

I645 Human Perceptual Systems and its Models

3. Sound representations and signal processing

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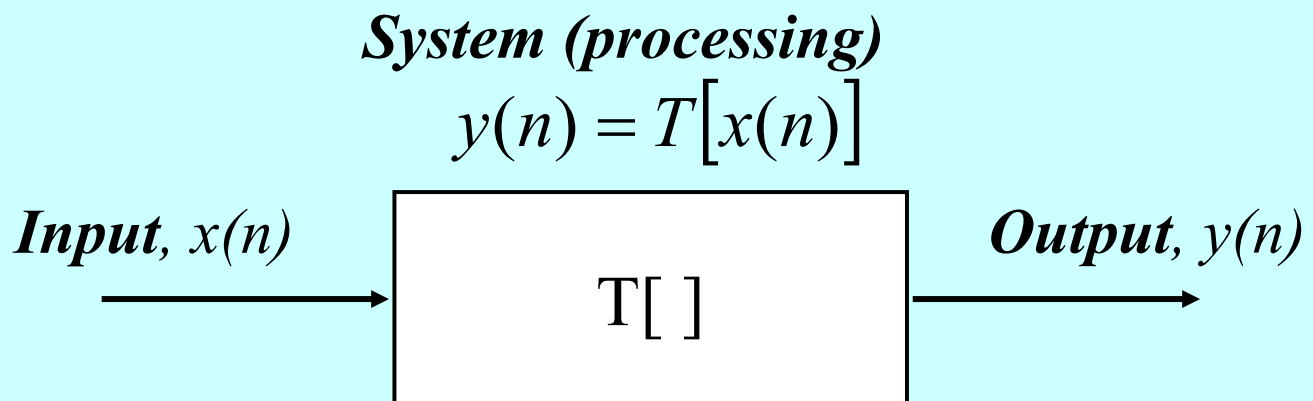
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0. Motivation

- Question 1:** *What is the difference between linear and nonlinear processing?*



- Question 2:** *Which is linear or nonlinear processing?*

Fourier transform, Laplace transform, wavelet transform, z transform, Audio systems, Human auditory system

1. Introduction

■ “Hearing”

- a *crucial sense* for humans
- *central* to the interaction of human beings with other human beings
- *importance* to our interactions with our environments

■ *Question: Is hearing a linear system?*

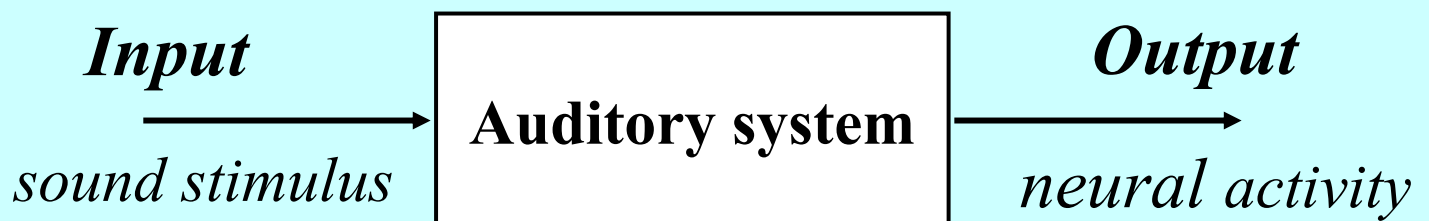
Answer: No!

■ *How is hearing investigated?*

- Auditory physiology
- Auditory psychophysics (Psychoacoustics)

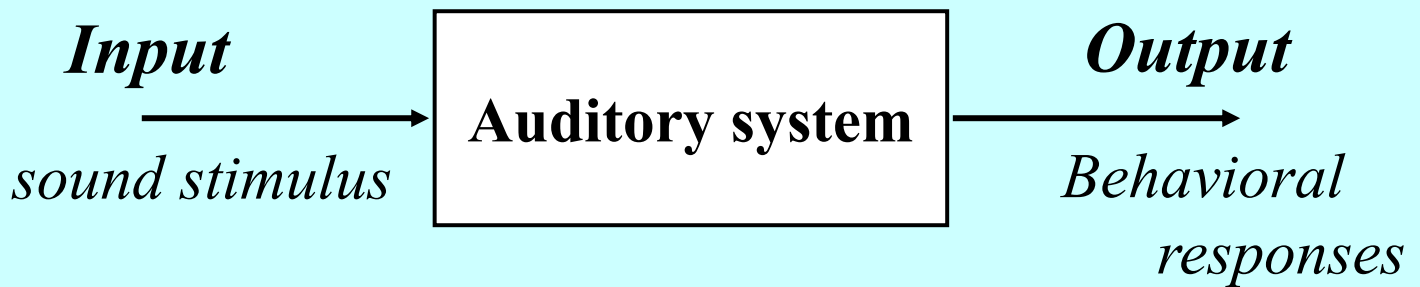
■ Auditory physiology

- Internal workings of the auditory system: how sound is processed by the cells and structures in the ear and brain
- *Direct/indirect* measurements of the biological systems
 - by *Surgery*
 - *Neurophysiological* techniques (electrical activity)
 - Modern “*brain imaging*” techniques (fMRI)



■ Psychoacoustics

- *Behavioral* study of hearing — behavioral in that the participant is required to make a response to the sounds that are presented.



- **Importance:** to combine *physiological* experiments with experiments that employ *behavioral* techniques

2. Sound

■ What is “sound”

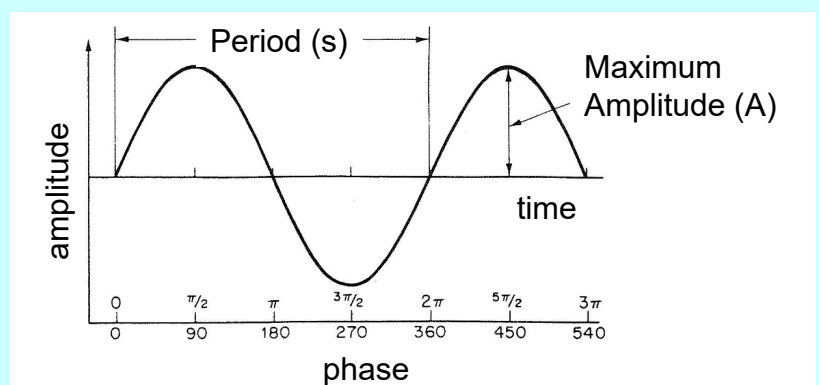
- Sound *waveforms* (physical meaning)
- *Sensations* evoked by sound (psychological meaning)

■ Characteristics of sound

- Variation of the air pressure $x(t) = A \sin(2\pi ft + \theta)$
- The simplest types of sound: **sine wave**

