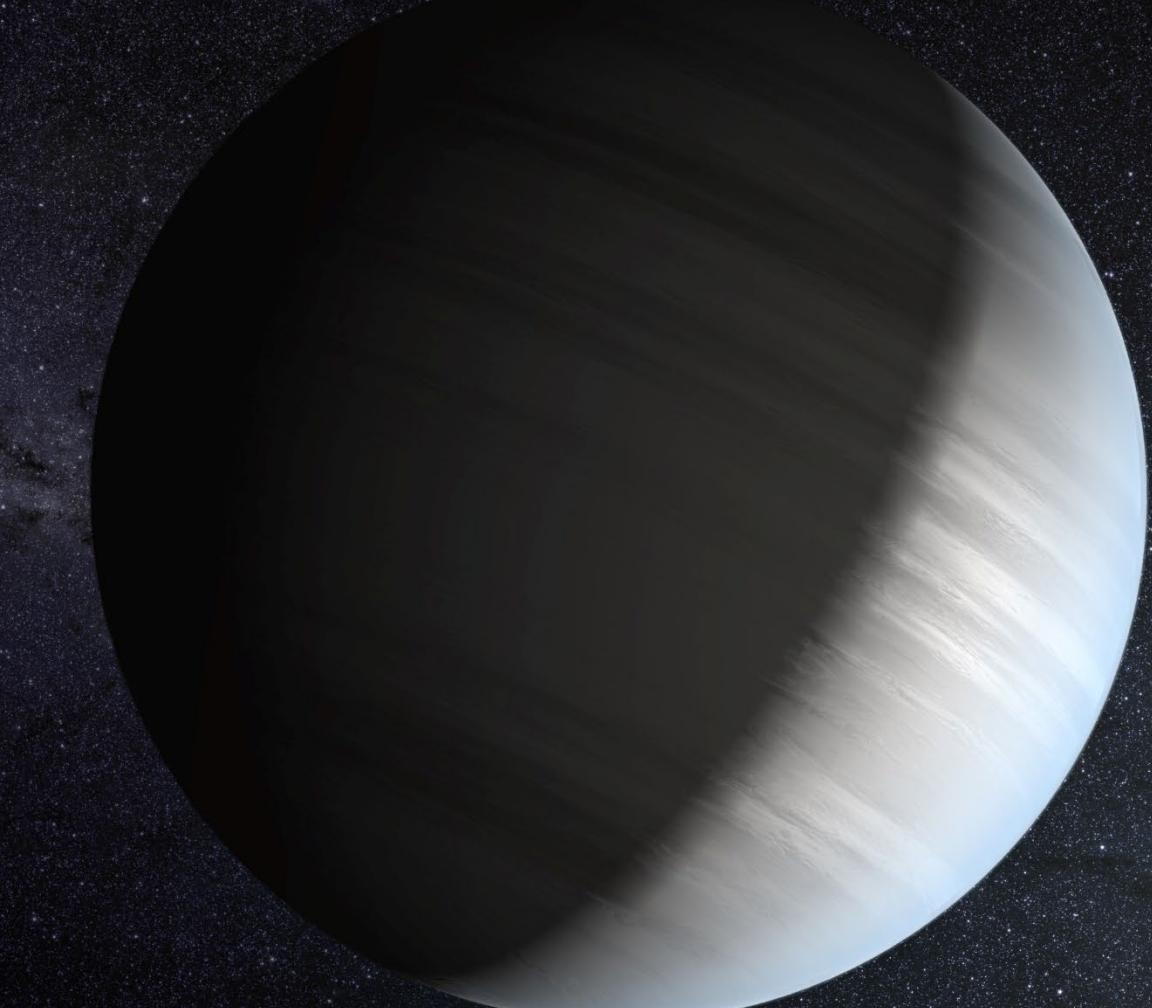


Searching for Habitable Planets

We are going to begin in other solar systems and develop a sense of the range of possible planet types, then return to our own solar system to examine individual planets up close.



We refer to planets orbiting stars other than the Sun as extrasolar planets or **exoplanets**.

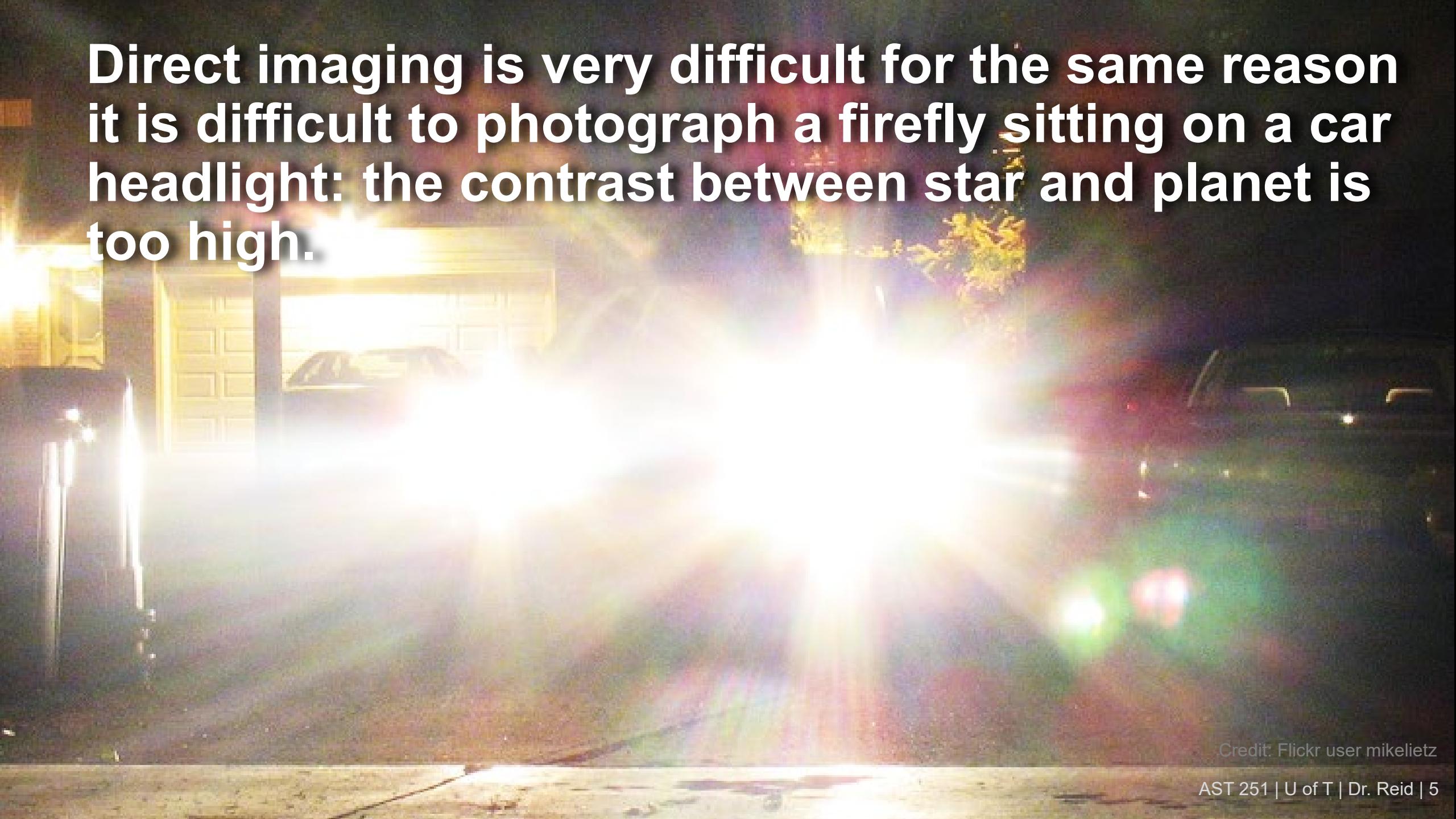


Credit: NASA Ames/JPL-Caltech/T. Pyle

The most obvious way to find an exoplanet is simply to photograph another star and examine the image for orbiting planets.

This technique is known as direct imaging.

Direct imaging is very difficult for the same reason it is difficult to photograph a firefly sitting on a car headlight: the contrast between star and planet is too high.



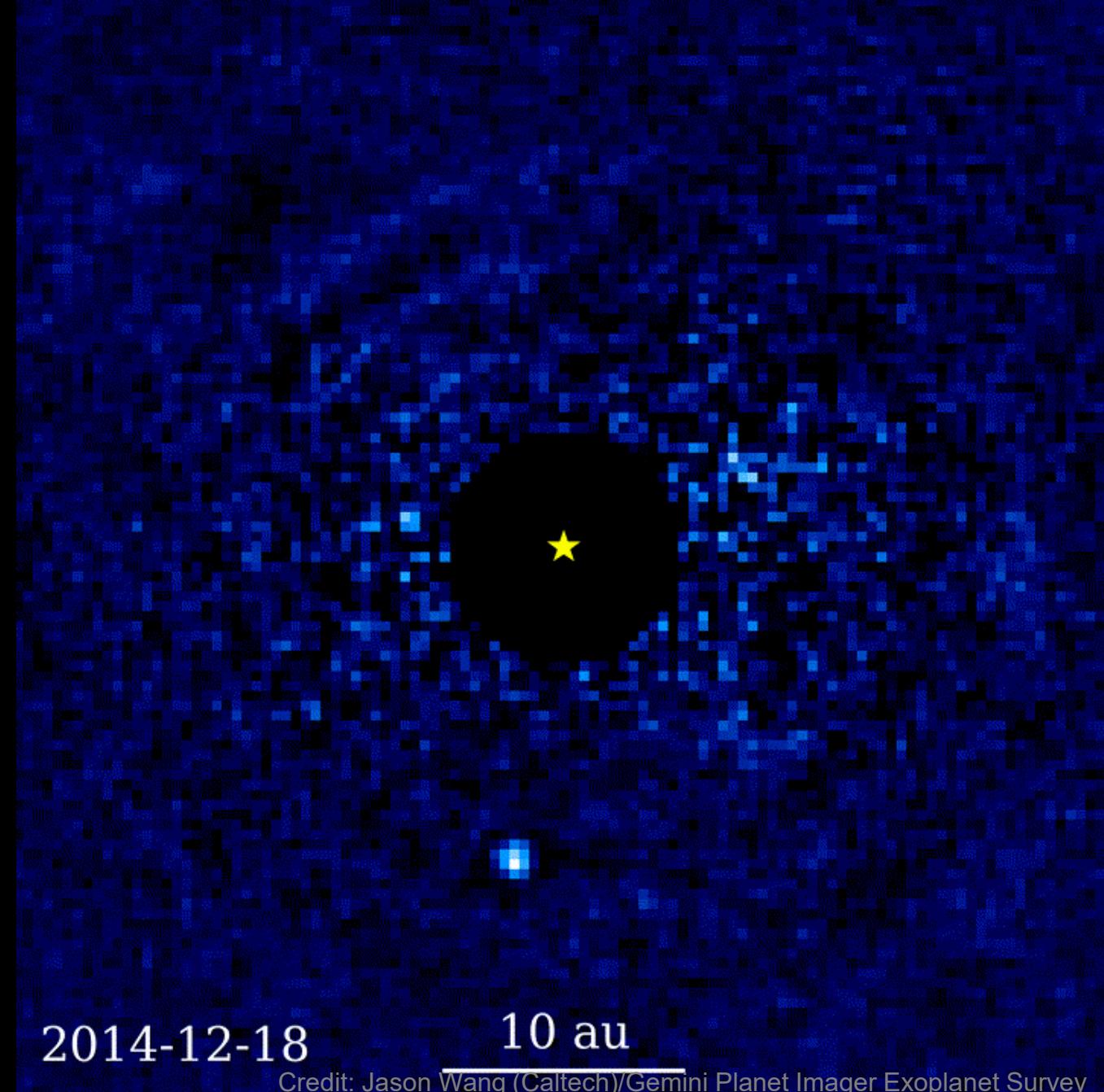
Credit: Flickr user mikelietz

**Young, giant planets
orbiting the star HR 8799.**

**This is typical of the level
of detail we can see with
direct imaging**



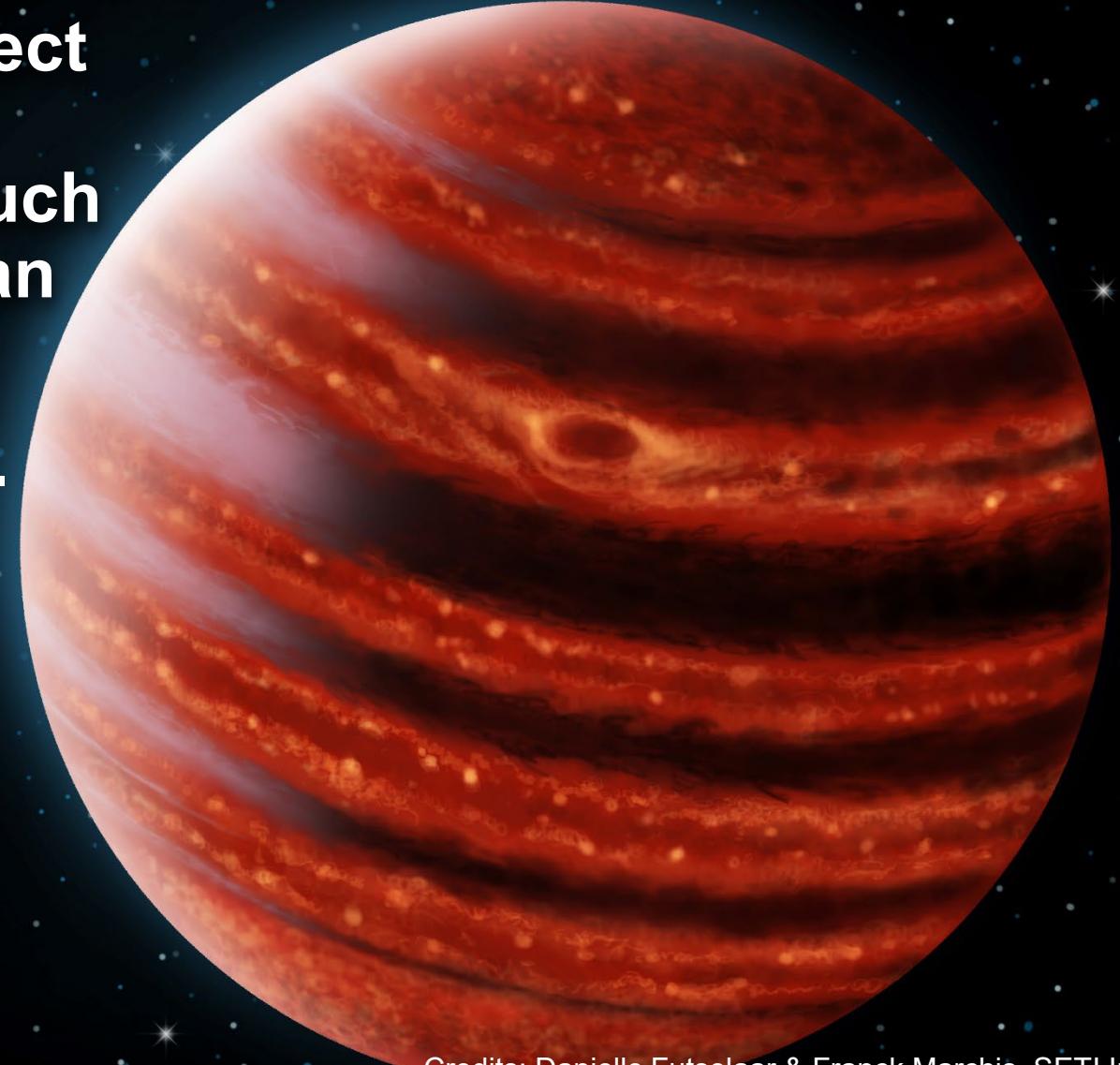
**So far, direct imaging
has detected only
around 150
exoplanets.**



Credit: Jason Wang (Caltech)/Gemini Planet Imager Exoplanet Survey

The planets we can currently detect using direct imaging are mostly young Jovian planets orbiting much farther from their parent stars than Jupiter orbits the Sun.

They are not likely homes for life.



Credits: Danielle Futselaar & Franck Marchis, SETI Institute

Direct imaging is the only method in which exoplanets are actually seen.

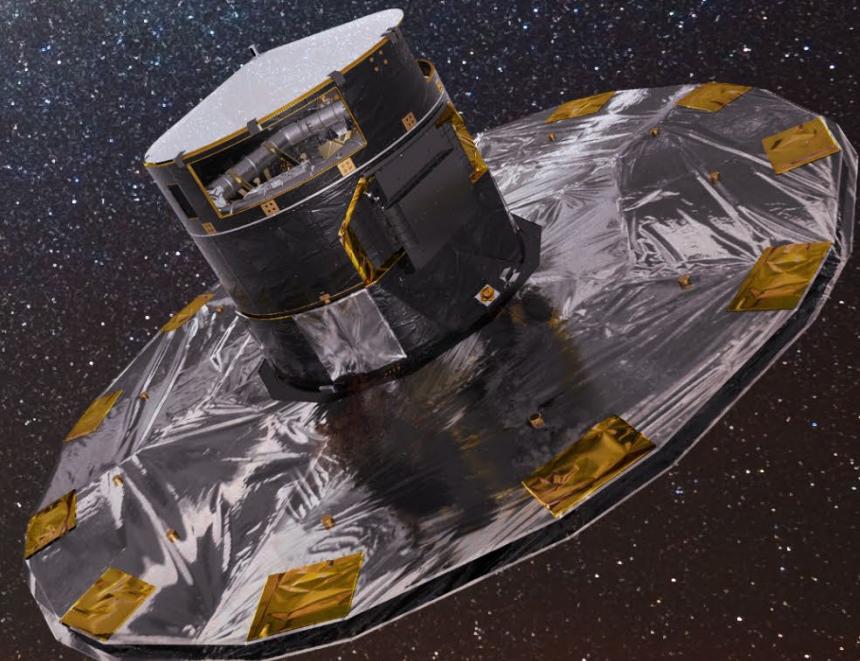
All of the other methods are indirect, meaning that the **existence** and **properties** of the planets are deduced from observations of the host star.

The astrometric method finds exoplanets by observing the motions of their hosts.



The astrometric method has only found a few exoplanets because the precision of the required measurements is beyond the capability of most telescopes.

