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# Journal of Membrane Science

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# Gas permeation through single-crystal ZIF-8 membranes

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#### ARTICLE INFO

Keywords:
Metal-organic framework
Single crystal
ZIF-8
Gas permeation
Ideal selectivity

#### ABSTRACT

Grain boundaries are an unavoidable microstructural feature in intergrown polycrystalline metal-organic framework (MOF) membranes. They have been suspected to be less size-selective than a MOF's micropores, resulting in suboptimal separation performances – a speculation recently confirmed by transmission electron microscopy of MOF ZIF-8. Single-crystal membranes, without grain boundaries, should confine mass transport to micropores and reflect the intrinsic selectivity of the porous material. Here, we demonstrate the feasibility of fabricating single-crystal MOF membranes and directly measuring gas permeability through such a membrane using ZIF-8 as an exemplary MOF. Our single-crystal ZIF-8 membranes achieved ideal selectivities up to 28.9, 10.0, 40.1 and 3.6 for gas pairs  $CO_2/N_2$ ,  $CO_2/CH_4$ ,  $He/CH_4$  and  $CH_4/N_2$  respectively, much higher than or reversely selective to over 20 polycrystalline ZIF-8 membranes, unequivocally proving the non-selectivity of grain boundaries. The permeability trend obtained in single-crystal membranes aligned with a force field that had been validated against multiple empirical adsorption isotherms.

### 1. Introduction

Metal-organic frameworks (MOFs) are commonly defined as potentially porous coordination polymers made of metal nodes and organic ligands extending in two or three dimensions [1]. Reticular syntheses [2] afforded MOFs a wide range of tailorable pore apertures from 3.0 Å in ZIF-11 [3] to 98 Å in IRMOF-74-XI [4], corresponding to diverse molecular sizes from those of small gases (e.g. hydrogen) to natural proteins. Post-synthetic modifications can usually alter the reactivity of a MOF through its linkers [5]. These two developments have made MOFs strong contenders in adsorption- and membrane-based separations [6,7]. In the domain of membrane-based gas separations, MOFs are typically used as either the selective layer in polycrystalline pure-MOF membranes [8], or the stability- and permeability-enhancing filler in mixed-matrix membranes (MMMs) [7,9]; a few MOFs even simultaneously increase permeability and selectivity of MMMs [10,11].

From a design point of view, polycrystalline pure-MOF membranes are theoretically advantageous over MMMs because a pure-MOF membrane's selectivity should be predictable – close to the optimal, molecular-sieving selectivity of the MOF's pore aperture size [7] – as long as the membrane is properly intergrown and crack-free. Many endeavours have been dedicated to fabricating a crack-free polycrystalline MOF membrane over a substrate by optimising a) chemistry of the precursor solutions [12], b) chemistry of the substrate [13,14], c)

membrane growth method or set-up [15–17], or d) a combination of the aforementioned three [18,19]. One of such well-engineered polycrystalline ZIF-8 (Zn(MeIM) $_2$ , MeIM = 2-methylimidazole) membranes used the pore aperture of ZIF-8 (3.4 Å) to score an exceptional separation factor of 105 for propene (kinetic diameter: 4.0 Å) over propane (kinetic diameter: 4.3 Å) [12].

Despite these remarkable developments, polycrystalline membranes, by their very nature, always contain grain boundaries that have been suspected to be non-size-selective thus undermining separation performances [6,20–23] (Fig. 1). A recent breakthrough in transmission electron microscopy (TEM) imaging by Zhu et al. revealed for the first time the grain boundary structure in a MOF [24]. They recreated the self-assembly process of the interface between two ZIF-8 crystals joint via the (110) plane by molecular dynamics simulation, Two of the three interconnected channels at the grain boundary ( $\sim$ 8.2 Å and  $\sim$ 3.8 Å in diameter) were larger than the six-membered-ring channels (3.4 Å in diameter) of ZIF-8; self- and transport-diffusivities of guest molecules were higher in samples with grain boundaries.

Single-crystal membranes (SCMs) are widely recognised as the ideal tool to study a material's intrinsic permeation selectivities [6,20,21,25], and are the assumed model in computational predictions of MOF-membranes' separation performances [26–28]. Single crystals have proved useful for studying intrinsic diffusion properties – infra-red imaging monitored the CO<sub>2</sub> uptake and revealed the concentration

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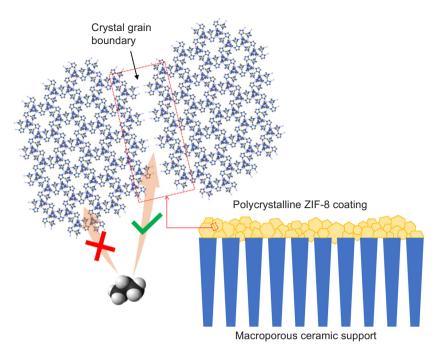


Fig. 1. A schematic diagram showing the possible grain boundary structure in a polycrystalline ZIF-8 membrane. A molecule, such as propane, that is too large to go through the six-membered-ring channel of ZIF-8 may be able to permeate through the larger grain boundary structure (red dotted rectangle). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

evolution within a ZIF-8 crystal [29] and at the crystal-polymer interface [30]. However, there are very limited attempts at using single crystals in a membrane configuration to investigate the intrinsic permeation properties because of lack of practical applications of these membranes [31] and fabrication difficulties [32,33]. Since single-crystal zeolite membranes fabricated more than three decades ago [32,34,35], only one one-dimensional coordination polymer (i.e. by definition, not a MOF [1]) [Cu<sub>2</sub>(bza)<sub>4</sub>(pyz)]<sub>n</sub> (bza = benzoate; pyz = pyrazine)[21] and its analogues [36,37] have been made into SCMs. There was, regrettably, no comparison between these SCMs and polycrystalline membranes of the same materials in terms of permeance or selectivity. In our proof-of-concept study of gas permeation through a single-crystal MOF membrane, ZIF-8 was chosen as a representative material because of the readily available data on ceramic-supported polycrystalline ZIF-8 membranes for comparison.

