

$$\frac{\partial}{\partial b} MSE = \frac{\partial}{\partial b} \sum_{i=1}^N (y_i - a + wx_i)^2$$

$$= \frac{\partial}{\partial b} \sum_{i=1}^N (w^2 x_i^2) + 2w(b+y)x_i + (b+y)^2$$

$$= \sum_{i=1}^N 2wx_i + 2b.$$

$$b_0 : 0 = \sum_{i=1}^N 2wx_i + 2b_0 = 2 \sum_{i=1}^N wx_i + 2 \sum_{i=1}^N b_0$$

$$\cancel{b_0} = - \sum_{i=1}^N wx_i$$