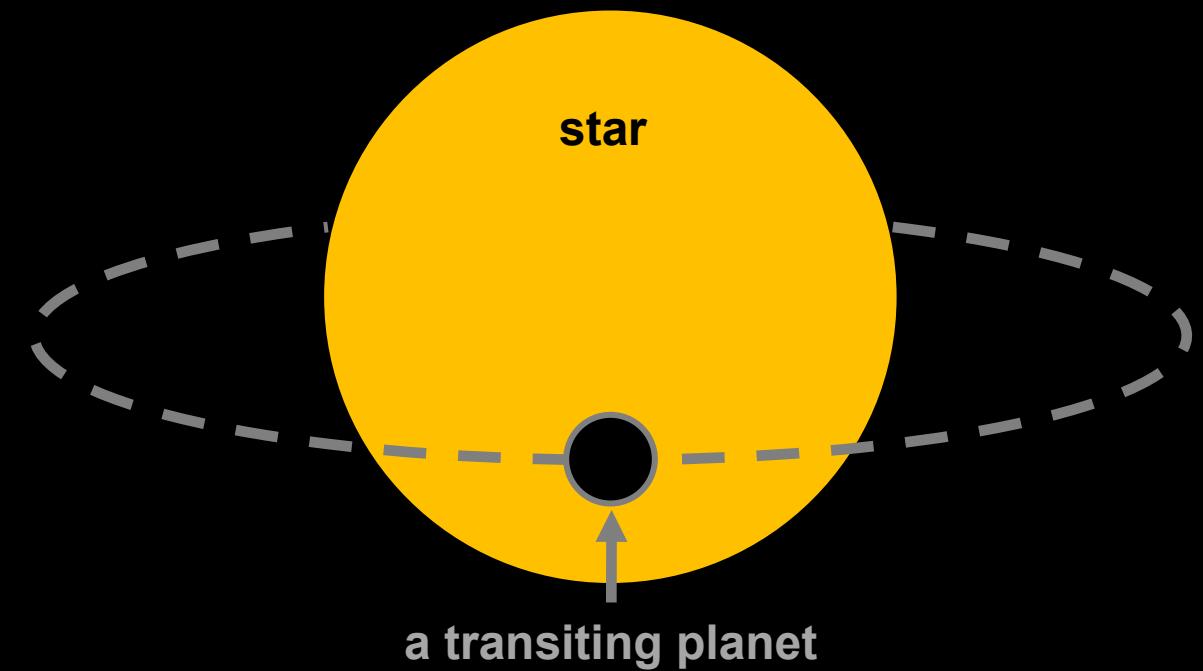
However, the **GAIA** spacecraft is expected to discover around 10,000 exoplanets using the astrometric method within the next few years.



There are several other detection methods, but overwhelmingly the two most successful ones have been the **transit method** and the **radial velocity method**.

We will start with the transit method and later combine it with the radial velocity method.

A **transit** occurs when one astronomical object passes in front of another from our point of view.



A transit of the Moon across the Sun, as seen by the STEREO spacecraft

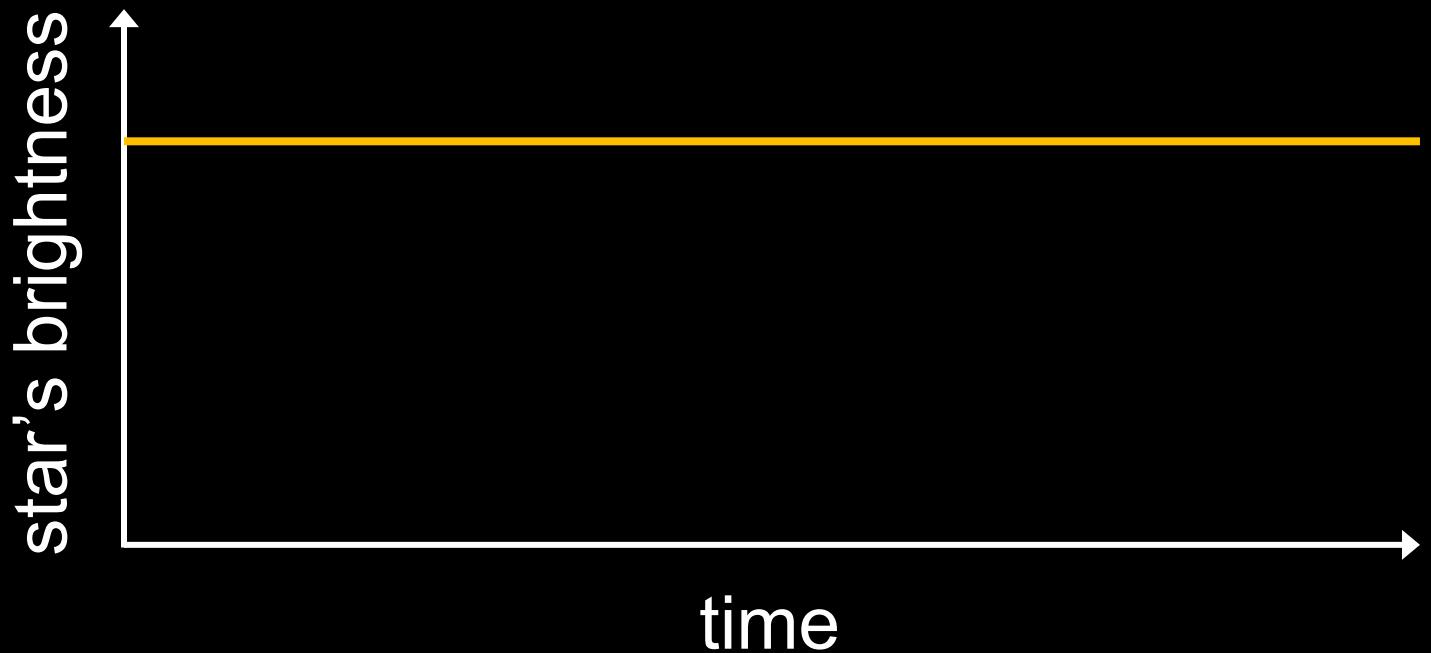
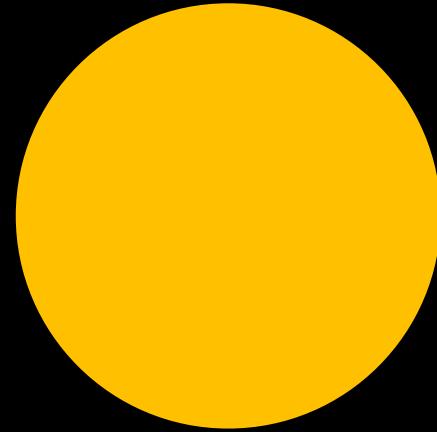


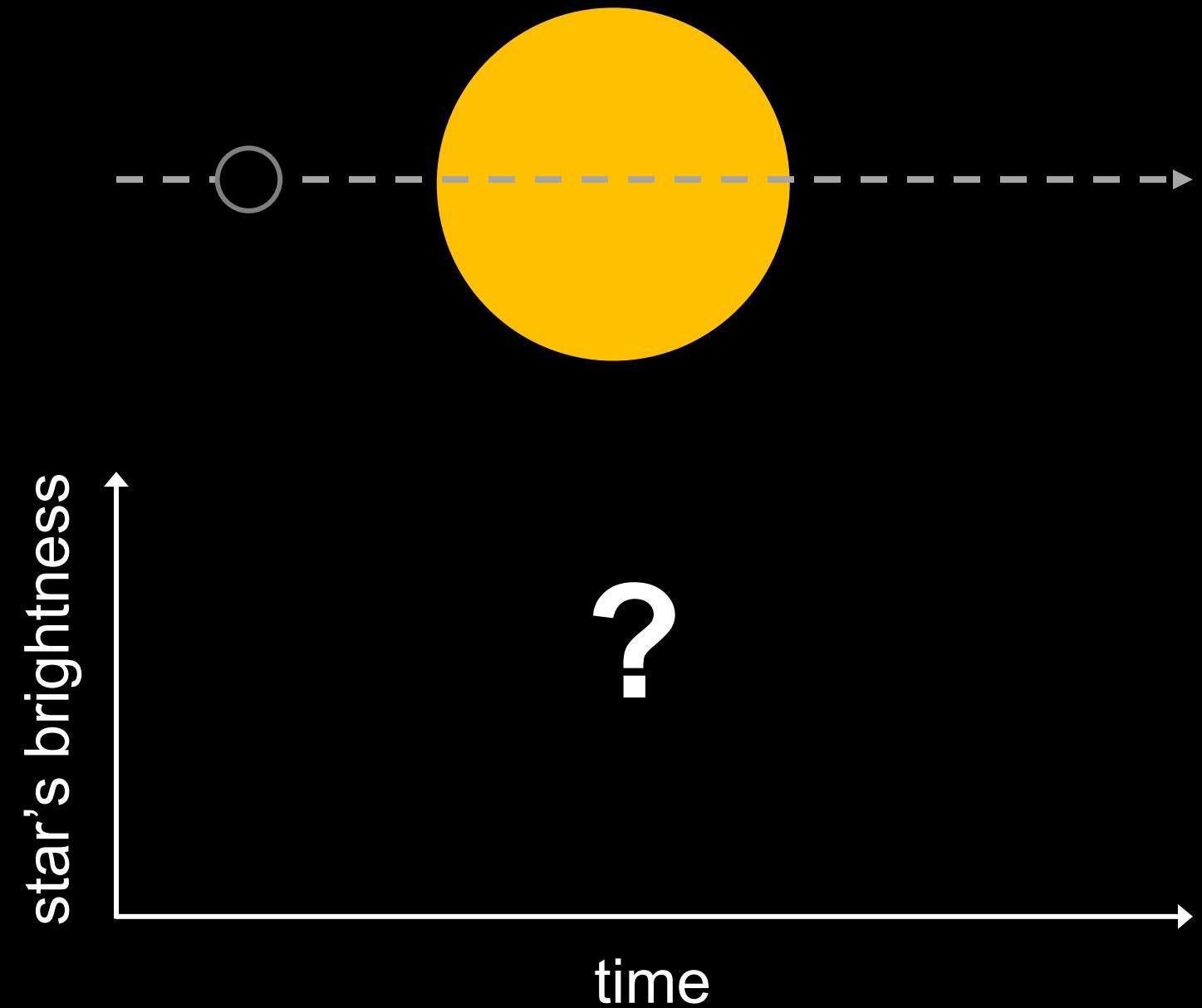
Credit: NASA/STEREO

Our current telescopes aren't powerful enough to actually *photograph* exoplanets transiting.

However, we can spot transits in a star's light curve.

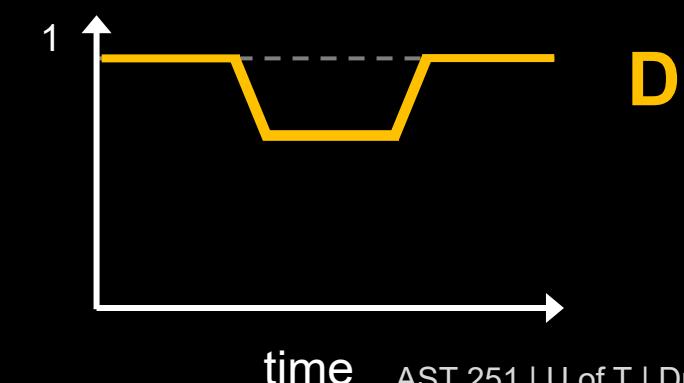
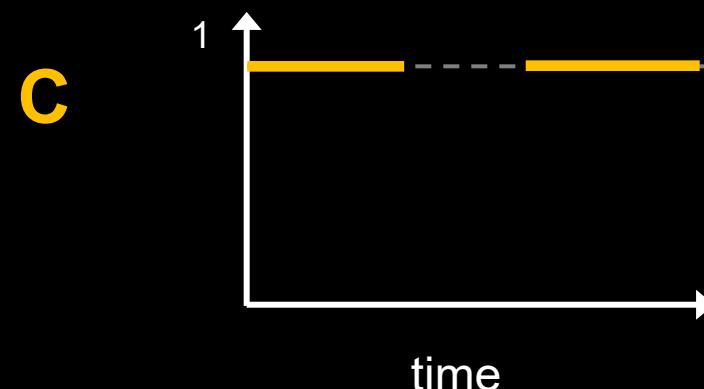
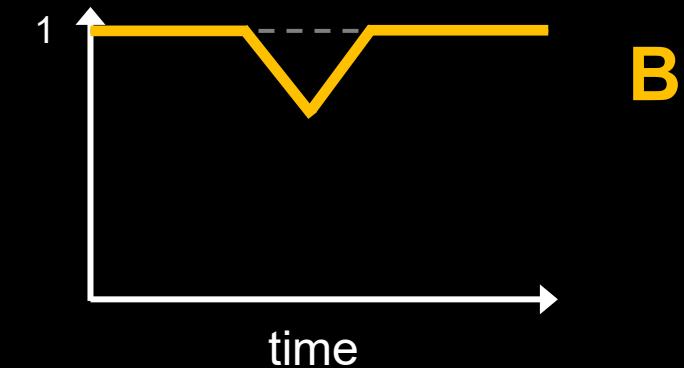
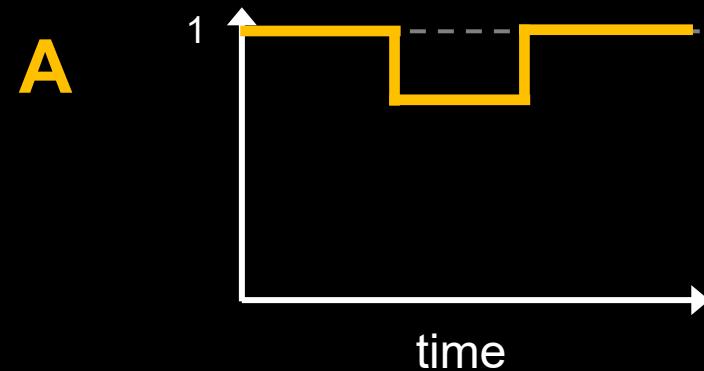
The **light curve** of a star is a graph of the star's brightness versus time





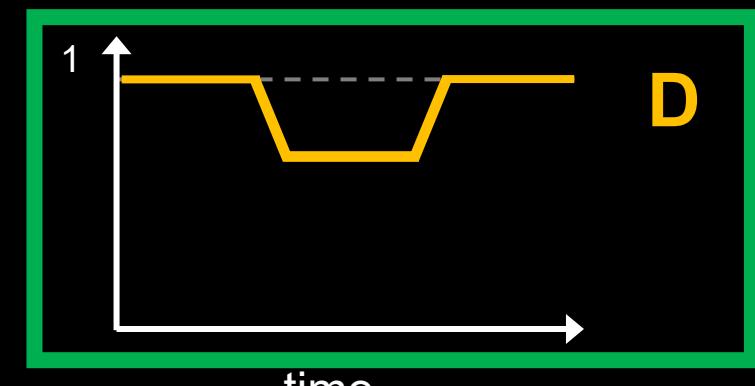
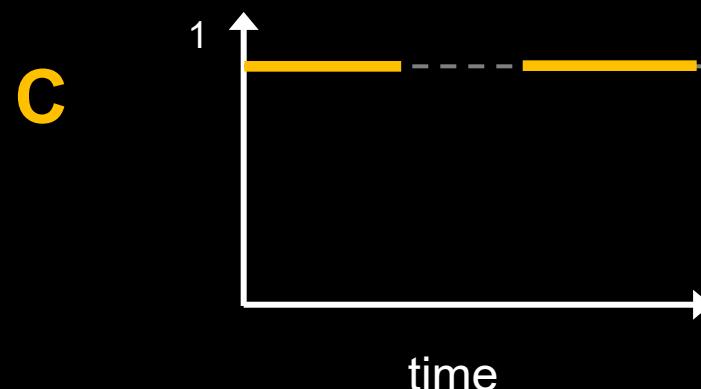
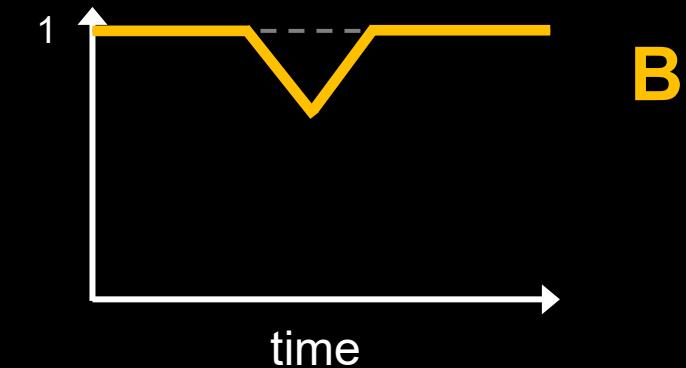
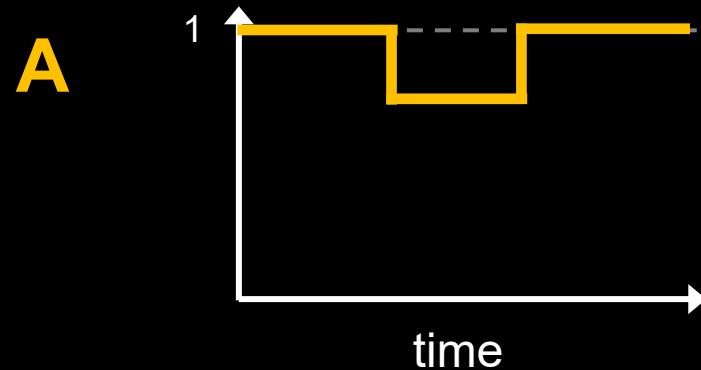
Concept Check

Which of the following would best illustrate the light curve for a planet transiting across the midplane of star?



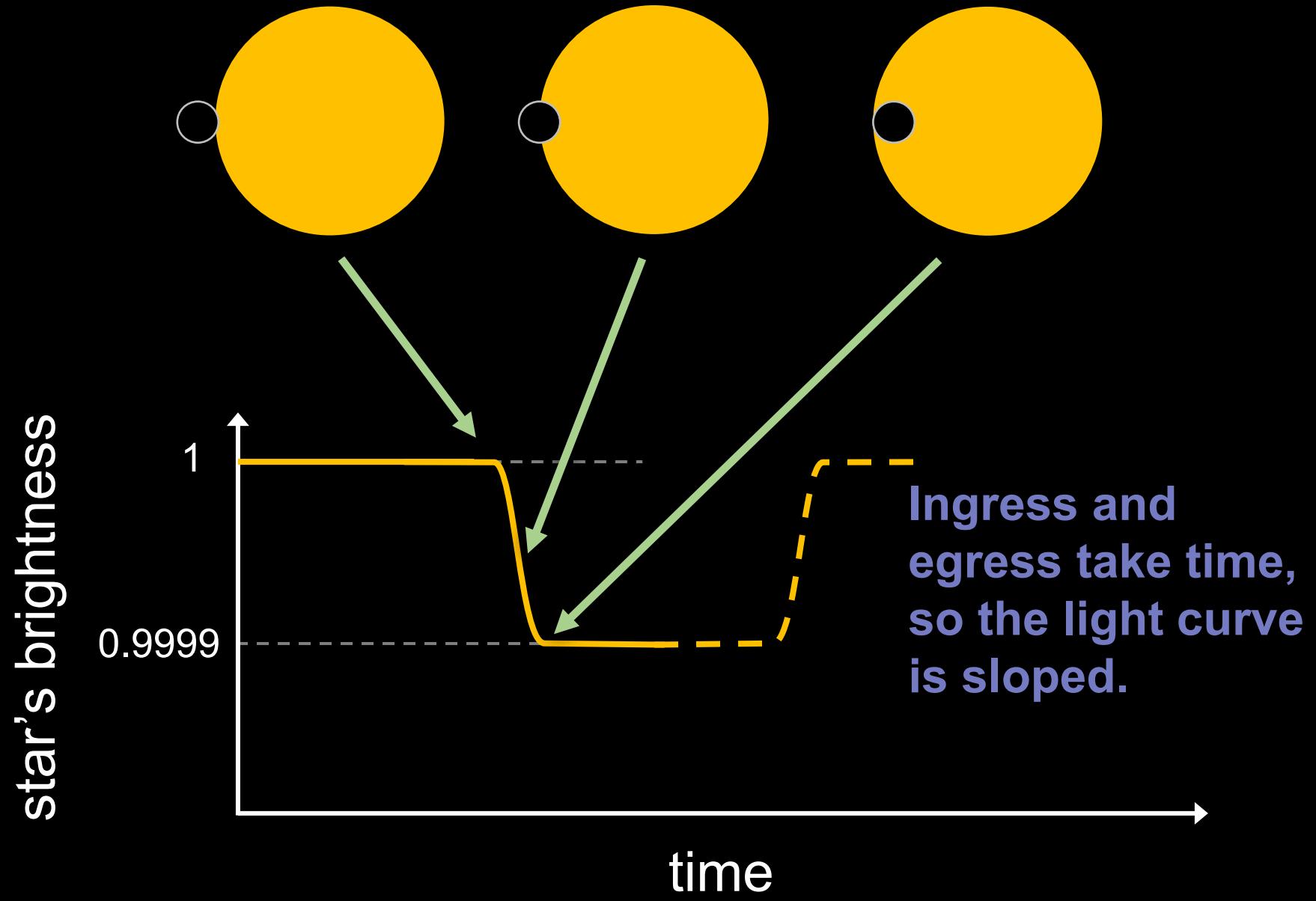
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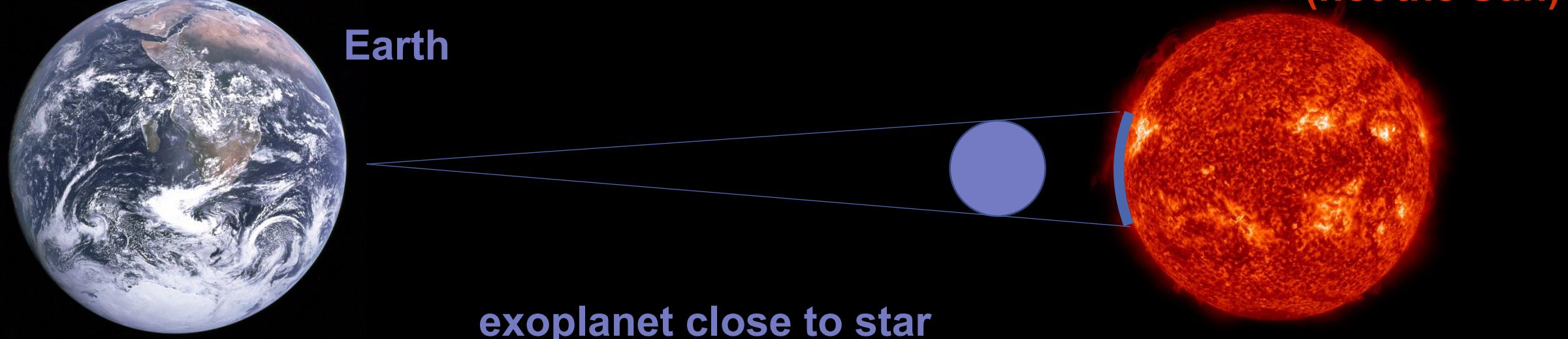
Credit: NASA