A large crystal is a prerequisite for single-crystal membranes for practical reasons – it would be prohibitively difficult to manually pick up and orient the crystal in the subsequent stage of membrane fabrication. Based on our experience, crystals of at least 100 micrometres are worth being considered for further processing. In order for the downstream pressure to be measured with better accuracy, we needed crystals of a few hundred micrometres – a demanding size as most crystallisation studies aimed to make nanosized crystals [38]; this is also pushing the upper limit of ZIF-8 size reported to date (around  $300 \,\mu\text{m}$ ) – first synthesised by Chmelik et al. [39] and reproduced or adapted in many other studies [31,40–45]. Crystal growth is a highly complex and intractable process [46]. It is impossible and beyond the capacity of this work to predict a complete set of parameters that will guarantee the unusually large crystals; instead, we built upon methods that have produced the largest ZIF-8 crystals reported.

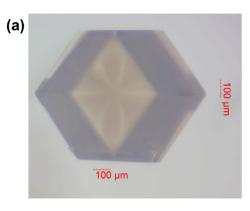
Here we report permeabilities of light gases (helium, carbon dioxide, nitrogen and methane) through a single-crystal membrane of ZIF-8, and compare the single-crystal ideal selectivities with polycrystalline ZIF-8 membranes. These light gases constitute industrially relevant separations. Carbon dioxide and nitrogen are the main impurities in natural gas [47], which is also an important source of the increasingly demanded helium [26,48]. Separating  $CO_2$  from  $N_2$ , the largest component of flue gas, is essential to curbing  $CO_2$  emission [49]. To the best of our knowledge, this is the first direct measurement of gas permeation through a single-crystal MOF membrane. Without

interference from non-selective grain boundaries or inter-crystalline defects, the single-crystal ideal selectivities can be considered intrinsic to ZIF-8 as permeation occurs through micropores only. We believe that intrinsic selectivities are of great interest to the microporous membrane community as these values could provide a benchmark for polycrystalline ZIF-8 membranes' performance.

### 2. Experimental

### 2.1. Synthesis of ZIF-8 (optimised protocol)

1.764 g (5.93 mmol) of zinc nitrate hexahydrate (≥98%, Sigma-Aldrich) was dissolved in 15 ml of methanol (≥99.8% HiPerSolv CHROMANORM® grade, VWR UK). 0.9739 g (11.86 mmol) of 2-methylimidazole (99%, Sigma-Aldrich) and 0.4034 g (5.93 mmol) of sodium formate (99%, Sigma-Aldrich) were dissolved in 25 ml of methanol. The two solutions were combined and mixed briefly for 5 min on a stirring plate. Meanwhile, 3 new 20-ml crimp-cap glass vials (Kinesis UK) were rinsed with methanol and set aside with their caps loosely placed over them to prevent dust or any particulates from entering the vials. 13 ml of the combined precursor solution was drawn by a syringe and passed to each glass vial through a 0.2-µm polytetrafluoroethylene (PTFE) syringe filter (VWR UK). The vials were sealed by a manual crimper (Kinesis UK) and placed in a 90-°C oven for 24 h. The vials were left to cool naturally in the oven until they were safe to touch. Large crystals on the wall of vials (Fig. S7) were carefully picked up by PTFE tweezers with fine, pointed ends and released into a small snap-cap vial of fresh methanol. Both the manually selected crystals and the leftover crystals were soaked in fresh methanol replaced every 24 h for 2 days - the extensive solvent exchange was to increase the chance of removing unreacted precursor chemicals. The crystals were dried in a vacuum oven at 25 °C for 6 h. The manually selected crystals were inspected under an optical microscope. Single, visually defect- and crackfree crystals with the characteristic dodecahedron shape of ZIF-8 were kept for membrane fabrication and single-crystal XRD. The leftover crystals were kept in another container for powder XRD, nitrogen adsorption and other characterisation studies.



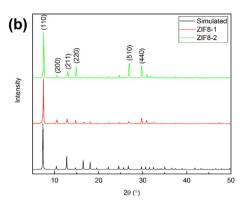


Fig. 2. (a) A micrograph of a millimetre-sized single crystal ZIF-8 viewed along [110] axis. (b) Powder X-ray diffraction (PXRD) pattern of two batches of ZIF-8 from which large, single crystals were selected to make membranes. The two batches were made with the same conditions (in methanol at 90 °C for 24 h, i.e. the optimised protocol in Section 2.1). After large, single crystals were isolated, the remaining product was used for PXRD. The simulated pattern was from Park et al. [3].

#### 2.2. PXRD studies

Powder X-ray diffraction spectra were collected by an PANalytical X'Pert Pro diffractometer with a CuK $\alpha$  X-ray source (40 kV, 20 mA) and a reflection-transmission spinner sample stage at ambient conditions. Large crystals were ground before pressed onto the sample holder to obtain a flat surface.

#### 2.3. Nitrogen sorption

Nitrogen sorption measurement was performed on a Micromeritics 3Flex volumetric instrument at 77 K. The sample was evacuated at  $100\,^{\circ}$ C under vacuum overnight, followed by 2 h of in situ degassing at  $100\,^{\circ}$ C under vacuum prior to the start of nitrogen sorption analysis. BET surface area was estimated from the quantities adsorbed at relative pressures between 0.045 and 0.299.

#### 2.4. Construction of single-crystal membranes

We adapted the single-crystal zeolite membrane model designed by Geus et al. [35] because of its simplicity and compatibility with a commercially available membrane holder (Merck Millipore, XX4404700). Steel plates (47 mm in diameter, 0.37 mm in thickness) with a 400-µm-diameter hole drilled in the centre were made in-house and cleaned with acetone. The construction was carried out under an optical microscope. Epoxy (Araldite, rapid 2-component epoxy) was spread around the hole and pushed to the rim of the hole as closely as possible without going over the rim. Five minutes later, a ZIF-8 crystal, held by high-precision plastic tweezers (ideal-tek, 707 A.DG), was placed over the epoxy with its large flat base parallel to the steel plate, and secured in place by a gentle push. We allowed the first layer of epoxy to partially set so that it would not overflow the rim of the hole and cover the bottom of the crystal. A fresh batch of epoxy was made and spread around the crystal to ensure a gas-tight seal. The membrane assembly was left at ambient conditions overnight for the epoxy to cure.

