Speeding up Generalized Fuzzy k-Means Clustering Algorithm by GPUs

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ABSTRACT

The graphics hardware is becoming increasingly more powerful and programmable with the introduction of Graphics Processing Units (GPU) like the NVidia GeForce series. The GPU’s exceed the ordinary general purpose CPU’s ability to do ﬂoating point operations due to the massively parallel architecture in the GPU’s.

With the newest GPU’s one actually have enough programmable freedom to do other computations than computer graphics processing. This project will take advantage of this in order to get high performance implementations of image analysis algorithms.

In this project we will implement an image analysis algorithm, which is Generalized Fuzzy k-Means Clustering Using m nearest Cluster Centers (GFKM) [1], on a GPU. We also make comparisons with CPU based implementations and analysis the pros and cons of using GPU’s in image analysis. Our experimental results show that our GPU-based GFKM algorithms are four to seven times faster than on CPU.

I. INTRODUCTION

II. RELATED WORK

We first briefly introduce the GPU architecture, and then review the GFKM algorithms.

A. The GPU architecture

B. The GFKM algorithm

1. Input an initial set of cluster centers *SC*0 = {**C***j*(0)} and the values of ε and *M*. Set *p* = 0. Let, *NNTi*, and *DNNTi* responding to the squared Euclidean distance between **X***i* and **C***j*, the set of *M* nearest cluster centers for the data point**,** and the set of *M* corresponding shortest distances for the data point****. Then, we calculateand initialize *NNTi* and *DNNTi*.
2. Given the set of cluster centers *SCp*, update membership **** using equation (1). If **C***j*∈*NNTi* is the *l*th nearest neighbor of **X***i*, set  = ****; otherwise let  = 0.

**** = , for *r* = 1 to *N* and *s* = 1 to *M* (1)

1. Compute the center for each cluster using equation (2) to obtain a new set of cluster representatives *SCp+*1 = {**C***j*(*p*+1)}.

**C***j* =  , for S *j* = {**X** *i*: **X** *i*∈ *NNTj*, *i* = 1 to *N*} (2)

1. Calculate, update *NNTi* and *DNNTi* for *i* = 1 to *N*, and calculate distortion value *J* using equation (3).

*J* =  (3)

1. If < ε, then stop, where ε > 0 is a very small positive number. Otherwise set *p = p + 1* and go to step (2).

The computational complexity of GFKM is also O(*Nkt*), where *t* is the number of iterations. The pseudocode of algorithm as follows:

Algorithm 1: CPU-based GFKM

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III. Design of GPU-based parallel GFKM algorithm

The steps of the GFKM algorithm are: (1) calculating  andinitializing *NNTi* and *DNNTi*, (2) updating memberships , (3) computing the new center for each clusters, (4) calculate  andupdating *NNTi* and *DNNTi*, (5) calculating distortion value *J*. The GPU-based parallel GFKM algorithm is designed as follows:

* Step (1), (2), and (4): We utilize the GPU on-chip registers to minimize the latency of data access [2].
* Step (3): The first, we use the GPU-based counting sort algorithm for sorting array *NNT* with keys and values are cluster indices and point indices, respectively. To reduce  and points for each centroid, we use the GPU-based parallel reduction algorithm [3]. Each kernel processes each dimension of each centroid, and the kernels run concurrently.
* Step (5): We use the GPU-based parallel reduction algorithm for this step [3].

A. Calculating  andinitializing *NNTi* and *DNNTi*

Algorithm 2: Calculating  andinitializing *NNTi* and *DNNTi* based on CPU

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Algorithm 3: Calculating  andinitializing *NNTi* and *DNNTi* based on GPU

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The CPU-based algorithm of calculating  andinitializing *NNTi* and *DNNTi* is shown in Algorithm 2. The first method parallelizes computing the distance between each data point and each centroid in Algorithm 2. One data point is dispatched to one thread, and then each thread calculates the distance from a corresponding data point to k centroids, and then initializes *NNTi* and *DNNTi*, as shown in Algorithm 3. Line 1 and 2 show how the algorithm designs the thread block and gird. Line 3 to 6 calculate the position of the corresponding data point, NNT, and DNNT for each thread in global memory. Line 7 loads the data point into the register. Lines 8-13 calculate the distance and initialize *NNTi* and *DNNTi*.

Algorithm 3 only has one level of loop instead of two levels in Algorithm 2, because the loop for *N* data points has been dispatched to N threads, which decreases the time consumption significantly because many threads are working in parallel. It is worth pointing out that the key step of achieving high efficiency is loading the data points into the on-chip registers, which ensures that reading the data point from global memory happens only once when calculating the distances between the data point and *K* centroids. Obviously, reading from register is much faster than reading from global memory. Besides, coalesced access to the global memory also decreases the reading latency.

B. Updating memberships

We apply the design as described in the section A. Note here that *NNTi* and *DNNTi* were initialized and updated after step (1) and step (4), respectively.