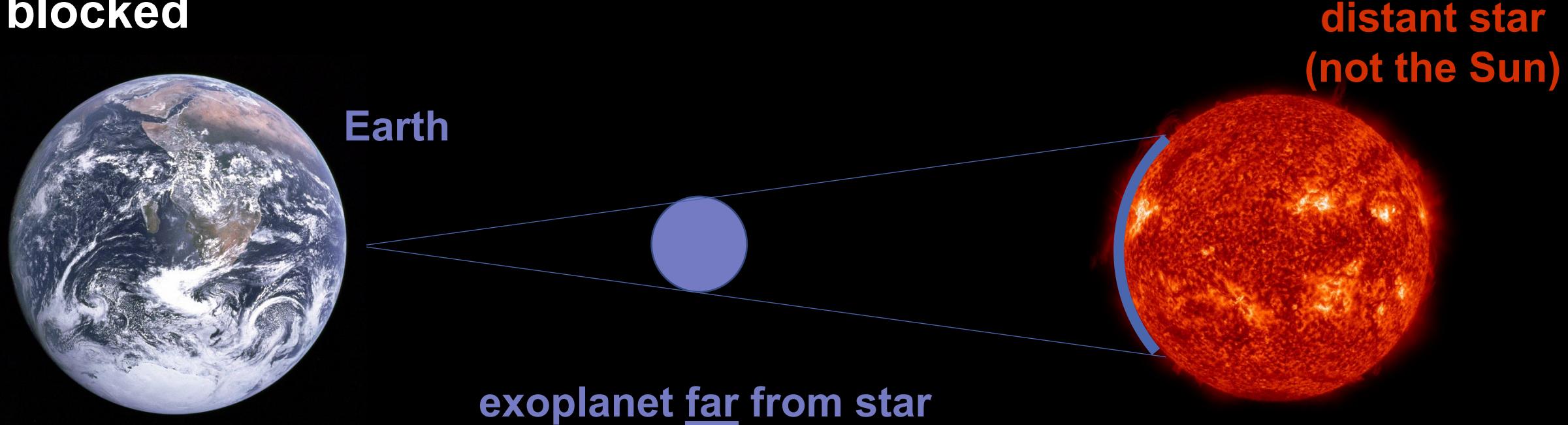
The amount of light blocked by a planet varies with the size of the planet.

So, we can use the transit method to directly measure the size of the planet, even *without seeing the planet!*

At first, it may seem that it's the distance between the star and the exoplanet that determines how much of the star's light is blocked

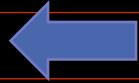


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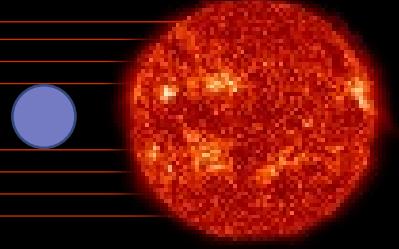


In reality, the Earth is so far away that the light rays received from the other star are almost parallel. Larger planets simply block more of them.

to distant Earth



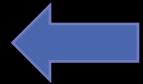
distant star (not
the Sun)



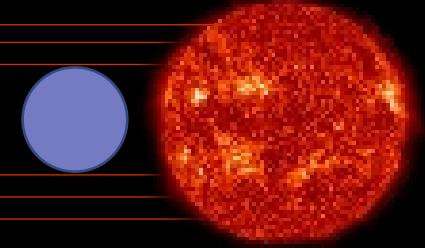
smaller exoplanet

In reality, the Earth is so far away that the light rays received from the other star are almost parallel. Larger planets simply block more of them.

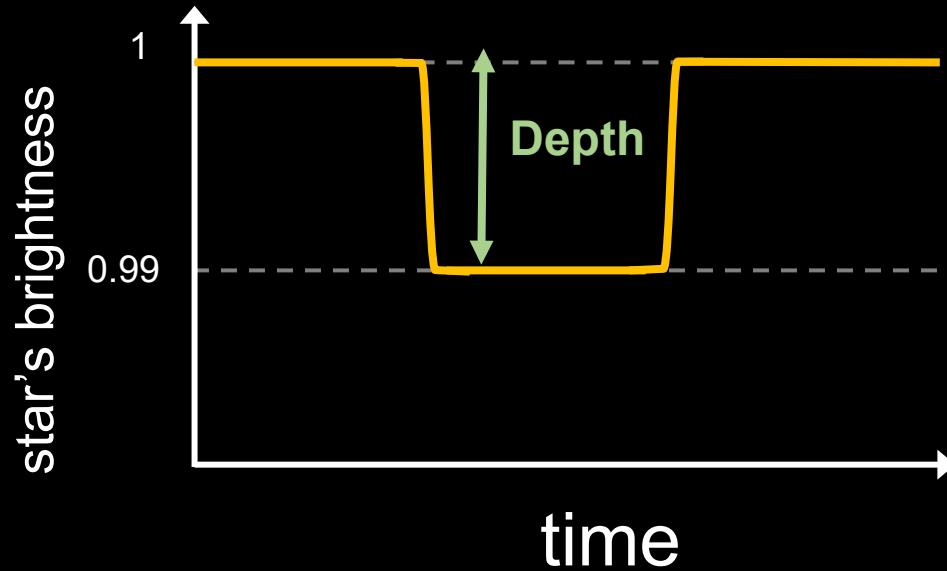
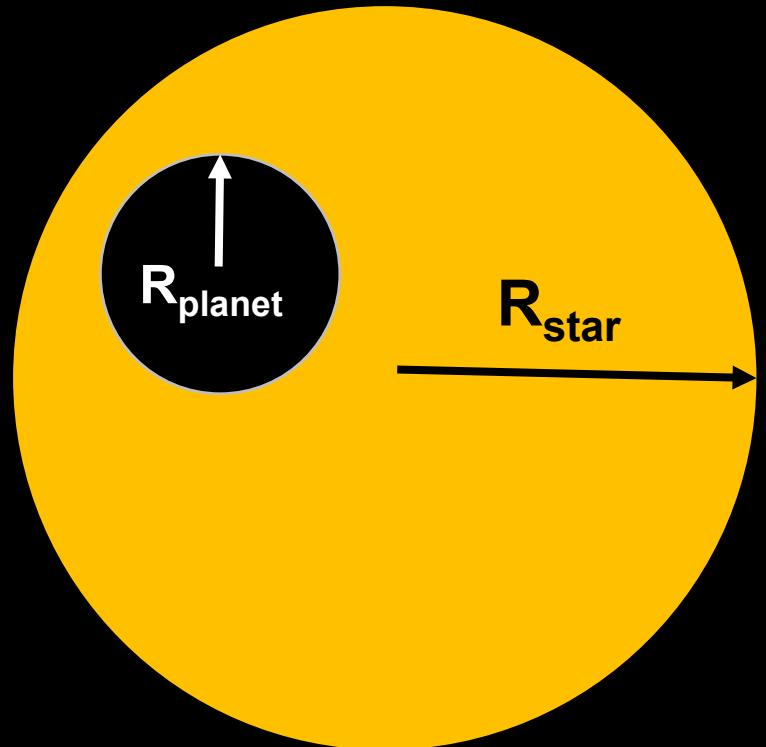
to distant Earth



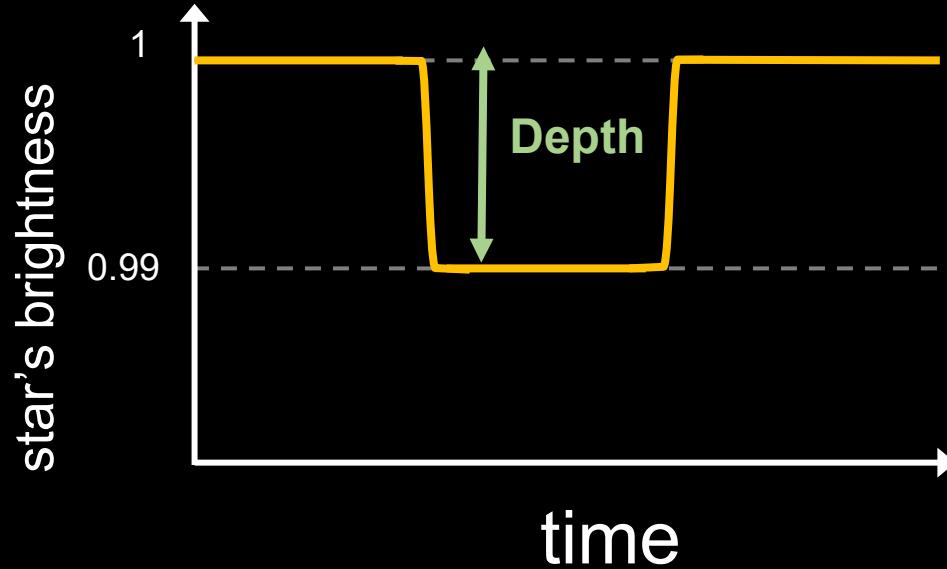
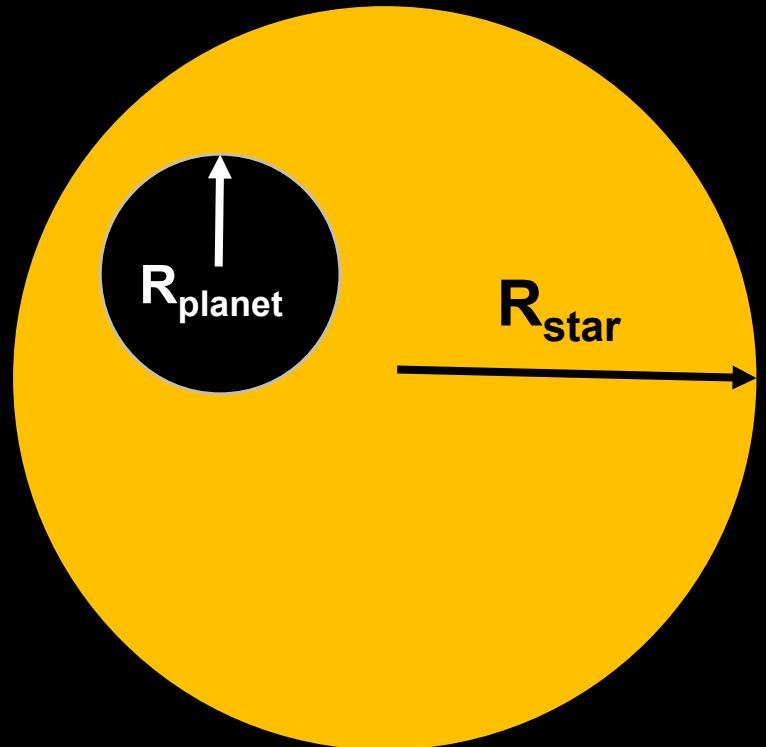
distant star (not
the Sun)



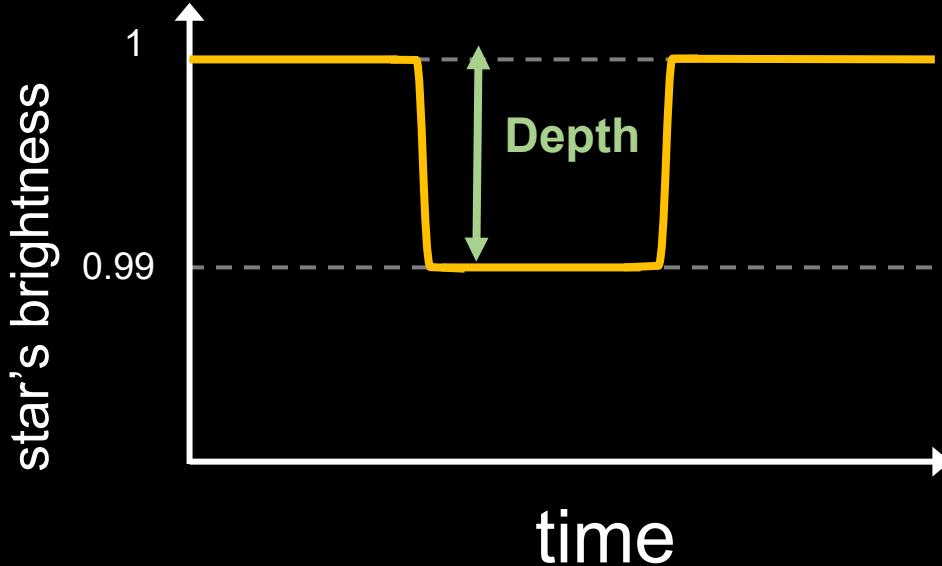
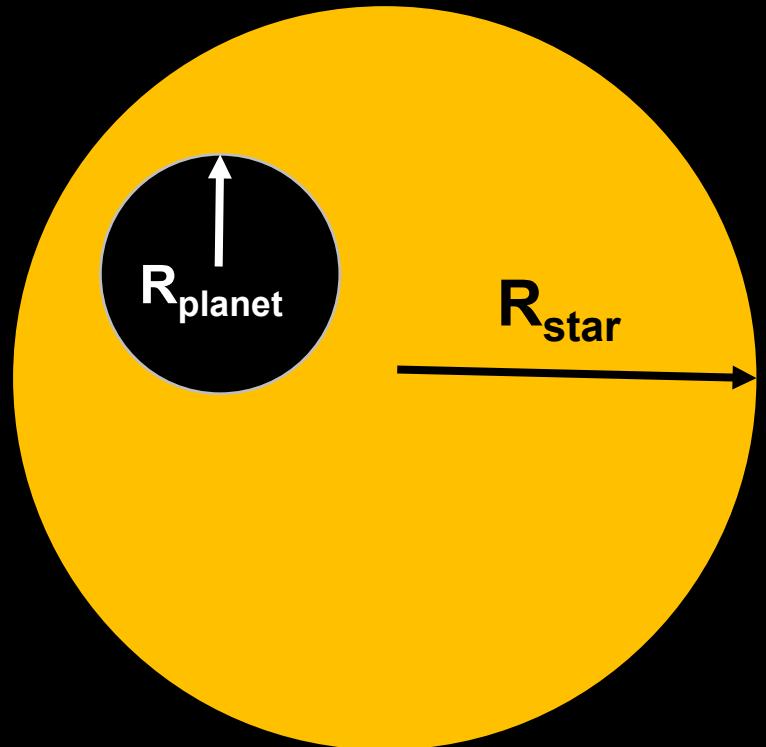
larger exoplanet



$$\text{Depth} = \frac{\text{cross-sectional area of planet}}{\text{cross-sectional area of star}}$$



$$\text{Depth} = \frac{\text{cross-sectional area of planet}}{\text{cross-sectional area of star}}$$
$$\text{Depth} = \frac{\pi R_{\text{planet}}^2}{\pi R_{\text{star}}^2}$$



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$$R_{\text{planet}} = R_{\text{star}} \sqrt{\text{Depth}}$$

Concept Check

Observations of a star 2.1 times the radius of the Sun reveal a transit with a depth of 0.0033. What is the radius of the transiting planet?