■ Sinusoidal wave

- A : amplitude
- f : frequency
- θ : phase



Various sounds around our life



Speech sound

■ *Are these speech or non-speech?*



■ **Speech sound/voice**



evoked sound by (human) glottis

3. Sound representations

Fourier analysis and spectrum representations

Discrete Fourier series

Fourier coefficients

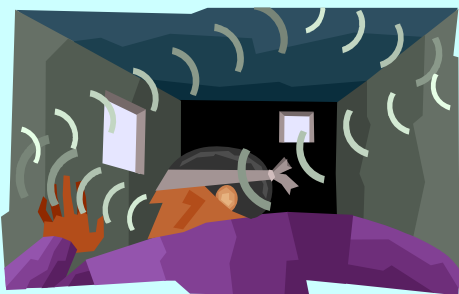
$$\left\{ \begin{array}{l} c_k = \int_{-T/2}^{T/2} \tilde{x}_a(t) e^{-jk\omega_0 t} dt \\ \tilde{x}_a(t) = \frac{1}{T} \sum_{k=-\infty}^{\infty} c_k e^{jk\omega_0 t} \end{array} \right.$$

Discrete Fourier transform

Fourier component

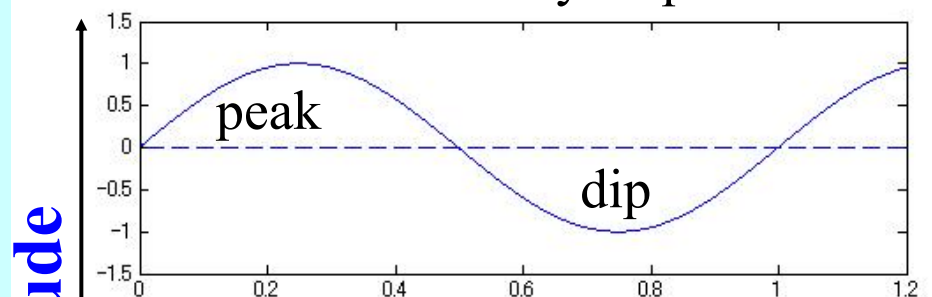
$$\left\{ \begin{array}{l} \tilde{X}(k) = \sum_{n=0}^{N-1} \tilde{x}(n) W_N^{kn} \\ \tilde{x}(n) = \frac{1}{N} \sum_{k=0}^{N-1} \tilde{X}(k) W_N^{-kn} \end{array} \right.$$

Vibrations — Frequency

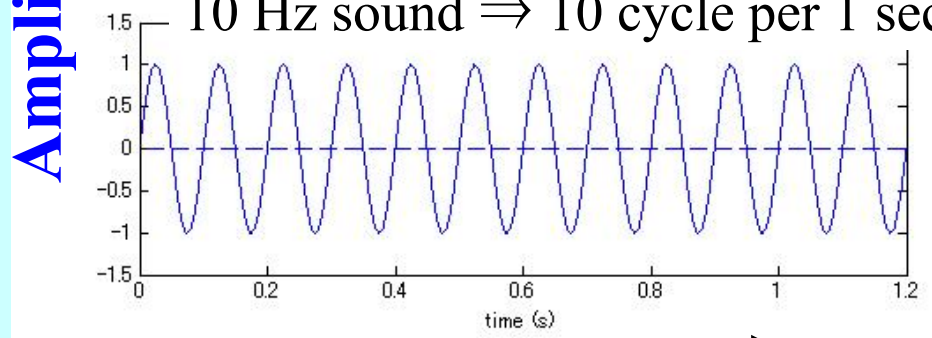


“waveform”

1 Hz sound \Rightarrow 1 cycle per 1 sec.

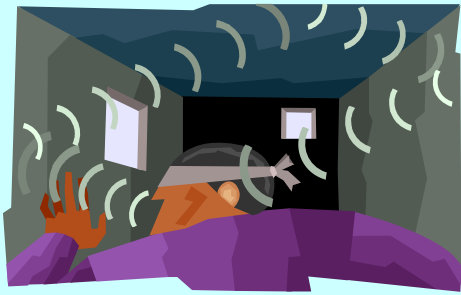


10 Hz sound \Rightarrow 10 cycle per 1 sec.

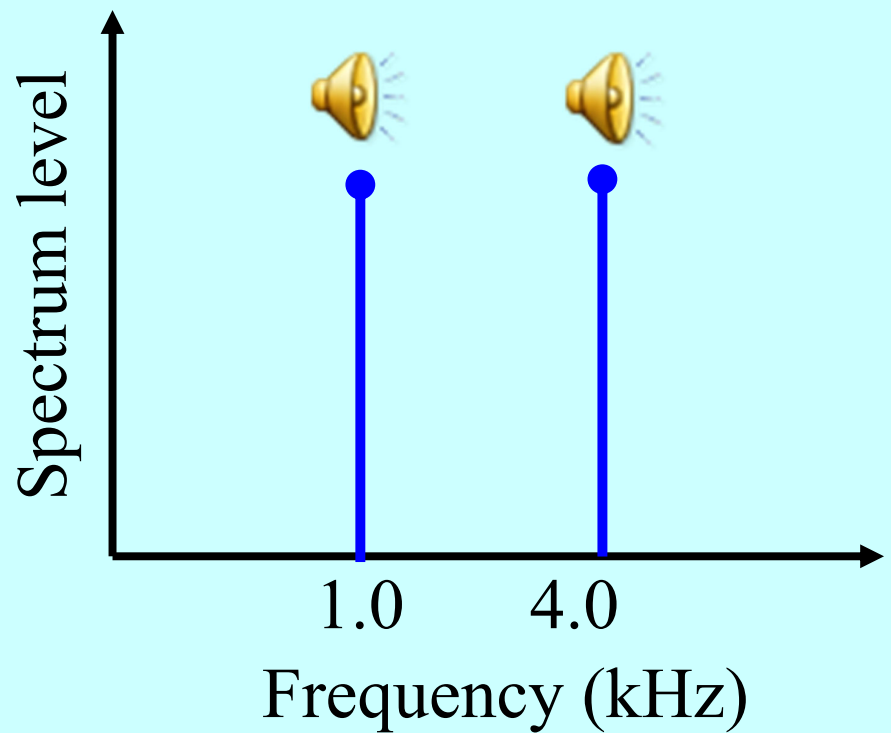


Time (s)

Vibrations - Spectrum



“waveform”