#### 2.5. Gas permeation measurements

The constant-volume, pressure-rise apparatus (Fig. S5) was used to measure gas permeation. After the membrane was placed in the permeation cell and sealed by a Viton O-ring, each segment of the rig was evacuated for 5–30 min depending on the size of the segment. Gas was introduced to the upstream tank until the pressure stabilised at around 2.1 bar absolute (or 31 psia). The system was left in this state for 2 days, which we observed was enough for the downstream air ingress to reach a steady-state, whilst the pressure gauges 1 and 2 (Fig. S5) were recording continuously. The valve V-2 was then opened; the upstream and downstream pressures were recorded for another 2 days.

#### 3. Results

#### 3.1. Synthesis of large, single crystals of ZIF-8

The plethora of chemical and process variables used to synthesise the same MOF makes it challenging to systemically and extensively investigate crystallisation processes. For example, ZIF-8 have been made from various Zn<sup>2+</sup> salts (nitrate, acetate, sulfate, chloride, bromide, iodide, perchlorate etc) [12,50,51], with or without [52,53] a modulator, in different solvents (water, alcohols, dimethylformamide, dimethyl sulfoxide, acetone etc) [52-54] with different molar ratios of reactants at a range of temperatures [55]. To further complicate the matter, the variables may not be independent from each other - one could behave differently when combined with different sets of other variables. For example, sodium formate, a common modulator in ZIF-8 syntheses, was observed to accelerate nucleation and result in smaller ZIF-8 crystals in a solvothermal synthesis [41]; the same modulator served the opposite purpose (i.e. slowing down nucleation and facilitating the formation of bigger ZIF-8 crystals) in an ambient-condition synthesis with stirring [40]. Some studies have tried to control the crystal size of ZIF-8 by adjusting a few variables [50,56]; however, the large array of variables means our understanding of crystal size engineering is merely fragments of the whole picture. In view of these challenges, it is more realistic to fine-tune existing protocols than designing the optimal one ab initio.

On the basis of the largest-to-date ZIF-8 [31,39], we formulated a reproducible synthesis protocol that made large single crystals of ZIF-8 up to 1 mm (Fig. 2a). Most of the crystals that appeared to be single, crack-free under the microscope were above 500 µm (Fig. S2a). The optimal protocol was finalised after varying the zinc salt, synthesis temperature and the modulator concentration (Supplementary Information 1.1); the observations did not always agree with what previous studies suggested, highlighting limitations of the current knowledge of crystal size engineering. For example, we consistently obtained larger crystals from zinc nitrate than from zinc chloride, whilst the opposite was reported in the literature [12,50]. Also, we postulated that two opposing roles - deprotonation agent and competitive ligand of the modulator were present instead of just one (Supplementary Information 1.1). Connecting the fragments of existing insights to form the complete picture of ZIF-8 size control is well beyond the capacity of this work; nonetheless, we found that a few simple steps of removing undesired nucleation sites (filtering the precursor solution, using highpurity solvent and rinsing new glass vials with high-purity solvent) helped achieve bigger crystals than the original methods [31,39] and ensure the reproducibility of our protocol.

Single-crystal X-ray diffraction (Table S3) and powder X-ray diffraction spectra (Fig. 2b) were collected to confirm that the product was indeed high-quality ZIF-8. A Type 1 adsorption isotherm characteristic of microporous materials [57] was obtained from nitrogen sorption at 77 K (Fig. S1), from which the Brunauer–Emmett–Teller surface area

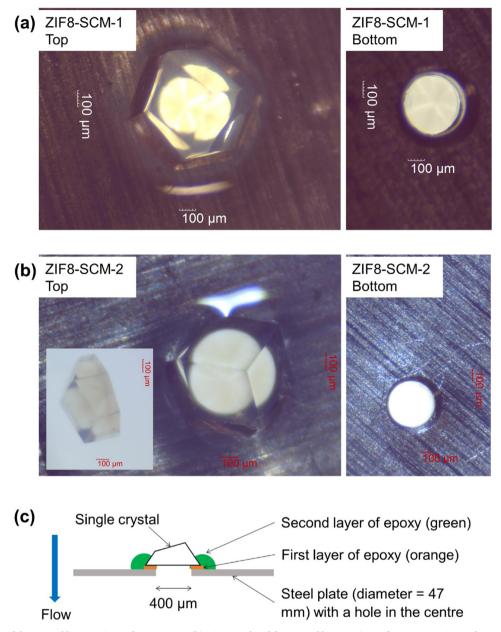


Fig. 3. (a) Micrographs of the top and bottom views of ZIF8-SCM-1. (b) Micrographs of the top and bottom views of ZIF8-SCM-2, inset: the crystal that was embedded in ZIF8-SCM-2. (c) A schematic side-view of the single-crystal membrane assembly.

was calculated to be  $1490\,\mathrm{m^2~g^{-1}}$ , within the range of literature values from 960 to  $1918\,\mathrm{m^2~g^{-1}}$  compiled by Huang et al. [58].

# 3.2. Single-crystal membrane fabrication

In order to test gas permeation through a SCM in a commercially available permeation test cell (Merck Millipore, XX4404700), we glued the selected single crystal to a steel plate (47 mm in diameter, 0.37 mm in thickness) with a 400-µm-diameter hole drilled in the centre. Two single-crystal ZIF-8 membranes, ZIF8-SCM-1 and ZIF8-SCM-2 (Fig. 3a and b) containing single crystals ZIF8-1 and ZIF8-2 respectively, were fabricated and tested. ZIF8-1 and ZIF8-2 were perfect-looking single crystals of ZIF-8 selected from two identical syntheses detailed in Methods.

Although ZIF-8 is isotropic and has identical six-membered channels along the [111] direction, it has another set of inaccessible four-membered channels in the [100] direction [18,59]. Therefore, having the pressure gradient in the [111] direction makes the ideal orientation;

and [100] direction, the most unfavourable because of a more torturous permeation path. We did not engineer the growth direction of ZIF-8 crystals. Serendipitously, most of the single crystals harvested from the wall of a glass vial grew along similar directions – somewhat between [111] and [110] – as seen by comparing the Fig. 3a and b with Fig. S4. Conveniently, they were 'half crystals' – half of a whole rhombic dodecahedron – with a large, flat surface (Fig. 3b inset) originally in contact with the wall. This large, flat surface became the base parallel to the steel plate and perpendicular to the pressure gradient direction (Fig. 3c). Therefore, harvesting single crystals from the wall of glass vials proved beneficial in two ways – a) it reduced the chance of picking up intergrown crystals, and b) it helped ensure a rather consistent orientation of the embedded crystal in the membrane assembly.