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$$R_{\text{planet}} = 2.1 R_{\text{Sun}} \sqrt{0.0033}$$

$$R_{\text{planet}} = 0.12 R_{\text{Sun}}$$

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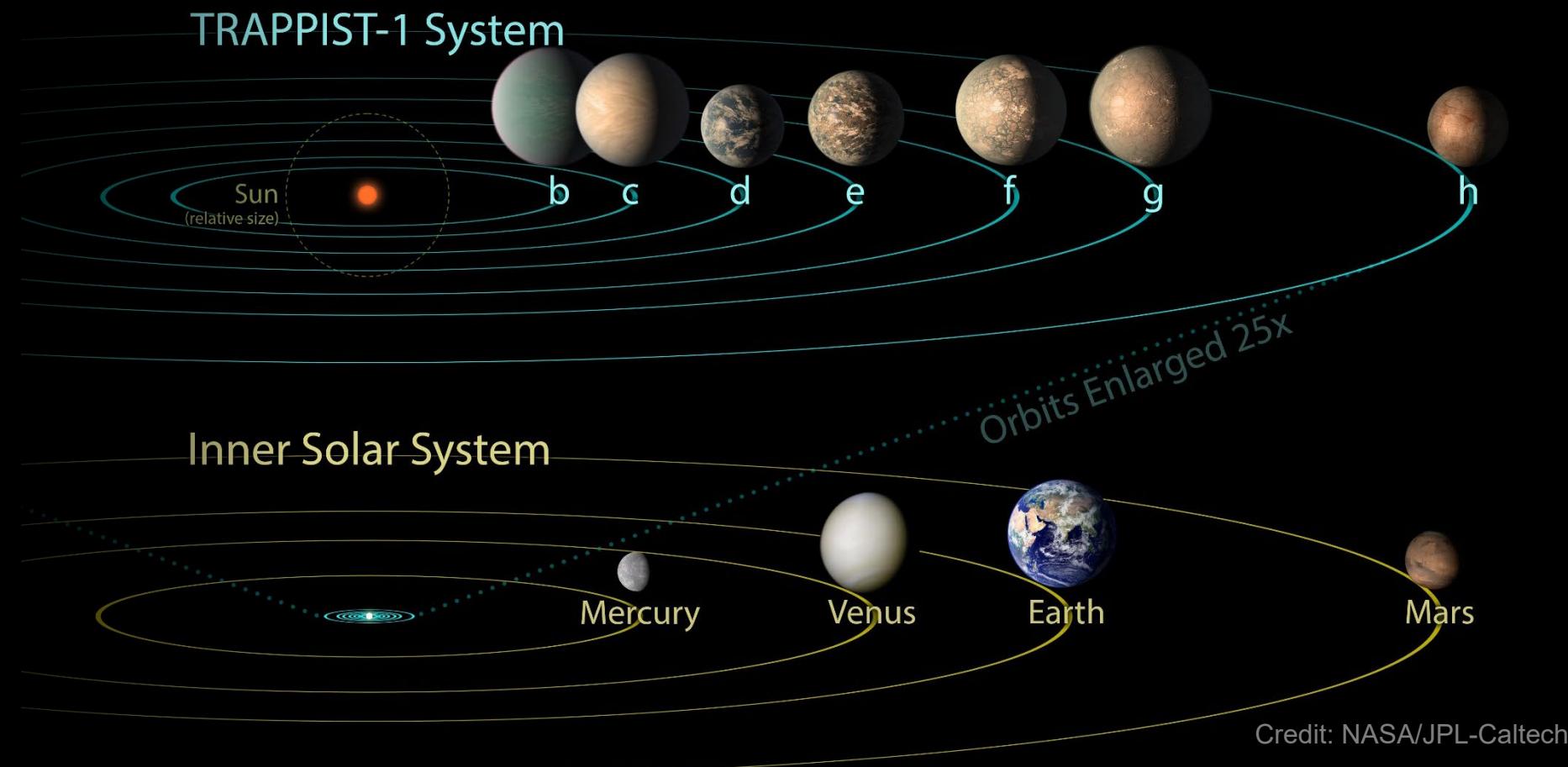
$$R_{\text{planet}} = R_{\text{star}} \sqrt{\text{Depth}}$$

$$R_{\text{planet}} = 2.1 R_{\text{Sun}} \sqrt{0.0033}$$

$$R_{\text{planet}} = 0.12 R_{\text{Sun}}$$

Sanity check—is this a reasonable size for a planet?

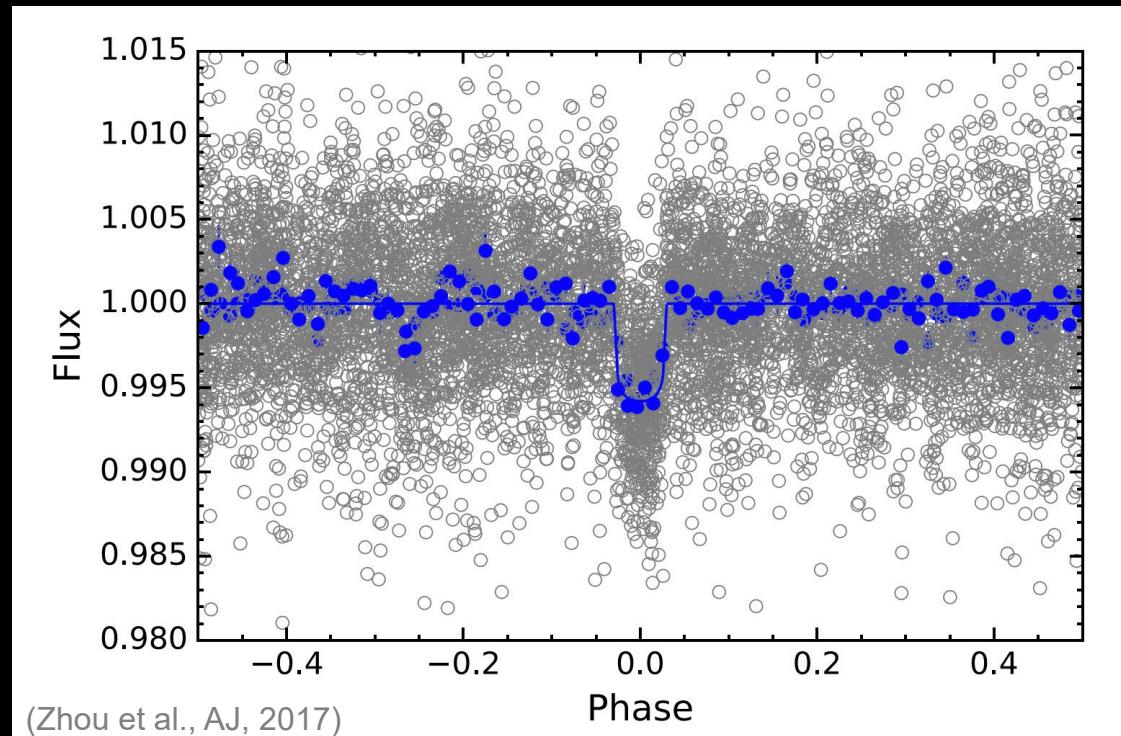
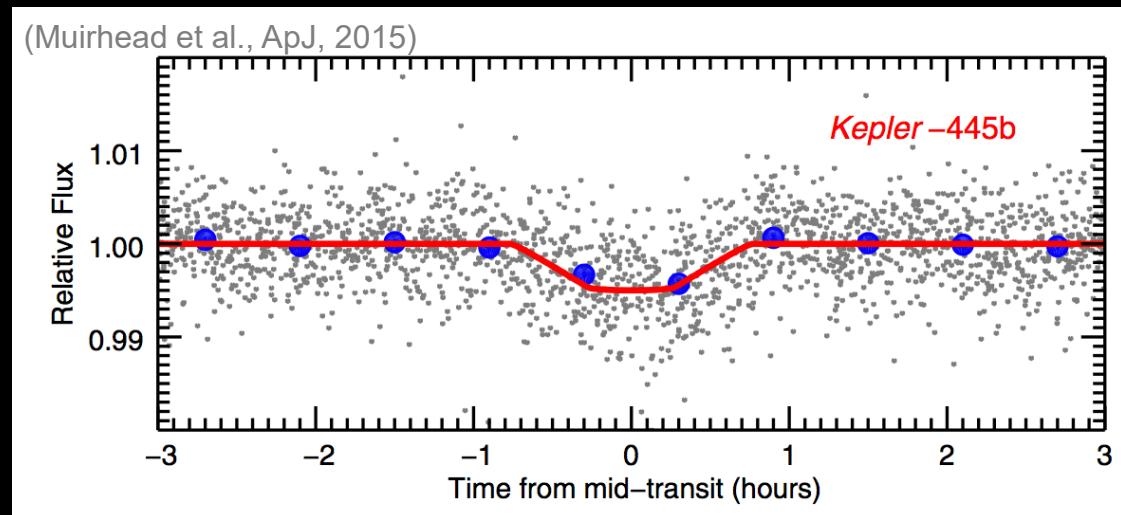
Measuring transit depths allows us to measure the sizes of each planet in an exoplanetary system, even though we can't see the planets themselves.



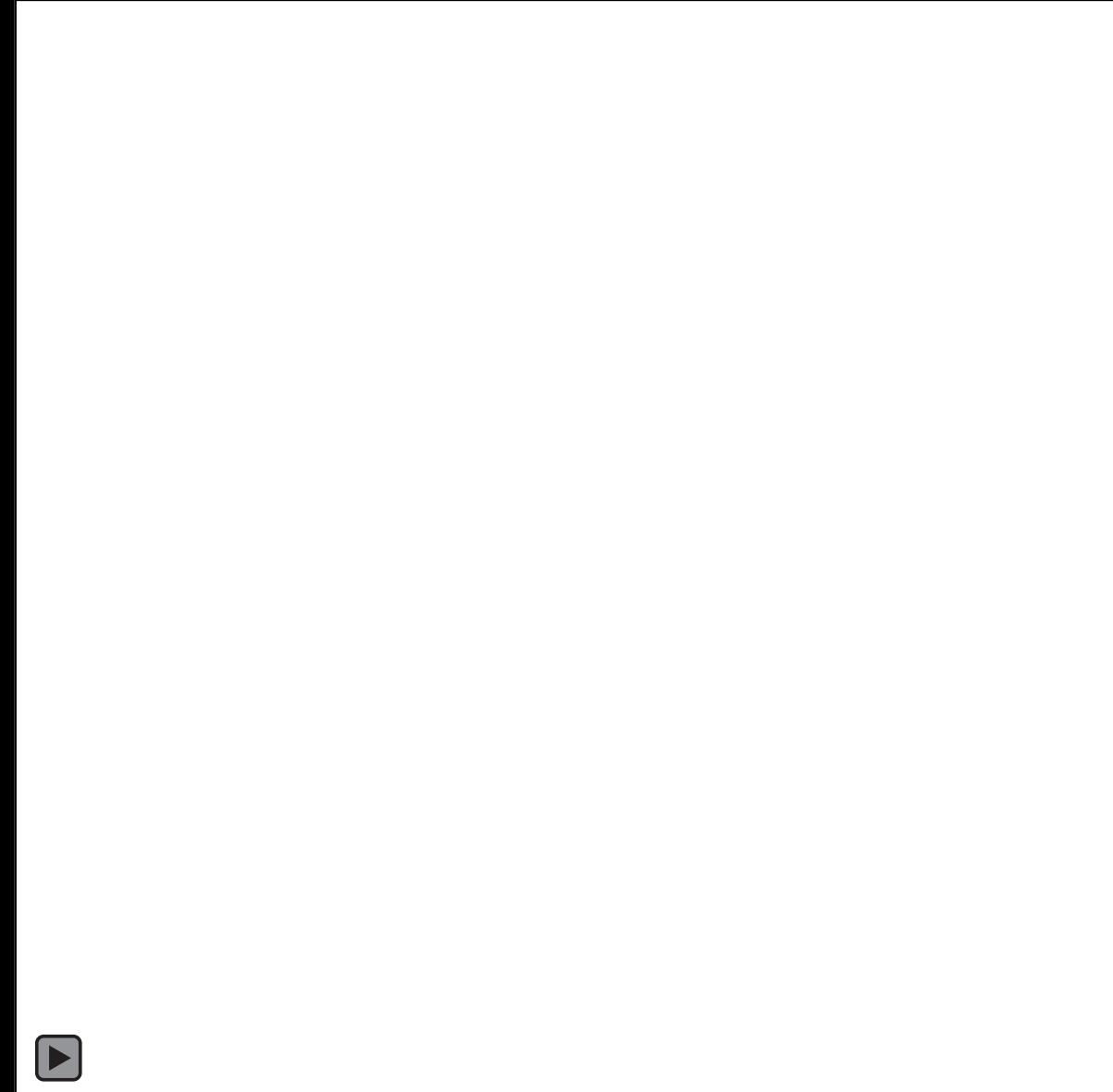
Numerous factors can make it challenging to interpret light curves and identify planets.

Can you think of anything other than a transiting planet that might cause a dip in a star's light curve?

The light curves of real stars contain some amount of “noise”, which can make it more difficult to distinguish the transits and measure their depths accurately.

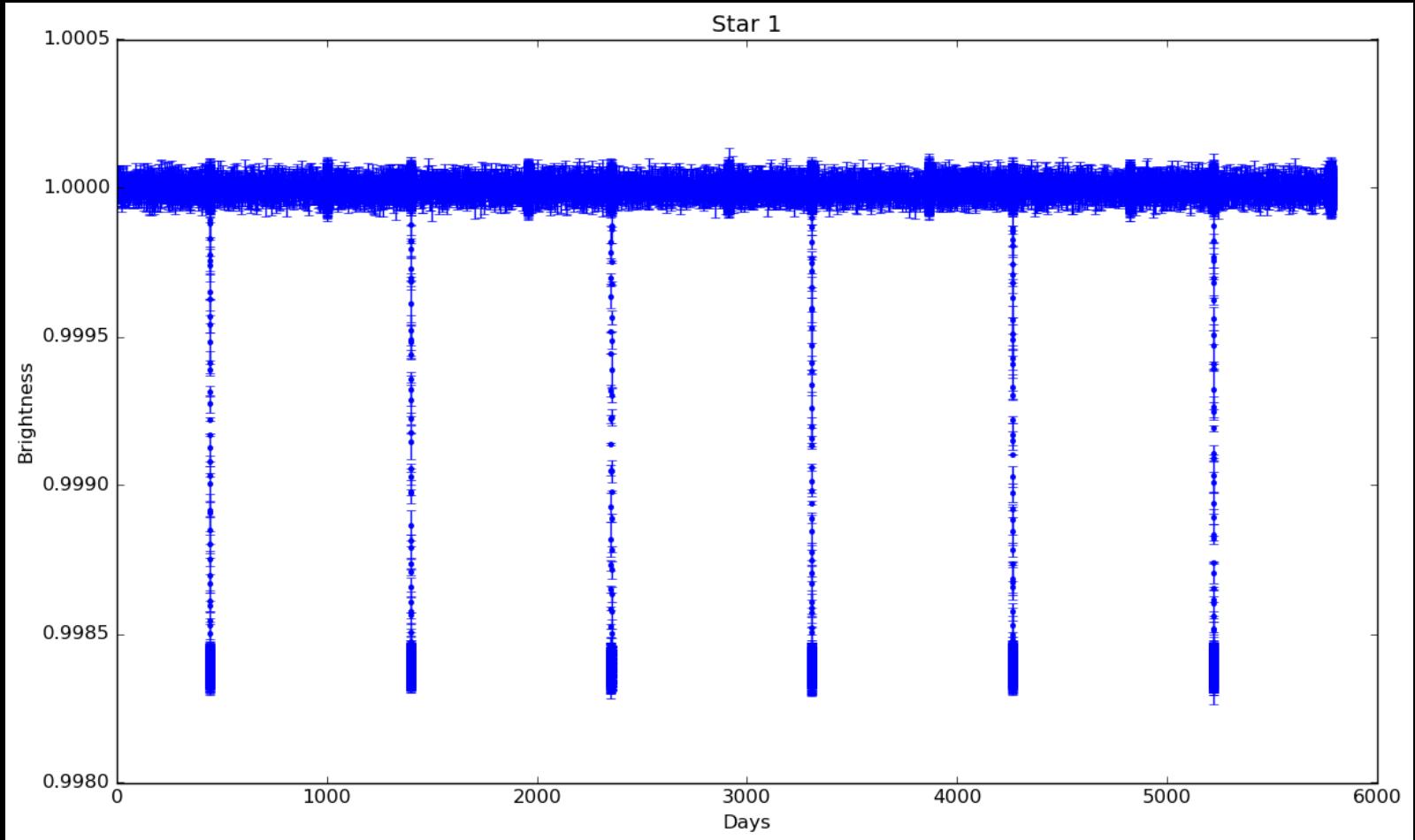


A sunspot on the host star can produce an effect similar to a transiting planet.



Credit: NASA/SDO

To confirm that a transit is caused by a planet, we look for multiple transits of the same depth repeating at regular intervals, corresponding to successive orbits of the planet.



Concept Check

If aliens were monitoring our Sun for transits of Earth, how often would they see them?

- A. Once a day
- B. Once a week
- C. Once a month
- D. Every six months
- E. Once a year

Concept Check

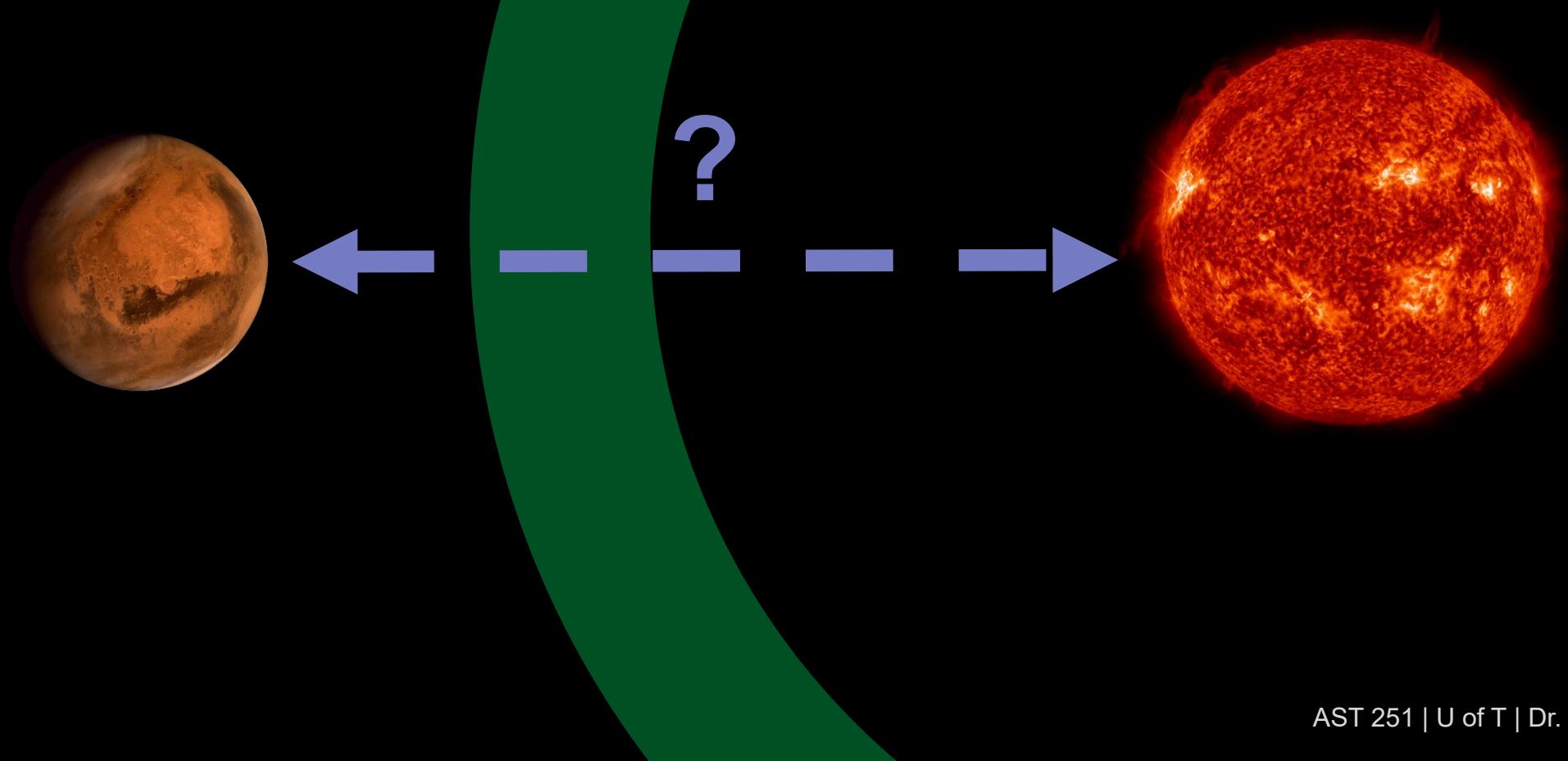
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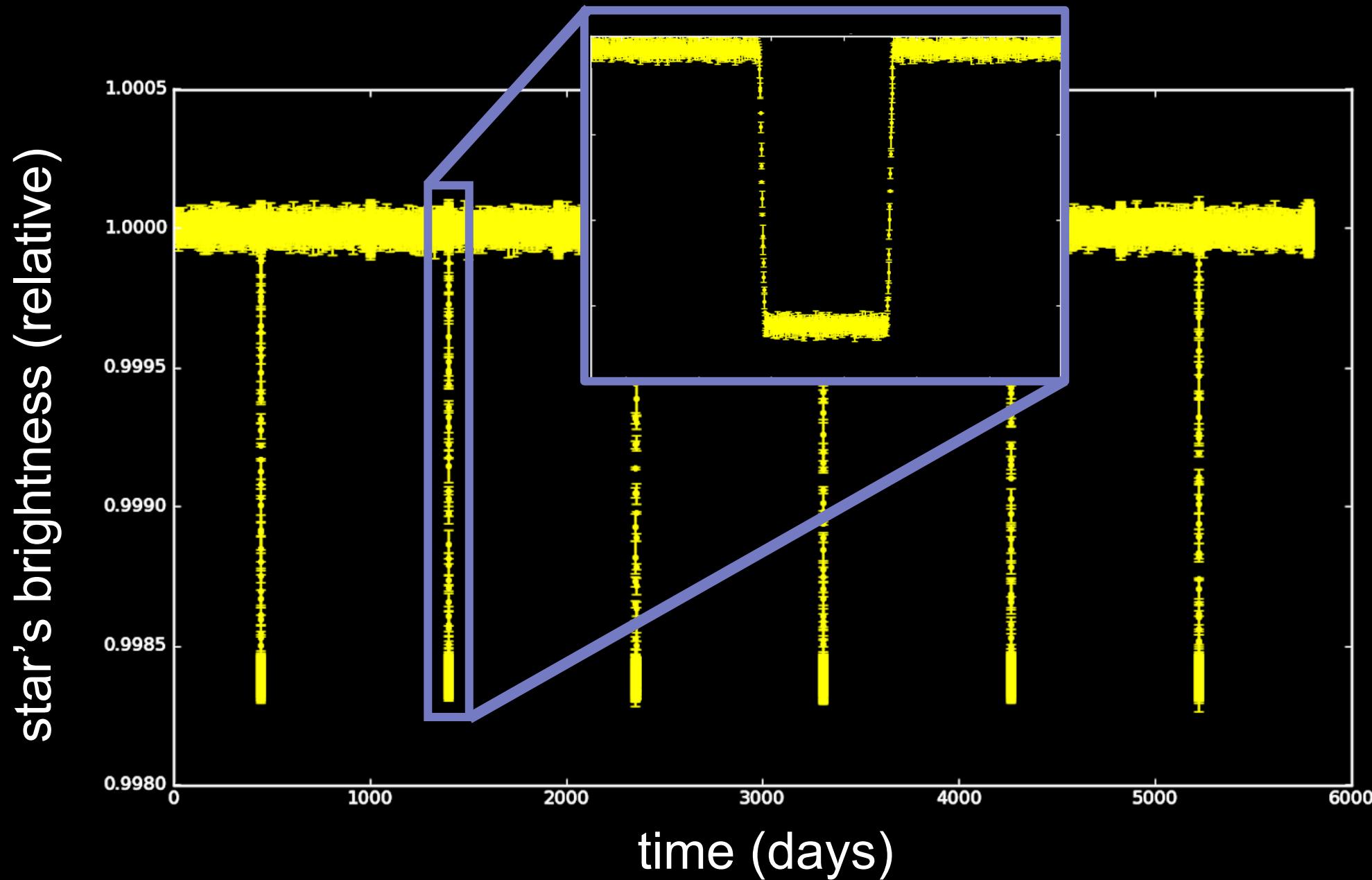
How to Decide Whether a Transiting Planet is in the Habitable Zone

