## HANOI UNIVERSITY OF SCIENCE AND TECHNOLOGY School of Information and Comunication Technology

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### GRADUATION THESIS

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### Chapter 1

## Introduction

Meta-heuristic optimization algorithms are becoming more and more popular in engineering application due to their advantages: they (i) have simple concepts and the ease of implementation; (ii) do not require gradient information; (iii) have the ability to avoid local minima and (iv) can be utilized in a wide range of real-world problems covering different aspects. Among those optimization models, there is a group of algorithm that are called nature-inspired meta-heuristic algorithms. They solve optimization issues by mathematically modelling biological or physical phenomena. They can be divided into three main categories (see Fig \*\*\*): evolution-based, swarm-based and physics-based methods.

Evolution-based algorithm are derived from evolutionary laws in nature. The search process starts with randomly generated solutions which is continuously evolved over the course of generation. Each generation commonly contains the following components: reproduction, fitness evaluation and selection. Specifically, in the reproduction process, from which new-born solutions are generated, often adopts generic operators such as crossover or mutation; the fitness evaluation process obtains the quality of each solution in current population by assigning their fitness values; and selection process is willing to determine candidates with superior values among the population to survive in the next generation. The strength point of this kind of algorithms is that the best individuals are always chosen to generate potential candidate for the subsequent generation. This move the population towards and come closer to the optimal value. The most popular evolution-based algorithm is Generic Algorithm (GA) [27], which mathematically mimicks the Darwinian's evolutionary laws. Other later algorithms are Generic Programming (GP) [38], Differential Evolution (DE) [18], Biogeography-based optimization (BBO) [56] and Coral Reefs Optimization Algorithm (CRO) [55].

The second category is physics-based methods, which imitate physical principles in the universe including Big-Bang Big-Crunch(BBBC) [17], Gravitational Search Algorithm (GSA) [50],

Charged System Search (CSS) [32], Central Force Optimization (CFO) [19], Artificial Chemical Reaction Optimization Algorithm (ACROA) [1], Black Hole (BH) algorithm [25], Ray Optimization (RO) algorithm [31], Small-World Optimization Algorithm (SWOA) [15].

The third group of nature-inspired meta-heuristic optimization is swarm-based algorithms (or swarm intelligence (SI)). SI refers to the collectively intelligent activities emerging from a group of individuals called population, so swarm-based optimization is algorithms being inspired by living and foraging behaviors of animals in the nature. Unlike evolution-based methods, SI methods are based on artificial search agents' movement in a pre-defined search space. Such algorithms take advantages of exploration and exploitation phases and lead the population closer and closer to the optimal result over the course of iteration. For example, one of the most famous and widely used algorithm in SI group is Particle Swarm Optimization (PSO) [16], which uses the information both from the best agent and all the agents' best experience to search for the optima of a fitness function. Another popular swarm-based algorithm is Ant Conoly Optimization (ACO) [14], which is inspired by social foraging process of ants. This algorithm uses the idea of the social intelligence of ants in finding the closest path from the nest and a source of food. A pheromone matrix is enhanced over the course of iteration by the candidate solutions. Several other SI algorithms have been regularly proposed, some of them are listed in Table \*\*\*. In general, this group of methods started to become more attractive since PSO is proven to be very competitive with evolution-based and physics-based algorithms. In fact, swarm-based methods have some advantages over the others. For example, swarm-based algorithms find new better by preserving the information from previous iterations, while evolution-based methods such as GA discard any information immediately when a new generation is formed. Also, they are usually formed of less updating operators compared to the others (crossover, mutation, selection etc.) and therefore it is easier to implement.

It is worth mentioning here that there is a group of methods derived from human's activities in daily life. They are human-based optimization algorithms. Some of the well-known algorithms are Harmony Search (HS) [21], Teaching Learning Based Optimization (TLBO) [49], League Championship Algorithm (LCA) [30], Tabu Search (TS) [13] and Colliding Bodies Optimization (CBO) [34].

Because of their prominent advantages, such algorithms have been applied to various aspects including solving travelling salesman problem [62], application to electric power system [65], image processing [29] [28] and even optimizing artificial neural networks [5] [44].

Due to the wide range of applications of these algorithms, in recent years, many bioinspired optimization algorithms have been introduced, going along with their variants and applications. Sea Lion Optimization (SLnO) is among these algorithms. It was first introduced in [43] for solving global-scale optimization problems. SLnO imitates the hunting behaviors of sea lions consisting of the way they encircle and capture preys or how they use their tail as well as their whiskers. It has been proven that SLnO can provide very competitive results compared with other well-known algorithms such as Particle Swarm Optimization (PSO), Grey Wolf Optimization (GWO) and Whale Optimization Algorithm (WOA) when working on different benchmark functions. However, like many other methods in swarm-based optimization, SLnO still faces demerits with regard to slow convergence speed, low precision and easily being stuck into local minimums due to the degradation of population diversity over the course of iteration. To improve the performance of these algorithms, there is a number of techniques proposed, and they are proven that they can work very effectively on different algorithms such as Levy-Flight trajectory-based method [9] or opposition-based learning [61] [48] [59].

According to the knowledge of authors, there have not been any improvement versions of SLnO as well as any proposed models based on this algorithm to solve a practical engineering problems. Therefore, in this paper, we propose an improved version of SLnO call Improved Sea Lion Optimization (ISLO) by embracing the idea from PSO, taking the best experience of each individual into account to improve SLnO's exploitation ability, and the idea of opposition-based learning for enhacing the use of exploration phase in SLnO. ISLO's performance is tested by 30 benchmark functions belonging to 4 kinds of functions: unimodal functions, multimodal functions, hybrid functions and composition functions. The results provided by ISLO are compared with other well-known meta-heuristic algorithms including GA, PSO, WOA, TWO, QSO and the original SLnO. The results show that ISLO provides superior final fitness values as well as decent convergence speed compared with the others.

As aforementioned, meta-heuristic algorithms are used as optimizers in ANNs. In the last three decade, ANNs have been developed and widely applied to classification, parttern recognition regression and forecasting problems. The ANNs' efficiency mostly affected by their learning process. For Multi-Layer Perceptron (MLPs), which is the most popular category of ANNs, the main method for training is gradient-based methods. The backpropagation algorithms and its variants [53] are considered as the most well-known method for training MLPs. However, using gradient-based algorithms for optimizing MLPs still remains several advantages such as tendency being trapped in local minima, slow convergence and significant dependence on the initial stage of its parameters. In order to avoid complex gradient information as well as the disadvantages of gradient-based optimization, meta-heuristic optimization algorithms have been proposed as a reliable alternative for optimizing MLPs in the perspectives of parameters and network's structure. For example, as introduced in [42], GA and PSO algrithms are utilized to optimize parameters of Wavelet-MLP for wind speed prediction, or in [2] WOA is applied to simple MLPs for solving classification problems. Some other interesting applications of these optimizers on MLPs can be

found in [7], [46] and [35].

### Chapter 2

## Materials and background

### 2.1 Meta-heuristic Optimization

### 2.1.1 Particle Swarm Optimization (PSO)

PSO [36] is a very first swarm-based optimization, which is the premise of many other algorithms proposed in recent years. It emulates the behaviors of birds, fish and so forth when they forage for food and communicate as a swarm. In PSO system, a swarm contains several candidate solutions (also known as particles), which coexist in the search space of the problem with D dimensions. The solution often cooperate and fly together to land on personal optimal positions. Over the course of time, the best personal position (its own best position in the past) of each particle and the global best position (the current best position of entire swarm) are recorded. The next position of a particle is updated based on the personal best (cognitive behavior) and the global best (social communication). With this approach, PSO combines local search (through personal best) with global search (through global best) to balance exploitation and exploration processes. PSO operation workflow is presented in Figure 2.1.

Thus, each particle i in swarm is described by two properties: its velocity  $v_i$  and position  $x_i$  in the search space. In each iteration, they are updated following the equation:

$$v_i^{t+1} = \omega \cdot v_i^t + c_1 \cdot r_1 (p_i^t - x_i^t) + c_2 \cdot r_2 (g^t - x_i^t)$$
(2.1)

$$x_i^{t+1} = x_i^t + v_i^t (2.2)$$

where

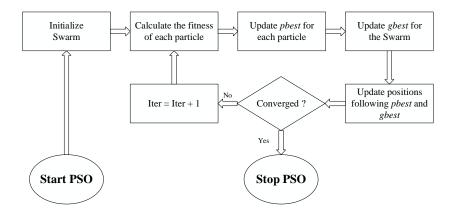


Figure 2.1: PSO flowchart

- $\omega$  is inertia weight reduced linearly to zero through time;
- $v_i^t$   $v_i^t = [v_{i1}, v_{i2}, ..., v_{iD}]$  and is the velocity;
- $x_i^t$   $x_i^t = [x_{i1}, x_{i2}, ..., x_{iD}]$  and is the position of particle i in current time t respectively;
- $p_i^t$  is its personal best position in current time t;
- $g^t$  is global best position ever of entire swarm up to time t;
- $c_1, c_2$  are acceleration coefficients that pull particles faster to personal best and global best respectively;
- $r_1, r_2$  are random number which is uniformly distributed in [0, 1];

### 2.1.2 Sea Lion Optimization Algorithm (SLnO)

Sea lions are considered as one of the most intelligent animals in wildlife which live on both lands and the oceans. They usually live in a large swarm with thousands of members, and this large swarm may contains many subgroups with their own hierarchy as well. In each subgroup, there is a dominant sea lion playing a role as the leader of the subgroup. All activities of subgroups are decided following the leader ship of that sea lion.

The intelligence of sea lions can be seen through the way they organize their groups and hunt the prey. Hunting as a group allow sea lions to have more opportunities of obtaining more food especially when the amount of fish is quite large. Usually, sea lions capture their prey together by circling the prey in a narrow ball, and the size of this "ball" continues to be decrease until the prey is totally wiped out. The main phases of hunting behaviors of sea lions can be illustrated as 3 steps as follows:

• Tracking and chasing the prey using their senses.

### Algorithm 1: Sea Lion Optimization (SLnO)

```
1 Initialize the Sea Lion population X_i (i = 1, 2, ..., n) randomly.
 2 Calculate fitness of each solution (sea lion).
 3 X_* \leftarrow the best solution
 4 for Iter = 0 \rightarrow Iter_{max} do
       Calculate the value of C
 5
       for SeaLion in population do
 6
           Calculate SP_{leader} using Eq. 2.5
 7
          if SP_{leader} < 0.25 then
 8
              if |C| < 1 then
 9
10
                   Update the location of the current search agent using Eq. 2.3
              else
11
                  Choose a random search agent SL_{rand}
12
                  Update the location of current search agent by Eq. 2.10
13
              end
14
           else
15
              Update the location of the current search agent by Eq. 2.8
16
17
           Evaluate population: fix if any solutions go beyond the boundary
18
           Recompute the fitness of all solutions
19
           Check and update X_* if a better solution is found.
20
21
       end
22 end
23 Results: X_*, f(X_*)
```

- Calling other members to gather and implement encircling strategy around the prey.
- Attack towards the prey which is captured in the circle.