Our SCM assembly has its limitations. Firstly, the embedded crystal does not have a set of parallel surfaces (Fig. 3c), resulting in uneven thickness – the average thickness was used in permeability calculations. There are errors associated with averaging and even the method of using the average thickness (Supplementary Information 1.4.4);

however, they will not affect the ideal selectivities of each membrane because when taking the ratio of two permeabilities, the thickness term disappears (Supplementary information 1.4.1). Secondly, the thickness far exceeds what is conventionally acceptable for a membrane. This is the side effect of using a large ZIF-8 crystal as the crystal grows in all three dimensions. We decided not to polish the brittle crystal to protect its integrity. Future work may consider polishing methods that do not damage the crystal, or using MOFs that naturally have a plate-like morphology. Lastly, the extremely small permeation area (i.e. the area of the hole on the steel plate) presents a challenge to the downstream pressure measurement. We kept the downstream volume of the rig (Fig. S5) is kept to the minimum – just the internal volume of the necessary tubing – so that the pressure transducer can pick up any change caused by the small amount of permeate.

### 3.3. Single-gas permeation and ideal selectivities

Single-gas permeabilities of both single-crystal membranes agree with the trend reported by other ZIF-8 membranes – permeability is generally inversely proportional to the kinetic diameter of the permeant, and framework flexibility [31,60] allows transport of molecules larger than the aperture size (Table S1 and Fig. S6). We compared our SCMs' ideal selectivities of four industrially important separations ( $CO_2/N_2$ ,  $CO_2/CH_4$ ,  $He/CH_4$  and  $CH_4/N_2$ ) with over 20 polycrystalline ZIF-8 membranes that measured single-gas permeation of common small gases at room temperature (Fig. 4 and Table S2). Some

polycrystalline ZIF-8 membranes such as the those reported by Brown et al. [61] and Marti et al. [62] were not included in the comparison because the Torlon polymer substrate showed an ideal  $\text{CO}_2/\text{N}_2$  selectivity of 0.90 [63] – higher than the Knudsen value of 0.8. The macroporous substrate might have affected permeation through adsorption.

Despite the disparity in our two SCMs' ideal selectivities, they are almost always well above the Knudsen selectivities and polycrystalline ZIF-8 membranes' selectivities for all four gas pairs. Most of the polycrystalline selectivities do not reflect a remarkable improvement from – some were even below – Knudsen selectivities, suggesting that the molecular sieving potential of ZIF-8 was not fully achieved in those membranes. Interestingly, both SCMs were  $CH_4$ -selective whereas most polycrystalline ZIF-8 membranes had ideal  $CH_4/N_2$  selectivities fluctuating around unity, showing no selectivity or marginal N2-selectivity (Fig. 4d). Two membranes [64,65] showed superior or similar  $CO_2/CH_4$  selectivity to ours (Fig. 4b), but neither membrane could match our results in other gas pairs. Thus, their exceptional  $CO_2/CH_4$  selectivities should not be generalised to indicate superior membrane performance.

Unlike polycrystalline ZIF-8 membranes that are mostly non-selective or  $N_2$ -selective over CH<sub>4</sub> (Fig. 4d), our SCMs showed reverse selectivity for CH<sub>4</sub> over  $N_2$ . Experimental single-component adsorption isotherms at  $25-30\,^{\circ}\text{C}$  revealed that ZIF-8's uptake of CH<sub>4</sub> almost double that of  $N_2$  between 0 and 1 bar [66], i.e. the adsorptive CH<sub>4</sub>/ $N_2$  selectivity is around 2. The linear isotherms suggest that we can expect the adsorptive selectivity to continue being 2 at our upstream pressure

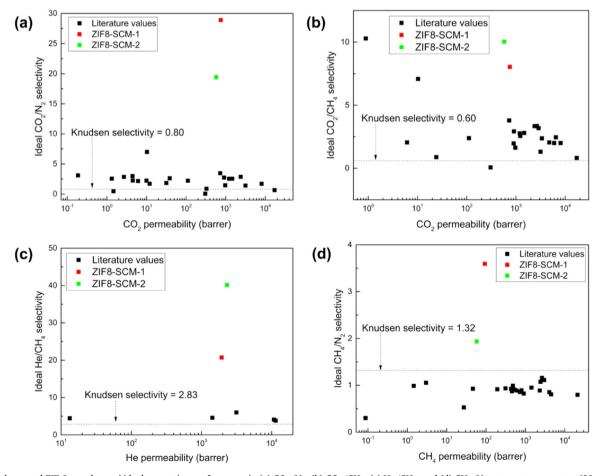


Fig. 4. Single-crystal ZIF-8 membranes' ideal separation performance in (a)  $CO_2/N_2$ , (b)  $CO_2/CH_4$ , (c)  $He/CH_4$ , and (d)  $CH_4/N_2$  at room temperature (20 – 25 °C). The ideal selectivities are compared with polycrystalline ZIF-8 membranes (Table S2) and Knudsen selectivity. Knudsen selectivity is commonly used to benchmark a membrane's performance – molecular sieving if membrane's selectivity is above the Knudsen selectivity; containing pinholes or mesopores otherwise. There are fewer literature values available for helium as it has not been as extensively tested as other small gases. The effective/average thicknesses of ZIF8-SCM-1 and ZIF8-SCM-2 were around 382  $\mu$ m and 292  $\mu$ m respectively. The method of calculating the average thickness is explained in Supplementary Information 1.4.4 and Fig. S10.

of 2 bar. On the other hand, the small difference in the two molecules kinetic diameters ( $N_2$ : 3.64 Å, CH<sub>4</sub>: 3.8 Å), coupled with ZIF-8 framework flexibility, means the diffusive selectivity of  $N_2$  over CH<sub>4</sub> should be marginal. Indeed, the ratio of total diffusion coefficients  $N_2$ /CH<sub>4</sub> in ZIF-8 was predicted to be 1.38 computationally by Battisti et al. [67], giving a diffusive CH<sub>4</sub>/ $N_2$  selectivity of 1/1.38 = 0.724. The adsorption-diffusion model suggests that the permeability (or membrane) selectivity is approximately the product of adsorptive and diffusive selectivities [68,69], the permeability selectivity should therefore be approximately 2 × 0.724 = 1.45, making ZIF-8 CH<sub>4</sub>-selective over  $N_2$ , in line with our SCMs' performances.