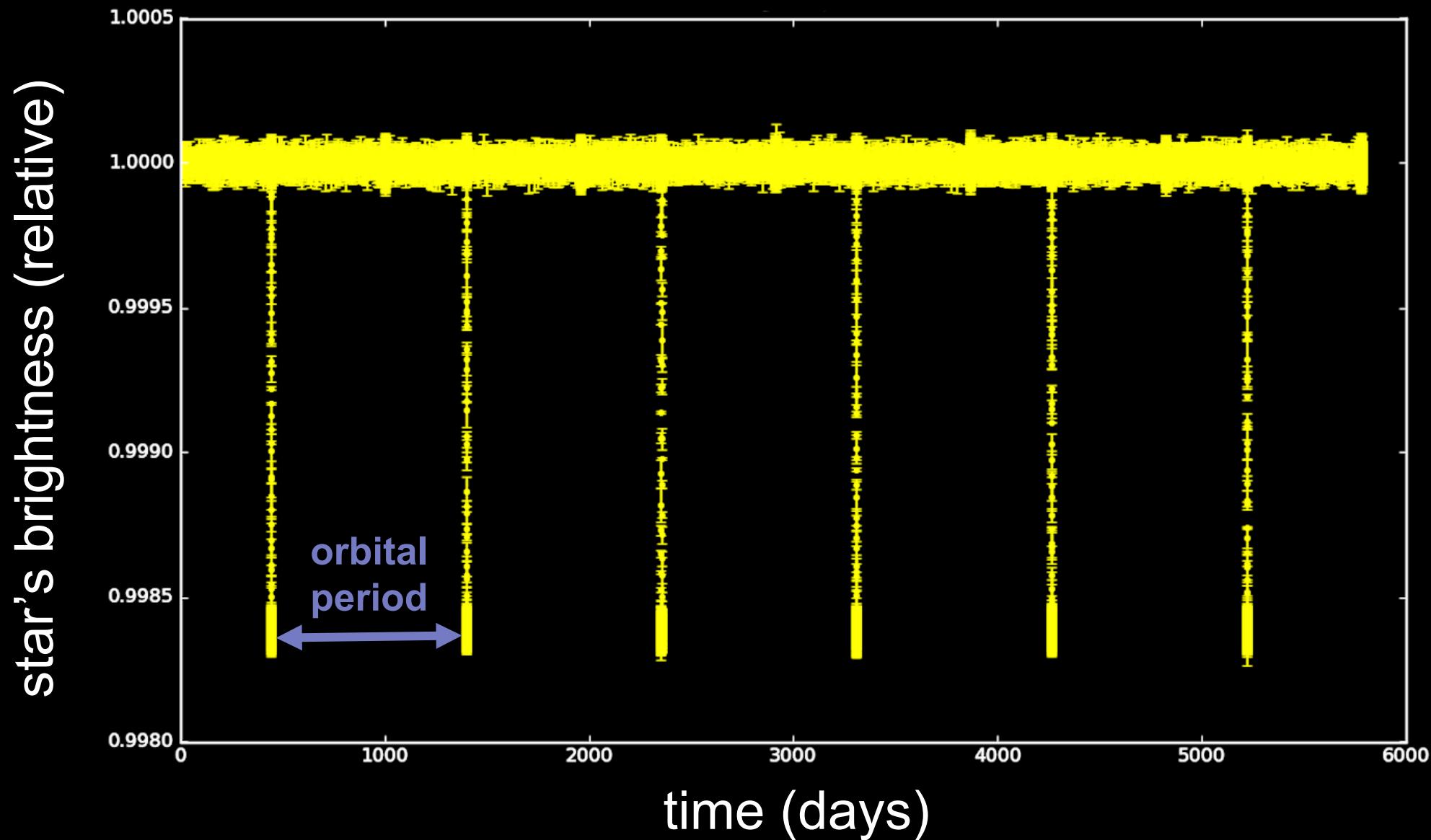
**What can we learn from a
transit light curve,
beyond that a planet
exists and its radius?**

One critical piece of information is how far the planet orbits from the star. Is it in the habitable zone?



The distance at which a planet orbits is directly related to the time it takes to orbit, called its **orbital period**.





The relationship between a planet's orbital period and its distance from its parent star can be worked out from Kepler's third law.

**German astronomer
Johannes Kepler
(1571-1630) worked
out the three laws of
planetary.**

**Kepler's laws are
actually just
consequences of
Newton's Law of
Gravity, which hadn't
been discovered in
Kepler's time.**

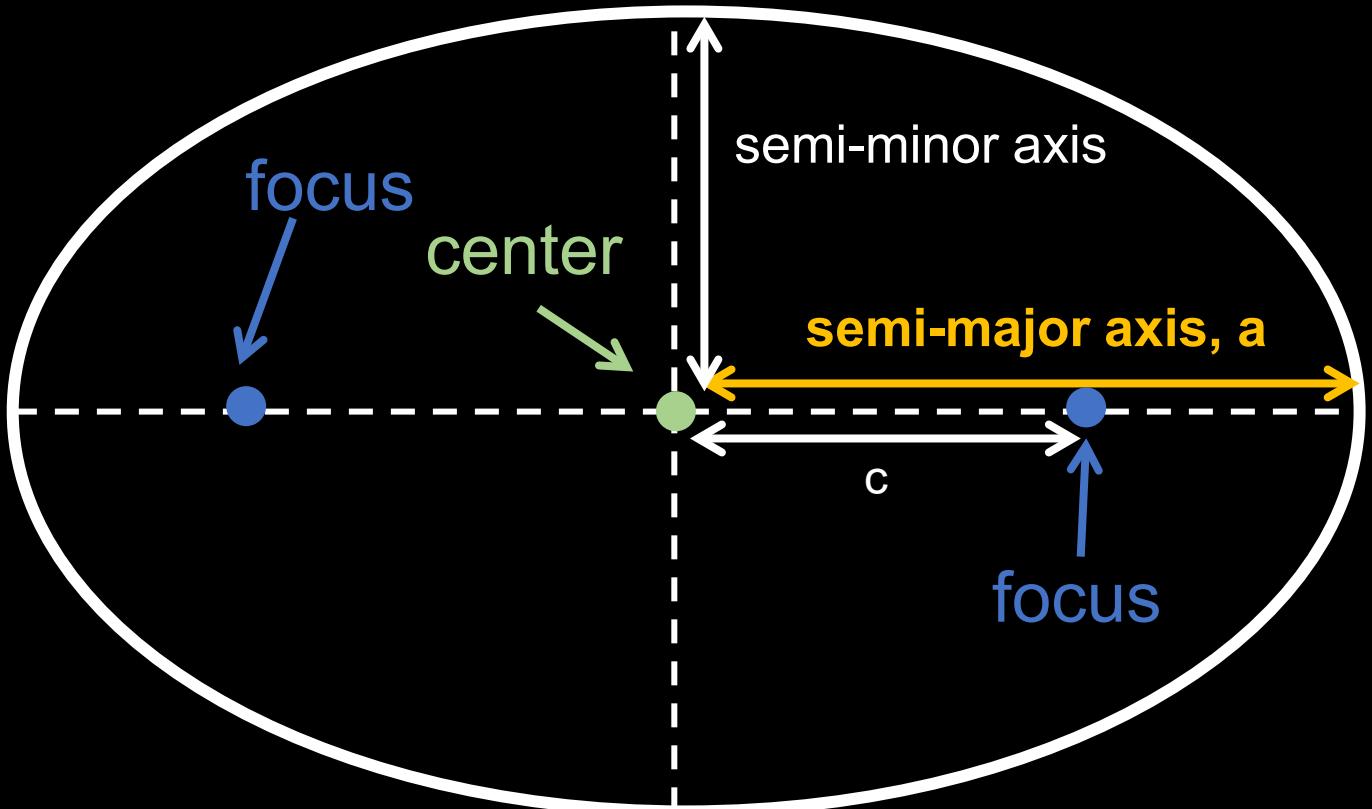


Credit: Public domain

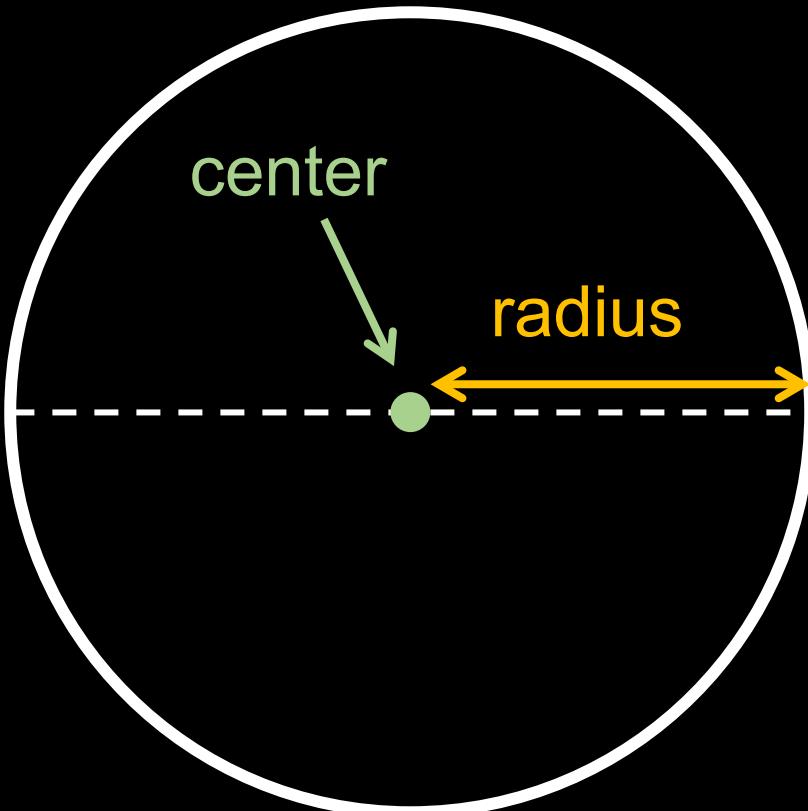
Kepler's First Law

All planets orbit their parent stars in elliptical orbits with the star* at one focus.

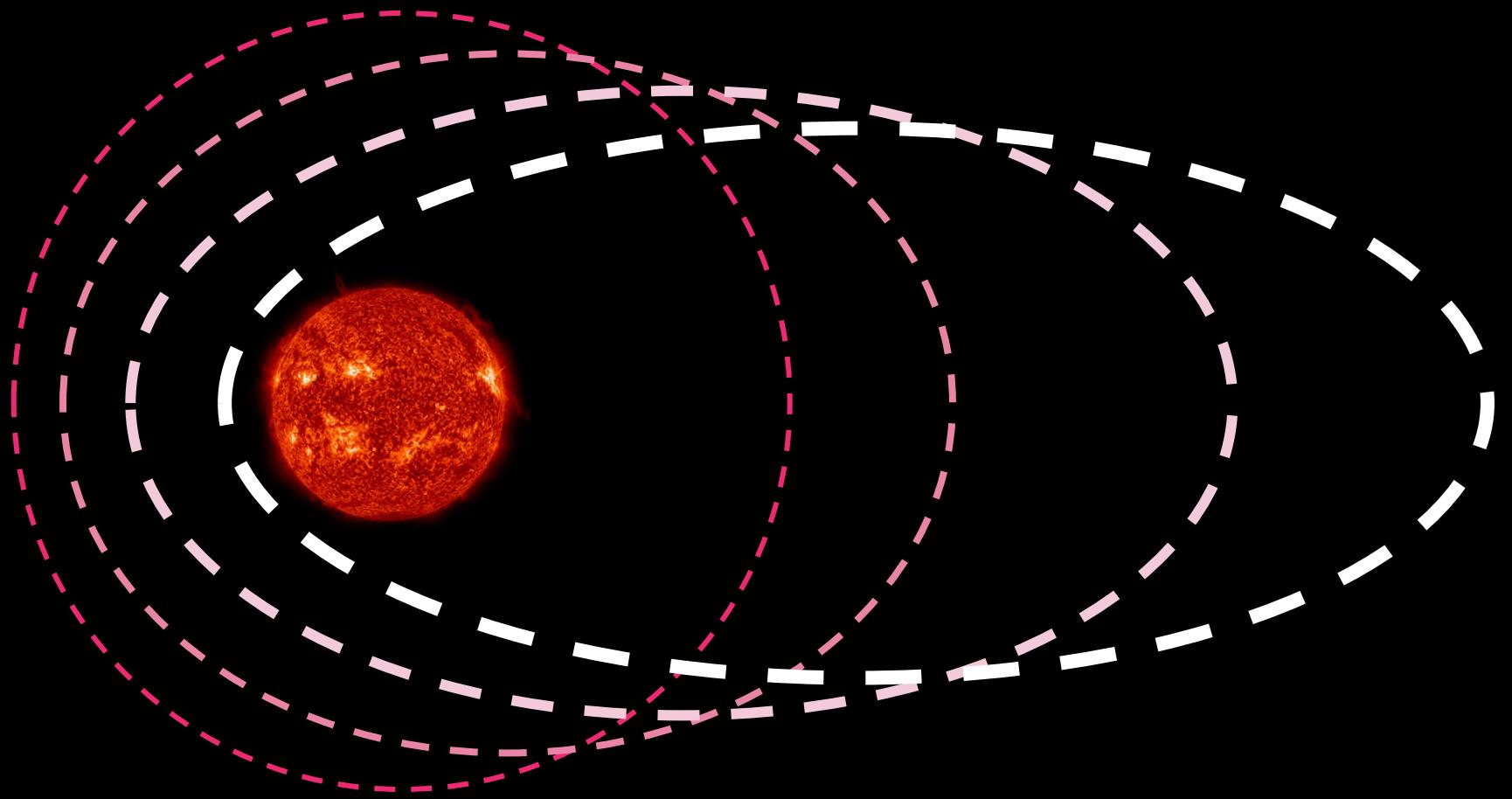
*This is technically not correct—the center of mass of the system is at one focus. However, in the general case that the star is much more massive than any of its planets, the difference is small. We will return to this point.