Algorithm 4: Updating memberships based on CPU

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Algorithm 5: Updating memberships based on GPU

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C. Computing the new center for each clusters – Updating centroids

Algorithm 6: Updating centroids based on CPU

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The sequential code of the updating centroids step is shown in Algorithm 6 with the computational complexity O(NMd+kd). Each data point ****belonging to *M* nearest cluster centers determined by *NNTi*, and the data points belonging to the same centroid constitute one cluster. It is difficult to be fully parallelized. If we assign each element in *NNT* to a thread, it will generate write conflict when adding the data to the shared memory. On the other hand, if we assign each centroid to a thread, the computing power of the GPU cannot be fully utilized. However, if we sort array *NNT* first with keys and values are cluster indices and point indices, respectively, then the calculating new centroids can run in parallel on each centroid and also each dimension of centroid. We use the counting sort algorithm for sorting array *NNT*, it is divided into four steps as in Table 1.

Table 1: The sequential code of counting sort for sorting array *NNT*

|  |  |  |
| --- | --- | --- |
| Steps | Function | Pseudocode |
| 1 | Initialize histogram | **for** *i* = 1 **to** *k* **do** *histogram*[*i*] = 0; |
| 2 | Calculate histogram | **for** *i* = 0 **to** *N\*M* **do** *histogram*[ *NNT*[*i*] ]++; |
| 3 | Calculate exclusive prefix sums (scan) | *scan*[1] = 0;  **for** *i* = 1 **to** *k-1* **do** *scan*[*i+1*] *= histogram*[*i*] *+ scan*[*i*]; |
| 4 | Sort | **for** *i* = 0 **to** *N\*M* **do** *ouput*[ scan[ NNT[*i*] ]++] = *i*/*M*; |

The first, the algorithm loops over the items of *NNT*, calculating a histogram of the number of times each cluster index occurs within *NNT*. It then performs a prefix sum computation to determine, for each cluster index, the starting position in the output array of the items having that cluster index. Finally, it loops over the items again, moving each corresponding point index of item into its sorted position in the output array.

Algorithm 7: Calculating the histogram of *NNT* using atomicAdd operation based on GPU

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Algorithm 8: Calculating the starting index for each cluster based on GPU

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Algorithm 9: Counting sort based on GPU

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Algorithm 10: Reducing ****for the *j*th clusterusing the parallel reduction algorithm based on GPU

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1. ;




7. s
9. s
11. s
12. s
13. s
14. s
15. s
16. s

Algorithm 11: Reducing ****for the *j*th cluster and the *l*th dimensionusing the parallel reduction algorithm based on GPU

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1. ;







10. s
12. s
14. s
15. s
16. s
17. s
18. s
19. s

D. Calculating, updating *NNTi* and *DNNTi*

Algorithm 12: Calculating, updating *NNTi* and *DNNTi*, and also calculating distortion value *J* based on CPU

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Algorithm 13: Calculatingand , updating *NNTi* and *DNNTi*, based on GPU

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E. Calculating distortion value *J* using the parallel reduction algorithm based on GPU

Algorithm 14: Calculating distortion value *J* using the parallel reduction algorithm based on GPU

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7. s
9. s
11. s
12. s
13. s
14. s
15. s
16. s

IV. EXPERIMENTAL RESULTS

The GFKM algorithm is implemented using CUDA version 6.5. The experiments are conducted on a PC with an NVIDIA GeForce GTX 760 GPU and an Intel(R) Core(TM) i5-4690 CPU. GTX 760 has six SIMD multi-processors, and each one contains 192 processors and performs at 1.5 GHz. The memory of the GPU is 2GB with the peak bandwidth of 192.2 GB/s. The CPU has four cores running at 3.50 GHz. The main memory is 8 GB with the peak bandwidth of 25.6 GB/s. To show the speedup effect more clearly, the time of the application is measured after the file I/O.

Example 1: The data set generated from three real images: “Lena,” “Baboon,” and “Peppers.”

In this example, the data set consists of 49,152 data points with *d* = 16. The values *M* = 2, *k =* 8, and ε = 1e-8,is used for the test. The running time each step of GFKM algorithm at iteration #1 and total running time after 126 iterations on CPU and GPU are shown in Table 2. The updating membership step on GPU is seven times faster than on CPU. The updating centroids step on GPU is nearly two times faster than on CPU. The updating *NNT* and *J* step on GPU is fifteen times faster than on CPU. In this example, the running on GPU is about seven times faster than on CPU.

Table 2: The computing time of the GFKM algorithm based on CPU and GPU using the data set generated from three real images: “Lena,” “Baboon,” and “Peppers”.

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| --- | --- | --- | --- |
| GFKM | CPU  (4 processors) | GPU  (1152 processors) | Speedup |
| Initializing NNT | 20.531 | 1.170 | 17.5 |
| Update membership at iteration #1 | 10.583 | 1.471 | 7.2 |
| Update centroids at iteration #1 | 4.322 | 2.587 | 1.7 |
| Update NNT and J at iteration #1 | 22.375 | 1.444 | 15.5 |
| Total time of iteration #1 | 37.280 | 5.502 | 6.8 |
| Total time after 126 iterations | 4835.127 | 664.967 | 7.3 |

REFERENCES

[1] Franklin J. C. Lai, Eric Y. T. Juan, and Jim Z. C. Lai, Generalized Fuzzy k-Means Clustering Using m nearest Cluster Centers, 2013.

[2] You Li, Kaiyong Zhao, Xiaowen Chu, and Jiming Liu, Speeding up K-Means Algorithm by GPUs, 2010.

[3] Mark Harris, Optimizing Parallel Reduction in CUDA, NVIDIA Developer Technology, 2007.