Fourier Analysis/Synthesis

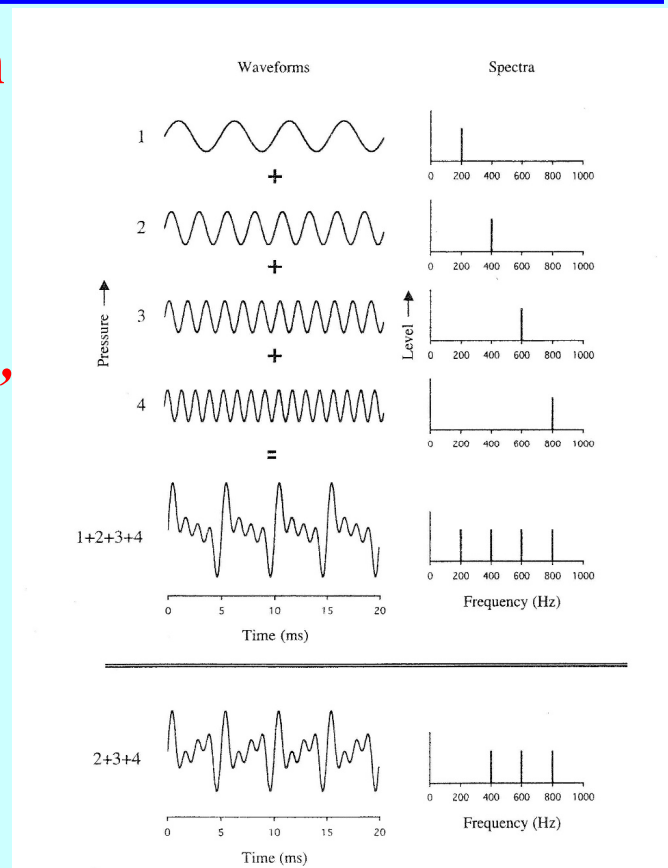
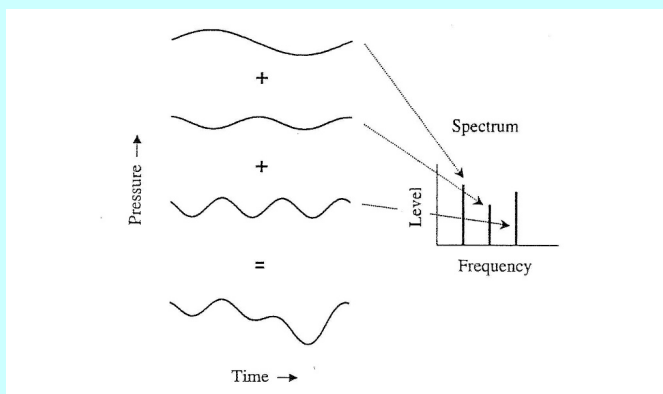
■ Concept of decomposition

Periodic sound =

DC

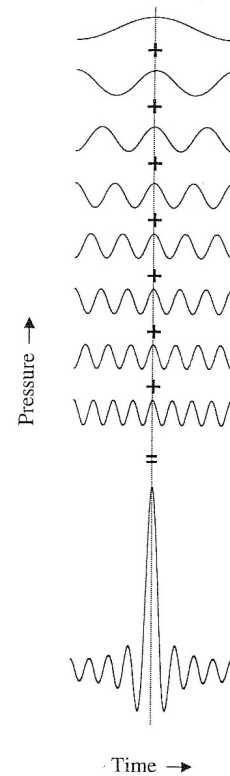
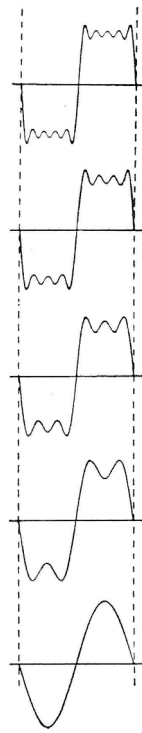
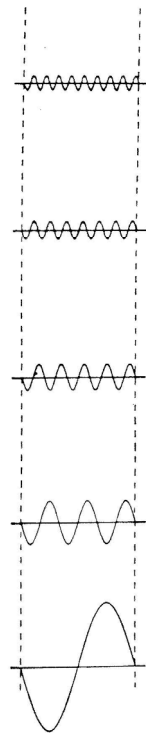
+ summation of “sine”

+ summation of “cosine”