This ellipse has **eccentricity** = $c/a = 0.6$



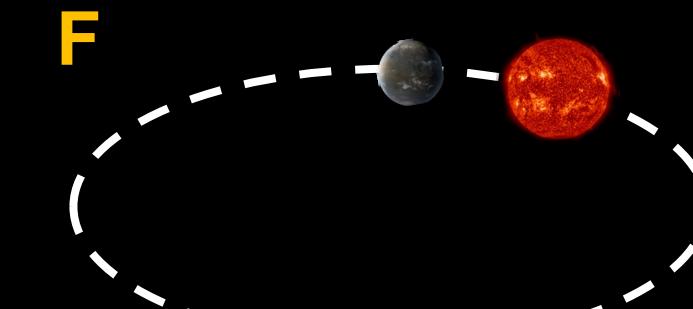
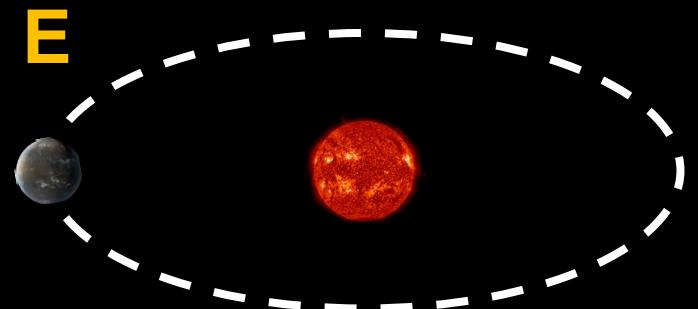
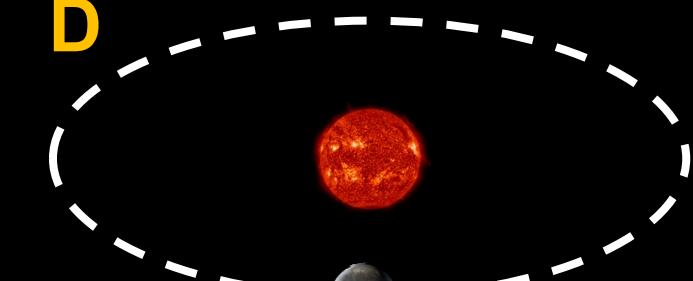
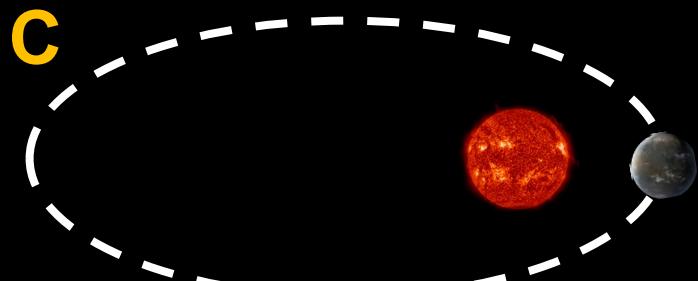
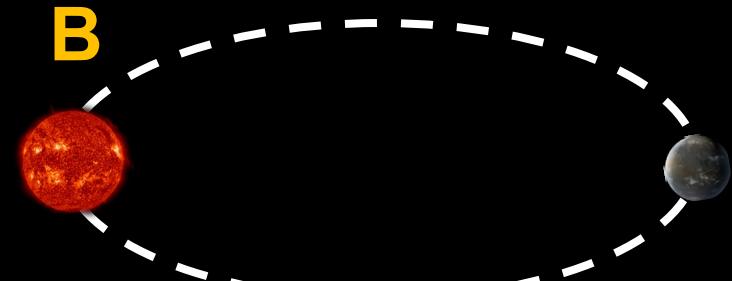
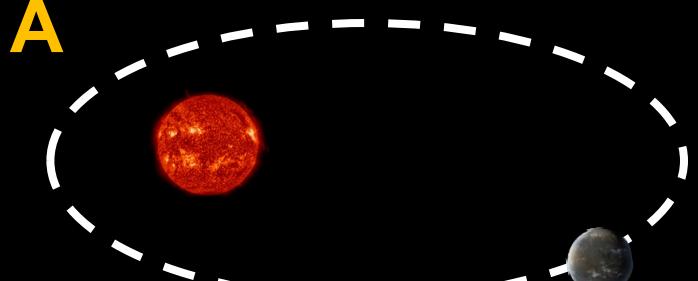
This ellipse has **eccentricity** = 0 (i.e. it's a circle)



**Orbits with different eccentricities
(thicker line → higher e)**

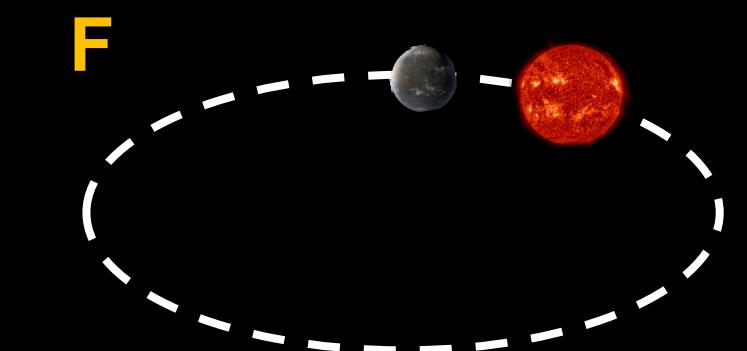
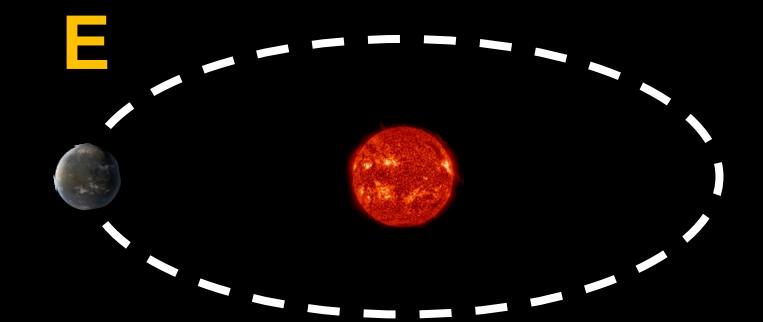
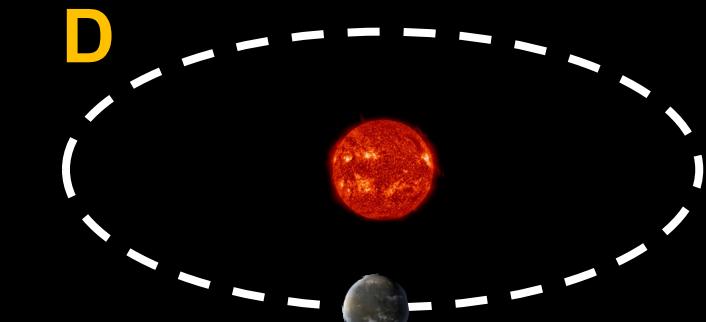
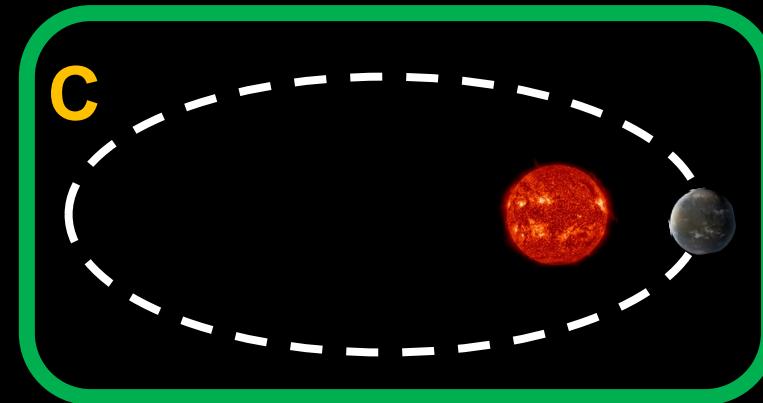
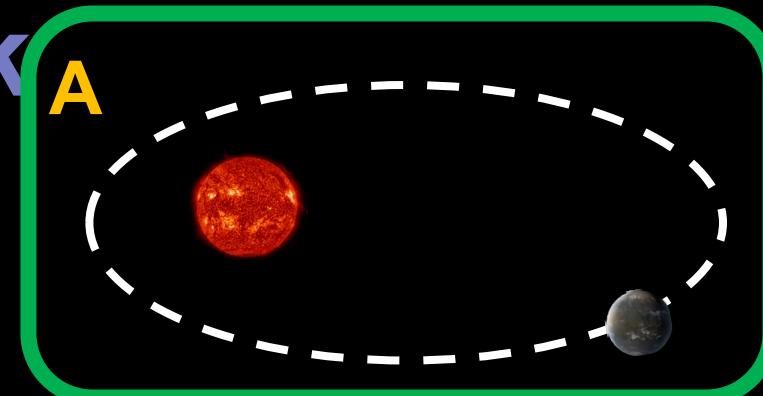
Concept Check

Which of these diagrams shows a planet orbiting a star in a way that follows Kepler's first law? All diagrams are viewed from directly overhead.



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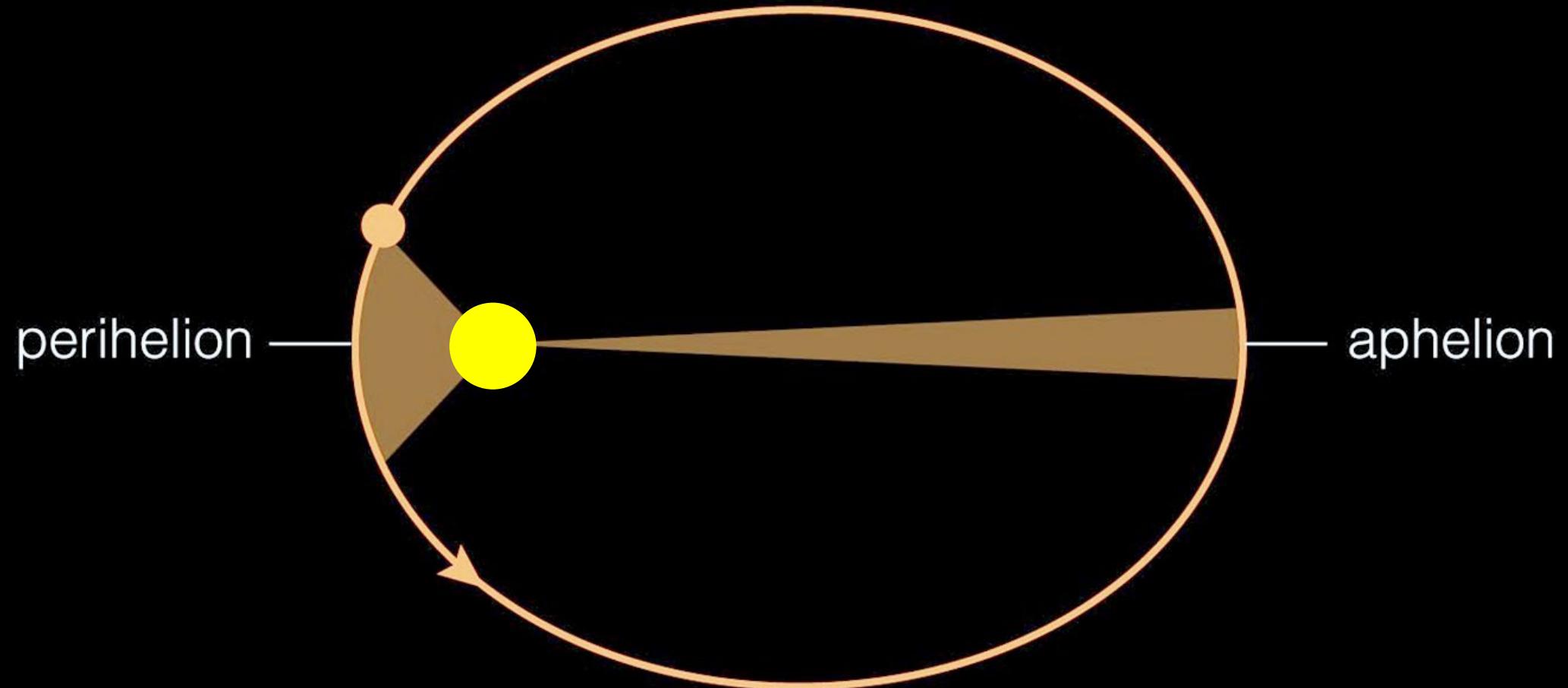


Credit: YouTube user Ms. Edge
AST 251 | U of T | Dr. Reid | 56

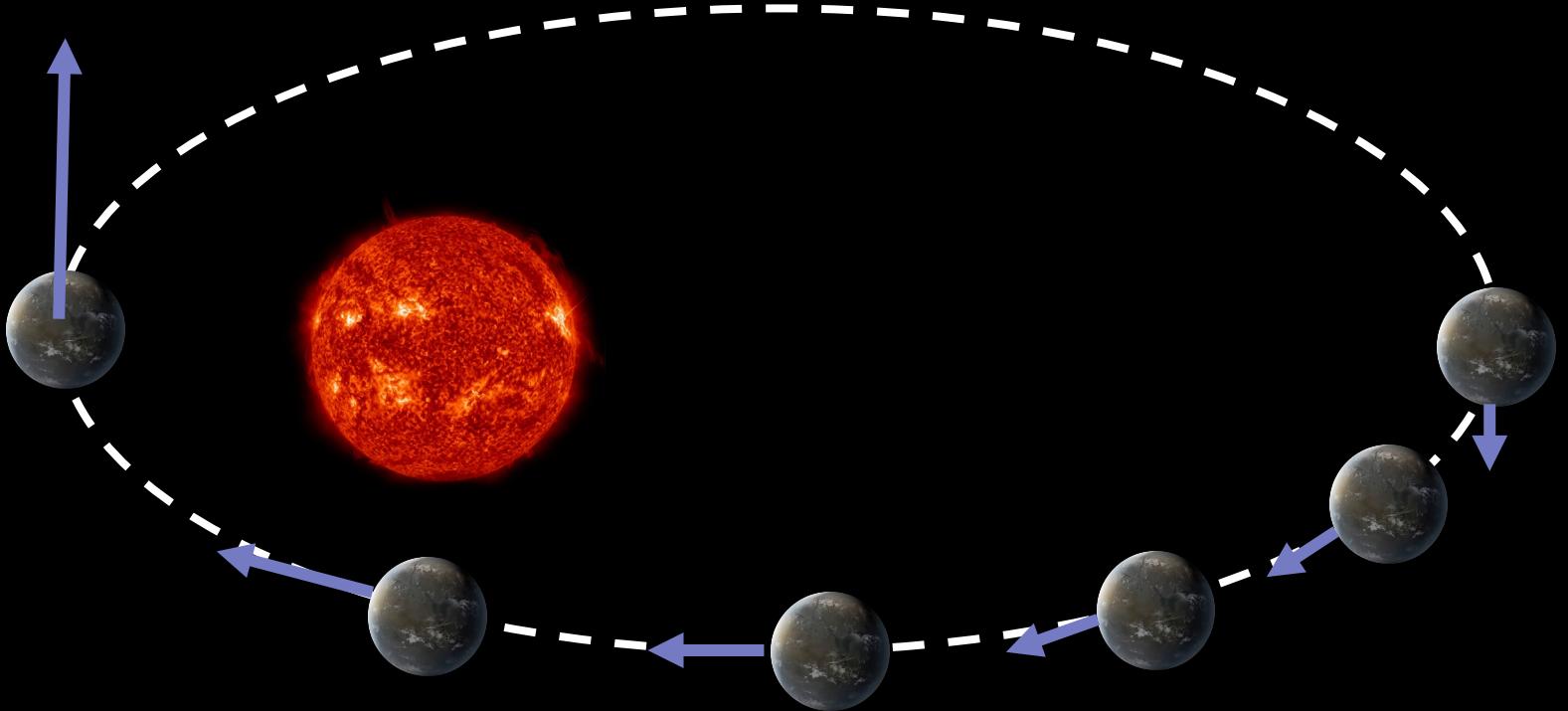
Kepler's Second Law*

**As they orbit, planets sweep
out equal areas in equal
times.**

*This is the one that confuses everyone. It's really a statement of the conservation of angular momentum.



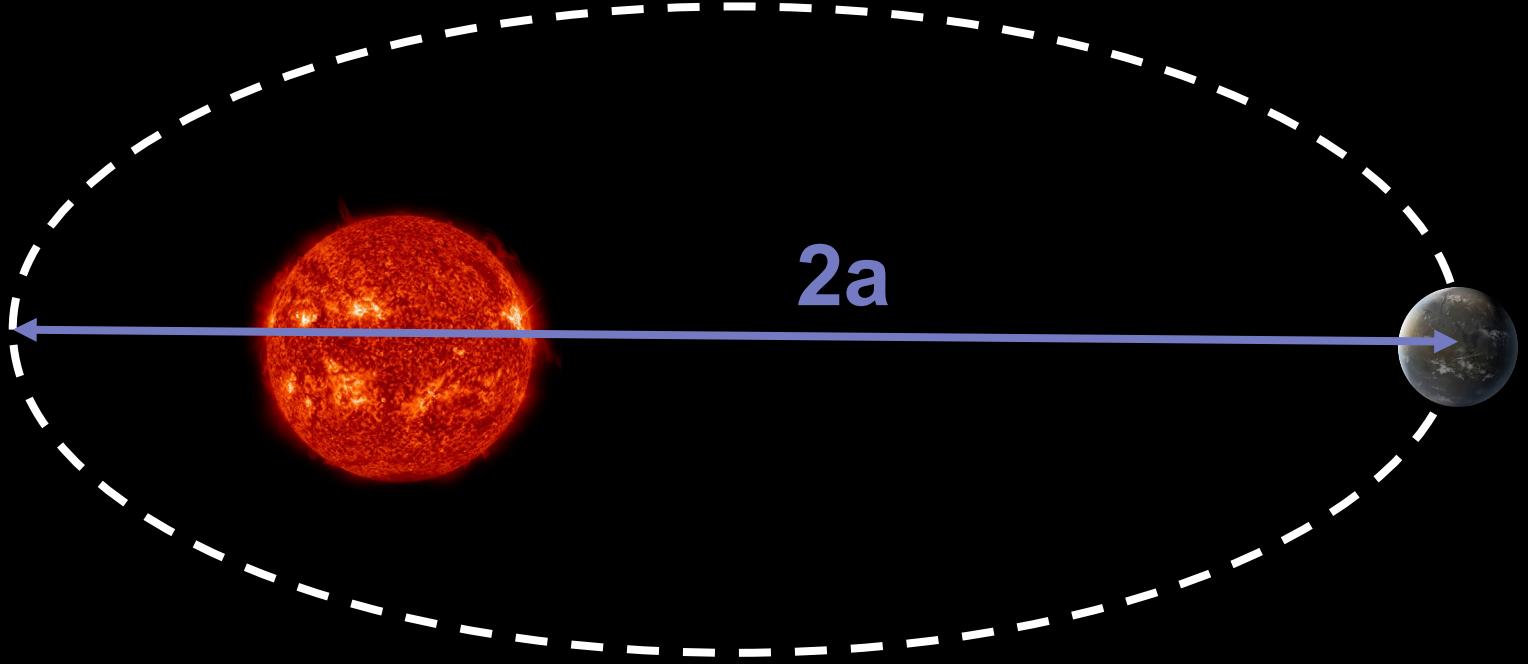
Credit: Pearson Education



**Snapshots of an orbiting planet
spaced at equal times—the planet
moves faster closer to the star.**

Kepler's Third Law

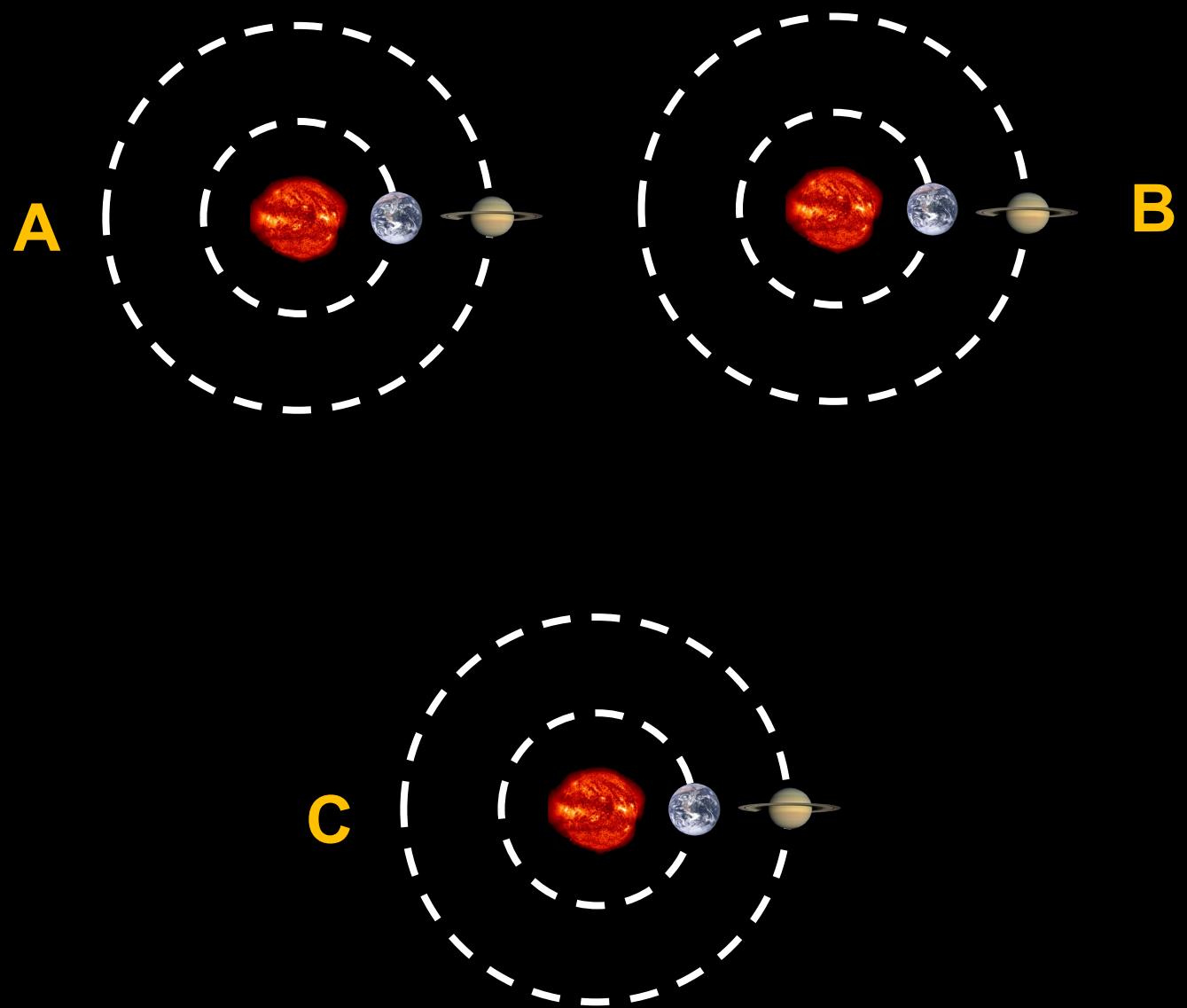
The square of a planet's orbital period is proportional to the cube of its orbital semi-major axis.