Those behaviors is the inspiration for the Sea Lion Optimization (SLnO) which was first introduced in [43]. The algorithm mimics the amazing social behaviors and interesting hunting activities of sea lions. The formulas of the phases *Detecting and tracking phase*, *Vocalization phase* and *Attacking phase* illustrate perfectly encircling mechanisms which is utilized by sea lions. We summarize and discuss briefly each phase in the algorithm as below, meanwhile the pseudo-code of SLnO is provided in details in **Algorithm 1**.

#### 1. Detecting and tracking phase

Sea lions can identify the location of the prey and gather other members that will join the subgroup to organize the net following the encircling mechanism. This sea lion plays an important role as a leader for this hunting behavior and other members' position will be updated following the position of the prey. In SLnO algorithm, the prey is considered as the current best solution or the solution closest to the optimal solution. This behaviors is presented mathematically using Eq. (2.3) and Eq. (2.4) as follows:

$$Dist = |2B.P(t) - SL(t)| \tag{2.3}$$

$$SL(t+1) = P(t) - Dist.C$$
(2.4)

Where Dist indicates the distance between the prey and the current sea lion; P(t) and SL(t) represent the position vectors of best solution and the sea lion in iteration t respectively; B is random vector in the range [0,1] which is multiplied by 2 to increase the search space, helping the search agent find optimal or near optimal position. SL(t+1) is the new position of search agent after updating and C is linearly decreased from 2 to 0 over the course of iteration, indicating the encircling mechanism of sea lion group when they move towards the prey and surround them.

### 2. Vocalization phase

When a sea lion recognize a group of their prey (such as fish), it will call other sea lions in their group for gathering and creating a net to capture the prey. That sea lion is considered as the leader and it will lead the group of sea lions moving towards and decide the behaviors of the group. These behaviors are modeled mathematically as shown in Eq. (2.5), (2.6) and (2.7):

$$SP_{leader} = |(V_1(1+V_2)/V_2)|$$
 (2.5)

$$V_1 = \sin(\theta) \tag{2.6}$$

$$V_2 = \sin(\phi) \tag{2.7}$$

Where  $SP_{leader}$  is the value that illustrates the decision of the leader followed by other sea lions in the group;  $\theta$  and  $\phi$  are the angles of its voice's reflection and refraction in the water, respectively.

### 3. Attacking phase (Exploitation phase)

The hunting activities of sea lions are led by the leader. In SLnO algorithm, the target prey is considered the current best candidate solution. In order to mathematically mimic the hunting behaviors of sea lions, two phases are introduced as follows:

- Dwindling encircling technique: This behavior depends on the value of C in Eq. 2.4. C is linearly decreased from 2 to 0 over the course of iteration, so this allows the search space around the current best position to shrink and force other search agents to updated in this search space as well. Therefore, a new updated position of a sea lion can be located anywhere in the search space between its current position and the location of the present best agent.
- Circling updating position: Sea lions chase bait ball of fishes and hunt them starting from edges. Eq. 2.8 is proposed in this regard:

$$SL(t+1) = |P(t) - SL(t)| \cdot \cos(2\pi m) + P(t)$$
(2.8)

Where |P(t) - SL(t)| illustrates the distance between the best optimal solution (the prey) and the current search agent in t-th iteration, || means the absolute value and m is a random number in the range [-1, 1].

4. Searching for prey (Exploration phase) In exploration phase, the search agents update their positions based on a randomly selected sea lion. The condition that allows exploitation phase to happen is when the value of C becomes greater than 1, and the process of finding a new agent is presented by Eq. (2.9) and (2.10) as below:

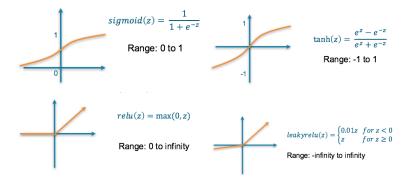
$$Dist = |2B.SL_{rnd}(t) - SL(t)| \tag{2.9}$$

$$SL(t+1) = SL_{rnd}(t) - Dist.C (2.10)$$

Where  $SL_{rnd}(t)$  is a random sea lion that is selected randomly from current population.

### 2.2 Artificial Neural Network (ANN)

### 2.2.1 Activation functions



Figure~2.2:~Activation~functions.~Source:~https://medium.com/@srnghn/deep-learning-overview-of-neurons-and-activation-functions-1d98286cf1e4

Activation functions also known as transfer functions are used to map input nodes to output nodes in certain fashion. Activation functions are extremely important for an ANN to learn and figure out features and characteristics of data which need a non-linear transformation to become outputs. There are the four most popular functions used in Deep Learning, their names are Sigmoid, Hyperbolic Tangent (Tanh), Rectified Linear Units (ReLU), Leaky ReLU and Exponential Linear Unit (ELU) (See in Fig. 2.2).

• **Sigmoid function**: takes a number as input and returns a value in [0,1].

$$f(x) = \frac{1}{1 + e^x}$$

• Hyperbolic Tangent (Tanh) function: is also like Sigmoid function but better, the range of the output from Tanh function is in [-1,1].

$$f(x) = \frac{2}{1 + e^{-2x}} = 2\sigma(2x) - 1$$

• Rectified Linear Unit (ReLU) function: is a function having threshold at 0 value. It helps accelerate the training process in ANN, so it is used in almost all the complicated deep learning models such as RNNs and CNNs.

$$f(x) = max(0, x)$$

• Leaky ReLU function: is like ReLU function, but instead of setting thresholf value at 0, Leaky ReLU extends the domain to  $\alpha x$ .

$$f(x) = \begin{cases} x, & \text{if } x > 1\\ \alpha x, & \text{otherwise} \end{cases}$$

#### 2.2.2 Loss functions

Neural Networks are trained by backpropagation algorithm, which updates the weights parameters of ANN according to a loss value. The loss value is calculated by a loss function, so loss functions are totally vital when an ANN model is built for learning information from data. These functions will essentially measure how poorly a model is performing by comparing what the model is predicting with the actual value it is supposed to output. Therefore, choosing a loss function that is appropriate for penalizing model effectively is one of the most important tasks while working with data. There are a number of loss functions for deep learning models, and each of them have its own pros and cons. The common loss functions that are widely used in time-series forecasting will be presented as below:

• Mean Absolute Error (MAE):

$$MAE = \frac{\sum |e_t|}{N}$$

• Sum Square Error (SSE):

$$SSE = \sum (e_t^2)$$

• Mean Square Error (MSE):

$$MSE = \frac{\sum (e_t^2)}{N}$$

Algorithm 2: Backpropagation algorithm applied for FFNN with 1 hidden layer

```
1 Initialize randomly weights' value w_p
 2 repeat
           Calculate output value(s) according to weights and input
 3
           for j = 1 to h do
                H_j = \phi(\sum_{i=1}^{n} x_i * w_{ij}^{[1]} + b_{ij}^{[1]})
 6
           \widehat{y_j} = \phi(\sum_i^h H_i * w_j^{[2]} + b_j^{[2]}) Calculate Loss value by loss function
           L(w) = loss(\widehat{y_j}, y_j)
           Backpropagating Loss to weights
10
           \triangle(w_{ij}^2) = \frac{\partial(L(w))}{\partial(w_{ij}^2)}
\triangle(w_{ij}^1) = \frac{\partial(L(w))}{\partial(w_{ij}^1)}
11
12
           Update weights' value w_{ij}^2 = w_{ij}^2 - \eta * \triangle(w_{ij}^2) w_{ij}^1 = w_{ij}^1 - \eta * \triangle(w_{ij}^1)
14
16 until Until convergence or the number of iterations is enough;
```

• Root Mean Square Error (RMSE):

$$RMSE = \sqrt{MSE}$$

• Mean Absolute Percentage Error (MAPE):

$$MAPE = \frac{1}{N} \sum \left| \frac{e_t}{y_t} \right|$$

Where N is the number of data points,  $y_t$  is the actual output value,  $d_t$  is the output value predicted by models,  $e_t = d_t - y_t$  is the error value of the data point t.

### 2.2.3 Backpropagation - the ANN Training Algorithm

Back-propagation algorithm is undoubtedly the most fundamental building block in an ANN. It It was first introduced in 1960s and almost 30 years later (1989) popularized by Rumelhart, Hinton and Williams in [54]. The algorithm is used to effectively train a neural network through a method called chain rule. In simple terms, after each forward pass through a network (propagation phase), back-propagation performs a backward pass while adjusting the model's parameters (weights and biases) (weights updating phase).

### 2.2.3.1 Forward propagation phase

1. The input values will be fed into ANN through input layer, going forward to hidden layers, and finally to output layer, creating predicted output values. While propagation process,

each layer uses its own activation function (sec. 2.2.1)

2. Error values are calculated by the loss function and propagated back to previous layers.

#### 2.2.3.2 Weights updating phase

- 1. Calculating gradients of loss function in weights and biases following the chain rule.
- 2. Updating weights and biases is done according to gradients' values

These two phases are repeated in each iteration during training. The algorithm will be stopped when the error from loss function reach a acceptable value or when the training iteration is large enough. The algorithm's pseudo code is presented in short in Algorithm 2.

# 2.3 Time-series prediction and Auto-scaling problem in Cloud Computing

### 2.3.1 Cloud Computing

### 2.3.2 Auto-scaling problem

## 2.3.3 Well-known machine learning models for Auto-scaling in cloud computing

Recent developments in cloud computing including resource management have resulted in a significant interest in resource usage prediction. Various methods have been proposed for solving this problem with different aspects, objectives and applications [3]. In this section, we focus on several Artificial Neural Network (ANN) models that are used for tackling the time-series characteristic in resource usage forecast in cloud computing environment. Deep Feed-forward Neural Network, also called Feed-forward Neural Network (FFNN) are the quintessential deep learning models. The goal of all FFNN is to approximate some functions  $f^*$ . In Regression problems,  $y = f^*(x)$  maps an input x to a value y. A feed-forward network defines a mapping  $y = f(x, \theta)$  and learns the value of the parameters  $\theta$  that result in the best function approximation. [23]. These models are called feed-forward because information flows through the function being evaluated from x, through the intermediate computations used to define f, and finally to the output y. There are no feedback connections in which outputs of the model are fed back into itself.

When feed-forward neural networks are extended to include feedback connections, they are called recurrent neural networks, which will be discussed in 2.3.3.3.

In general, Multi-Layer Perceptrons (MLPs) models contain several disparate layers. The first layer is input layer taking information x as input for the network. The last layer is called output layer, whose value is the result of y with input x. The layers between the input and output layers are hidden layers. The structures of hidden layers are extremely diverse, varying from model to model. As presented in Fig. 2.3, a hidden layer of a simple FFNN is a group of neurons with no connection to each other, while in Recurrent Neural Networks (RNN), and Convolution Neural Network (CNN) hidden layer is a recurrent layer, and convolution layer respectively.

