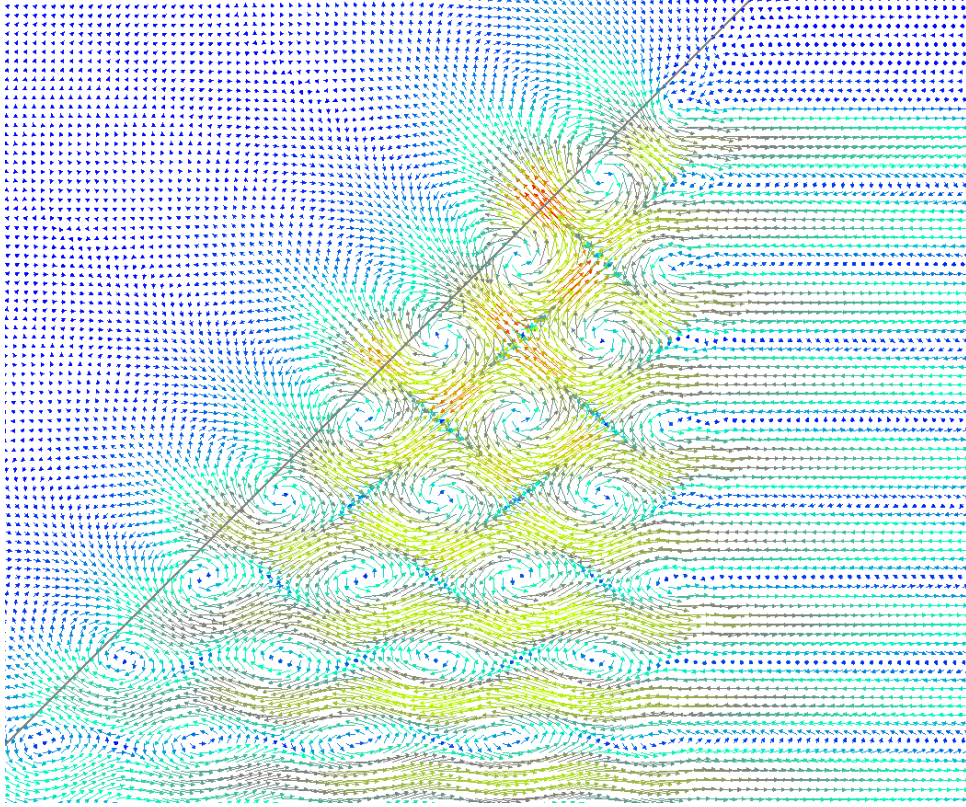


Figure 3:  $\mathbf{H}$  for  $\epsilon_r = 3 \rightarrow \epsilon_r = 1$

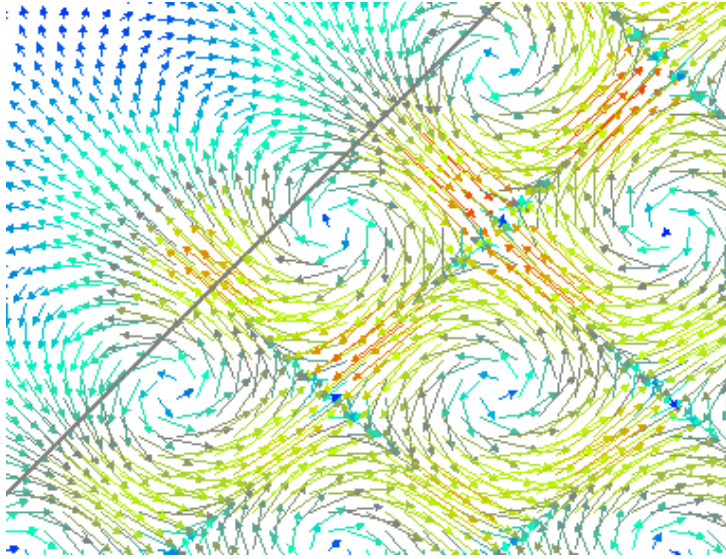


Figure 4: Inset view of Fig. 3

## 4.2 Brewster angle

**Task 9** *Design a Brewster angle interface for zero reflection transmission of a plane wave from air to a dielectric with  $\epsilon_r = 4$ . The Brewster angle for this interface is:*

$$\tan \theta_B = \sqrt{\frac{\epsilon_2}{\epsilon_1}} \implies \theta_B = \tan^{-1}(2) = 63.435^\circ$$

The second medium is designed with a base of 200 mm and height of 400 mm to ensure an incidence angle of  $\theta_B$ . This is shown in Fig. 5.