Decomposition of Rect. and Impulsive signals

Rectangular signal



Impulsive signal

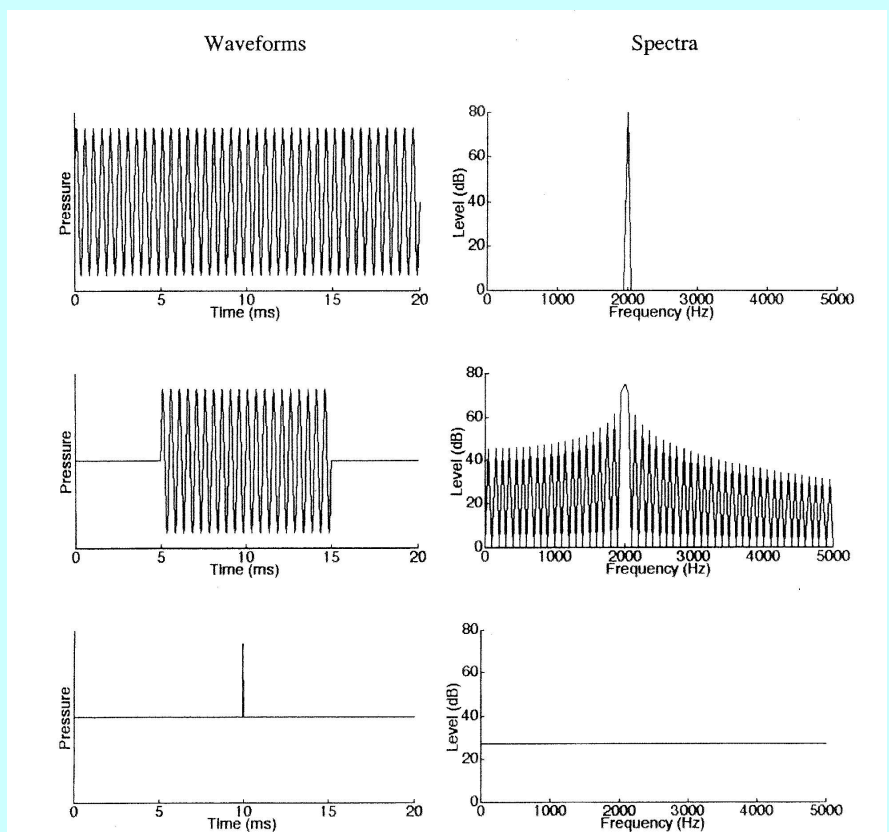
Relation between signal and spectrum ①

When signal duration could be shorter,

■ Sine wave

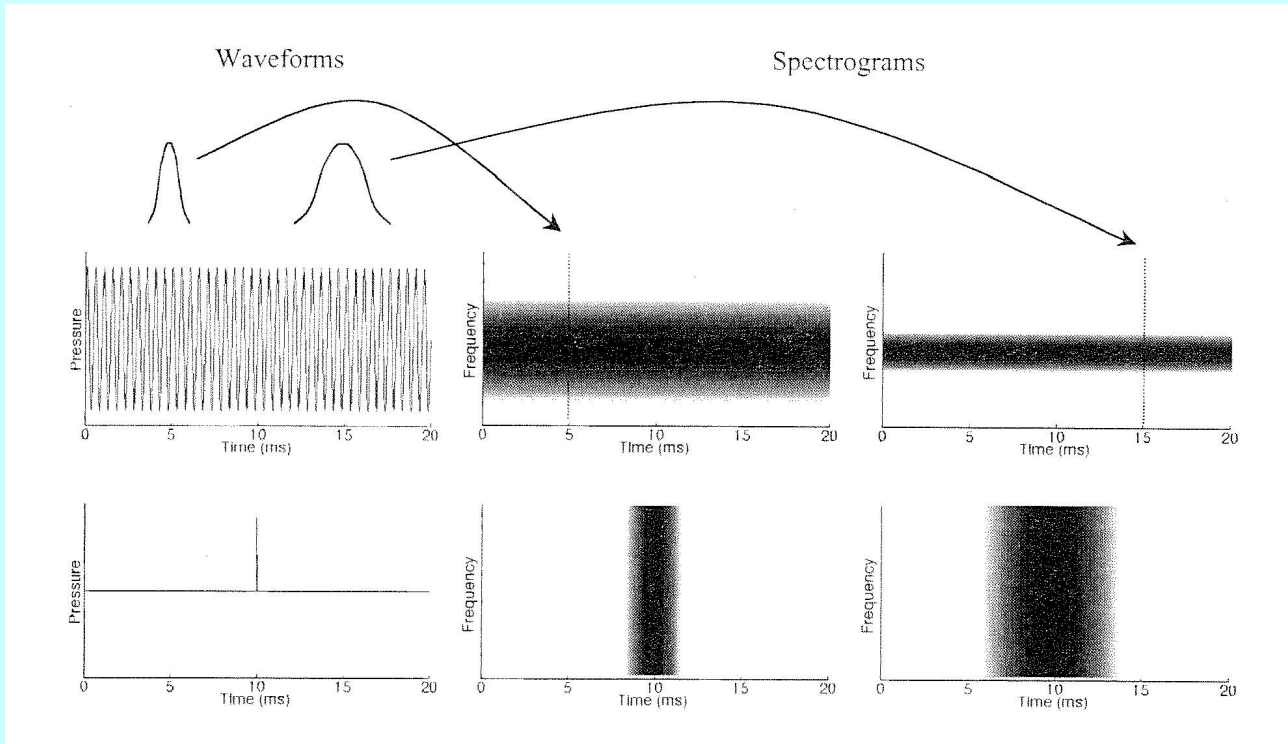
■ Tone-burst

■ Impulse



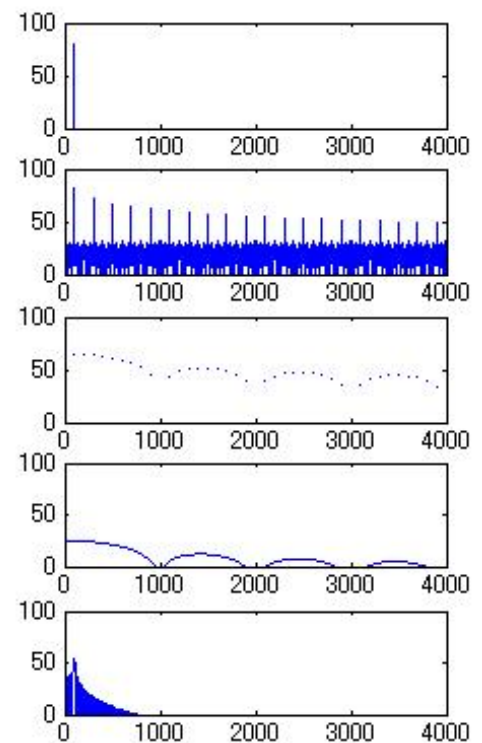
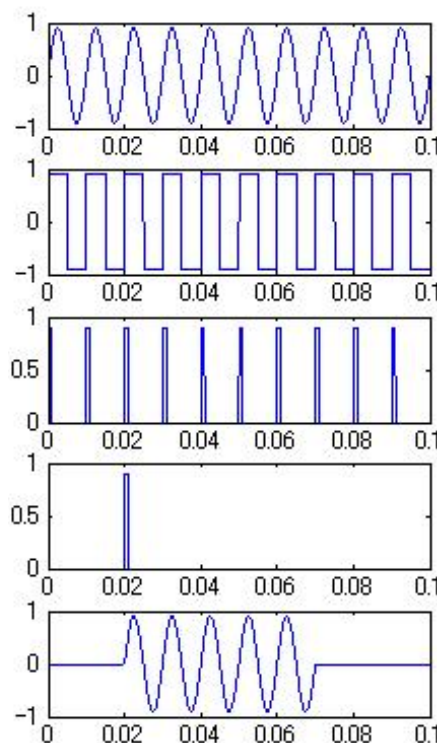
Relation between signal and spectrum ②

■ Windowing dependence

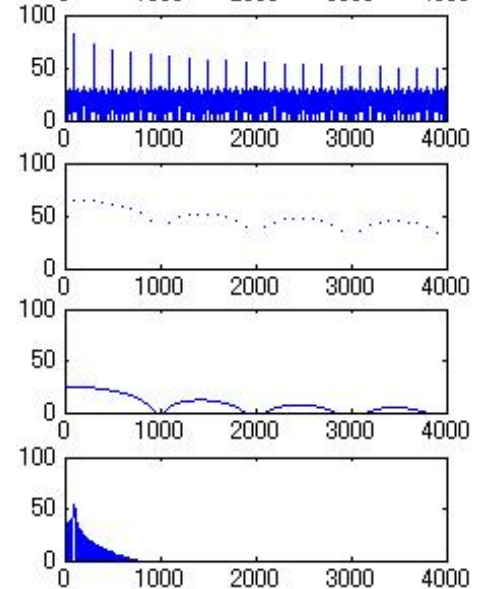
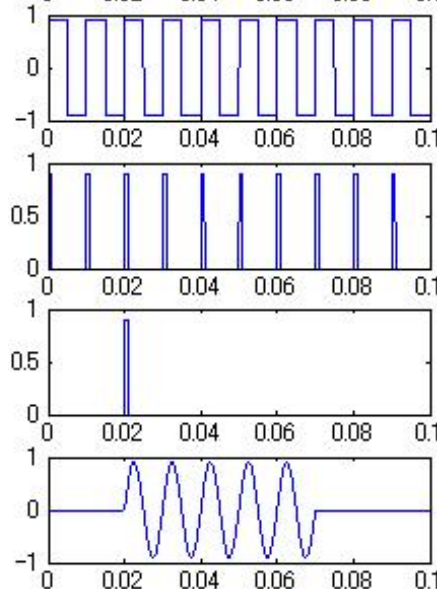


