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A PD SLIDING MODE CONTROLLER FOR TWO-WHEELED SELF-BALANCING ROBOT BỘ ĐIỀU KHIỆN PD TRƯỚT CHO ROBOT HAI BÁNH TỰ CẦN BẮNG

Nguyen Gia Minh Thao, Duong Hoai Nghia, Phan Quang An Ho Chi Minh City University of Technology

ABSTRACT

This paper presents a method to design and control a two-wheeled self-balancing robot focuses on hardware description and PD sliding mode controller design. The signals from anow sensors are filtered by a discrete Kalman filter before being fed to the PD sliding mode controller. The objectives of the proposed controller are twofold: regulation of the pitch angle and tracking the desire position. The proposed controller has two loops. The first loop is a sliding mode pitch angle regulate. The second loop is a PD position tracking controller. Simulations and experimental results show the proposed controller has good performance and robust against disturbances.

Keywords: Two wheeled self-balancing robot, Discrete Kalman filter, PID control, Sliding mode controller.

Accelerator, Gyroscope.

TÓM TẤT

Bài báo này trình bày một phương pháp để thiết kế và điều khiến robot hai bánh tự cân báng. Các nội dung chính bao gồm mô tá phần cứng robot và thiết kế bộ điều khiến PD trượt. Các tín hiệu the các cảm biến góc được lọc bởi bộ lọc Kalman trước khi đưa vào bộ điều khiến PD trượt. Mục tiêu cư bộ điều khiển được đề xuất là ốn định hóa góc nghiêng thân robot và robot bám theo vị trí mong muốt bộ điều khiến được đề xuất gồm hai vòng. Vòng thứ nhất là một bộ điều khiến trượt để ổn định gó nghiêng thân robot. Vòng thứ hai là một bộ điều khiển PD để điều khiến vị trí của robot. Các kết quả m phỏng và thực nghiệm cho thấy bộ điểu khiển được để xuất có chất lượng tốt và bển vững với nhiều

I. INTRODUCTION

Two-wheeled self-balancing robot is a multivariable uncertain nonlinear system [1,2,7,8]. The performance of the robot depends heavily on the signal processing technique and the control method in use. In recent years, the number of researches on sliding mode (SM) control has increased [4,5,6,9]. The SM approach provides a powerful design tool for nonlinear system. So it is of great interest and feasible to use SM approach to design a compatible controller for two-wheeled self-balancing robot when the mathematical model of the robot is identified.

The designed two-wheeled self-balancing robot is given in Fig. I. Signals from angle sensors are filtered by a discrete Kalman filter before being fed to the PD sliding mode controller. The purposes of the controller are to stabilize the robot and to keep the motion of the robot tracking a reference signal. The proposed PD SM controller has two loops (Fig. 7). The first loop is a nonlinear controller based on SM

approach to maintain the tracking error of the pitch angle at zero. The second loop uses a 20 controller to control the position of the robot

II. HARDWARE DESCRIPTION

2.1. The hardware of the robot





Figure 1. The prototype two-wheelst self-balancing robot

The prototype design of the robot shown in Fig.1, Fig.2. It has an aluminum chassis, two 24V-30W DC-servo motors to actuation, an acceleration sensor and a gyroscope sensor for measuring the pitch angle.

and the angular velocity of the body, two incremental encoders for measuring the position of the wheels. The signal processing and control derithm are embedded in a 16-bit two-core muo-controller MC9S12XDP512. The ocrations of the robot (upright and balance, oving forward, moving backward, etc.) can be all from buttons on the central control module or from a RF remote controller.

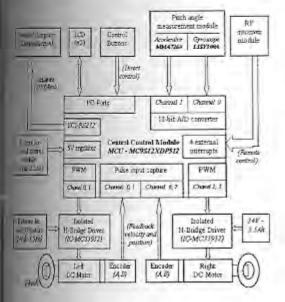


Figure 2, Hardware description

12. Sensor Signal Processing

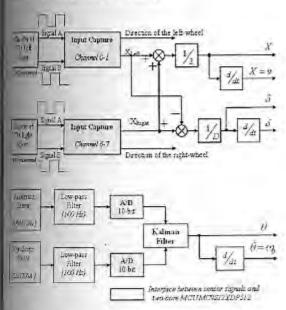


Figure 3. Sensor signal processing

An acceleration sensor, a gyroscope sensor and two incremental encoders provide full state of the robot (Fig.3). The signals from the acceleration sensor and the gyroscope sensor are filtered by a discrete Kalman filter (presented in Section III) before being fed to the PD sliding mode controller.