We also compared our ideal selectivities with four sets of in silico results based on four widely used flexible force fields [70-74] for molecular simulations of ZIF-8 (Supplementary Information 1.5). Helium was not modelled because of its nearly non-adsorbing nature at room temperature. We believe the force field proposed by Wu et al. [71] is more accurate than the other three because it was validated against the experimental adsorption isotherms of N2, CO2 and CH4 at 298 K whereas others were only compared with one of the gases. The ideal selectivities obtained from Wu et al.'s force field (Table S7) agree with our permeability trend of  $CO_2 > CH_4 > N_2$  (Table S1) – an additional validation of their force field. The grain boundary structure may provide an explanation on why polycrystalline ZIF-8 membranes tend to be N2 selective over CH4. There is an extra layer of the 2-methylimidazolate ligands at the grain boundary [24] which are the binding sites for N<sub>2</sub> [72]. Therefore, with additional imidazolate rings at grain boundaries, a polycrystalline membrane may have higher N<sub>2</sub> adsorption capacity than that in a single crystal, giving a lower and even reverse CH<sub>4</sub>/N<sub>2</sub> membrane selectivity.

We do not know with absolute certainty what caused the disparities in the two SCMs' selectivities. The disparity is larger when the gas pair involves a slow-permeating gas such as  $N_2$  and  $CH_4$ . A small quantity of ingress air could not be avoided during the extended test period – a method to correct for this is described in the Supplementary Information 1.3. As only a small amount of  $N_2$  or  $CH_4$  will accumulate in the downstream over the duration of a measurement, it is much more crucial to account for air ingress when testing  $N_2$  and  $CH_4$  than a fast-permeating species like He. Our method of background subtraction may not be robust enough for  $N_2$  and  $CH_4$ ; a high-vacuum set-up in the downstream or a sweep gas in conjunction with a gas chromatography may improve the consistency across different membranes. Having said that, we are aware that it is common to observe nonuniformity among single crystals because of variations in crystal quality [34].

## 4. Discussion

Our work is a proof of concept that direct measurements of gas permeabilities through a single-crystal MOF membrane can be achieved. More importantly, it provided like-for-like comparisons between polycrystalline and single-crystal MOF selectivities. The postulation that a single-crystal zeolite membrane may have higher separation factors than the polycrystalline version is not new [32]; however, there was no direct comparison in any SCMs [21,32,34,35] prior to our work. Such comparison was either not part of the objectives of those studies, or unachievable due to the lack of polycrystalline membranes or the lack of data under similar test conditions. By choosing an extensively studied MOF ZIF-8, we showed that by eliminating grain boundaries and constraining gas transport to intracrystalline pores, single-crystal ZIF-8 offered consistently higher ideal selectivities than polycrystalline ZIF-8 membranes for all gas pairs of interest.

This implies that grain boundaries indeed provide a less-selective route than ZIF-8's 6-membered-ring channels. With better-engineered synthetic protocols, it is possible to fabricate intergrown, macroscopic-defect-free polycrystalline membranes; but the corollary of a polycrystalline membrane is the presence of grain boundaries. Our results corroborated Zhu et al.'s conclusion from molecular dynamics

simulations of small gases and kinetic vapour adsorption of toluene and 1,3,5-trimethylbenzene in ZIF-8 structures with and without interfacial structures – that the larger interfacial openings in ZIF-8 increase the transport diffusivities of guest molecules. The discovery that larger molecules' mass transport is increased by a greater extent [24] means the diffusive selectivity  $D_i/D_j$  where D is diffusion coefficient, i is the smaller molecule and j the larger, is reduced by grain boundaries. Since permeability selectivity is the product of adsorptive and diffusive selectivities, polycrystalline ZIF-8 membranes will exhibit lower permeability selectivity than a SCM.

#### 5. Conclusions

We measured single-gas permeabilities of He, CO2, N2 and CH4 through two single-crystal ZIF-8 membranes and obtained ideal selectivities that are intrinsic to the chemistry and porous structure of ZIF-8 in the absence of other transport routes such as less selective grain boundaries. Our single-crystal membranes displayed consistently higher ideal CO<sub>2</sub>/N<sub>2</sub>, CO<sub>2</sub>/CH<sub>4</sub> and He/CH<sub>4</sub> selectivities of than an overwhelming majority of ceramic-supported polycrystalline membranes reported in the literature, and reverse CH<sub>4</sub>/N<sub>2</sub> selectivity compared with most polycrystalline membranes. The reverse CH<sub>4</sub>/N<sub>2</sub> selectivity was supported by simulation and could be explained by the extra imidazole rings, where N2 interacts with strongly, at grain boundaries. It is not our slightest intention to trivialise the breakthroughs in the field of polycrystalline membranes; they are, after all, a beacon of hope for the commercialisation of MOF membranes. What we want to demonstrate through our work is that grain boundaries in ZIF-8 contribute to mass transport and reduce ideal selectivity. With the accuracy of single-crystal membrane measurements improved in the future, they could provide useful empirical results for validation of new force fields.

#### Acknowledgements

C.C. thanks Nicholaus Prasetya for assistance with the gas permeation rig. We thank Dr Andrew White for collecting and refining single-crystal X-ray diffraction data, and staff at the Imperial Chemical Engineering Department Workshop for making the steel plates.

#### Appendix A. Supplementary material

Supplementary data associated with this article can be found in the online version at doi:10.1016/j.memsci.2019.01.027. The full computer simulation files are freely available from the open repository at https://doi.org/10.5281/zenodo.1435643.