Relation between signal and spectrum ③

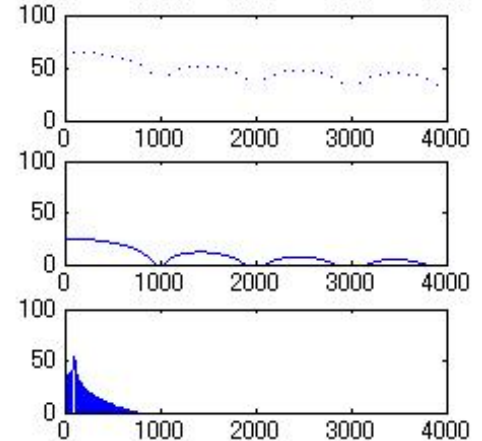
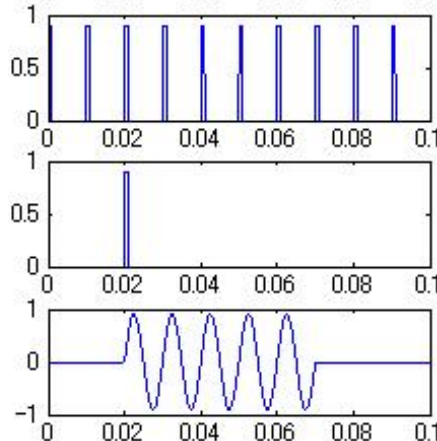
Sinusoidal wave



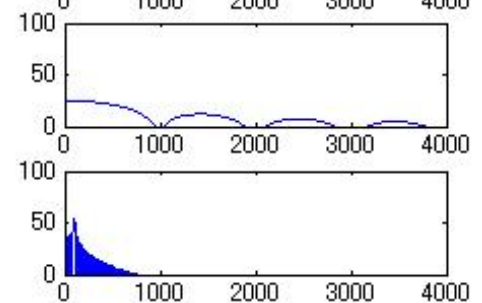
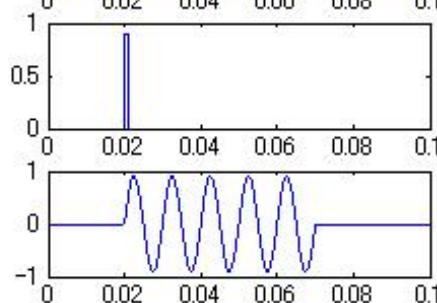
Rectangular tone



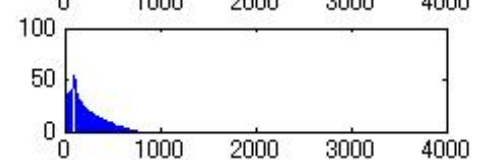
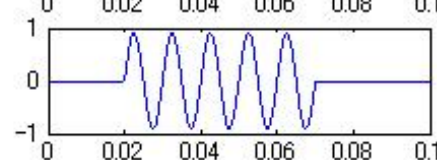
Pulse train