The Deep Neural Networks that are applied for Time series prediction will have input neurons presenting the historical data. The models utilize information from data in the past for forecasting future data. Input data presented as  $x_1, x_2, ..., x_t$  is considered as historical values up to time t, which is used to predict the value at the time t+1. In other words, Deep Neural Networks will learn from data and approximate a function transforming the historical data up to time t to the data at the time t+1 as follows:

$$x(t+1) = y = f(x_1, x_2, ..., x_t)$$
(2.11)

In this section, we summarize several Deep Neural Network models, which are widely used for time series forecasting. They are simple Multi-Layer Perceptrons (MLPs), Cascade Forward Neural Network (CFNN) and Recurrent-based Neural Network including traditional Recurrent Neural Network (RNN), Long-Short Term Memory (LSTM) and Gated Recurrent Units (GRU). Each method will be presented below with brief ideas and mathematical formulas.

### 2.3.3.1 Multi-Layer Perceptrons (MLPs)

The additional layers added between input layer and output layer make network architecture contain hidden layers and called Multi-Layer Perceptrons (MLPs). The input data is fed through input layer to hidden layers in the weighted form. The information from input data X is distributed to the neurons in hidden layers and then processed by an activation function. The activation function in hidden layers are non-linear function playing a role as a transfer function, helping MLPs learn non-linear characteristics of the data. The information after being processed by hidden layers then are sent to output layer in the weighted sum, and also go through an activation function as well, creating the output value y. MLPs model is used in predicting time series data [4], [37]. Fig. 2.3 shows a MLPs with a 4-neuron input layer and one output layer. In

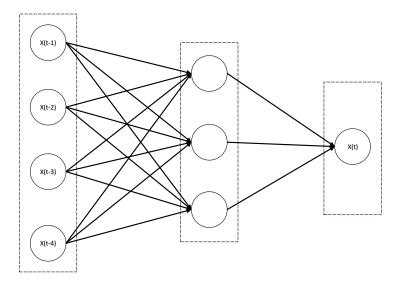


Figure 2.3: An example of MLPs model in time-series prediction.

general, the mathematical equation of the MLPs architecture can be written as follows:

$$H = f_h(W_h^T X + b_h) (2.12)$$

$$y = O = f_o(W_o^T H + b_o) (2.13)$$

Where X is the input data, H and O are the information after being fed through the hidden and output layers.  $W_h$ ,  $b_h$  and  $W_o$ ,  $b_o$  are weights and biases, while  $f_h$  and  $f_o$  are activation functions of hidden layer and output layer, respectively.

### 2.3.3.2 Cascade Forward Neural Network (CFNN)

The main difference between CFNN and MLPs is that in CFNN, perceptron connection is added directly between neurons in input layer and output layer, while in MLPs, that connection is indirect through the hidden layer. The output layer of CFNN perceives both transformed information that is output of hidden layer, and the raw information from input data. This Deep Neural Network model was first used for forecasting monthly palm oil price in the Europe market in [63]. The architecture of CFNN with 4-neuron input layer is illustrated in Fig. 2.4, and the mathematical formulas for CFNN model are presented as follows:

$$H = f_h(W_h^T X + b_h) (2.14)$$

$$C = f_c(W_c^T X) + b_c (2.15)$$

$$y = O = f_o(W_o^T H + b_o) + C (2.16)$$

where  $f_c$  is the activation function from the input layer to output layer, C is the output value of  $f_c$ , and  $W_c$ ,  $b_c$  are weights and biases of the connection, respectively.

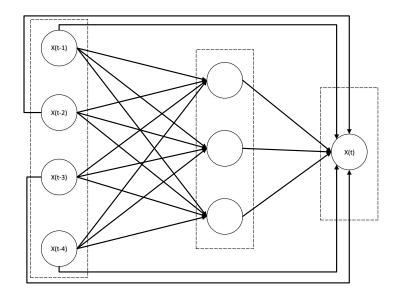
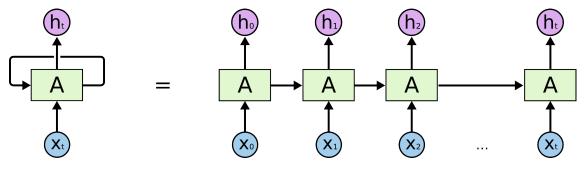


Figure 2.4: An example of CFNN model in time-series prediction.

### 2.3.3.3 Recurrent Neural Network (RNN)

Recurrent neural networks (RNNs) are dynamical systems that are specifically designed for temporal problems, as they have both feed-back and feed-forward connections (Fig. 2.3.3.3). RNN remembers the past and its decisions are influenced by what it has learned from the past. RNNs can take one or more input vectors and produce one or more output vectors and the output(s) are influenced not just by weights applied on inputs like a regular MLPs, but also by a state vector representing the context based on prior input(s)/output(s), so the same input could produce a different output depending on previous inputs in the series. For that reason, RNN is one of the most popular models being used for modeling time series data [66], [11], [8]. There are two popular and efficient RNN models that work really well: Long Short-Term Memory (LSTM) and Gated Recurrent Unit (GRU) which are discussed below.



 $\label{eq:source:https://colah.github.io/posts/2015-08-understanding-LSTMs/} In the property of the property$ 

### 2.3.3.4 Long Short-Term Memory (LSTM)

Long short-term memory (LSTM) [26] is a special kind of RNN created for learning long-term dependencies. LSTM units have 3 gates managing the contents of the memory. These gates are simple logistic functions of weighted sums, where the weights might be learnt by back-propagation. It means that, even though it seems a bit complicated, the LSTM perfectly fits into the neural network and its training process. With combining a forget gate in LSTM units, LSTM is capable to determine what it needs to remember and forget, so LSTM can work very well with dependent data, especially with time series data [22], [24], [20]. The architecture of LSTM units is illustrated in Fig. 2.6, and its mathematical model is briefly described as follows: The input gate (2.17) and the forget gate (2.18) manage the cell state (2.20), which is the long-term memory. The output gate (2.19) produces the output vector or hidden state (2.21), which is the memory focused for use. This memory system enables the network to remember for a long time, which was badly missing from vanilla recurrent neural networks.

$$i_t = sigmoid(W_i x_t + U_i h_{t-1} + b_i)$$

$$(2.17)$$

$$f_t = sigmoid(W_f x_t + U_f h_{t-1} + b_f)$$

$$(2.18)$$

$$o_t = sigmoid(W_o x_t + U_o h_{t-1} + b_o)$$
(2.19)

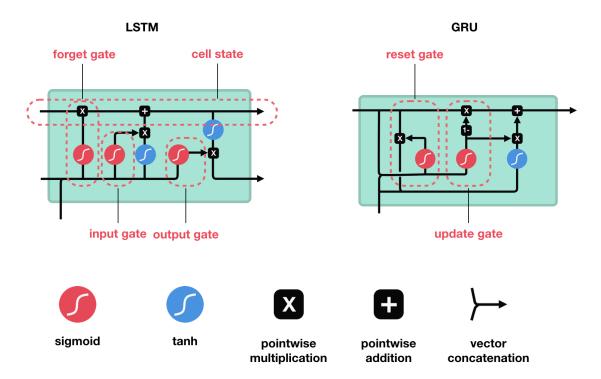
$$c_t = f_t \odot c_{t-1} + i_t \odot tanh(W_c x_t + U_c h_{t-1} + b_c)$$
(2.20)

$$h_t = o_t \odot tanh(c_t) \tag{2.21}$$

### 2.3.3.5 Gated Recurrent Units (GRU)

Gated recurrent unit (GRU) [10] is essentially a simplified LSTM. Different form LSTM, GRU uses two gated called update gate and reset gate. Basically, these gates are two vectors managing what information should be passed to the output. In GRU, its gates can be trained to keep information from long ago, without washing it through time or remove information which is irrelevant to the prediction. It has the exact same role as LSTM in the network. The main difference is in the number of gates and weights - GRU is somewhat simpler. Like LSTM, GRU is also a widely chosen solution for time series forecasting such as in [39] and [6] The structure of GRU units is presented in Fig. 2.6 following the mathematical model as below:

The update gate 2.22 controls the information flow from the previous activation, and the addition of new information as well 2.24, while the reset gate 2.23 is inserted into the candidate



Figure~2.6:~LSTM~and~GRU~architechture.~Source:~https://towardsdatascience.com/illustrated-guide-to-lstms-and-gru-s-a-step-by-step-explanation-44e9eb85bf21

activation. Overall, it is pretty similar to LSTM. From these differences alone, it is hard to tell, which one is the better choice for a given problem.

$$z_t = sigmoid(W_z x_t + U_z h_{t1} + b_z) (2.22)$$

$$r_t = sigmoid(W_r x_t + U_r h_{t1} + b_r) (2.23)$$

$$h_t = z_t \odot h_{t-1} + (1 - z_t) \odot \tanh(W_h x_t + U_h(r_t h_{t-1}) + b_h)$$
(2.24)

## Chapter 3

Improved Sea Lion Optimization
(ISLO) algorithm and Proposed
Model for Auto-Scaling
(ISLO-CFNN)

### 3.1 Improved Sea Lion Optimization (ISLO)

Sea Lion Optimization (SLnO) is one of the newest swarm-based optimization algorithm. In experiments in SLnO original paper [43], SLnO is proved that it outperformed several well-known bio-inspired model such as Generic Algorithm (GA), Particle Swarm Optimization (PSO) and Whale Optimization Algorithm (WOA). However, like many other algorithms, SLnO also faces the problem of local minimum, slow convergence and diversity degradation of population. In SLnO's exploitation phase, the updating operation 2.4 only takes the distance between the current agent and the best solution into account, which makes updated position always oriented to one direction, leading to poverty of exploitation ability. Also, in exploration phase, although the participation of two agents that already exist in population in the updating operation 2.10 helps the new-born solution inherits current decent features of population, new solution has no way to reach another position outside of existing positions. This results in a dramatic decrease in the diversity of population, and significantly influences the ability of escaping local minimum of SLnO algorithm. All things considered, we decided to enhance those 2 operators by taking individual information into account for exploitation phase, and using a technique called opposition-based operation for

### Algorithm 3: Improved Sea Lion Optimization (ISLO)

```
1 Initialize the Sea Lion population X_i (i = 1, 2, ..., n) randomly.
 2 Calculate fitness of each solution (sea lion).
 3 X_* \leftarrow the best solution
 4 for Iter = 0 \rightarrow Iter_{max} do
       Calculate the value of C
 5
       for SeaLion in population do
 6
           Calculate SP_{leader} using Eq. 2.5
 7
          if SP_{leader} < 0.25 then
 8
              if |C| < 1 then
 9
                   Calculate Dist_1 and Dist_2 using Eq. 3.1 and 3.2 Update the location of the
10
                   current search agent using Eq. 3.3
              else
11
                  Choose a random search agent SL1_{rand} and SL2_{rand}
12
                  Update the location of current search agent by Eq. 3.4
13
              end
14
           else
15
              Update the location of the current search agent by Eq. 2.8
16
17
          Evaluate population: fix if any solutions go beyond the boundary
18
          Recompute the fitness of all solutions
19
           Check and update X_* if a better solution is found.
20
21
       end
22 end
23 Results: X_*, f(X_*)
```

exploration phase. These two improvements form a new version of SLnO called Improved Sea Lion Optimization (ISLO) algorithm. The pseudo code of the algorithm is presented in Algorithm 3, and our improvements would be discussed in detail in 3.1.1 and 3.1.2 as below.