### References

- [1] S.R. Batten, N.R. Champness, X.-M. Chen, J. Garcia-Martinez, S. Kitagawa, L. Öhrström, M. O'Keeffe, M. Paik Suh, J. Reedijk, Terminology of metal-organic frameworks and coordination polymers (IUPAC recommendations 2013), Pure Appl. Chem. 85 (2013).
- [2] O.M. Yaghi, M. O'Keeffe, N.W. Ockwig, H.K. Chae, M. Eddaoudi, J. Kim, Reticular synthesis and the design of new materials, Nature 423 (2003) 705–714.
- [3] K.S. Park, Z. Ni, A.P. Côté, J.Y. Choi, R. Huang, F.J. Uribe-Romo, H.K. Chae, M. O'Keeffe, O.M. Yaghi, Exceptional chemical and thermal stability of zeolitic imidazolate frameworks, Proc. Natl. Acad. Sci. USA 103 (2006) 10186–10191.
- [4] H. Deng, S. Grunder, K.E. Cordova, C. Valente, H. Furukawa, M. Hmadeh, F. Gándara, A.C. Whalley, Z. Liu, S. Asahina, H. Kazumori, M. O'Keeffe, O. Terasaki, J.F. Stoddart, O.M. Yaghi, Large-pore apertures in a series of metal-organic frameworks, Science 336 (2012) 1018–1023.
- [5] H. Furukawa, K.E. Cordova, M. O'Keeffe, O.M. Yaghi, The chemistry and applications of metal-organic frameworks, Science 341 (2013).
- [6] J.-R. Li, J. Sculley, H.-C. Zhou, Metal-organic frameworks for separations, Chem. Rev. 112 (2012) 869–932.
- [7] M.S. Denny, J.C. Moreton, L. Benz, S.M. Cohen, Metal–organic frameworks for membrane-based separations, Nat. Rev. Mater. 1 (2016) 16078.
- [8] A. Bétard, R.A. Fischer, Metal-organic framework thin films: from fundamentals to applications, Chem. Rev. 112 (2012) 1055–1083.
- [9] J.E. Bachman, Z.P. Smith, T. Li, T. Xu, J.R. Long, Enhanced ethylene separation and

- plasticization resistance in polymer membranes incorporating metal-organic framework nanocrystals, Nat. Mater. 15 (2016) 845.
- [10] G. Liu, V. Chernikova, Y. Liu, K. Zhang, Y. Belmabkhout, O. Shekhah, C. Zhang, S. Yi, M. Eddaoudi, W.J. Koros, Mixed matrix formulations with MOF molecular sieving for key energy-intensive separations, Nat. Mater. 17 (2018) 283–289.
- [11] J. Dechnik, C.J. Sumby, C. Janiak, Enhancing mixed-matrix membrane performance with metal-organic framework additives, Cryst. Growth Des. 17 (2017) 4467–4488.
- [12] G. Ramu, M. Lee, H.K. Jeong, Effects of zinc salts on the microstructure and performance of zeolitic-imidazolate framework ZIF-8 membranes for propylene/propane separation, Microporous Mesoporous Mater. 259 (2018) 155–162.
- [13] M. Navarro, B. Seoane, E. Mateo, R. Lahoz, G.F. de la Fuente, J. Coronas, ZIF-8 micromembranes for gas separation prepared on laser-perforated brass supports, J. Mater. Chem. A 2 (2014) 11177–11184.
- [14] M.C. McCarthy, V. Varela-Guerrero, G.V. Barnett, H.-K. Jeong, Synthesis of zeolitic imidazolate framework films and membranes with controlled microstructures, Langmuir 26 (2010) 14636–14641.
- [15] O. Shekhah, R. Swaidan, Y. Belmabkhout, M. du Plessis, T. Jacobs, L.J. Barbour, I. Pinnau, M. Eddaoudi, The liquid phase epitaxy approach for the successful construction of ultra-thin and defect-free ZIF-8 membranes: pure and mixed gas transport study, Chem. Commun. 50 (2014) 2089–2092.
- [16] Y. Pan, Z. Lai, Sharp separation of C<sub>2</sub>/C<sub>3</sub> hydrocarbon mixtures by zeolitic imidazolate framework-8 (ZIF-8) membranes synthesized in aqueous solutions, Chem. Commun. 47 (2011) 10275–10277.
- [17] R. Ameloot, F. Vermoortele, W. Vanhove, M.B.J. Roeffaers, B.F. Sels, D.E. De Vos, Interfacial synthesis of hollow metal–organic framework capsules demonstrating selective permeability, Nat. Chem. 3 (2011) 382.
- [18] O. Shekhah, M. Eddaoudi, The liquid phase epitaxy method for the construction of oriented ZIF-8 thin films with controlled growth on functionalized surfaces, Chem. Commun. 49 (2013) 10079–10081.
- [19] H.T. Kwon, H.-K. Jeong, A.S. Lee, H.S. An, T. Lee, E. Jang, J.S. Lee, J. Choi, Defect-induced ripening of zeolitic-imidazolate framework ZIF-8 and its implication to vapor-phase membrane synthesis, Chem. Commun. 52 (2016) 11669–11672.
- [20] S. Qiu, M. Xue, G. Zhu, Metal-organic framework membranes: from synthesis to separation application, Chem. Soc. Rev. 43 (2014) 6116–6140.
- [21] S. Takamizawa, Y. Takasaki, R. Miyake, Single-crystal membrane for anisotropic and efficient gas permeation, J. Am. Chem. Soc. 132 (2010) 2862–2863.
- [22] Y.-S. Li, F.-Y. Liang, H. Bux, A. Feldhoff, W.-S. Yang, J. Caro, Molecular sieve membrane: supported metal-organic framework with high hydrogen selectivity, Angew. Chem. Int. Ed. 49 (2010) 548-551.
- [23] J. Gascon, F. Kapteijn, Metal-organic framework membranes—high potential, bright future? Angew. Chem. Int. Ed. 49 (2010) 1530–1532.
- [24] Y. Zhu, J. Ciston, B. Zheng, X. Miao, C. Czarnik, Y. Pan, R. Sougrat, Z. Lai, C.E. Hsiung, K. Yao, I. Pinnau, M. Pan, Y. Han, Unravelling surface and interfacial structures of a metal-organic framework by transmission electron microscopy, Nat. Mater. 16 (2017) 532–536.
- [25] B. Liu, Metal-organic framework-based devices: separation and sensors, J. Mater. Chem. 22 (2012) 10094–10101.
- [26] O. Kadioglu, S. Keskin, Efficient separation of helium from methane using MOF membranes, Sep. Purif. Technol. 191 (2018) 192–199.
- [27] G. Yilmaz, A. Ozcan, S. Keskin, Computational screening of ZIFs for CO<sub>2</sub> separations, Mol. Simul. 41 (2015) 713–726.
- [28] E. Atci, I. Erucar, S. Keskin, Adsorption and transport of CH<sub>4</sub>, CO<sub>2</sub>, H<sub>2</sub> mixtures in a Bio-MOF material from molecular simulations, J. Phys. Chem. C 115 (2011) 6833–6840.
- [29] C. Chmelik, Characteristic features of molecular transport in MOF ZIF-8 as revealed by IR microimaging, Microporous Mesoporous Mater. 216 (2015) 138–145.
- [30] S. Hwang, R. Semino, B. Seoane, M. Zahan, C. Chmelik, R. Valiullin, M. Bertmer, J. Haase, F. Kapteijn, J. Gascon, G. Maurin, J. Karger, Revealing the transient concentration of CO<sub>2</sub> in a mixed-matrix membrane by ir microimaging and molecular modeling, Angew. Chem. Int. Ed. Engl. 57 (2018) 5156–5160.
- [31] C. Zhang, R.P. Lively, K. Zhang, J.R. Johnson, O. Karvan, W.J. Koros, Unexpected molecular sieving properties of zeolitic imidazolate framework-8, J. Phys. Chem. Lett. 3 (2012) 2130–2134.
- [32] J.E. Lewis, G.R. Gavalas, M.E. Davis, Permeation studies on oriented single-crystal ferrierite membranes, AlChE J. 43 (1997) 83–90.
- [33] D.B. Shah, H.Y. Liou, Time-lag measurements for diffusion of aromatics through a silicalite membrane, Zeolites 14 (1994) 541–548.
- [34] D.L. Wernick, E.J. Osterhuber, Permeation through a single crystal of zeolite NaX, J. Membr. Sci. 22 (1985) 137–146.
- [35] E.R. Geus, A.E. Jansen, J.C. Jansen, J. Schoonman, H. van Bekkum, Permeability studies on a silicalite single crystal membrane model, Stud. Surf. Sci. Catal. 65 (1991) 457–466.
- [36] Y. Takasaki, S. Takamizawa, Gas permeation in a molecular crystal and space expansion, J. Am. Chem. Soc. 136 (2014) 6806–6809.
- [37] Y. Takasaki, S. Takamizawa, A preferable molecular crystal membrane for H2 gas separation, Chem. Commun. 50 (2014) 5662–5664.
- [38] F. Gandara, T.D. Bennett, Crystallography of metal-organic frameworks, IUCrJ 1 (2014) 563–570.
- [39] C. Chmelik, H. Bux, J. Caro, L. Heinke, F. Hibbe, T. Titze, J. Kärger, Mass transfer in a nanoscale material enhanced by an opposing flux, Phys. Rev. Lett. 104 (2010) 085902
- [40] J. Cravillon, R. Nayuk, S. Springer, A. Feldhoff, K. Huber, M. Wiebcke, Controlling zeolitic imidazolate framework nano- and microcrystal formation: insight into crystal growth by time-resolved in situ static light scattering, Chem. Mater. 23 (2011) 2130–2141.
- [41] J. Cravillon, C.A. Schroder, H. Bux, A. Rothkirch, J. Caro, M. Wiebcke, Formate