III. DISCRETE KALMAN FILTER

The Kalman filter estimates a process by using a form of feedback control [3]. The filter estimates the process state at some times and then obtains feedback in the form of measurements. The equations of the discrete Kalman filter can be decomposed into two groups: Time Update equations and Measurement Update equations, as shown in Fig. 4.

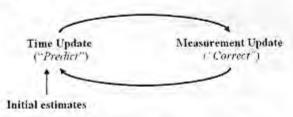


Figure 4. The discrete Kalman filter algorithm

Time Update equations

$$\hat{\mathbf{x}}_{k}^{-} = \mathbf{A}\hat{\mathbf{x}}_{k-1} + \mathbf{B}\mathbf{u}_{k} \tag{1}$$

Project the error covariance ahead

$$P_{\nu}^{-} = AP_{\nu-1}A^{T} + Q \qquad (2)$$

Measurement Update equations

Compute the Kalman gain

$$K_k = P_k^- H^T (H P_k^- H^T + R)^{-1}$$
 (3)

Update estimate with measurement zk

$$\hat{\mathbf{x}}_{k} = \hat{\mathbf{x}}_{k}^{-} + \mathbf{K}_{k} \left(\mathbf{z}_{k} - \mathbf{H} \hat{\mathbf{x}}_{k}^{-} \right) \tag{4}$$

Update the error covariance

$$P_{k} = (I - K_{k}H)P_{k}^{-}$$
(5)

The parameters of the discrete Kalman filter are as follows

$$\begin{split} A = &\begin{bmatrix} 0 & -1 \\ 0 & 0 \end{bmatrix}; \ B = \begin{bmatrix} 0 \\ 0 \end{bmatrix}; \ X = \begin{bmatrix} angle \\ gyro \end{bmatrix}; \ R = 0.17 \\ P_{initial} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}; \ Q = \begin{bmatrix} 0.002 & 0 \\ 0 & 0.005 \end{bmatrix}; \ H = \begin{bmatrix} 1 & 0 \end{bmatrix} \end{split}$$

Where: R and Q are determined by a trial and error method.

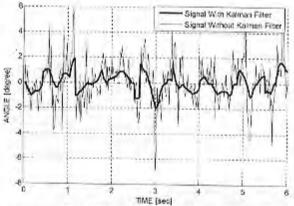


Figure 5. Filtered and unfiltered angle, measurement

IV. MATHEMATICAL MODEL

The coordinate system of the robot is shown in Fig.6. The mathematical model of the robot is derived based on Newton's 2nd law of motion [1,2,7,8].

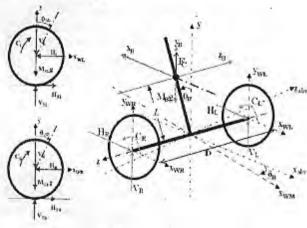


Figure 6. The coordinate system

Where:

θ: Pitch angle [rad]; δ: Yaw angle [rad].

Mw: Mass of wheel, 0.5[kg].

M_B: Mass of body, 7[kg].

R : Radius of wheel, 0.07[m].

L ;Distance between the centre of the wheels and the robot's centre of gravity, 0.3[m].

D : Distance between the contact patches of the wheels, 0.41[m].

g: Acceleration of gravity, 9.8 [ms2].

 C_L, C_R : Input torque for left and right wheels [Nm].

 $V_{TL}, V_{TR}, H_{TL}, H_{TR}, H_{L}, H_{R}, V_{L}, V_{R}$; Reaction forces [N].

 For the left wheel (same as for the july wheel).

$$\mathbf{M}_{\mathbf{W}}\ddot{\mathbf{x}}_{\mathbf{WL}} = \mathbf{H}_{\mathbf{TL}} - \mathbf{H}_{\mathbf{L}} \tag{6}$$

$$M_w \ddot{y}_{wL} = V_{TL} - V_L - M_w g \qquad (7)$$

$$J_{WL}\ddot{\theta}_{WL} = C_L - H_{TL}R \tag{8}$$

$$x_{WL} = \theta_{WL} R \qquad (0)$$

$$J_{WL} = \frac{1}{2} M_{WL} R^2 \tag{10}$$

· For the body of the robot.