### 3.1.1 Exploitation phase improvement

Following that idea, we apply the information sent from best individual experiment in the same way as best agent position. The formulas of new updating mechanism for exploitation phase is as follows:

$$Dist_1 = |2B.P(t) - SL(t)| \tag{3.1}$$

$$Dist_2 = |2B.P_i(t) - SL(t)| \tag{3.2}$$

$$SL(t+1) = c_1 r_1(P(t) - Dist_1.C) + c_2 r_2(P_i(t) - Dist_2.C)$$
(3.3)

where  $P_i(t)$  is the personal best position of agent i up to time t,  $c_1$ ,  $c_2$  2 are positive constant parameters called acceleration coefficients and  $r_1$ ,  $r_2$  are random numbers in range [0,1].

In new operation 3.3, the new-updated position of an individual is the result of adding two vectors, one is the vector presenting the direction of that individual towards the best agent, and another is the direction towards its own experiences in history. The influences of both two factors are determined by two random numbers  $r_1$  and  $r_2$ .  $r_1$  and  $r_2$  play an extremely important role in the updating mechanism, because they create random characteristics for the operation, helping ISLO avoiding local minimum and taking advantages of the two factors. Without the appearance of  $r_1$  and  $r_2$ , the updated position is always affected exactly half by best agent and half by its experience, which may lead to degradation of the diversity of population.

### 3.1.2 Exploration phase improvement

In original SLnO algorithm, new-born agents that are created in exploration phase cause a poor exploration search ability because of inheriting features of existing solutions. In order to tackle this problem, exploration phase is required the operation to have the ability of creating a decent new-born solution. New updated position need to satisfy two characteristics: carrying random features for ensuring a strong capability of exploration phase, and landing in a position decent enough (close enough to the best agent position) for updating positions in the next generation. From that motivation, a method called Opposition-based Learning (OBL) [58], which is successfully applied for enhancing bio-inspired optimization algorithms such as GA [58], PSO [60] [57] in solving several optimization problems including finding parameter for deep learning models [51] [47] is utilized as a base model for our improvement in exploration operation of SLnO.

The idea of OBL is applied in the operation in the way of finding a new random optimal solution, but still retain a part of features from existing solutions. This is done by calculating the opposed position to the current position of an living agent in population. For ensuring random characteristics of new found position, a random agent from population, and a random agent in the search space will be chosen for participating in this operation. The mathematical formulas are given as follows:

- 1. Select a random solution  $SL1_{rand}$  in the search space.
- 2. Select a random existing solution  $SL2_{rand}$  in the population.
- 3. Create a new solution  $SL_{rand}$  by calculating the opposed position to  $SL1_{rand}$  through  $SL2_{rand}$ .

$$SL_{rand} = 2 * SL2_{rand} - SL1_{rand} \tag{3.4}$$

# 3.2 Proposed model for auto-scaling problem in Cloud Computing

In chapter 2, we generally discussed about Cloud Computing and the problem of autoscaling with the existing methods for solving this. In general, it is relatively necessary to build cloud computing servers with the capacity of automatically expanding and shrinking the resources allocated. Although there are a number of solutions proposed for tackling this issue, they all have their own drawbacks.

The FFNN model, which is widely used for solving many real-world issues, is too simple to capture the characteristics of time-series data because after feed-forwarding through hidden layers, the original information of the input neural could be forgotten. On the other hand, RNN-based models such as LSTM or GRU have to face the problem of extremely complex structures that potentially lead to over-fitting, or the huge number of hyper-parameters which are needed to tuned.

The CFNN can take the advantages of its structure and diminish the problem raising when the model structures are too simple (FFNN) or too complex (LSTM, GRU) because of the connection added between the input layer and output layer. However, the gradient descent (GD) algorithm which is used for optimizing CFNN still have its own drawback of being stuck in local minimum and slow convergence speed.

All thing considered, we proposed a new model ISLO-CFNN to improve the weak points of original CFNN model by replacing GD algorithm by above proposed ISLO algorithm in optimizing the parameters of the network while training process. Also, in order to evaluate the performance of our proposed model, we would build both our model and existing models for the purposes of evaluation and comparison.

Fig. 3.1 illustrates the skeleton of forecasting system designed. There are four main phases, each of them is indispensable in our model. The phases are Collecting data, Data preprocessing, Building and Training model and Deploy prediction model. Firstly, historical records about resources used are collected and saved in lines in a log file. These information is extracted and pre-processed before being used for training the prediction model that is designed. In the final stage, the trained model is applied for data in current time, and it will predict the amount of resources needed. Specifically, in Building and Training model stage, CFNN model is built with fixed nodes in all layers, and it will be optimized by ISLO algorithm, which is discussed in detail in Section 3.1. We will discuss about each phase as below.

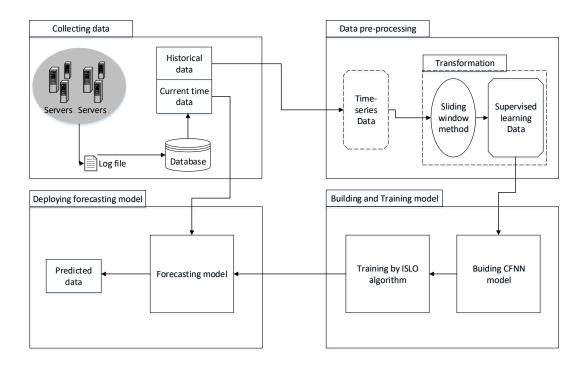


Figure 3.1: Proposed model design

Table 3.1: Time-series data and Supervised learning data comparison

Time-series data	Supervised Learning data
1. Time 1, value 1	1. Input 1, output 1
2. Time 2, value 2	2. Input 2, output 2
3. Time 3, value 3	3. Input 3, output 3

### 3.2.1 Collecting data

Before building any forecasting systems, the very first and the most important task that must be done is collecting data. Therefore, we collect data recording the resource usage of Google (Google Cluster Trace data) and Internet Traffic data collected from a private internet service provider (ISP) in Europe and the United Kingdom (these datasets will be discuss in detail in Chapter 4. The data collected contains two main parts: the data from history that we use for training, and current time data that we use for predicting resource usage in the future.

### 3.2.2 Data pre-processing

This phase play a role as a pre-processor transforming the raw data into the kind of data that can be used in neural networks. In order to learn, models need both training data and testing data. We create the data for models through several steps as follows:

• Evaluate and choose carefully which columns of data are needed for the forecasting model.

Time-series data	Transformed data				
		Input			
Time $(t=4)$ , Value 4	Value 1	Value 2	Value 3	Value 4	
Time $(t=5)$ , Value 5	Value 2	Value 3	Value 4	Value 5	
Time $(t=6)$ , Value 6	Value 3	Value 4	Value 5	Value 6	
Time $(t=7)$ , Value 7	Value 4	Value 5	Value 6	Value 7	

Table 3.2: Example of data transformation using Sliding window method

- The parts of data chosen are then normalized in the range [0,1].
- Transform time-series data into supervised learning data using Sliding window technique.
- Divide processed data into two sets: training set and testing set.

The step 3th of the pre-processing phase is necessary because time-series data is the data recorded through time, and there is no term of features and output data. Therefore, we need to transform this data into supervised learning data, that contains input features, and output. Table 3.1 depicts the difference between time-series data and normal data used in supervised learning.

In order to create data for supervised learning, we use the method called *Sliding window*. This method takes the data of k values before the time t as the features and output data is the value at the time t. For example, when k=3, the results of data transformation is shown as in Table 3.2.

### 3.2.3 Building and Training model

In this phase, pre-processed data is used for training our proposed model called ISLO-CFNN, which is CFNN being trained by the optimization of ISLO algorithm. ISLO algorithm is applied to train a CFNN model with one hidden layer. There is two key aspects needed to be taken into consideration: firstly, the formation of an agent in ISLO and the selection of fitness function.

Firstly, each agent in the population in ISLO are presented as one solution for CFNN model, which means that a search agent is a one-dimensional vector created by concatenating weights and biases of CFNN. Therefore, the features of a search agent contains three elements: a set of weights connecting the input layer with hidden layer, a set of weights connecting the hidden layer with output layer and also and a set of weights connecting the input layer with output layer. Therefore, the length of a solution can be calculated by Eq. 3.5.

Solution 
$$length = (1+i) * h + (1+h) * o + (1+i) * o$$
 (3.5)

Where i, h, o is the number of input, hidden and output neurons, respectively (in time-series prediction, the number of output neurons is one).

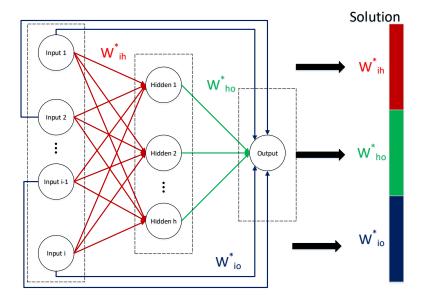


Figure 3.2: Encoding process transforming a parameter set in CFNN into an agent in ISLO algorithm. ( $W^*$  indicates weights and biases between 2 layers)

Secondly, the fitness value of each agent in ISLO is considered as the loss value of the CFNN model with the parameter set from the agent and input data. We utilize the loss function Mean Square Error (MSE) to calculate the difference between the actual and predicted output values by generated agent for all samples in the training set.

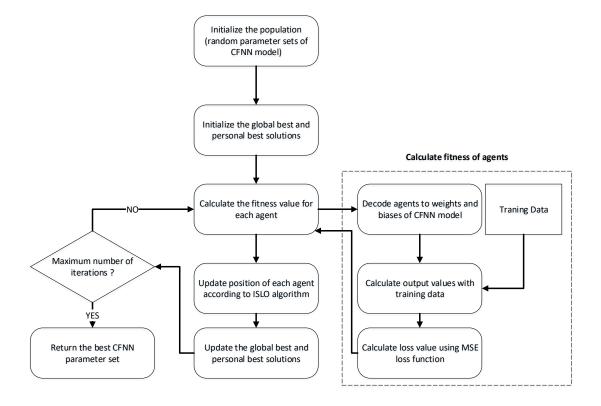


Figure 3.3: The work flow of ISLO-CFNN model.

The workflow of ISLO applied in this work for training CFNN are depicted in Fig. 3.3,

and can be generally presented by the following steps:

- 1. Initialization: pre-define the number of search agents in ISLO, which are randomly generated in the range [-1, 1]. Each parameter set of CFNN model is encoded to a vector playing a role as an agent in ISLO population. (See in Fig. 3.2)
- 2. Calculate fitness value for each search agent: The quality of a solution is measured by the loss value of CFNN output. After being decoded into weights and biases vectors, a solution will be applied to form a CFNN model. Data samples in training set is then feed-forwarded through the network, generating predicted output values. Finally, the fitness value is calculated as the difference between predicted and actual output values through the MSE loss function.
- 3. Update positions of all search agents following formulas of ISLO algorithm.
- 4. Steps 2 and 3 are repeated until the difference is close enough, or the maximum number of iterations is reached.
- 5. Return the best CFNN parameter set.

### 3.2.4 Deploy prediction model

After obtaining CFNN model with the best parameter set by ISLO algorithm, the model is installed on servers and ready to predict the demand for resources in the future based on historical data.