Pulse



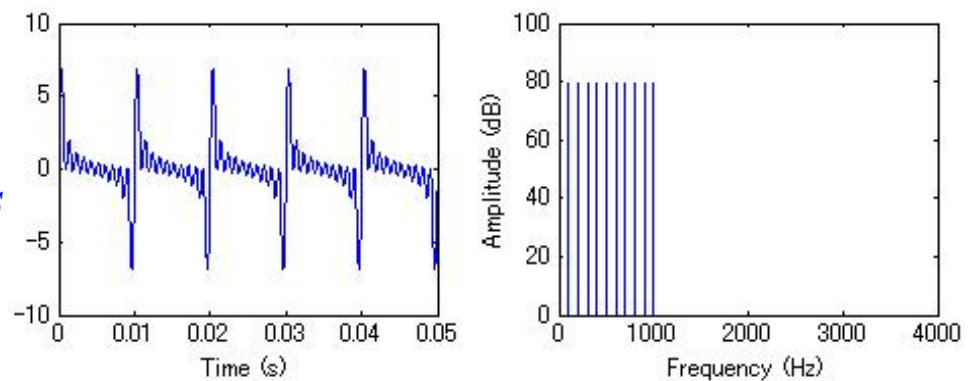
Tone-burst



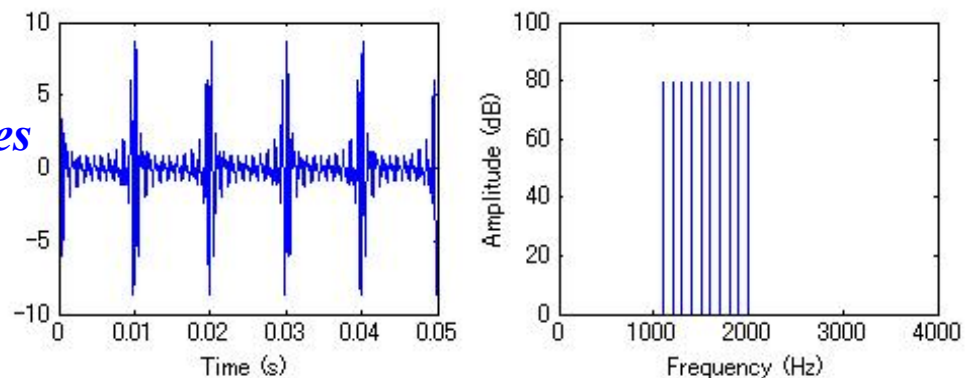
Relation between signal and spectrum ④

*Harmonic
sound*

Lower frequencies



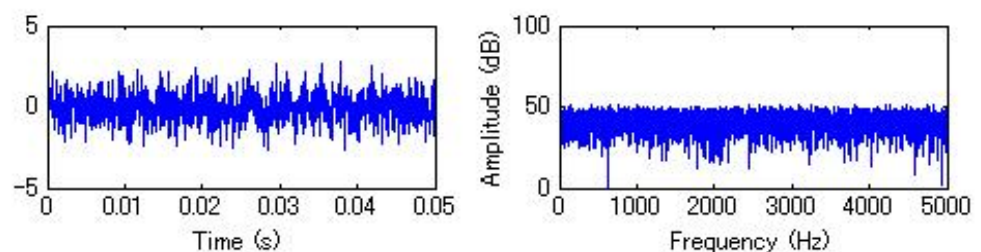
Higher frequencies



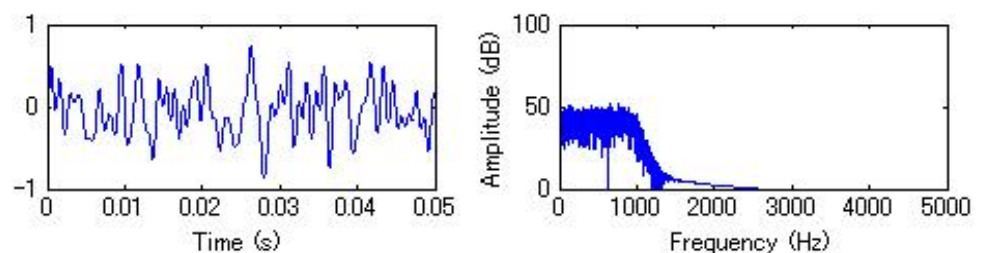
Relation between signal and spectrum ⑤

White noise

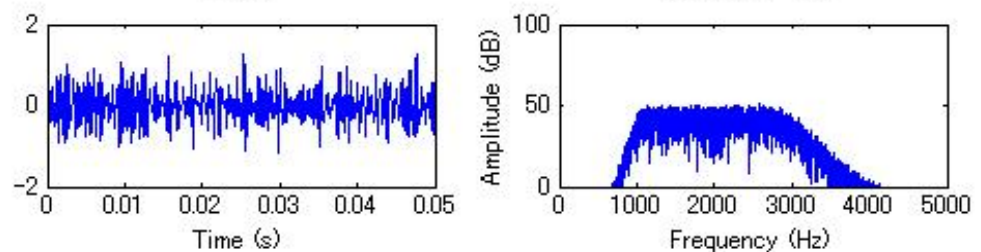
whole-band



Low-passed



Band-limited



4. Characteristics of sound

■ ***Power***

- The energy transmitted per second

■ ***Sound intensity***

- The sound power transmitted through a given unit area in a sound field (e.g., a square meter of air) every second
- Unit: watt per square meter [W/m^2]
- $10^{-12} \text{ W/m}^2 = 2 \times 10^{-5} \text{ N/m}^2 = 20 \mu\text{Pa}$

■ ***Proportional relation***

$$I = kP^2$$

I : the intensity, P : the rms pressure

■ ***Sound level in dB***

$$\text{decibel scale} = 10 \log_{10}(I_o/I_i) \quad (\text{dB})$$

I_i : Intensity of the input, I_o : Intensity of the output

e.g., 60 dB SPL

→ 60 dB higher in the reference level of 0 dB

Intensity of 10^{-6} W/m^2

the ratio of intensities by 10 (or $1/10$)

→ 10 dB ***increases*** (or ***decreases***)

the ratio of intensities by 2 (or $1/2$)

→ 3 dB ***increases*** (or ***decreases***)

■ **Sound level in dB**

decibel scale $= 20 \log_{10}(P_o/P_i)$

P_i : rms pressure of the input

P_o : rms pressure of the output

■ RMS value \rightarrow root-mean-square value of sound pressure

SPL (Sound Pressure Level) in dB

SL (Sensational Level) in dB

e.g. SL of 60 dB will be 60 dB above the absolute threshold

■ Energy density Energy per 1 Hz band

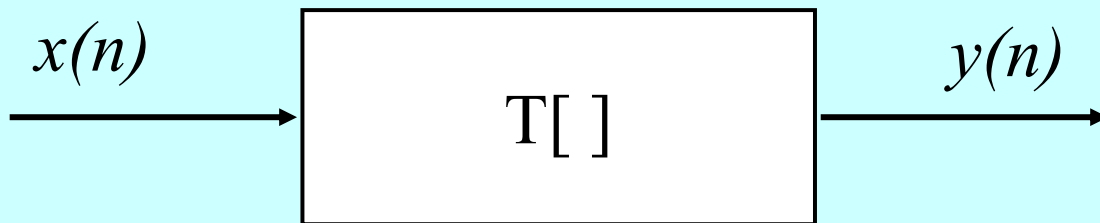
Relationship between dB, intensity, and Pressure ratios

Level SPL in dB	Intensity I/I_0	Pressure P/P_0	Typical case
140	10^{14}	10^7	<i>Gunshot</i>
120	10^{12}	10^6	<i>Loud rock group</i>
100	10^{10}	10^5	<i>Shouting</i>
80	10^8	10^4	<i>Heavy Traffic</i>
70	10^7	3.16×10^3	<i>Normal conversation</i>
50	10^5	316	<i>Quiet conversation</i>
30	10^3	31.6	<i>Library</i>
20	10^2	10	<i>Quiet Forest</i>
0	1	1	<i>Absolute Threshold</i>

5. Linear/nonlinear systems

Linearity

$$y(n) = T[x(n)]$$



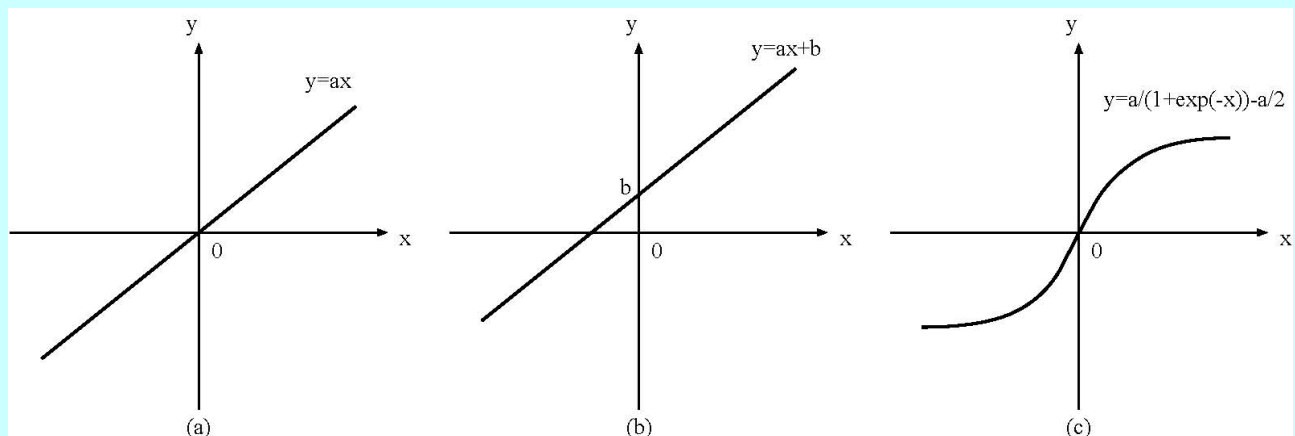
$$\begin{aligned} T[ax_1(n)] + T[bx_2(n)] &= aT[x_1(n)] + bT[x_2(n)] \\ &= ay_1(n) + by_2(n) \end{aligned}$$

Requirement for linearity

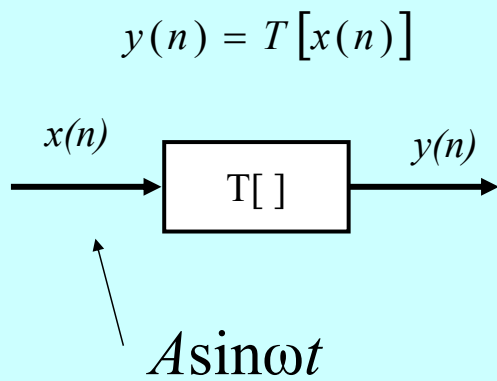
- *Additivity* property
- *Homogeneity* property
- *Superposition* property

otherwise,
nonlinearity

Question: Which is a linear system?