- modulated solvothermal synthesis of ZIF-8 investigated using time-resolved in situ X-ray diffraction and scanning electron microscopy, CrystEngComm 14 (2012)
- [42] A.-K. Pusch, T. Splith, L. Moschkowitz, S. Karmakar, R. Biniwale, M. Sant, G.B. Suffritti, P. Demontis, J. Cravillon, E. Pantatosaki, F. Stallmach, NMR studies of carbon dioxide and methane self-diffusion in ZIF-8 at elevated gas pressures, Adsorption 18 (2012) 359–366.
- [43] K. Zhang, R.P. Lively, C. Zhang, W.J. Koros, R.R. Chance, Investigating the intrinsic ethanol/water separation capability of ZIF-8: an adsorption and diffusion study, J. Phys. Chem. C 117 (2013) 7214–7225.
- [44] H. Bux, C. Chmelik, J.M. van Baten, R. Krishna, J. Caro, Novel MOF-membrane for molecular sieving predicted by IR-diffusion studies and molecular modeling, Adv. Mater. 22 (2010) 4741–4743.
- [45] C. Chmelik, J. van Baten, R. Krishna, Hindering effects in diffusion of CO<sub>2</sub>/CH<sub>4</sub> mixtures in ZIF-8 crystals, J. Membr. Sci. 397–398 (2012) 87–91.
- [46] M.W. Anderson, J.T. Gebbie-Rayet, A.R. Hill, N. Farida, M.P. Attfield, P. Cubillas, V.A. Blatov, D.M. Proserpio, D. Akporiaye, B. Arstad, J.D. Gale, Predicting crystal growth via a unified kinetic three-dimensional partition model, Nature 544 (2017) 456–459.
- [47] Z. Sumer, S. Keskin, Adsorption- and membrane-based CH<sub>4</sub>/N<sub>2</sub> separation performances of MOFs, Ind. Eng. Chem. Res. 56 (2017) 8713–8722.
- [48] F. Cao, C. Zhang, Y. Xiao, H. Huang, W. Zhang, D. Liu, C. Zhong, Q. Yang, Z. Yang, X. Lu, Helium recovery by a Cu-BTC metal-organic-framework membrane, Ind. Eng. Chem. Res. 51 (2012) 11274–11278.
- [49] J. Yu, L.-H. Xie, J.-R. Li, Y. Ma, J.M. Seminario, P.B. Balbuena, CO<sub>2</sub> capture and separations using MOFs: computational and experimental studies, Chem. Rev. 117 (2017) 9674–9754.
- [50] A. Schejn, L. Balan, V. Falk, L. Aranda, G. Medjahdi, R. Schneider, Controlling ZIF-8 nano- and microcrystal formation and reactivity through zinc salt variations, CrystEngComm 16 (2014) 4493–4500.
- [51] L. Sheng, F. Yang, C. Wang, J. Yu, L. Zhang, Y. Pan, Comparison of the hydrothermal stability of ZIF-8 nanocrystals and polycrystalline membranes derived from zinc salt variations, Mater. Lett. 197 (2017) 184–187.
- [52] E.L. Bustamante, J.L. Fernández, J.M. Zamaro, Influence of the solvent in the synthesis of zeolitic imidazolate framework-8 (ZIF-8) nanocrystals at room temperature, J. Colloid Interface Sci. 424 (2014) 37–43.
- [53] Y. Pan, Y. Liu, G. Zeng, L. Zhao, Z. Lai, Rapid synthesis of zeolitic imidazolate framework-8 (ZIF-8) nanocrystals in an aqueous system, Chem. Commun. 47 (2011) 2071–2073.
- [54] X. Feng, T. Wu, M.A. Carreon, Synthesis of ZIF-67 and ZIF-8 crystals using DMSO (Dimethyl Sulfoxide) as solvent and kinetic transformation studies, J. Cryst. Growth 455 (2016) 152–156.
- [55] S. Watanabe, S. Ohsaki, T. Hanafusa, K. Takada, H. Tanaka, K. Mae, M.T. Miyahara, Synthesis of zeolitic imidazolate framework-8 particles of controlled sizes, shapes, and gate adsorption characteristics using a central collision-type microreactor, Chem. Eng. J. 313 (2017) 724–733.
- [56] P.Y. Moh, M. Brenda, M.W. Anderson, M.P. Attfield, Crystallisation of solvother-mally synthesised ZIF-8 investigated at the bulk, single crystal and surface level, CrystEngComm 15 (2013) 9672–9678.
- [57] P. Webb, C. Orr, C. Micromeritics, Instrument, Analytical methods in fine particle technology, Micromeritics Instrument Corp., Norcross, Ga, 1997.
- [58] H. Huang, W. Zhang, D. Liu, B. Liu, G. Chen, C. Zhong, Effect of temperature on gas adsorption and separation in ZIF-8: a combined experimental and molecular simulation study, Chem. Eng. Sci. 66 (2011) 6297–6305.
- [59] H. Bux, A. Feldhoff, J. Cravillon, M. Wiebcke, Y.-S. Li, J. Caro, Oriented zeolitic imidazolate framework-8 membrane with sharp H<sub>2</sub>/C<sub>3</sub>H<sub>8</sub> molecular sieve separation, Chem. Mater. 23 (2011) 2262–2269.
- [60] D. Fairen-Jimenez, S.A. Moggach, M.T. Wharmby, P.A. Wright, S. Parsons, T. Düren, Opening the gate: framework flexibility in ZIF-8 explored by experiments and simulations, J. Am. Chem. Soc. 133 (2011) 8900–8902.
- [61] A.J. Brown, N.A. Brunelli, K. Eum, F. Rashidi, J.R. Johnson, W.J. Koros, C.W. Jones, S. Nair, Interfacial microfluidic processing of metal-organic framework hollow fiber membranes, Science 345 (2014) 72–75.
- [62] A.M. Marti, W. Wickramanayake, G. Dahe, A. Sekizkardes, T.L. Bank, D.P. Hopkinson, S.R. Venna, Continuous flow processing of ZIF-8 membranes on polymeric porous hollow fiber supports for CO<sub>2</sub> capture, ACS Appl. Mater. Interfaces 9 (2017) 5678–5682.
- [63] K.-S. Jang, H.-J. Kim, J.R. Johnson, W.-g. Kim, W.J. Koros, C.W. Jones, S. Nair, Modified mesoporous silica gas separation membranes on polymeric hollow fibers, Chem. Mater. 23 (2011) 3025–3028.
- [64] Y. Liu, Y. Peng, N. Wang, Y. Li, J.H. Pan, W. Yang, J. Caro, Significantly enhanced separation using ZIF-8 membranes by partial conversion of calcined layered double hydroxide precursors, ChemSusChem 8 (2015) 3582–3586.
- [65] A. Huang, Q. Liu, N. Wang, Y. Zhu, J. Caro, Bicontinuous zeolitic imidazolate framework ZIF-8@GO membrane with enhanced hydrogen selectivity, J. Am. Chem. Soc. 136 (2014) 14686–14689.
- [66] J. McEwen, J.-D. Hayman, A. Ozgur Yazaydin, A comparative study of  $CO_2$ ,  $CH_4$  and  $N_2$  adsorption in ZIF-8, Zeolite-13X and BPL activated carbon, Chem. Phys. 412 (2013) 72–76.
- [67] A. Battisti, S. Taioli, G. Garberoglio, Zeolitic imidazolate frameworks for separation of binary mixtures of CO<sub>2</sub>, CH<sub>4</sub>, N<sub>2</sub> and H<sub>2</sub>: a computer simulation investigation, Microporous Mesoporous Mater. 143 (2011) 46–53.
- [68] J. Caro, Are, MOF membranes better in gas separation than those made of zeolites? Curr. Opin. Chem. Eng. 1 (2011) 77–83.
- [69] R. Krishna, Describing the diffusion of guest molecules inside porous structures, J. Phys. Chem. C 113 (2009) 19756–19781.

