

Fundamental of Mobile Robot AUT-710

Exercise 5

Muhamad Fikri Widhi Atman 15.3.2024, **SA205**, 10:15 - Finish



General Plan for Exercises

- Exercise 4: Implementation of model + Basic Control
- 10 point

- Exercise 5: Collision Avoidance with SI model
 - Point obstacle switching behavior with obstacle avoidance
 - non-point obstacle switching behavior with wall-following
 - Point obstacles QP-based controller

20 point

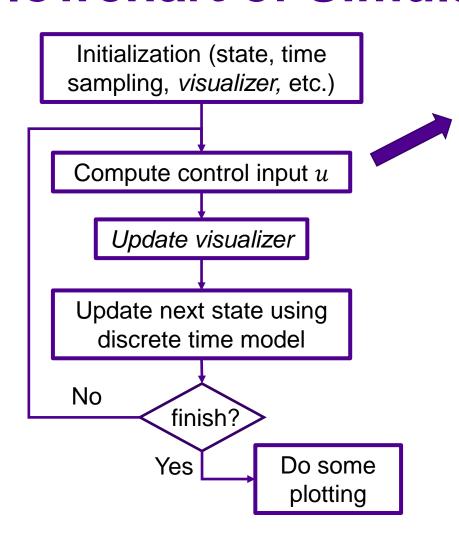
Deadline: Monday 01.04.2024 at 23:59

- Exercise 6: Control of Unicycle
- Mini Projects (optional)





Flowchart of Simulator



If you are interested in implementing this to ROS

Subscribe to all required information (state, sensor, etc.)

Compute control input *u*

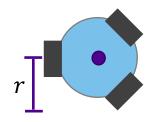
Publish *u* to robot / low level controller

Specifications (for Exercise 5)

Time sampling T = 10ms

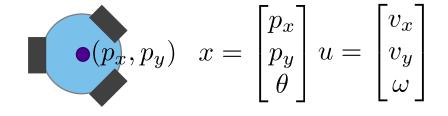
Robot's radius = 0.21 m

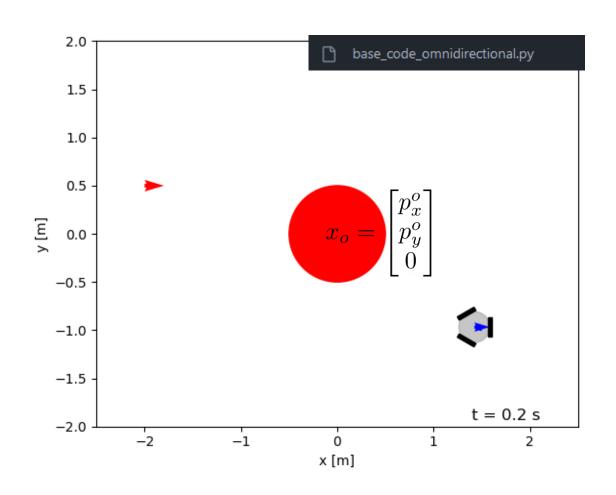
Max translational vel. $(v_x^2 + v_y^2)^{\frac{1}{2}} = 0.5$ m/s Max rotational vel. $(|\omega|) = 5$ rad/s





Exercise 5.1 – Scenario





Model: omnidirectional mobile robot (singleintegrator model)

Initial Position: $x[0] = \begin{bmatrix} 1.5 & -1 & * \end{bmatrix}^T$

Goal: static at $x^d = [-2 \ 0.5 \ 0]^T$.

Key Scenario:

- We assume the robot/controller can identify a circular obstacle (centroid and radius) once it is near. Here, the obstacle is centered at $p_x^o = 0$, $p_y^o = 0$ with radius 0.5m.

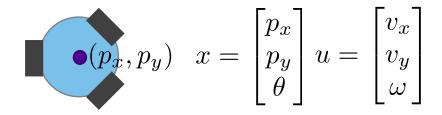
Control Objective:

Reach the goal while avoiding contact/collision with obstacle

^{*} Can be any orientation at goal position



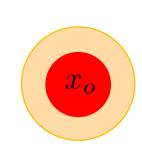
Exercise 5.1 – Task



By taking account of the robot's size and limitation, design and implement the following switched controller

$$||x - x_o|| < d_{safe}$$

$$||x - x_o|| \ge d_{safe} + \epsilon$$



Describe your approach in designing u_{gtg} , u_{avo} , d_{safe} , and ϵ , as well as your observation on the resulting controller.