$$x_{B} = L \sin \theta_{B} + \left(\frac{x_{WL} + x_{WR}}{2}\right) \tag{I}$$

$$y_{B} = -L(I - \cos\theta_{B}) \tag{1}$$

$$M_B\ddot{x}_B = H_L + H_R \tag{(1)}$$

$$\begin{split} M_B\ddot{y}_B &= V_L + V_R - M_B g + F_C \\ &= V_L + V_R - M_B g + \frac{\left(C_L + C_R\right)}{L} \sin\theta_B \end{split}$$

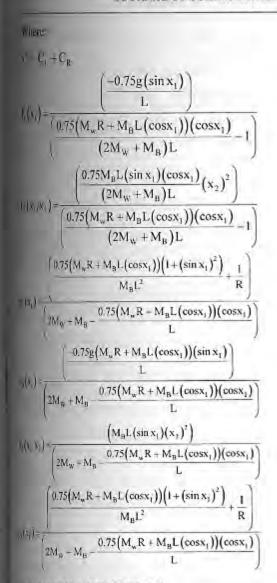
$$J_{B}\ddot{\theta}_{B} = (V_{L} + V_{R})L\sin\theta_{B} - (H_{L} + H_{R})L\cos\theta_{B} - (C_{L} + C_{R})$$
(18)

$$J_{B} = \frac{1}{3}M_{B}L^{2} \tag{1}$$

$$\theta = \theta_{\rm B} \approx \theta_{\rm W}$$

Let
$$x_1 = 0$$
, $x_2 = 0$, $x_3 = x$, $x_4 = x$. We state equations follow from (6)-(17)

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = f_1(x_1) + f_2(x_1, x_2) + g_1(x_1)C \\ \dot{x}_3 = x_4 \\ \dot{x}_4 = f_3(x_1) + f_4(x_1, x_2) + g_2(x_1)C \end{cases}$$
(8)



A CONTROLLER DESIGN

The proposed control system (described a Fig.7) has two loops. The inner loop is a PD oution tracking controller with slow dynamic Fig.8). The output of this controller is clamped tweet ±25% of the rated torque. The outer op is a SM pitch angle regulator.

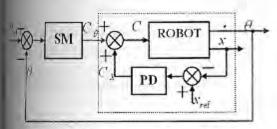


Figure 7. The proposed controller

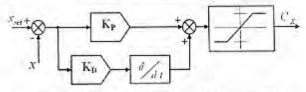


Figure 8. The PD position tracking controller

Define the tracking error as

$$e = x_{1ref} - x_1 \tag{19}$$

Where $x_{lref} = \theta_{ref}$ is the reference value of the pitch angle (0). We have

$$\dot{\mathbf{e}} = \dot{\mathbf{x}}_{1ref} - \dot{\mathbf{x}}_1 = \dot{\mathbf{x}}_{1ref} - \mathbf{x}_2$$
 (20)

$$\ddot{e} = \ddot{x}_{1ref} - \ddot{x}_1 = \ddot{x}_{1ref} - \dot{x}_2$$
 (21)

The sliding function is defined as

$$S = \tau \dot{e} + e \tag{22}$$

Where $\tau > 0$ is the desired time constant of the sliding phase. We have

$$\dot{S} = \tau \ddot{e} + \dot{e} \tag{23}$$

Substituting (20),(21) into (23), we obtain

$$\begin{split} \dot{S} &= \tau \left(\ddot{x}_{1ref} - \dot{x}_{2} \right) + \left(\dot{x}_{1ref} - x_{2} \right) \\ &= \tau \left(\ddot{x}_{1ref} - f_{1} \left(x_{1} \right) - f_{2} \left(x_{1}, x_{2} \right) - g_{1} \left(x_{1} \right) C \right) + \dot{x}_{1ref} - x_{2} \end{split}$$
(24)

Where $C = C_x + C_0$ (see Fig. 7)

The control signal C is determined such that

$$\dot{S} = -K[sat(S)] \tag{25}$$

Where

o sat(.) is the saturation function

$$sat(S) = \begin{cases} -0.4 , & \text{if } S < -0.4 \\ S , & \text{if } -0.4 \le S \le 0.4 \\ 0.4 , & \text{if } S > 0.4 \end{cases}$$
 (26)

The saturation value of sat(.) is chosen by a trial and error method.

• K is a positive constant. A large value of K results in a robust controller but it also causes chattering phenomenon.