$$P^2 = \frac{4\pi^2}{G(M_{\text{planet}} + M_{\text{star}})} a^3$$

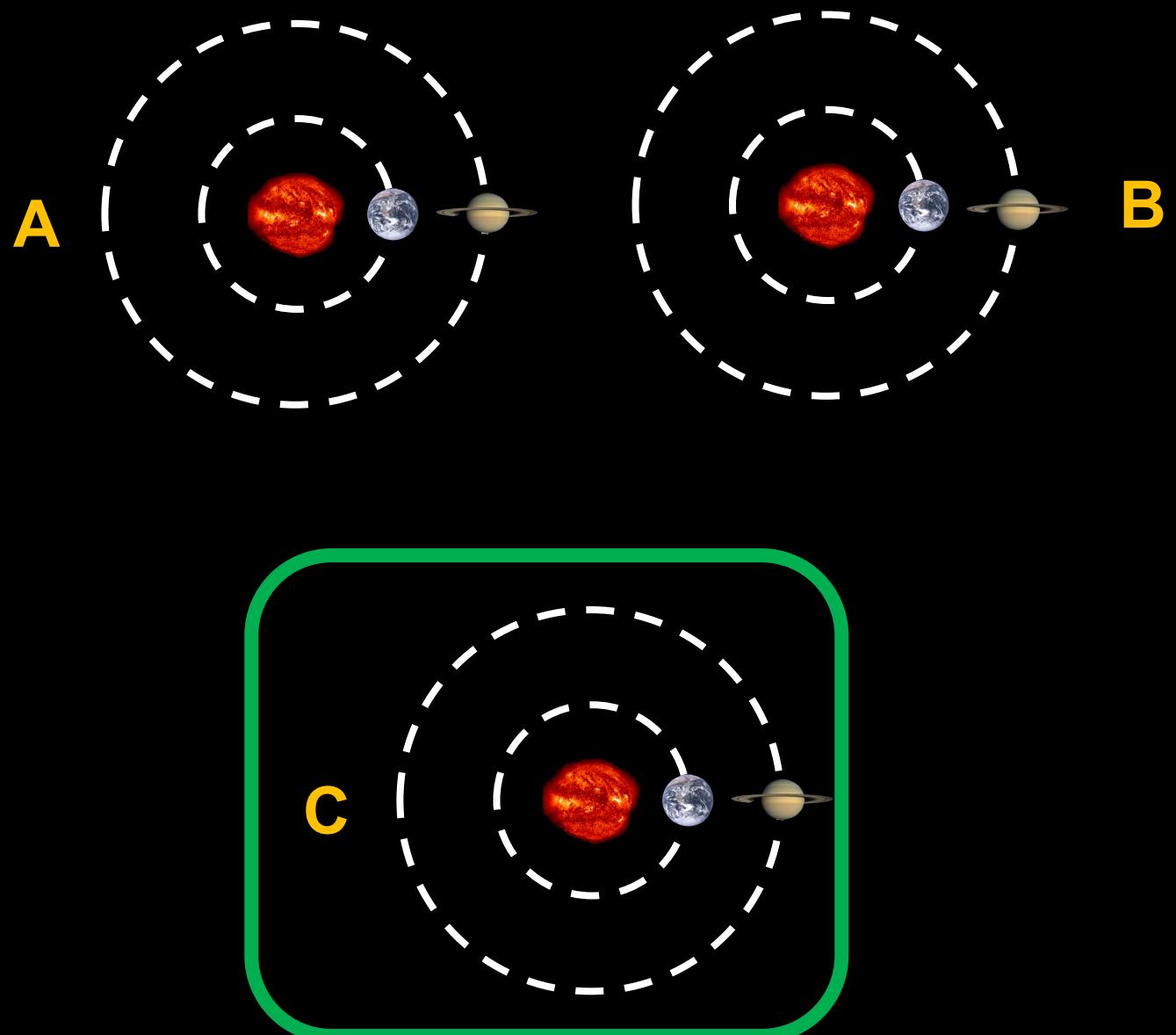
Concept Check

Which of these diagrams shows a set of planets orbiting in accordance with Kepler's third Law?



Concept Check

Which of these diagrams shows a set of planets orbiting in accordance with Kepler's third Law?



If we assume the mass of the planet is much less than the mass of the star, we can use Kepler's Third Law to work out the planet's orbital semimajor axis from its orbital period:

$$P^2 = \frac{4\pi^2}{G(M_{\text{planet}} + M_{\text{star}})} a^3$$
$$P^2 \cong \frac{4\pi^2}{GM_{\text{star}}} a^3$$



if $M_{\text{star}} \gg M_{\text{planet}}$

Let's say $P = 2.1$ years and $M_{\text{star}} = 2.0 M_{\odot}$. To find a , first convert everything to standard units (m, s, kg, etc.)

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Convert P to seconds:

$$P = (2.1 \text{ y})(365.24 \text{ days/y})(86400 \text{ s/day}) = 6.627 \times 10^7 \text{ s}$$

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$$M_{\text{star}} = 2M_{\text{Sun}} = (2)(1.989 \times 10^{30} \text{ kg}) = 3.978 \times 10^{30} \text{ kg}$$

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$$a \cong \left[\frac{(6.674 \times 10^{-11} \text{ m}^3 \text{kg}^{-1} \text{s}^{-2})(3.978 \times 10^{30} \text{ kg})}{4(3.14159)^2} (6.627 \times 10^7 \text{ s})^2 \right]^{1/3}$$

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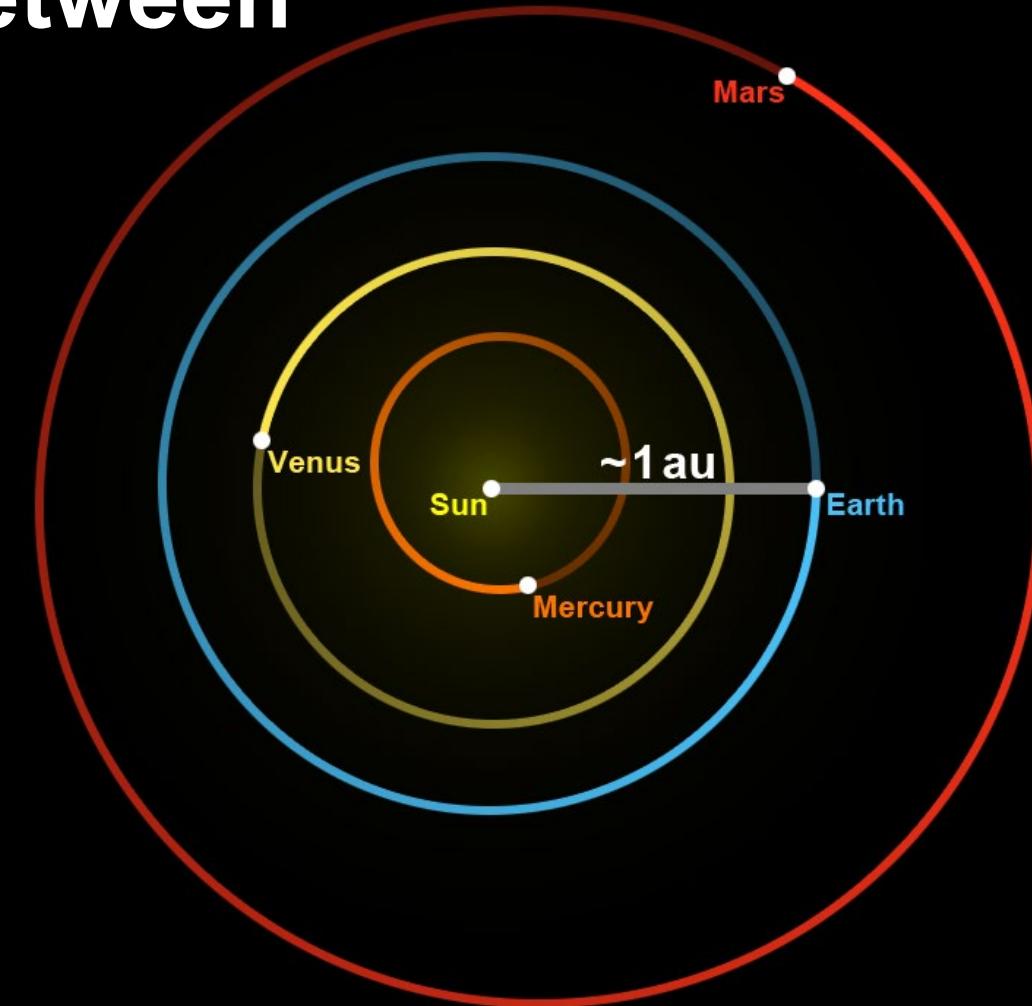
Convert M_{star} to kg:

$$M_{\text{star}} = 2M_{\text{Sun}} = (2)(1.989 \times 10^{30} \text{ kg}) = 3.978 \times 10^{30} \text{ kg}$$

$$a \cong \left[\frac{(6.674 \times 10^{-11} \text{ m}^3 \text{kg}^{-1} \text{s}^{-2})(3.978 \times 10^{30} \text{ kg})}{4(3.14159)^2} (6.627 \times 10^7 \text{ s})^2 \right]^{1/3}$$

$$a \cong 3.09 \times 10^{11} \text{ m} = 2.1 \text{ AU}$$

1 AU = 1 Astronomical Unit
≈ average distance between
Earth and the Sun
≈ 150 million km



Credit: Wikimedia Commons user Huritisho



WolframAlpha

PRO
FOR EDUCATORS

(G*2*(mass of the sun)*(2.1 years)^2/(4*pi^2))^(1/3)



Web Apps

Examples

Random

Assuming Newtonian gravitational constant for "G" | Use Gibbs or [more ▾](#) instead

Input interpretation:

$$\sqrt[3]{(G \text{ (Newtonian gravitational constant)}) \times 2 (M_{\odot} \text{ (solar mass)}) \times \frac{(2.1 \text{ years})^2}{4 \pi^2}}$$

Open code

Result:

3.09×10^{11} meters



Unit conversions:

192 million miles

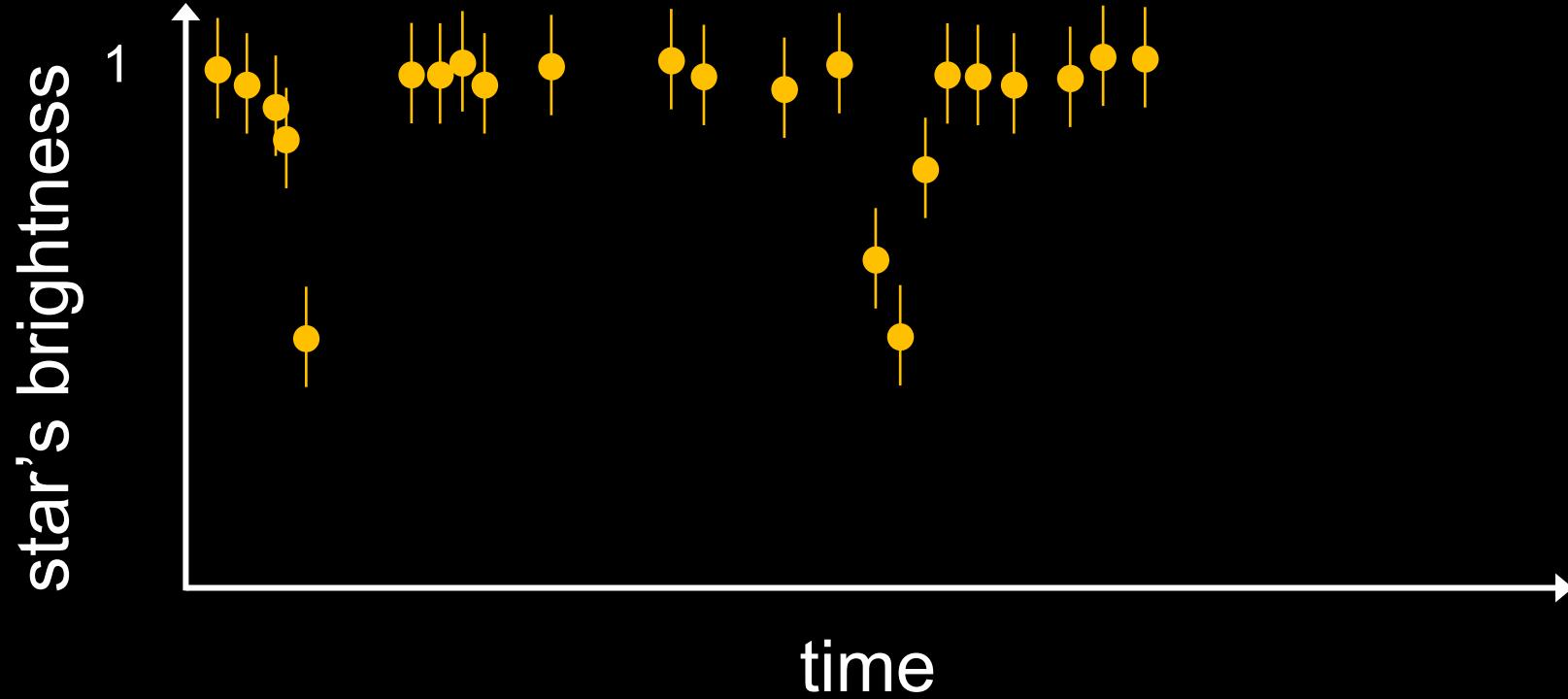
3.09×10^8 km (kilometers)

2.07 au (astronomical units)

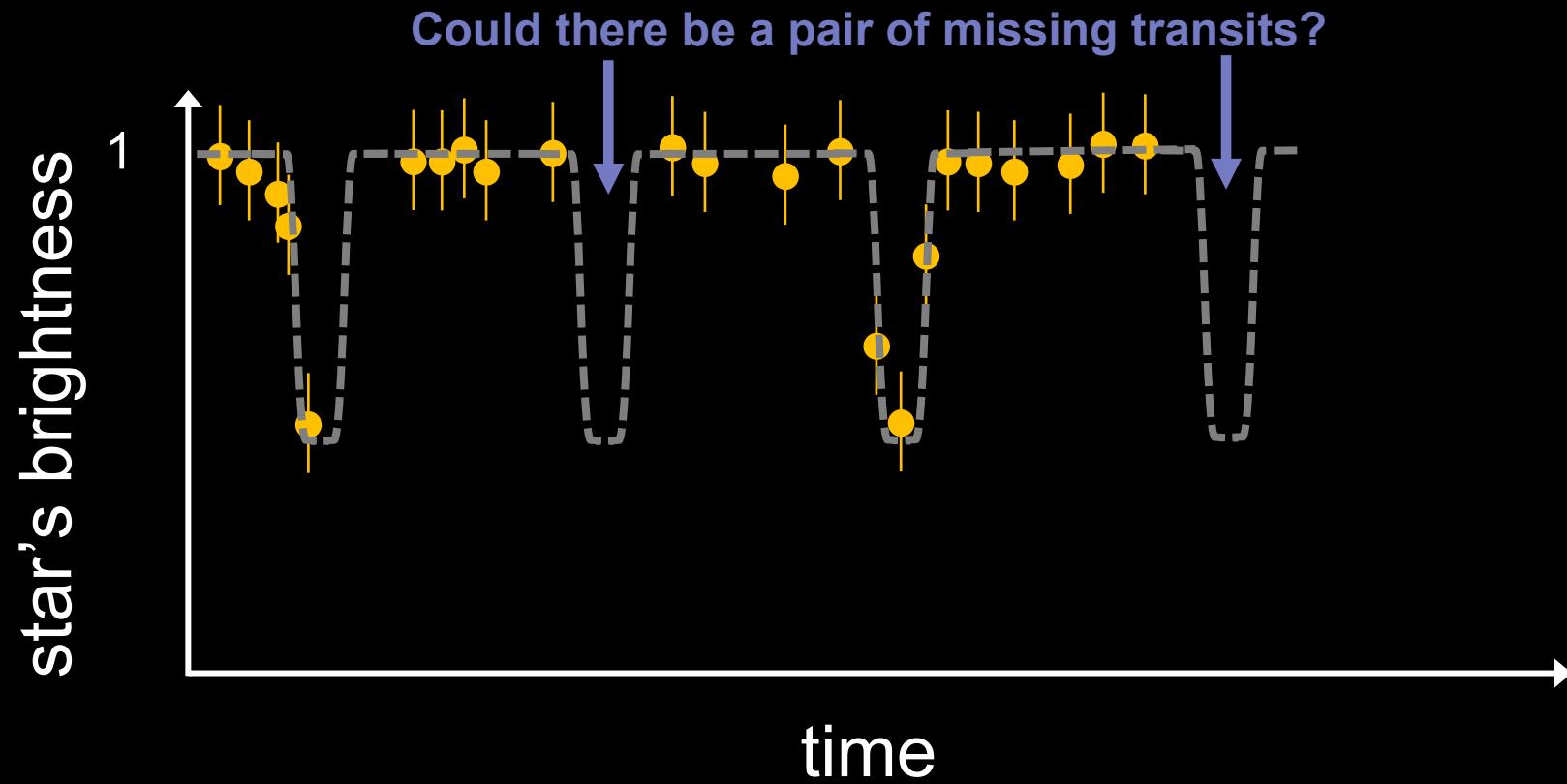
So, from the transit depth, we get the planetary radius.

From the orbital period, we get the orbital semimajor axis.