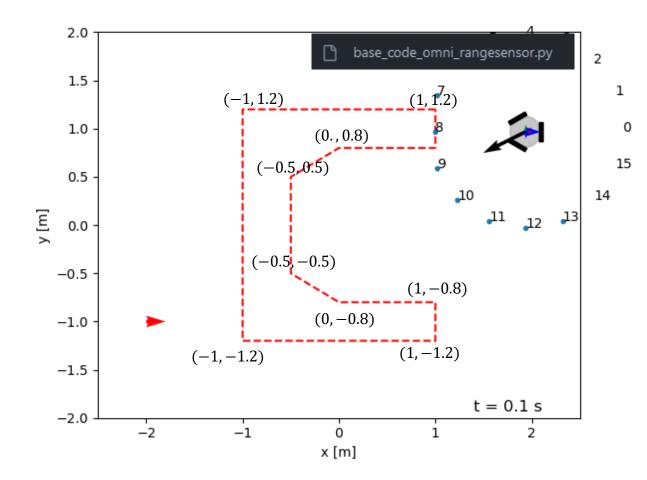
Show the result by plotting:

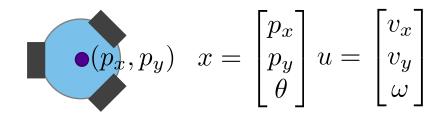
- time series of control input u and $(v_x^2 + v_y^2)^{0.5}$
- time series of error $(x^d x)$,
- time series of distance to obstacle $||x x_o||$
- time series of state trajectory x vs x^d , and
- XY **trajectory** of the robot (or final snapshot of the simulator).

Deadlock issue: Try to set the initial position to $x[0] = [2 -0.5 \ 0]^T$ and see what happen.



Exercise 5.2 – Scenario





Model: omnidirectional mobile robot (single-integrator model)

Initial Position: $x[0] = \begin{bmatrix} 2 & 1 & 0 \end{bmatrix}^T$

Goal: static at $x^d = \begin{bmatrix} -2 & -1 & * \end{bmatrix}^T$.

* Can be any orientation at goal position

Key Scenario:

- An obstacle presents in the field, but unknown to the robot/controller.
- The obstacle is detected by the reading from range sensor (< 1 m)

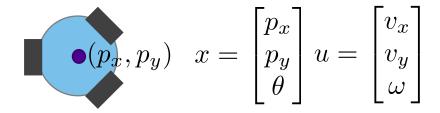
 Assume accurate readings from sensors.

Control Objective:

 Reach the goal while avoiding contact/collision with obstacle

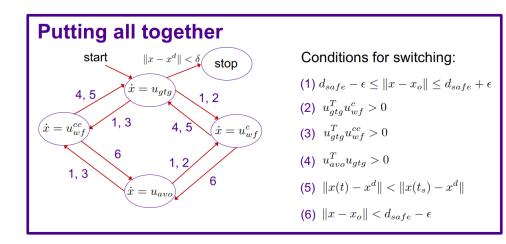


Exercise 5.2 – Task



By taking account of the robot's size and limitation, design and implement wall-following behavior to your switching controller in 5.1.

Describe your approach in designing u_{wf}^c , u_{wf}^{cc} , and computing x_o (and u_{avo}) from sensor readings as well as your observations on the resulting controller.



Show the result by plotting:

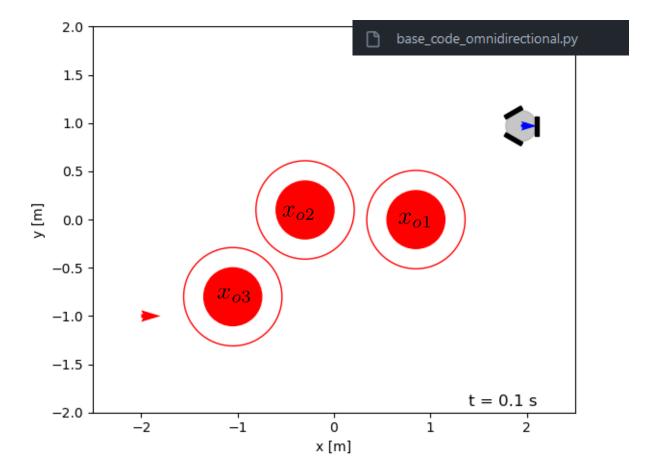
- time series of control input u and $(v_x^2 + v_y^2)^{0.5}$
- time series of error $(x^d x)$,
- time series of minimum reading distance from the sensor
- time series of state trajectory x vs x^d , and
- XY **trajectory** of the robot (or final snapshot of the simulator).

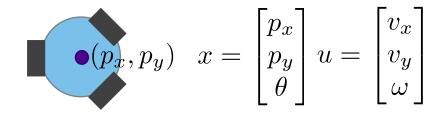
IMPORTANT TIPS:

- Use visualization to help debug (e.g., the $u_{gtg}, u_{avo}, u_{wf}^c, u_{wf}^{cc},$ etc.)
- Print every time the state changes



Exercise 5.3 – Scenario





Model: omnidirectional mobile robot (singleintegrator model)

Initial Position: $x[0] = \begin{bmatrix} 2 & 1 & 0 \end{bmatrix}^T$

Goal: static at $x^d = [-2 \ -1 \ *]^T$.

* Can be any orientation at goal position

Key Scenario:

- We assume the robot/controller can identify a **circular obstacle** (centroid and radius) once it is near. Here, 3 obstacle presents:
 - 1. centered at $p_x^{o1} = 0.85$, $p_y^{o1} = 0$ with radius 0.3m.
 - 2. centered at $p_x^{o2} = -0.3$, $p_y^{o2} = 0.1$ with radius 0.3m.
 - 3. centered at $p_x^{o3} = -1.05$, $p_y^{o3} = -0.8$ with radius 0.3m.