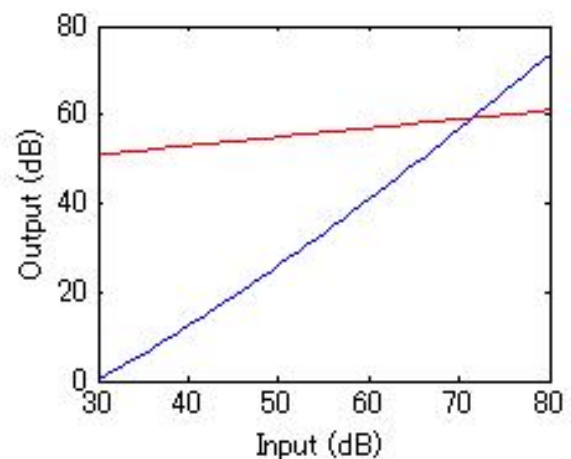
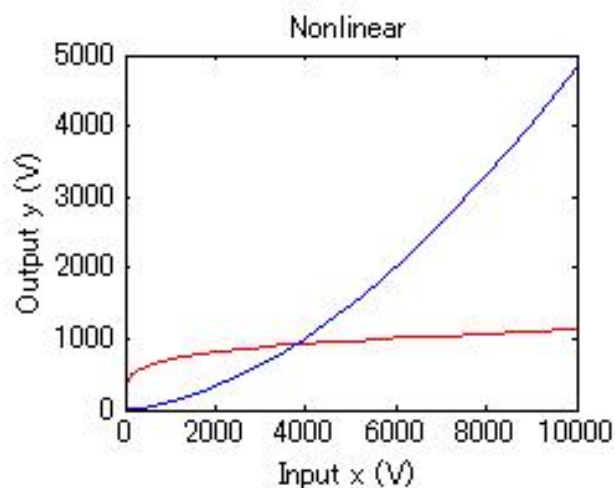
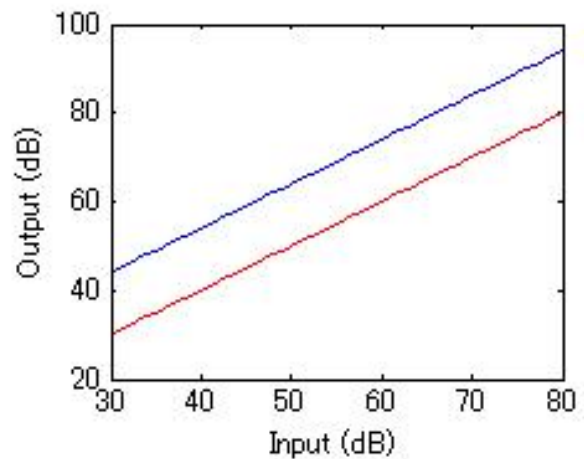
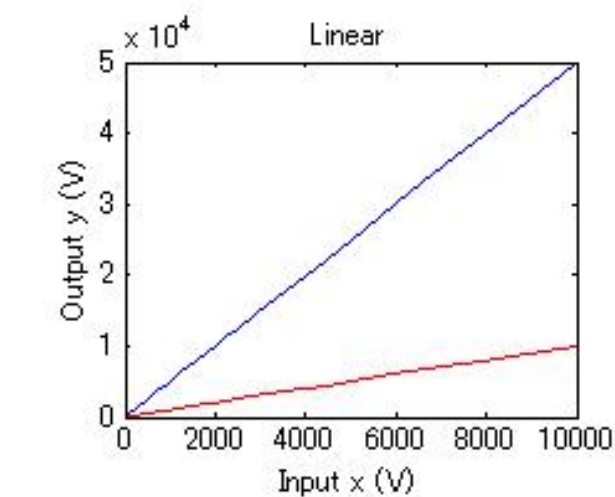
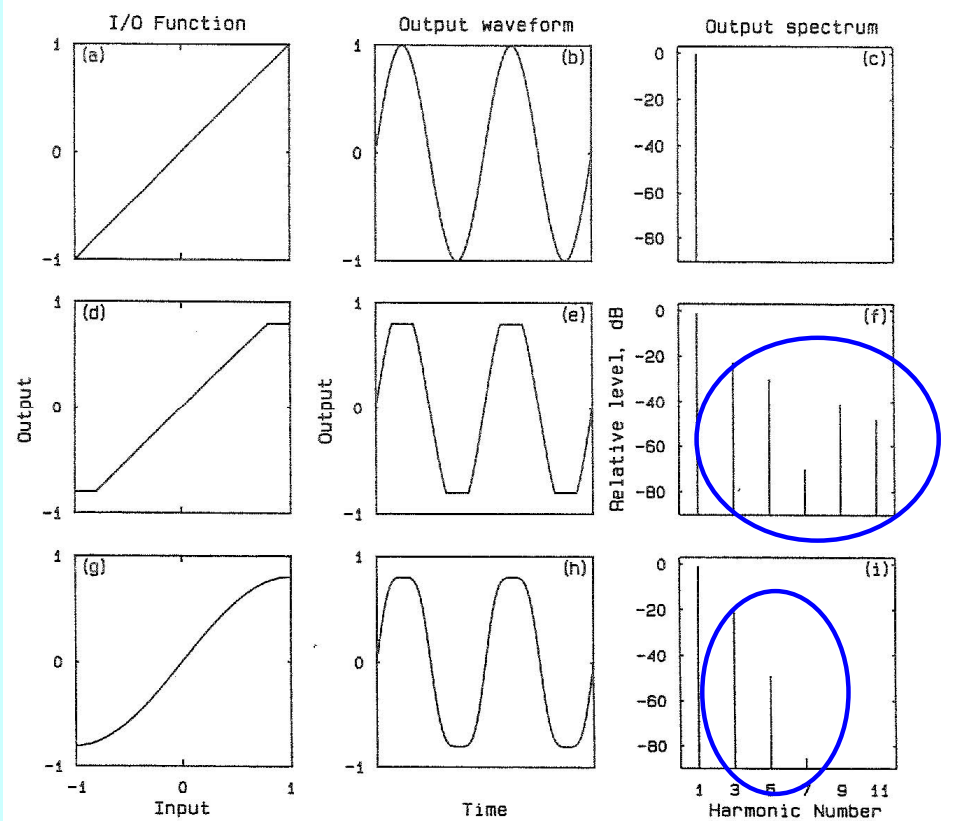


Example



Question:

Why can harmonicity be observed?