## Chapter 4

## **Experiments**

The optimization capacity of ISLO algorithm developed in this study would be tested by solving two experiments: one for theoretical test and another for an optimizing application in the real world.

In the theoretical test, 30 benchmark functions are used for testing the numerical efficiency of ISLO. The set of benchmark functions cover a wide range function groups including: classical unimodal and multimodal functions, hybrid functions and composition functions which are considered in CEC 2014 and CEC 2015 special session (See [40] and [41] for more information about the annual competition). ISLO will be compared with several well-known algorithms in all four groups in meta-heuristic optimization algorithms including evolutionary, swarm-based, physical-based and human-based algorithms.

On the other hand, the optimizing performance of ISLO is also tested in a time-series prediction problem. Specifically, the proposed model in 3.2 is used for the experiment with three real-world datasets, which are Google Trace data, EU Internet Traffic data and UK Internet Traffic data in different perspectives. The results are compared with that of several deep learning models that are widely used for time-series prediction, and additionally, the performance of ISLO in optimizing CFNN is also compared with several algorithms in the first experiment.

The detail of each experiment as well as results and analysis are presented as below.

### 4.1 Theoretical experiments

The performance of ISLO is theoretically experimented by 30 benchmark functions. They are divided into four groups of functions:

- Unimodal benchmark functions: they have only one global optimal point in the search space.
- Multimodal benchmark functions: they have one global optimal point going along with local minimum points.
- Hybrid functions: the variables are randomly divided into some sub-components and then different basic unimodal and multimodal functions are used for different sub-components.
- Composition functions: they merge the properties of the sub-functions better and maintains continuity around the global/local optima.

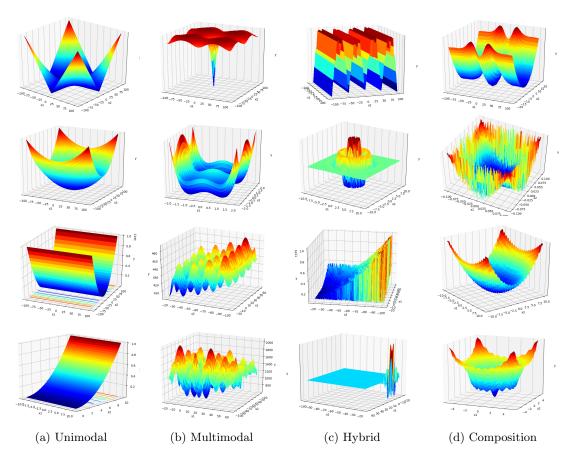


Figure 4.1: Examples of 3D plot for each kind of benchmark functions.

The detail such as name, formula, search space and optimal value of each function is shown in Table. [4.1-4.4]. Also, Fig. 4.1 presents the typical 3D plots of the cost function for some test cases considered in this study.

The performance of ISLO algorithm about optimizing 30 benchmark functions is compared with different optimizers including well-known algorithms as well as recent algorithms that belong to all four groups in nature-inspired meta-heuristic algorithms. Specifically, they are:

- Generic Algorithm (GA) [64] (Evolutionary algorithms)
- Particle Swarm Optimization (PSO) [36], Whale Optimization Algorithm (WOA) [45] and the original Sea Lion Optimization Algorithm (SLnO) [43] (Swarm-based algorithms)

Mathematical Definition	Range	$f_{min}$
$f_1(x) = \sum_{i=1}^n x_i^2$	[-500, 500]	0
$f_2(x) = \sum_{i=1}^n  x_i $	[-500, 500]	0
$f_3(x) = \max_{i=1,2,,n}  x_i $	[-500, 500]	0
$f_4(x) = \sum_{i=1}^{n}  x_i  + \prod_{i=1}^{n}  x_i $	[-500, 500]	0
$f_5(x) = \sum_{i=1}^n ix_i^2$	[-500, 500]	0
$f_6(x) = \sum_{i=1}^{n-1} (x_i^2)^{x_{i+1}^2 + 1} + (x_{i+1}^2)^{x_i^2 + 1}$	[-500, 500]	0
$f_7(x) = \sum_{i=1}^{n} (10^6)^{\frac{x_i-1}{n-1}} + 100$	[-500, 500]	100
$f_8(x) = \overline{x_1^2 + 10^6} \sum_{i=2}^{n} x_i^2 + 200$	[-500, 500]	200

Table 4.1: Description of unimodal benchmark functions

Table 4.2: Description of multimodal benchmark functions

Mathematical Definition	Range	$f_{min}$
$f_9(x) = -a.exp(-b\sqrt{\frac{1}{n}\sum_{i=1}^n x_i^2}) - exp(\frac{1}{n}\sum_{i=1}^n cos(cx_i)) +$	[-500, 500]	0
a + exp(1) with $a = 20$ and $b = 0.2$		
$f_{10}(x) = \left[ \left(   \mathbf{x}  ^2 - n \right)^2 \right]^{\alpha} + \frac{1}{n} \left( \frac{1}{2}   \mathbf{x}  ^2 + \sum_{i=1}^n x_i \right) + \frac{1}{2}$	[-500, 500]	0
$f_{11}(x) = \sum_{i=1}^{n} (x^2 - i)^2$	[-500, 500]	0
$f_{12}(x) = 1 - \cos(2\pi \sqrt{\sum_{i=1}^{D} x_i^2}) + 0.1 \sqrt{\sum_{i=1}^{D} x_i^2}$	[-500, 500]	0
$f_{13}f(x) = \sum_{i=1}^{n} [b(x_{i+1} - x_i^2)^2 + (a - x_i)^2]$	[-500, 500]	0
$f_{14}(x) = \sum_{i=1}^{n} \sum_{j=1}^{5} j \sin((j+1)x_i + j) + 300$	[-500, 500]	300
$f_{15}(x) = 10n + \sum_{i=1}^{n} (x_i^2 - 10\cos(2\pi x_i)) + 400$	[-500, 500]	400
$f_{16}(x) = 418.9829D - \sum_{i=1}^{n} x_i \sin(\sqrt{ x_i }). + 500$	[-500, 500]	500

- Tug of War Optimization (TWO) [33] (Physics-based algorithms)
- Queuing Search Optimization (QSO) [67] (Human-based algorithms)

### 4.1.1 Evaluation method and Parameter settings

With compared algorithms and functions mentioned above, the experimental results of each model are produced by calculating mean and standard deviation (std) value (Eq. 4.1 and 4.2) of 20 times running starting from randomly generated populations for each algorithms. For all the algorithms, a population size and maximum iteration equal to 100 and 500 have been utilized to run on each function with 50-dimension search space. The choices of parameters are based on existing setting up described in original paper of each algorithm.

$$mean = \frac{1}{n} \sum_{i=1}^{n} r_i \tag{4.1}$$

$$std = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (r_i - r)^2}$$
 (4.2)

where N is the number of values and  $r_i$  (i = 1, 2, ..., N) are observations.

For each function, after calculating *mean* and *std* values of each algorithm, the best results will be highlighted in both. The best results are determined by following rules:

Mathematical Definition Range  $f_{min}$  $f_{17}$  (function 17 in CEC 2014) 1700 p = [0.3, 0.4, 0.3][-500, 500]Modified Schwefel's, Rastrigin's and High Conditioned Elliptic Functions  $f_{18}$  (function 18 in CEC 2014) p = [0.3, 0.4, 0.3][-500, 500]1800 Bent Cigar, HGBat and RastriginâĂŹs Functions  $f_{19}$  (function 19 in CEC 2014) p = [0.2, 0.2, 0.3, 0.3][-500, 500]1900 GriewankâĂŹs, Weierstrass, RosenbrockâĂŹs and ScafferâAZs Functions  $f_{20}$  (function 20 in CEC 2014) p = [0.2, 0.2, 0.3, 0.3][-500, 500]2000 HGBat , Discus, Expanded GriewankâÁŹs plus RosenbrockâÅŹs and RastriginâĂŹs Functions  $f_{21}$  (function 6 in CEC 2015) 600 p = [0.3, 0.3, 0.4][-500, 500]Modified Schwefel's, Rastrigin's, High Conditioned Elliptic **Functions**  $f_{22}$  (function 7 in CEC 2015) p = [0.2, 0.2, 0.3, 0.3][-500, 500]700 Griewank's, Weierstrass, Rosenbrock's and Scaffer's Functions  $f_{23}$  (function 8 in CEC 2015) p = [0.1, 0.2, 0.2, 0.2, 0.3][-500, 500]800 ScafferâĂŹs, HGBat ,RosenbrockâĂŹs, Modified SchwefelâĂŹs and High Conditioned Elliptic Functions

Table 4.3: Description of hybrid benchmark functions

- mean values are considered at first. If in a case, an algorithm own the best mean value, it will be ranked as the best optimizer.
- In the case where there are two or more algorithms having the same *mean* value, the one that has the most stable *std* value will be chosen as the best one.

Finally, the experimental results of all functions and algorithms are shown in Table 4.5 and 4.6, and the convergence speeds of the algorithms in several functions are illustrated in Fig. 4.2 and 4.3.

### 4.1.2 Experiment results and discussion

#### 4.1.2.1 Unimodal and Multimodal benchmark functions

Functions  $f_1$  -  $f_{16}$  are unimodal and multimodal functions. These kinds of functions are selected following a couple of testing purposes. Specifically, unimodal functions allow us to evaluate exploitation capacity of meta-heuristic optimizers since they only have one global optimal minimum; multimodal functions help us see algorithms' exploration performance with a number of local minimum points, which exponentially increases following the increase in search space

Table 4.4: Description of composition benchmark functions

Mathematical Definition	Range	$f_{min}$
$f_{24}$ (function 9 in CEC 2015)		
$\sigma = [20, 20, 20]$	[-500, 500]	900
$\lambda = [1, 1, 1]$	[-500, 500]	
Schwefel's , Rastrigin's and HGBat Functions		
$f_{25}$ (function 10 in CEC 2015)		
$\sigma = [10, 30, 50]$	[-500, 500]	1000
$\lambda = [1, 1, 1]$	[ 300, 300]	
$f_{21}, f_{22}$ and $f_{23}$ Functions		
$f_{26}$ (function 11 in CEC 2015)		
$\sigma = [10, 10, 10, 20, 20]$	[-500, 500]	1100
$\lambda = [10, 10, 2.5, 25, 1e-6]$	[ 300, 300]	
HGBat , RastriginâÅŹs and Schwefel's, Weierstrass and		
High Conditioned Elliptic Functions		
$f_{27}$ (function 12 in CEC 2015)		
$\sigma = [10,20,20,30,30]$	[-500, 500]	1200
$\lambda = [0.25, 1, 1e-7, 10, 10]$	[ 000, 000]	
Schwefel's , Rastrigin's and High Conditioned Elliptic, Ex-		
panded ScafferâĂŹs and HappyCat Functions		
$f_{28}$ (function 13 in CEC 2015)		1000
$\sigma = [10, 10, 10, 20, 20]$	[-500, 500]	1300
$\lambda = [1, 10, 1, 25, 10]$	. , 1	
$f_{23}$ , Rastrigin's and $f_{21}$ , Schwefel's and Expanded Scaffer-		
âĂŹs Functions		
$f_{29}$ (function 14 in CEC 2015)		1.400
$\sigma = [10, 20, 30, 40, 50, 50, 50]$	[-500, 500]	1400
$\lambda = [10,2.5, 2.5, 10,1e-6,1e-6, 10]$		
HappyCat , GriewankâĂŹs plus RosenbrockâĂŹs, Schwe-		
fel's, Expanded ScafferâĂŹs, High Conditioned Elliptic,		
Cigar and and RastriginâÅŽs Functions		
$f_{30}$ (function 15 in CEC 2015)		1500
$\sigma = [10, 10, 20, 20, 30, 30, 40, 40, 50, 50]$	[-500, 500]	1500
$\lambda = [0.1, 2.5e-1, 0.1, 2.5e-2, 1e-3, 0.1, 1e-5, 10, 2.5e-2, 1e-3]$		
RastriginâĂŹs, Weierstrass, HappyCat, Schwefel's, Rosen-		
brock's, HGBat, Katsuura, Expanded ScafferâĂŹs, Ex-		
panded GriewankâĂŹs and Ackley Functions		

dimension. In general, it can be seen from the Table 4.5 that ISLO shows the best performance among all chosen algorithms in the most test cases except  $f_{11}$ . Furthermore, while optimizing several functions, ISLO is able to reach or nearly the optimal value with decent stability.