It follows from (24), (25) that

$$C_0 = \frac{\ddot{x}_{1ref} - f_1(x_1) - f_2(x_1, x_2) + \frac{K}{\tau} [sat(S)] - \frac{x_2}{\tau} - \frac{\dot{x}_{1esf}}{\tau} - C_X}{g_1(x_1)}$$
(27)

VI. SIMULATIONS, EXPERIMENTAL RESULTS

6.1. Simulations

Responses of the proposed PD SM controller are compared with a PID multi-loop controller (Fig. 9).

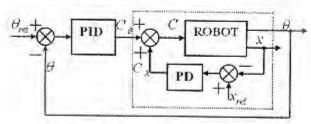


Figure 9. PID multi-loop controller

The parameters of the two controllers (Table.I) are chosen from simulations and experiments.

· Pitch angle regulation

$$\theta_{ref} = 0^0$$
, $x_{ref} = 0[m]$. (Fig.10)

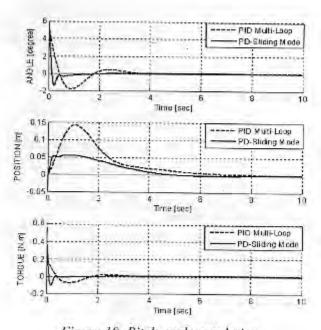


Figure 10. Pitch angle regulation

Table 1. Parameters of the controllers

PD SM	SM		t = 0.4; K=1.3\$	
controller	PD		K _P =0.21; K ₀ =0.30	
PID multi-loop	PID	Kı	Kp=4;K1=0.4; Kn=0.7	
	PD	k	$K_{\rm P} = 0.21$; $K_{\rm D} = 0.20$	

· Position tracking

$$\theta_{ref} = 0^{\circ}$$
, $x_{ref} = 1[m]$. (Fig.11)

We observe that the proposed controller has better performance in terms of settling invand overshoot.

6.2 Experimental Results

Pitch angle regulation.

$$(\theta_{ref} = 0^{\circ}, x_{ref} = 0 [m])$$
 (Fig. 12)

The pitch angle of the robot (θ) regulated under 1.1^0 , and the position of θ robot (x) is regulated under 0.04 [m].

• Response to disturbance. ($\theta_{ref} = 0^{\circ}$)

In this experiment, the robot is affect by an external disturbance (the robot is pushe at t=3[sec]). The result is given in Fig. 13.

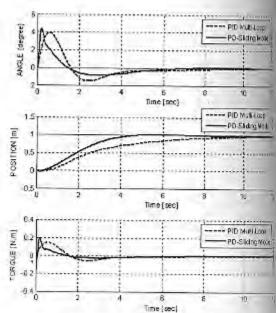


Figure 11. Position tracking

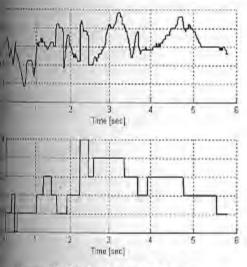


Figure 12. Pitch angle regulation

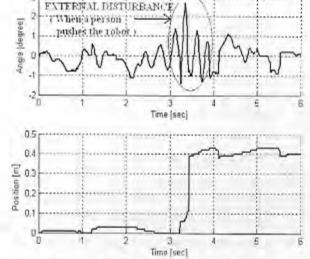


Figure 13. Response to disturbance

usilion tracking.

$$(\theta_{ref} = 0^0, x_{ref} = 1 [m])$$

The result is given in Fig.14. The robot to move at t=2[sec]. We see that the ug time is 6[sec].

CONCLUSION

This paper presented a method to and control a two-wheeled alancing robot. Simulations imental results show that the nonlinear oller based on SM approach has good mance (in terms of settling time, loot and robustness against disturbance). perations of the robot can be observed in [12]. We can conclude that the proposed 8M controller is compatible with a rear system as the two-wheeled mancing robot.

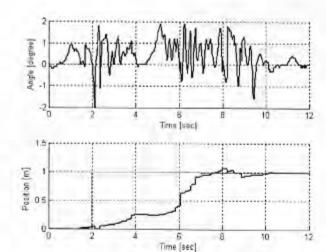


Figure 14. Position tracking.

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Author's address: Nguyen Gia Minh Thao – Tel: (+84)906.677.347; Email: ngmthao@hcmut.edu.w Ho Chi Minh City University of Technology No. 268, Ly Thuong Kiet, Dist 10, Ho Chi Minh City