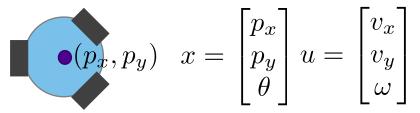
Control Objective:

Reach the goal while avoiding contact/collision with obstacle



Exercise 5.3





By taking account of the robot's limitation, implement the QP-based controller as follows

$$\begin{split} u &= \arg\min_{u^*} \ \|u_{gtg} - u^*\|^2 \\ \text{s.t.} \ \left(\frac{\partial h_{o1}}{\partial x}\right)^T u^* &\geq -\gamma(h_{o1}(x)) \\ \left(\frac{\partial h_{o2}}{\partial x}\right)^T u^* &\geq -\gamma(h_{o2}(x)) \\ \left(\frac{\partial h_{o3}}{\partial x}\right)^T u^* &\geq -\gamma(h_{o3}(x)) \end{split} \qquad \text{with } h_{oi} = \left\|\begin{bmatrix} p_x \\ p_y \end{bmatrix} - \begin{bmatrix} p_{vi}^{oi} \\ p_{y}^{oi} \end{bmatrix}\right\|^2 - R_{si}^2 \end{split}$$

 $x_{oi} = \begin{bmatrix} p_x^{oi} \\ p_y^{oi} \\ 0 \end{bmatrix}$

NOTE: u_{gtg} still need to comply with the robot's max speed. You can use u_{gtg} from 5.1.

Then, test the controller for $\gamma(h) = 0.2h$, $\gamma(h) = 10h$, and $\gamma(h) = 10h^3$ and describe your observation on what does the variation affects.

Show the result by comparing the plot for each γ function variation via:

- Time series comparison of control input u_{gtg} vs u (plot only v_{x} and v_{y})
- Time series comparison of function h_{o1} , h_{o2} , and h_{o3}
- Comparison of XY trajectory of the robot



How to show obstacle on Simulator?

Plot using the axis object in the sim_mobile_robot class → sim_visualizer.ax

Option 1: using patch in matplotlib (for simple shape: circle, rectangle, etc.)

```
if IS_SHOWING_2DVISUALIZATION: # Initialize Plot
    sim_visualizer = sim_mobile_robot( 'omnidirectional' ) # Omnidirectional Icon
    #sim_visualizer = sim_mobile_robot( 'unicycle' ) # Unicycle Icon
    sim_visualizer.set_field( field_x, field_y ) # set plot area
    sim_visualizer.show_goal(desired_state)
    sim_visualizer.ax.add_patch( plt.Circle( (0, 0), 0.5, color='r' ) )
    sim_visualizer.ax.add_patch( plt.Circle( (0, 0), d_safe, color='r', fill=False) )
    sim_visualizer.ax.add_patch( plt.Circle( (0, 0), d_safe + eps, color='g', fill=False) )
```

Example for 5.1

Draw (full) red circle for obstacle Draw empty red circle for d_{safe} Draw empty green circle for $d_{safe} + \epsilon$

Option 2: by defining obstacle's vertices and use line plot

Example for 5.2



How to implement QP for 5.3?

$$u = \underset{u^*}{\operatorname{arg \, min}} \|u_{gtg} - u^*\|^2$$
s.t.
$$\left(\frac{\partial h_{o1}}{\partial x}\right)^T u^* \ge -\gamma(h_{o1}(x))$$

$$\left(\frac{\partial h_{o2}}{\partial x}\right)^T u^* \ge -\gamma(h_{o2}(x))$$

$$\left(\frac{\partial h_{o3}}{\partial x}\right)^T u^* \ge -\gamma(h_{o3}(x))$$

Refer to lecture 10 on 22.3.2023

$$\min_{z} \frac{1}{2} z^{T} Q z + c^{T} z$$

s.t. $Hz \leq b$

import cvxopt Require cvxopt python package

```
OP-based controller
                                                                              z = \begin{bmatrix} v_x \\ v_y \end{bmatrix}
Q mat = 2 * cvxopt.matrix( np.eye(2), tc='d')
c mat = -2 * cvxopt.matrix( u gtg[:2], tc='d')
# Fill H and b based on the specification afterwards
                                                                              Change these
# --> row is number of constraints / specification
H = np.zeros([row, 2]) # TODO
                                                                              two lines to the
b = np.zeros([row, 1]) # TODO
                                                                              appropriate
# Resize the H and b into appropriate matrix for optimization
                                                                              values
H mat = cvxopt.matrix( H, tc='d')
b mat = cvxopt.matrix( b, tc='d')
# Solving Optimization
cvxopt.solvers.options['show_progress'] = False
                                                                        NOTE: These code only compute
sol = cvxopt.solvers.qp(Q mat, c mat, H mat, b mat, verbose=False)
                                                                        the linear velocity (x and y) which
current_input = np.array([sol['x'][0], sol['x'][1], 0])
                                                                        is sufficient for 5.3.
```



Question?

- Consult them via
 - Exercise sessions on 15.3.2024, 22.3.2024, and 29.3.2024
 - Teams channel