The accuracy and the stability: From the gained results of unimodal and multimodal funtions in Table. 4.5, it could be made the following observations:

• ISLO outperforms the others in all test cases except  $f_{11}$ . In the experiments with unimodal functions  $f_1$ - $f_8$ , ISLO is the best algorithm in the term of exploitation capacity, being ranked at the first position among all chosen algorithms. The results with functions  $f_1$  and  $f_3$  indicate that ISLO could lead the population relatively near the global optimal position. Additionally, along with the best results in term of accuracy, ISLO also performs good stability since the standard deviation values are below 1 in all cases, especially in  $f_1$  and  $f_3$ , the std values are mostly 0. The results prove that compared with the original SLnO, ISLO's exploitation

Table 4.5: Comparison of optimization results obtained for the unimodal and multimodal functions

mean   4.64E+01   9.69E+02   2.52E+25   2.26E+80   3.26E+120   1.06E+01   8.14E+01   std   7.54E+00   3.12E+02   7.11E+25   9.41E+80   8.45E+120   1.39E+00   3.08E+01   man   2.19E+02   1.99E+02   1.64E+01   2.98E+00   2.26E+01   2.24E+00   6.15E+01   man   2.19E+02   1.99E+02   1.64E+01   2.98E+00   2.26E+01   2.24E+00   6.15E+01   man   4.30E+01   3.42E+01   3.28E+00   5.86E+01   1.23E+01   2.24E+00   6.15E+01   man   4.30E+00   1.79E+01   7.58E+01   4.39E+01   2.24E+00   6.15E+01   man   4.30E+00   1.79E+01   7.58E+01   4.39E+01   2.24E+00   6.15E+01   man   4.30E+00   1.79E+01   7.58E+01   4.39E+01   2.24E+00   6.15E+01   man   4.30E+00   1.22E+02   1.92E+01   4.39E+01   2.24E+00   2.24E+00   man   1.21E+02   7.43E+02   4.07E+26   2.81E+00   1.66E+01   1.71E+32   1.70E+02   man   1.21E+02   7.43E+02   1.30E+27   7.00E+01   1.01E+01   7.33E+32   1.98E+02   man   1.36E+03   1.58E+04   2.01E+02   2.42E+00   3.32E+02   2.42E+03   3.24E+01   3.3EE+02   3.3EE+02	Function		GA	PSO	SLnO	WOA	ISLO	TWO	QSO
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Function	****							
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	r		·						
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$J_1$								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			-	· ·	_	-		_	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	e								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_2$								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								-	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_3$								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank	-				_	-	_
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_4$								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank	-	_	-			-	
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $		mean	1.36E+03			2.42E+00			2.43E+01
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_5$	std	3.87E + 02	5.57E + 03	$9.51E{+01}$	6.70E-01	6.06E-02	1.06E + 03	1.20E+01
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank	5	7	4	2	1	6	3
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		mean	1.27E+00	1.20E+00	3.27E-01		5.65E-05	1.02E+00	7.83E-02
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_6$	std	3.01E-02	4.08E-02	1.47E-01	1.40E-03	5.50E-05	2.21E-02	4.22E-02
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank	7	6	4	2	1	5	3
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		mean	8.70E + 06	2.34E+07	1.42E + 06	6.12E + 04	8.22E + 02	1.22E + 08	1.27E+04
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_7$	std			1.12E + 06				
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	<i>J</i> .								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		mean	4.54E + 08	7.70E+09	6.52E+07	7.83E+05	1.60E + 04	1.02E+08	1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{\circ}$							· ·	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	38								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			-		2.05E+01	2 82F-01		-	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{\Omega}$								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	J9								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			-	-	-	_		_	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{+0}$								1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	J 10								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					-			-	1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	f								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	J11								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			-		_		-	-	_
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	£								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	J12								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						-		_	-
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	r								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	J13								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			-	•	_			-	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	c								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\int 14$								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$				-			-	_	-
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	e								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{15}$								
$f_{16}$ std $4.48\text{E-}02$ $1.66\text{E-}01$ $1.75\text{E-}01$ $5.94\text{E+}00$ $\textbf{3.80\text{E-}01}$ $3.76\text{E-}02$ $1.99\text{E-}02$									
rank   5   6   7   2   1   3   4	$f_{16}$								
		rank	5	6	7	2	1	3	4

ability is significantly enhanced.

• The results in Table. 4.5 for multimodal functions  $f_9$ - $f_{16}$  indicate that ISLO also has a superior exploration ability. ISLO stands at the first ranking in 7 out of 8 functions, and with  $f_{14}$  and  $f_{16}$  ISLO reaches the global optimal values of the functions, accompanying with that is relatively small standard deviation values. It is notable that ISLO is less competitive at  $f_{11}$  where it stands at 5th position, being outperformed by WOA, TWO and original SLnO. However, in  $f_8$ ,  $f_9$ ,  $f_{10}$ ,  $f_{13}$ ,  $f_{14}$  and  $f_{16}$ , ISLO's results are much better than the others in both terms of accuracy and stability.

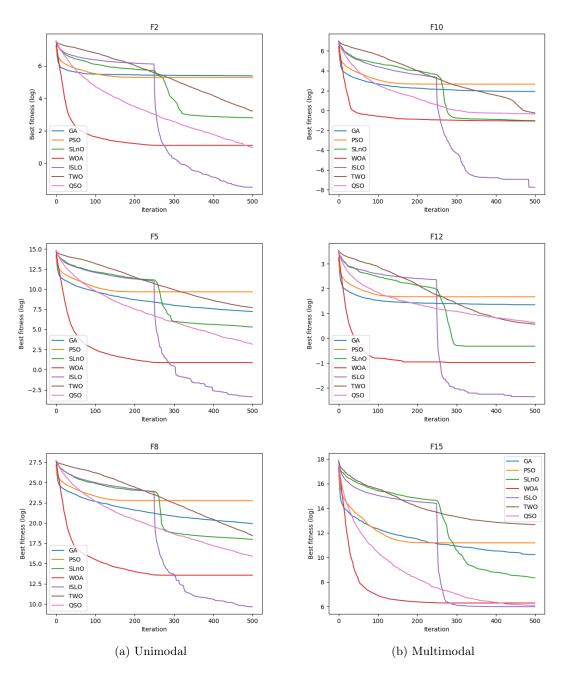


Figure 4.2: Convergence speed of each algorithm on unimodal (a) and multimodal (b) functions.

In summary, all gained results with unimodal and multimodal funtions figure out that ISLO has the excellent exploitation and exploration capacity. This is due to the fact that apart from considering and updating search agents' position following the best agent, taking the best experience of each agent into account (Eq. 3.3) helps ISLO exploits population's information far better than SLnO. Apart from this, opposition-based updating operation in the exploration phase enrichs the diversity of population, helping ISLO easily jumps out of local minimums.

The convergence speed: The convergence speed of all algorithms working on several functions are shown in Fig. 4.2. It is clear that ISLO always considerably enhance its global best fitness values in the second half of the iterations. The reason is that on the first half of the iterations, ISLO is in its exploration phase (since the value of C during that time is always greater

Table 4.6: Comparison of optimization results obtained for the hybrid and composition benchmark functions