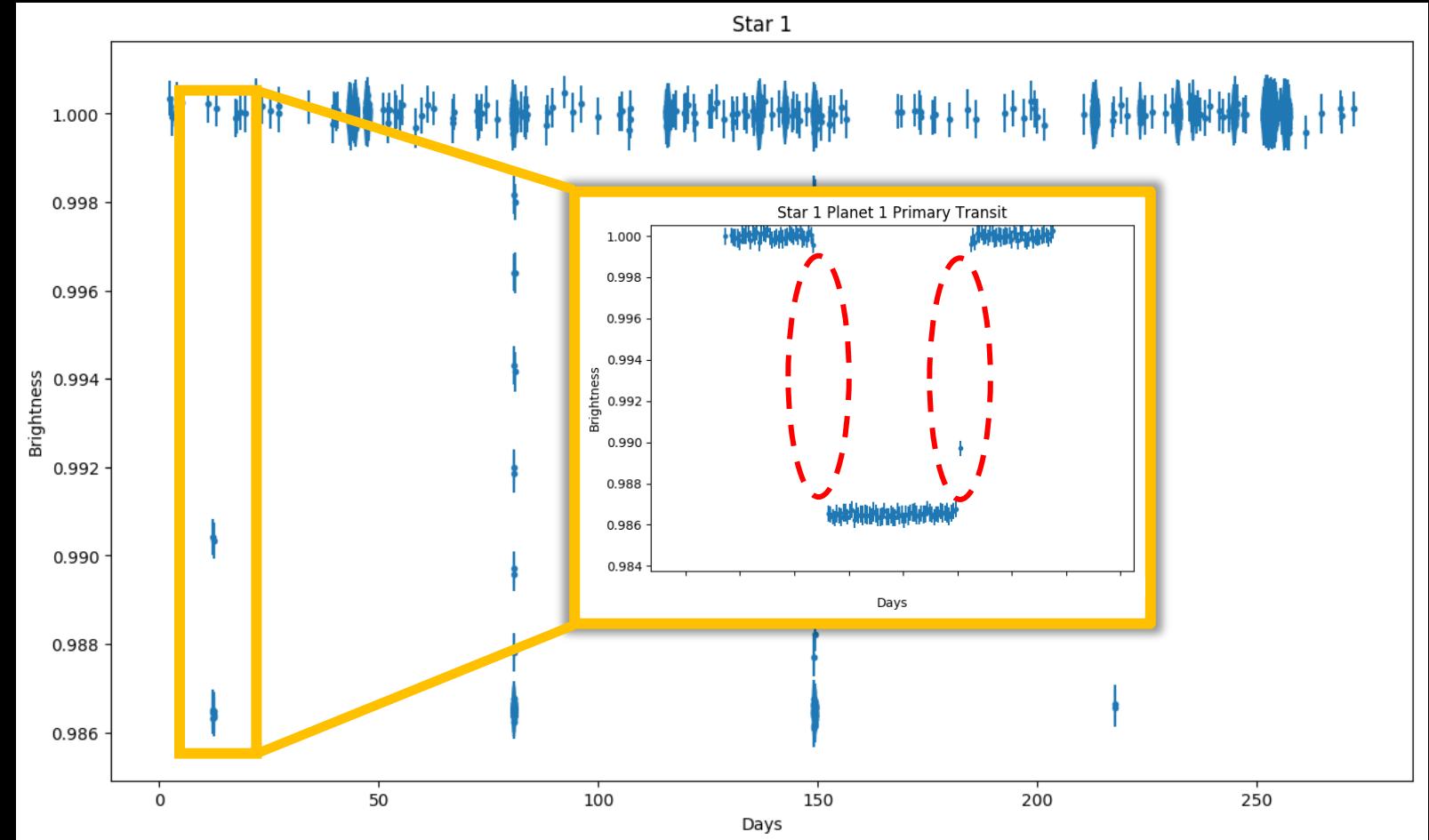
Thus, we can figure out roughly what type of planet we have, and whether it's in the habitable zone!



Low **cadence** observations can make it difficult to measure the orbital period correctly.



Low **cadence** observations can make it difficult to measure the orbital period correctly.

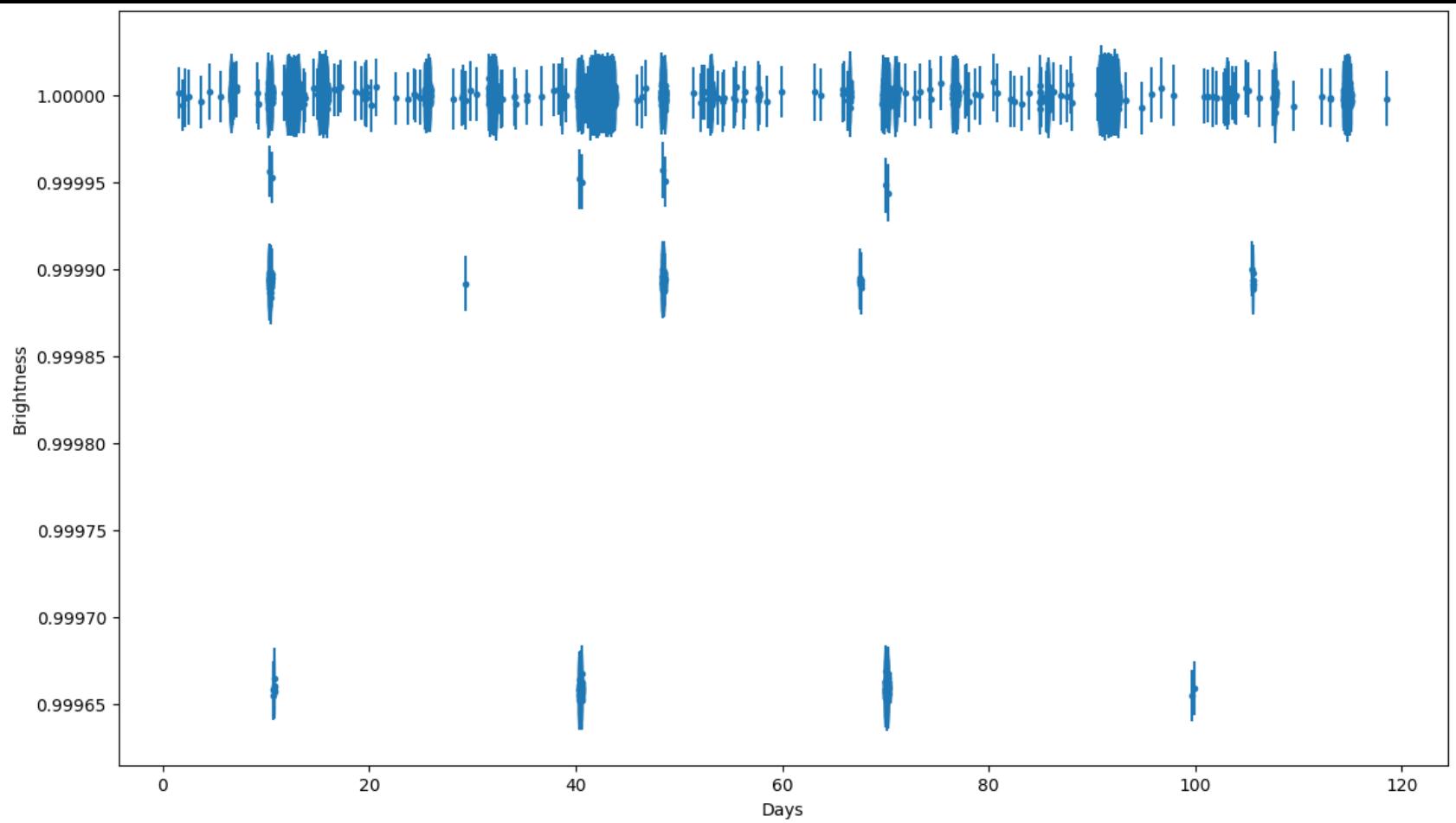


Lower cadence can also cause you to miss ingress and/or egress, which are typically very fast.

The interpretation of light curves is further complicated when there are multiple planets present, which is extremely common.

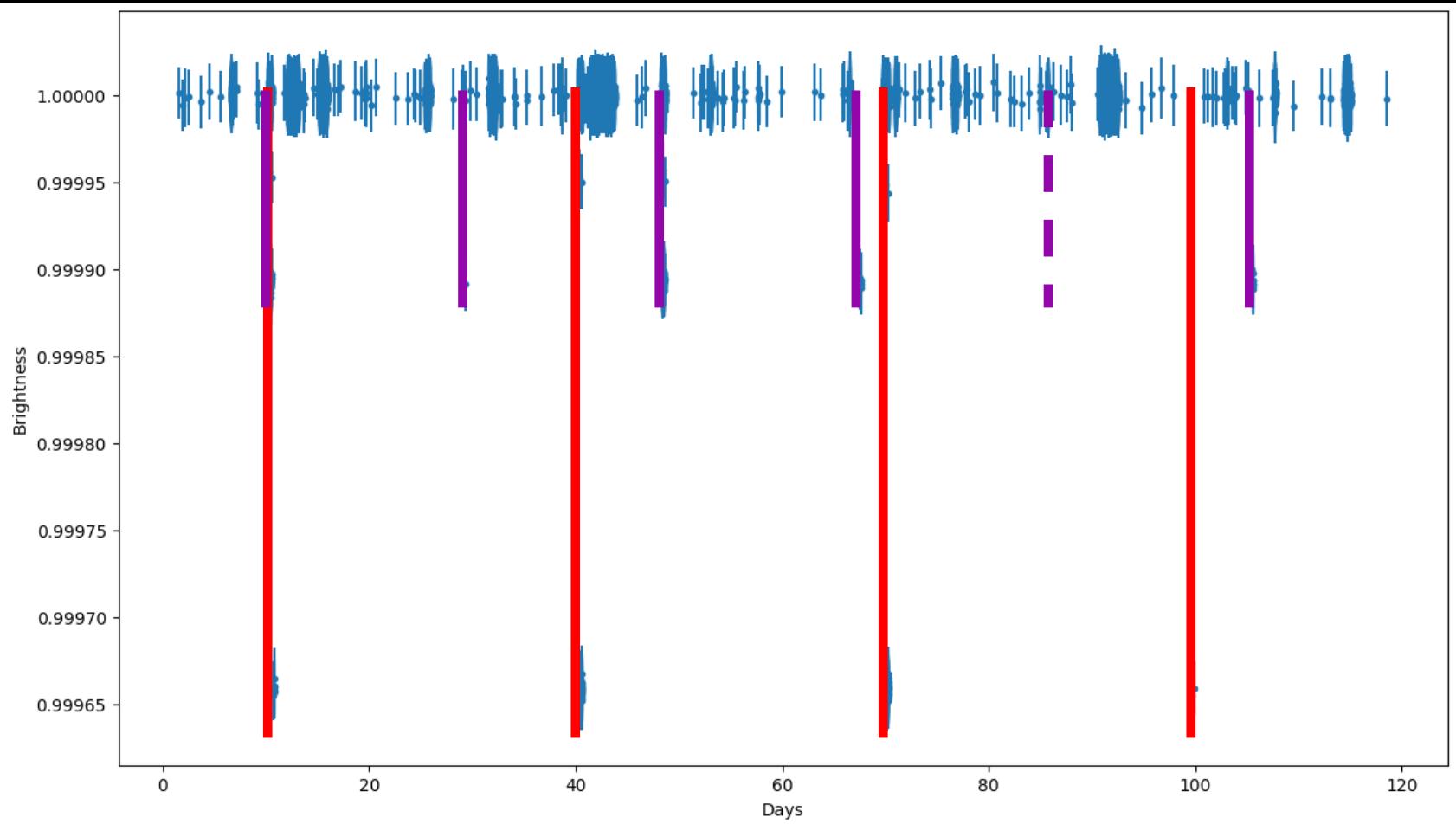
Concept Check

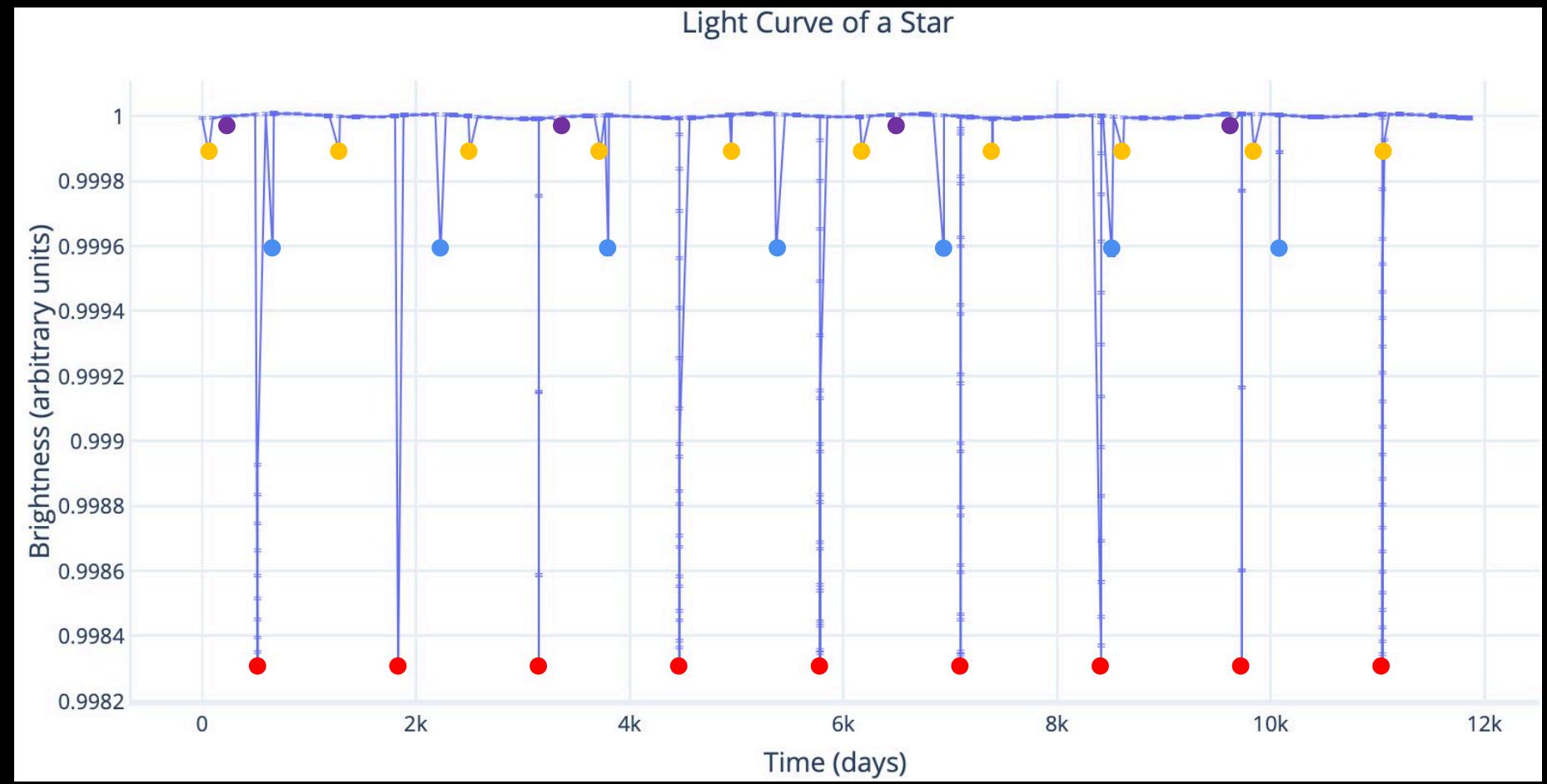
How many planets
do you see in this
light curve?



Concept Check

How many planets
do you see in this
light curve?



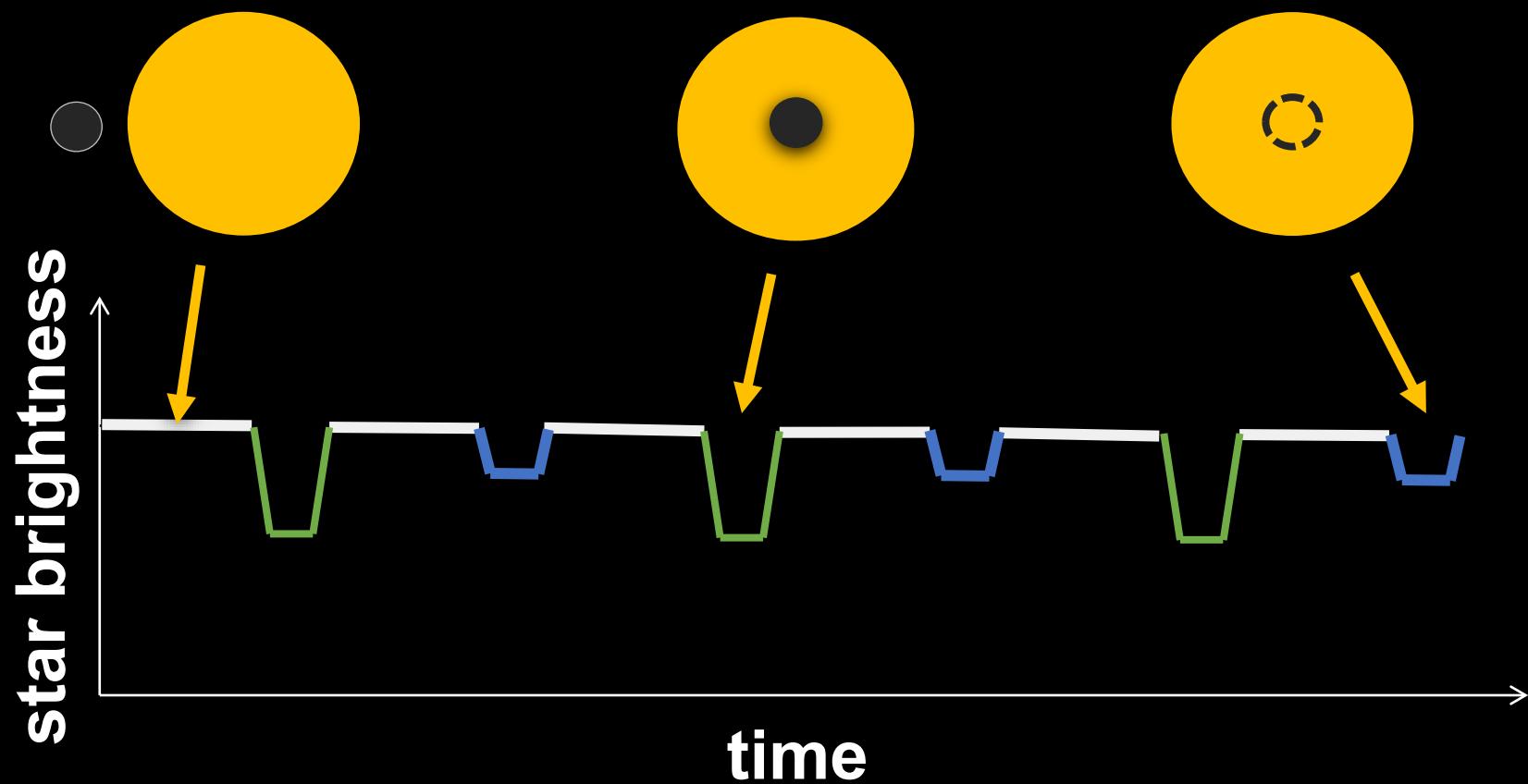


Planets themselves emit & reflect light, which means that there's a **secondary eclipse** when the planet passes behind the star.

no eclipse
**(we see all of the light
from the star and the
planet)**

primary transit
**(planet covers
star)**

secondary eclipse
(star covers planet)



You're now ready to:

1. Identify candidate planets using the transit method, including multi-planet systems
2. Distinguish planets from non-planets
3. Measure their sizes
4. Measure their distances from the host star and decide whether they're in the habitable zone