6. Filter

Types of the filter

LPF

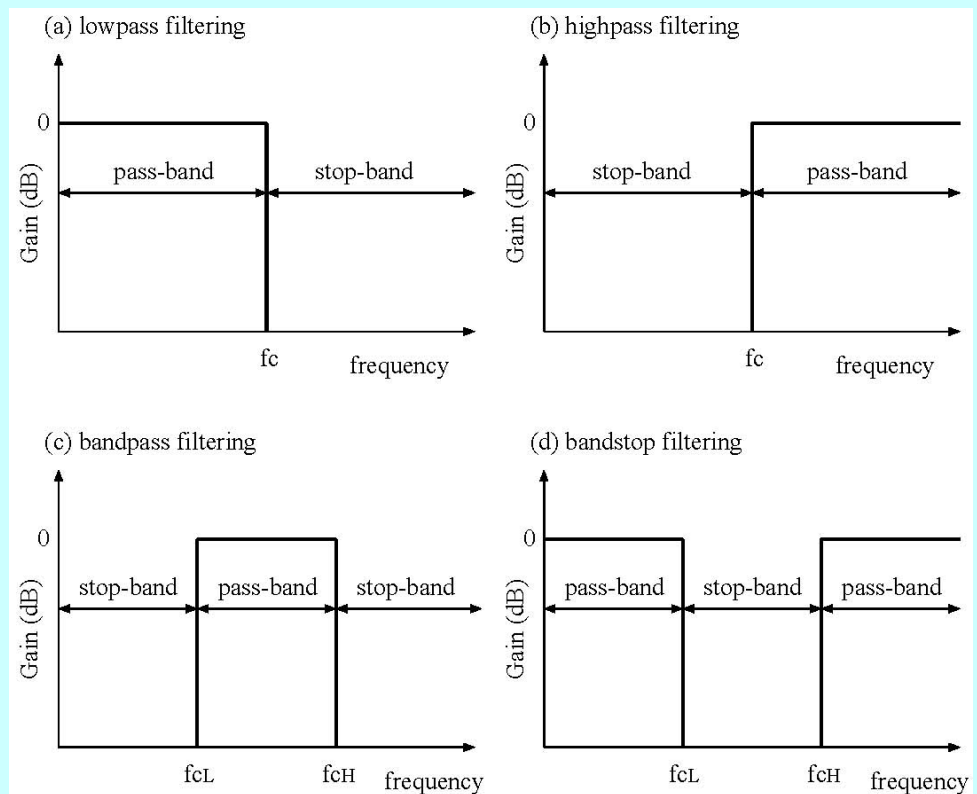
Low-pass filter

BPF

Band-pass filter

HPF

High-pass filter



Filter characteristics

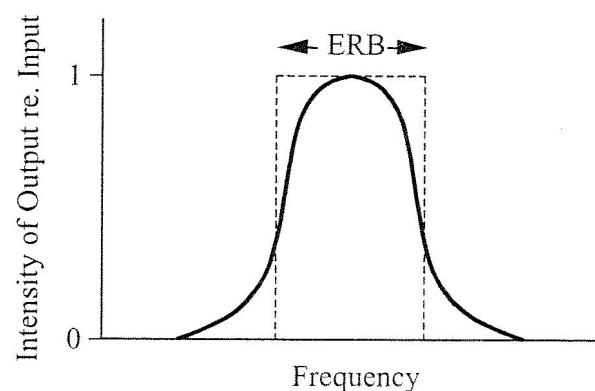
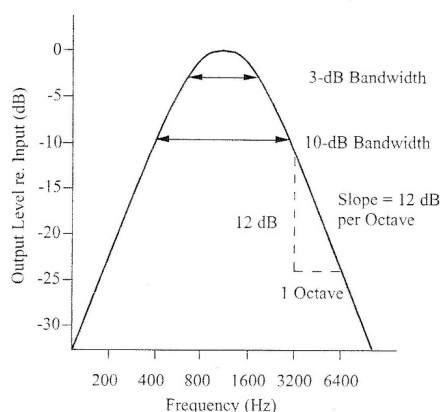
Bandwidth

■ 3-dB BW (or 10-dB BW)

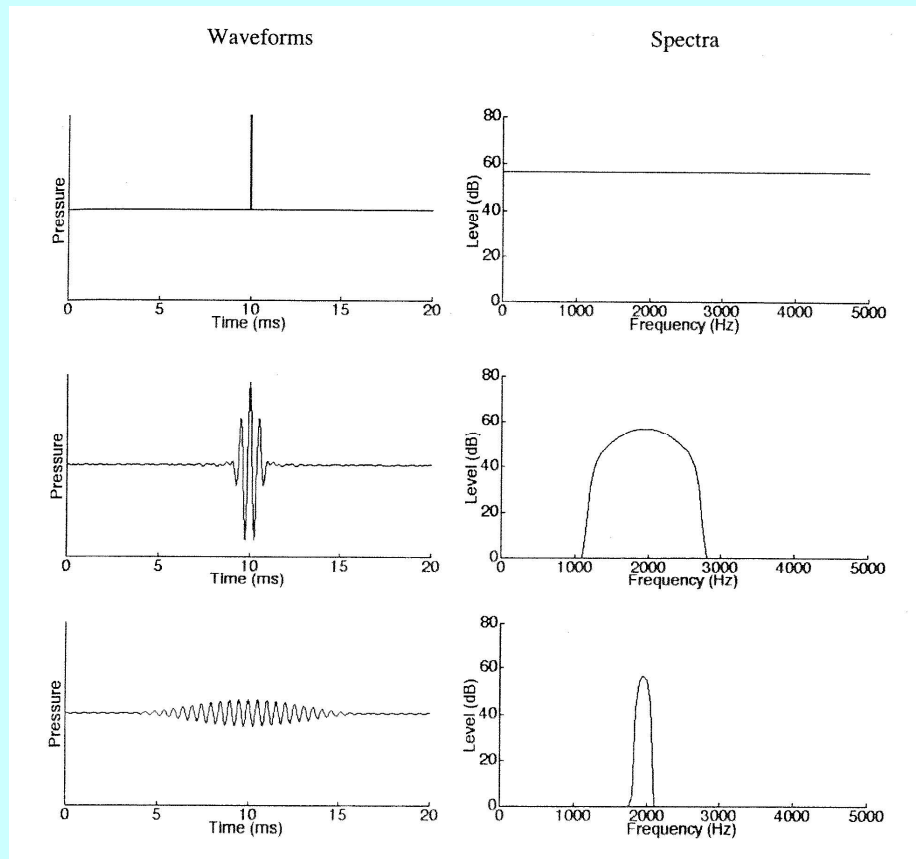
■ ERB (Equivalent Rectangular Bandwidth)

Filter-Q (tuning)

■ $Q = \text{center frequency} / \text{bandwidth}$



Filter bandwidths and impulse responses



7. Waveform manipulation

- Effect of compression
- Effect of half-wave rectification