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Function		GA	PSO	SLnO	WOA	ISLO	TWO	QSO
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		mean	2.19E+05	1.46E + 05	8.08E + 04	8.82E + 03	1.81E + 03	2.08E + 06	5.46E + 03
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{17}$	std	1.29E+05	7.68E + 04	4.92E + 04	2.63E + 03	1.95E + 02	7.79E + 05	5.00E + 02
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank	6	5	4	3	1	7	2
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{18}$	mean	6.43E + 06	3.15E + 04	9.29E + 05	8.12E + 03	4.46E + 03	4.73E + 05	3.49E + 03
$\begin{array}{c} \text{mean} & 8.97E + 03 & 2.36E + 03 & 2.48E + 03 & 1.92E + 03 & 9.67E + 03 & 2.01E + 03 \\ \text{std} & 2.87E + 03 & 9.31E + 02 & 8.36E + 02 & 4.45E + 01 & 2.08E + 00 & 2.02E + 04 & 1.25E + 02 \\ \text{rank} & 6 & 4 & 5 & 2 & 1 & 7 & 3 \\ \text{mean} & 1.82E + 05 & 2.52E + 04 & 1.49E + 04 & 2.81E + 03 & 2.12E + 03 & 4.53E + 05 & 1.77E + 04 \\ \text{std} & 2.14E + 05 & 1.24E + 04 & 6.90E + 03 & 6.75E + 02 & 8.47E + 01 & 1.03E + 06 & 5.70E + 04 \\ \text{rank} & 6 & 5 & 3 & 2 & 1 & 7 & 4 \\ \text{mean} & 7.97E + 06 & 5.51E + 07 & 1.04E + 08 & 2.00E + 05 & 3.19E + 03 & 1.79E + 08 & 4.43E + 08 \\ \text{std} & 2.95E + 06 & 3.76E + 07 & 1.00E + 08 & 4.37E + 05 & 3.19E + 03 & 8.02E + 07 & 1.46E + 08 \\ \text{rank} & 3 & 4 & 5 & 2 & 1 & 6 & 7 \\ \text{mean} & 2.28E + 05 & 1.26E + 07 & 1.85E + 08 & 8.72E + 02 & 7.16E + 02 & 1.17E + 08 & 2.57E + 08 \\ \text{std} & 7.52E + 04 & 1.27E + 07 & 6.11E + 08 & 2.55E + 02 & 9.38E - 01 & 1.29E + 08 & 1.73E + 08 \\ \text{rank} & 3 & 4 & 6 & 2 & 1 & 5 & 7 \\ \text{mean} & 5.29E + 06 & 6.08E + 07 & 2.65E + 08 & 3.59E + 04 & 1.26E + 03 & 2.74E + 08 & 9.76E + 08 \\ \text{rank} & 3 & 4 & 6 & 2 & 1 & 5 & 7 \\ \text{mean} & 5.29E + 06 & 6.08E + 07 & 2.65E + 08 & 3.59E + 04 & 1.26E + 03 & 2.74E + 08 & 9.76E + 08 \\ \text{rank} & 3 & 4 & 6 & 2 & 1 & 6 & 7 \\ \text{mean} & 1.12E + 04 & 2.96E + 04 & 3.46E + 03 & 1.81E + 03 & 1.57E + 08 & 4.46E + 08 \\ \text{rank} & 3 & 4 & 5 & 2 & 1 & 6 & 7 \\ \text{mean} & 1.12E + 04 & 2.96E + 04 & 3.46E + 03 & 1.81E + 03 & 1.5E + 05 & 2.23E + 03 \\ \text{std} & 2.35E + 03 & 1.71E + 04 & 1.04E + 03 & 4.11E + 01 & 1.62E + 00 & 4.71E + 04 & 6.89E + 02 \\ \text{rank} & 5 & 6 & 4 & 2 & 1 & 7 & 3 \\ \text{mean} & 8.17E + 06 & 1.26E + 08 & 8.62E + 08 & 1.33E + 05 & 2.95E + 03 & 2.64E + 08 & 6.89E + 08 \\ \text{std} & 3.59E + 02 & 3.76E + 02 & 9.84E + 02 & 9.60E + 02 & 2.03E + 03 & 2.82E + 03 \\ \text{std} & 3.59E + 02 & 3.76E + 02 & 9.84E + 02 & 9.60E + 02 & 2.03E + 03 & 2.85E + 03 & 2.85E + 03 \\ \text{std} & 6.99E + 01 & 1.18E + 02 & 1.66E + 02 & 3.28E + 00 & 1.50E + 00 & 2.58E + 01 & 6.04E + 00 \\ \text{rank} & 7 & 6 & 3 & 1 & 4 & 2 \\ \text{mean} & 3.77E + 05 & 1.13E + 07 & 2.17E + 1$		std	1.10E + 06	9.41E + 03	1.66E + 06	2.55E + 03	2.95E + 03	1.00E + 05	8.92E + 02
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank		4	6	3	2	-	1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		mean	8.97E + 03		2.48E + 03	1.95E + 03	1.92E + 03	9.67E + 03	2.01E + 03
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{19}$	std	2.87E + 03	9.31E + 02	8.36E + 02	4.45E + 01	2.08E + 00	2.02E+04	1.25E+02
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank	-	-	-				
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		mean							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{20}$	std	2.14E + 05	1.24E+04	6.90E + 03	6.75E + 02	8.47E + 01	1.03E + 06	5.70E + 04
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank	6	5	3	2	1	7	4
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								1.79E + 08	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{21}$	std	2.95E + 06	3.76E + 07	1.00E + 08	4.37E + 05	9.01E + 03	8.02E + 07	1.46E + 08
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank	-	-	-	_	-	-	1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{22}$	mean	2.28E + 05			8.72E + 02			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		std	7.52E+04	1.27E + 07	6.11E + 08	$2.55E{+02}$	9.38E-01	1.29E+08	1.73E + 08
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank	_	-		_	-	5	•
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		mean							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{23}$	1		2.72E + 07			1.19E + 03	1.57E + 08	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank		-		_	=	_	l -
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		mean	1.12E+04	2.96E+04	3.46E + 03	1.92E+03	1.81E + 03	1.15E + 05	2.23E+03
$f_{25} = \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{24}$	std	2.35E+03	1.71E + 04	1.04E + 03	4.11E + 01	1.62E + 00	4.71E + 04	6.89E + 02
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank			*	<del>-</del>	-	'	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{25}$	mean							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		std	2.42E+06	5.10E + 07	1.08E+09		4.98E + 02	1.09E+08	3.18E + 08
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank	_	-				-	-
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{26}$	mean	6.78E + 03				2.22E + 03		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			3.59E+02	3.76E + 02	9.84E+02		2.03E + 00	2.15E+02	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank		5	-		-	-	-
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{27}$	mean							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		std	6.09E+01	1.18E + 02	1.66E-02		1.50E + 00	2.58E+01	6.04E+00
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank		-		_	_	~	_
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{28}$	l							
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		1	6.99E+03	1.22E+04	5.84E + 03	7.98E + 03	3.86E + 04	3.89E + 03	1.81E + 00
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		rank		=	-	_	~		=
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$f_{29}$								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		std	2.07E+05	1.10E + 05	1.27E + 11		5.36E + 00	3.05E+11	1.90E+06
$f_{30}$ std $7.28E+02$ $1.94E+06$ $5.60E-01$ $2.30E+00$ $1.32E+00$ $1.54E+04$ $1.66E+02$		rank	_	~		_	=	'	-
	$f_{30}$	1							
rank 5 7 3 2 1 6 4			7.28E+02				1.32E + 00	1.54E+04	1.66E + 02
		rank	5	7	3	2	1	6	4

than 1, see Algorithm 3). After changing to exploitation phase, ISLO has the ability to exploit and converge to global minimum quickly, providing better results than the others. Fig. 4.2 indicates that ISLO is competitive with an acceptable convergence speed, and also providing decent fitness values in functions  $f_2$ ,  $f_5$ ,  $f_8$ ,  $f_{10}$ ,  $f_{12}$  and  $f_{15}$ . SLnO has the same pattern of convergence curves compared with ISLO, but it coverges to mediocre fitness values, especially in  $f_2$ ,  $f_5$  and  $f_{10}$ . Also, WOA and QSO are competitive compared with ISLO in function  $f_{15}$ , where the final results of them are extremely close to ISLO's.

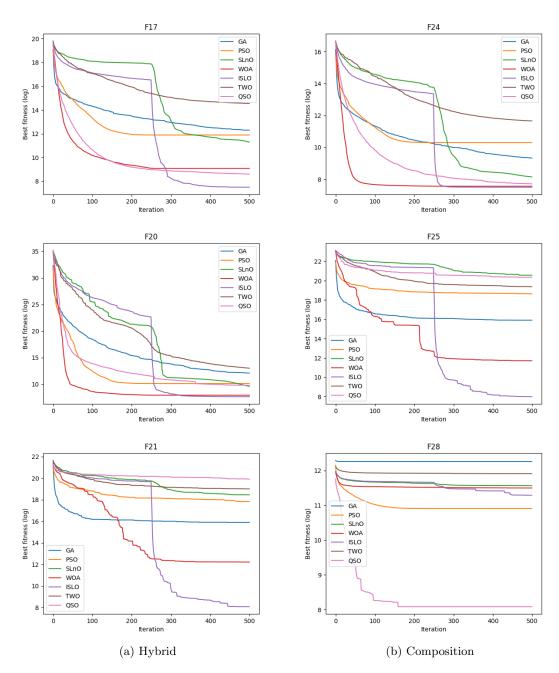


Figure 4.3: Convergence speed of each algorithm on hybrid (a) and composition (b) functions.

### 4.1.2.2 Hybrid and Composition benchmark functions

Functions  $f_{17}$ - $f_{30}$  are hybrid and composition functions. In hybrid functions ( $f_{17}$ - $f_{23}$ , the variables are randomly divided into subcomponents which play a role as input for different basic functions including both unimodal and multimodal functions. In order to work well on these functions, algorithms are required to be good at both exploitation and exploration capacity, because hybrid functions are both unimodal and multimodal, and they own different properties for different variables subcomponents. On the other hand, optimization of composite mathematical functions ( $f_{24}$ - $f_{30}$ ) is a very challenging task, because local optima is only avoided by a proper balance between exploitation and exploration. In general, Fig. 4.6 shows that ISLO owns the

best performance over all hybrid and compostion functions. The results from ISLO stand at first ranking in all cases except  $f_8$  and  $f_{28}$  where the first position belongs to QSO. Also, as what is observed in Fig. 4.3, ISLO's convergence curves are similar to those in unimodal and multimodal functions, and ISLO still has a very fast convergence after the first half of iteration because of its updating mechanism.

#### The accuracy and the stability:

To resolve the optimization problem in hybrid functions  $f_{17}$ - $f_{23}$ , it is evident that ISLO can work very well in almost cases. The results shown in Table. 4.6 indicates that ISLO has the superior results at functions  $f_{17}$ ,  $f_{19}$ ,  $f_{20}$  and  $f_{23}$  compared with state-of-the-art algorithms such as WOA and QSO. Furthermore, with functions  $f_{21}$  and  $f_{23}$ , ISLO's results are much better than the others', proving good capacity at both exploitation and exploration. Solving the case  $f_{18}$ , although ISLO does not account for the first place, it is still very competitive when its result is only worse than QSO's.

For composition functions, ISLO shows the best performance among all the algorithms by standing at the first place in 6 out of 7 functions. Specifically, in  $f_{24}$ ,  $f_{27}$ ,  $f_{29}$  and  $f_{30}$ , there is no big differences between ISLO'results and the others', while in  $f_{25}$  and  $f_{26}$ , mean and std values from Table. 4.6 indicates the dominance of ISLO in optimizing these functions. This proves that ISLO owns a superior balance between its exploitation and exploration while solving test problems. Also std values from ISLO in most cases are below 10, showing the decent stability of this algorithm compared with GA or PSO algorithms.

The convergence speed: As working on unimodal and multimodal functions, when working on hybrid and composite mathematical functions, ISLO still owns the fast convergence in the second half of iterations. The convergence curves in Fig. 4.3 shows that ISLO starts to converge very fast right after exploration phase comes to an end. In  $f_{17}$  and  $f_{24}$ , the convergence curves indicate that ISLO is very competitive with WOA because these 2 algorithm converge to almost one value. Also, the results comes from ISLO is far better than the original SLnO in all cases, proving that exploitation and exploration capacities in SLnO are considerably enhanced. QSO is observed to be superior in function  $f_{28}$ , in which the others including ISLO are stuck in local minimums.

## 4.2 Application

In this section, proposed model in Section 2.3 is utilized for solving time-series prediction in the auto-scaling problem in cloud computing. Our experiment is done with 4 datasets:

Google Trace CPU, Google Trace Memory, EU Internet Traffic and UK Internet Traffic. In this empirical study, ISLO-CFNN model is compared with several deep learning models such as simple MLP, the original CFNN, the original RNN and two well-known and widely used models in time-series forecasting: LSTM and GRU in terms of accuracy and run time. Also, optimizing capacity of ISLO on CFNN is compared with several swarm-based algorithms in Section 4.1. The bio-inspired models used to validate against ISLO-CFNN are PSO-CFNN and SLnO-CFNN, which are CFNN models optimized by PSO and SLnO algorithms, respectively.

We would first describe 4 datasets used in this experiment. Then, the parameter setting for each model and evaluation metrics are introduced in detail. Finally, ISLO-CFNN performance is compared with the deep learning models as well as bio-inspired models in different perspectives.