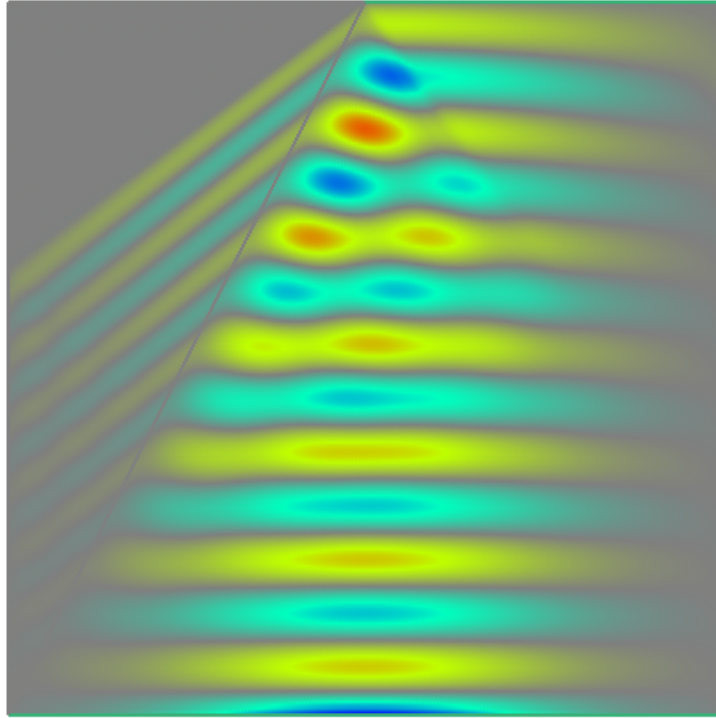


Figure 5: A Brewster angle interface

## 4.3 Rectangular waveguides and cavities

**Task 16** *Obtain the resonant frequencies of the constructed waveguide and compare it to the calculated values.*

Fig. 6 shows the response generated by the impulse function.

For  $TE_{11}$ , the cutoff frequency is:

$$f_c = \frac{u_{p0}}{2} \sqrt{\left(\frac{m}{a}\right)^2 + \left(\frac{n}{b}\right)^2} = \frac{c_0}{2} \sqrt{\left(\frac{1}{30 \text{ mm}}\right)^2 + \left(\frac{1}{20 \text{ mm}}\right)^2} = 9.007 \text{ GHz}$$

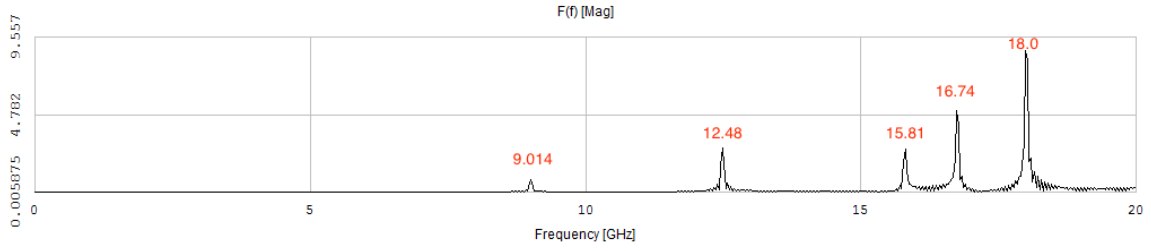


Figure 6: Frequency response of waveguide

verify calculation

This corresponds with the first peak of Fig. 6.

#### 4.4 Rectangular waveguide modes

**Task 20** Compare the propagation in a waveguide with  $TE_{10}$  and  $TE_{30}$ .

$TE_{30}$  has  $f_c \approx 4.5$  GHz. Any frequency above this value will propagate through the waveguide, but significantly higher frequencies will generate the best graphics. Fig. 7 was generated with a source at 50 GHz

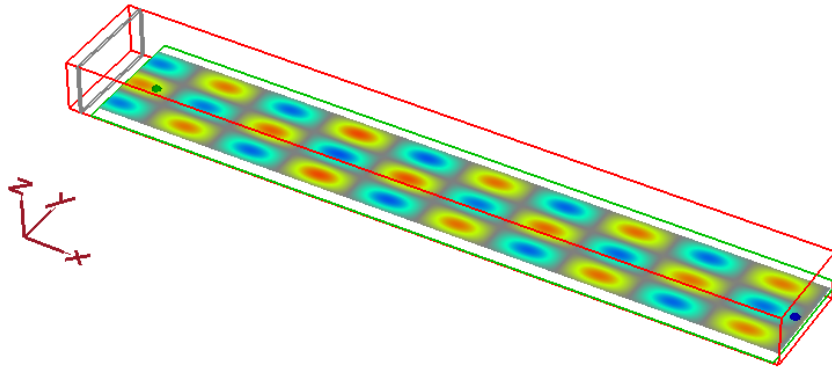


Figure 7: Transmission in a  $TE_{30}$  waveguide

## 5 Conclusion

Summarize the entire report and note any unresolved issues. This section will usually repeat the abstract.

## References

- [1] P. P. M. So, *Laboratory Manual for ELEC340 - Applied Electromagnetics and Photonics*, University of Victoria, 2016.