- [70] P. Krokidas, M. Castier, S. Moncho, E. Brothers, I.G. Economou, Molecular simulation studies of the diffusion of methane, ethane, propane, and propylene in ZIF-8, J. Phys. Chem. C 119 (2015) 27028–27037.
- [71] X. Wu, J. Huang, W. Cai, M. Jaroniec, Force field for ZIF-8 flexible frameworks: atomistic simulation of adsorption, diffusion of pure gases as CH<sub>4</sub>, H<sub>2</sub>, CO<sub>2</sub> and N<sub>2</sub>, RSC Adv. 4 (2014) 16503–16511.
- [72] L. Zhang, Z. Hu, J. Jiang, Sorption-induced structural transition of zeolitic
- imidazolate framework-8: a hybrid molecular simulation study, J. Am. Chem. Soc.  $135\ (2013)\ 3722-3728$ .
- [73] B. Zheng, M. Sant, P. Demontis, G.B. Suffritti, Force field for molecular dynamics computations in flexible ZIF-8 framework, J. Phys. Chem. C 116 (2012) 933–938.
- [74] B. Zheng, M. Sant, P. Demontis, G.B. Suffritti, Correction to "Force Field for Molecular Dynamics Computations in Flexible ZIF-8 Framework", J. Phys. Chem. C 117 (2013) (24662-24662).