### 4.2.1 Dataset and Set up

#### 4.2.1.1 Google Trace dataset

The most important dataset in our experiments is gathered by Google on a cluster of about 12500 machines [52] during 29 days, starting from May 2011. Resources requirement and usage data for each jobs are recorded by each machine in cluster, and then the data is managed by cluster's management system. In Google Trace dataset, there are two columns, which are about two extremely important information of Central Processing Unit (CPU) and Random Access Memory (RAM) required for each job. For that reason, we decide to choose these two information as two time-series datasets (called Google Trace CPU and Google Trace RAM from here). The datasets are processed and summarized in 5-minute interval, containing 8351 data points, and considered as the total demand for resources in the whole Google's cluster. Visualization of Google Trace CPU and Google Trace RAM datasets is illustrated in Fig. 4.4.

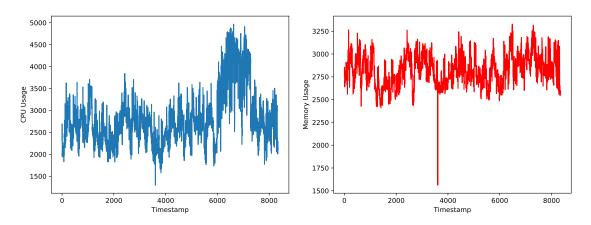


Figure 4.4: Visualization of Google Trace CPU (left) and Google Trace RAM (right) datasets.

#### 4.2.1.2 EU Internet Traffic and UK Internet Traffic datasets

These two sets of data, which is used for experiments in [12], are recorded by two distinct ISPs. The EU Internet Traffic dataset comes from a private ISP playing a role as a reporter with centers in 11 European cities. The data corresponds to a a transatlantic link and was collected from 06:57 hours on 7 June to 11:17 hours on 29 July 2005. The UK Internet Traffic is derived from m UKERNA and represents aggregated traffic in the United Kingdom academic network backbone. It was reported between 19 November 2004, at 09:30 hours and 27 January 2005, at 11:11 hours. Both of two datasets are processed and summarized in every 5 minutes, creating EU Internet Traffic (14773 records) and UK Internet Traffic (19989 records) as the input in our experiments. 2D visualization of the data is shown in Fig. 4.5 as below.

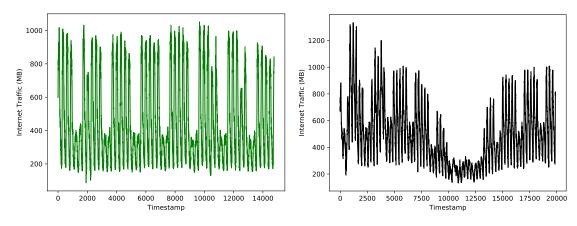


Figure 4.5: Visualization of EU Internet Traffic (left) and UK Internet Traffic (right) datasets.

#### 4.2.2 Parameter Setting and Evaluation Metrics

As mentioned above, ISLO-CFNN's performance is compared with 4 deep learning models: MLPs, CFNN, LSTM and GRU, and 2 bio-inspired models: PSO-CFNN and SLnO-CFNN models. The hyper-parameter settings for each model are described as below:

- 4 datasets used for these experiments are all divided into 2 sets: training set and testing set with the ratio 0.8:0.2. The training set accounts for the first 80% of the datasets, and the remaining is of testing set because of the sequential characteristic of time-series data.
- CFNN's architectures in all models are configured with the same structure with three layers: input layer, one hidden layer and output layer which contains only one neuron in time-series prediction.
- The input size for all models is 3 as we use 3 historical data points to predict the output in current time (mentioned in Section 2.3).

• RNN-based models as LSTM and GRU contains one input layer, LSTM (or GRU) blocks and one output layer with the same hyper-parameter setting as described in [20].

In all test, including with deep learning models and swarm-based algorithms, the number
of iterations is set to 1000. From the experiments, we figure out that the amount of 1000
iterations is enough for all algorithms to converge to their final results.

Besides the common settings for models, the following settings are applied for each swarm-based algorithms as they show the best empirical performance:

- The population size for each algorithm is set to 200.
- For PSO, based on the original paper [16], cognitive learning rates  $c_1 = c_2 = 2.05$ , and inertia factor w is set linearly reducing from 0.9 to 0.4 over the course of iteration.
- For SLnO and ISLO, hyper-parameters are set as described in original paper [43], and also,  $c_1$  and  $c_2$  in ISLO algorithm are the same as shown for PSO.

All 8 models' performance on 4 datasets are compared with each other in term of accuracy. In our experiments, mean absolute error (MAE) is used mainly for evaluation purposes. Beside MAE, root mean square error (RMSE) and median absolute error (MedAE) are also used as measurements for comparision. These three measurement methods are very popular and widely used for evaluation in time-series prediction. Table. 4.7 presents the results of all models on each dataset evaluated by MAE, RMSE and MedAE measurements. It is worth to mention here that the 2 best results on each evaluation measurement would be highlighted in bold. Also, Fig. 4.6 illustrates the comparision between predicted output and the ground truth from ISLO-CFNN and RNN-based models running on Google Trace CPU dataset, while Fig. 4.7 shows the performance of different optimizers including ISLO, SLnO, PSO and original Gradient Descent in optimizing CFNN parameters, running on Google Trace RAM dataset.

## 4.2.3 Results and Discussion

#### 4.2.3.1 Accuracy comparision

Table 4.7 illustrates the comparision between ISLO-CFNN and other models on each dataset by different measurements. In general, ISLO-CFNN is very competitive in working on all dataset. Also, while ISLO provides good results in MAE and MedAE, RNN-based models (RNN, LSTM, GRU) and original CFNN show decent performance by giving the best RMSE.

Table 4.7: Comparision between models on each dataset by different measurements.

Dataset	Model	RMSE	MAE	MedAE	SMAPE (%)
	CFNN	199.77	126.80	80.05	4.03
	FFNN	203.54	129.52	85.69	4.18
	LSTM	200.89	129.88	84.65	4.10
Google Trace CPU	GRU	201.88	130.50	82.96	4.12
Google Trace CF U	RNN	200.40	129.30	85.49	4.10
	PSO-CFNN	203.75	127.41	79.74	4.04
	SLnO-CFNN	201.40	126.60	79.64	4.02
	ISLO-CFNN	203.55	124.94	76.08	4.00
	CFNN	52.54	35.35	24.87	1.21
	FFNN	53.61	36.51	24.29	1.25
	LSTM	48.47	30.40	20.51	1.05
Coorlo Traca DAM	GRU	48.43	30.74	20.78	1.06
Google Trace RAM	RNN	47.00	28.86	18.90	0.99
	PSO-CFNN	49.09	31.33	20.67	1.08
	SLnO-CFNN	49.33	31.62	20.53	1.09
	ISLO-CFNN	47.53	29.80	19.65	1.03
	CFNN	15.85	11.30	8.01	2.91
	FFNN	16.48	11.79	8.41	3.03
	LSTM	15.84	11.37	8.30	2.92
EU Internet Traffic	GRU	17.39	13.09	10.29	3.51
EO Internet Traine	RNN	16.90	12.49	9.55	3.31
	PSO-CFNN	16.02	11.49	8.31	2.93
	SLnO-CFNN	16.37	11.74	8.47	3.00
	ISLO-CFNN	16.02	11.47	8.31	2.93
	CFNN	10.74	8.09	6.31	1.56
	FFNN	11.32	8.40	6.45	1.60
	LSTM	10.34	7.65	5.85	1.47
UK Internet Traffic	GRU	11.52	8.89	7.33	1.78
OK Internet Traine	RNN	11.27	8.38	6.39	1.62
	PSO-CFNN	10.43	7.59	5.63	1.44
	SLnO-CFNN	10.61	7.73	5.75	1.47
	ISLO-CFNN	10.46	7.64	5.77	1.45

On Google Trace CPU dataset, ISLO-CFNN shows its outstanding performance, giving the best results in MAE and MedAE measurements. It is obvious that compared with RNN-based models, our CFNN-ISLO shows the superior performance, and provides better results (see Fig. 4.6). Specifically, the model's figures are better than LSTM by 3.9% (with MAE) and about 10% (with MedAE). CFNN and RNN provides the smallest RMSE on the dataset, while bio-inspred models including SLnO-CFNN and PSO-CFNN have advantages in MAE and MedAE.

Working on Google Trace RAM and UK Internet Traffic datatests, ISLO shows a competitive performance compared with the others, standing at the second position in terms of all measurements. ISLO-CFNN's results ony stand behind original RNN (Google Trace RAM) and PSO-CFNN (UK Internet Traffic). With Google Trace RAM dataset, ISLO-CFNN's performance is more superior than that of original CFNN by 9.6% (RMSE) and 16% (MAE), and with the others the model also show its prominence. Furthermore, Table 4.7 shows that in both datasets, the gap between ISLO-CFNN's results and the best figures is trivial, proving that the model is able to work very well with them. It is worth mentioned here that compared with Gradient Descent,

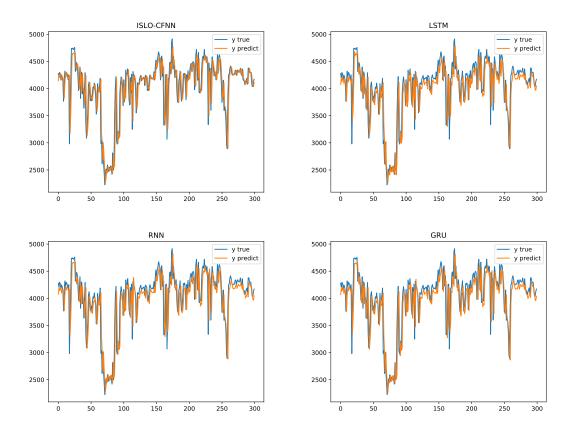


Figure 4.6: Performance comparision between ISLO-CFNN and different recurrent-based deep learning models on Google Trace CPU data.

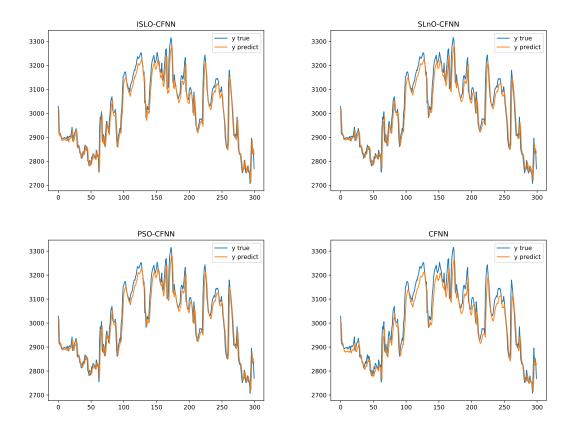


Figure 4.7: Performance comparision between ISLO and other algorithms including Gradient Descent, PSO and SLnO on optimizing CFNN (Google Trace RAM data).

swarm-based optimization algorithms such as ISLO, SLnO and PSO show better performance on optimizing CFNN, working on Google Trace RAM data (see Fig. 4.7)

With the results illustarted in Table 4.7 about EU Internet Traffic data, it is obvious that this is the data in which our model is less competitive than its performance on the other data. Original CFNN and LSTM provide the outstanding and mostly the same figures. Three swarm-based models including PSO-CFNN, ISLO-CFNN and SLnO-CFNN stand at right behind the best one, while GRU and RNN are much less competitive than the others.

### 4.2.3.2 Run-time comparision

# Chapter 5

# Conclusions and Future work

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