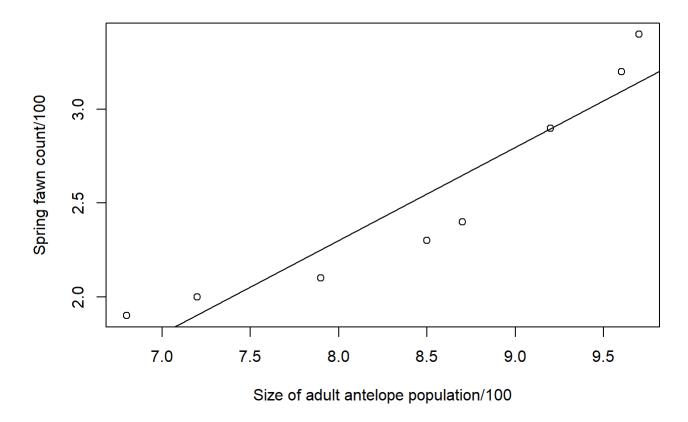
# 8WH

# Thulasiram Ruppa Krishnan March 10. 2019

```
library(RCurl)
## Loading required package: bitops
library(bitops)
library(gdata)
## gdata: Unable to locate valid perl interpreter
## gdata:
## gdata: read.xls() will be unable to read Excel XLS and XLSX files
## gdata: unless the 'perl=' argument is used to specify the location
## gdata: of a valid perl intrpreter.
## gdata:
## gdata: (To avoid display of this message in the future, please
## gdata: ensure perl is installed and available on the executable
## gdata: search path.)
## gdata: Unable to load perl libaries needed by read.xls()
## gdata: to support 'XLX' (Excel 97-2004) files.
##
## gdata: Unable to load perl libaries needed by read.xls()
## gdata: to support 'XLSX' (Excel 2007+) files.
##
## gdata: Run the function 'installXLSXsupport()'
## gdata: to automatically download and install the perl
## gdata: libaries needed to support Excel XLS and XLSX formats.
##
## Attaching package: 'gdata'
## The following object is masked from 'package:stats':
##
##
       nobs
```

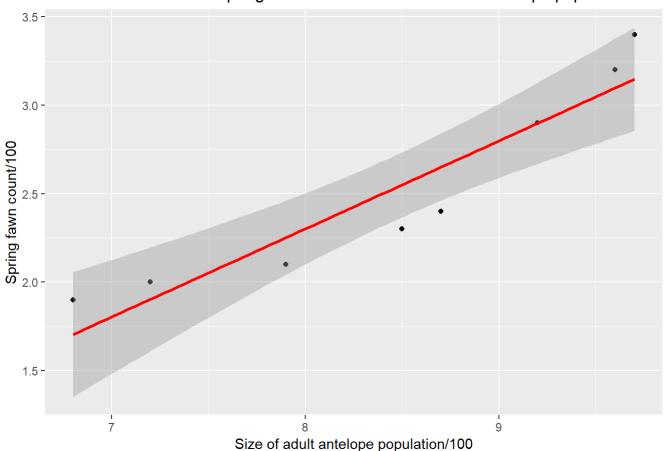
```
## The following object is masked from 'package:utils':
##
##
       object.size
## The following object is masked from 'package:base':
##
##
       startsWith
library(readx1)
library(ggplot2)
##Thunder Basin Antelope Study
##The data (X1, X2, X3, X4) are for each year.
##X1 = spring fawn count/100
##X2 = size of adult antelope population/100
##X3 = annual precipitation (inches)
##X4 = winter severity index (1=mild,5=severe)
mlr <- read excel("C:/Users/rkrishnan/Documents/01 Personal/MS/IST 687/mlr01.xls")</pre>
colnames(mlr) <-c("fawn_count","antelope_size","annual_precipitation","winter_severity")</pre>
str(mlr)
## Classes 'tbl_df', 'tbl' and 'data.frame':
                                                8 obs. of 4 variables:
  $ fawn count
                          : num 2.9 2.4 2 2.3 3.2 ...
## $ antelope size
                          : num 9.2 8.7 7.2 8.5 9.6 ...
  $ annual precipitation: num 13.2 11.5 10.8 12.3 12.6 ...
  $ winter severity
                          : num 2 3 4 2 3 5 1 3
##
summary(mlr)
##
      fawn_count
                    antelope size
                                    annual precipitation winter severity
##
   Min.
          :1.900
                    Min.
                           :6.800
                                    Min.
                                           :10.60
                                                          Min.
                                                                 :1.000
   1st Qu.:2.075
                    1st Qu.:7.725
##
                                    1st Qu.:11.10
                                                          1st Qu.:2.000
   Median :2.350
                                    Median :11.90
                                                         Median :3.000
                    Median :8.600
##
##
   Mean
          :2.525
                    Mean
                           :8.450
                                    Mean
                                           :12.04
                                                         Mean
                                                                 :2.875
                                    3rd Qu.:12.75
   3rd Qu.:2.975
                    3rd Qu.:9.300
##
                                                          3rd Qu.:3.250
##
   Max.
         :3.400
                    Max.
                           :9.700
                                    Max.
                                           :14.10
                                                          Max.
                                                                 :5.000
# Bivariate plot between fawn count and other variables (antelope size, precipitation, winter seve
rity)
# Let's plot the relationship between antelope_size and fawn_count
lm_apVsfc <- lm(formula = mlr$fawn_count ~ mlr$antelope_size,data=mlr)</pre>
plot(mlr$antelope_size,mlr$fawn_count,main ="Bivariate Plot between spring fawn count and size o
f adult antelope population",xlab = "Size of adult antelope population/100",ylab = "Spring fawn
count/100",type = "p" )
abline(lm apVsfc)
```

## Bivariate Plot between spring fawn count and size of adult antelope popula



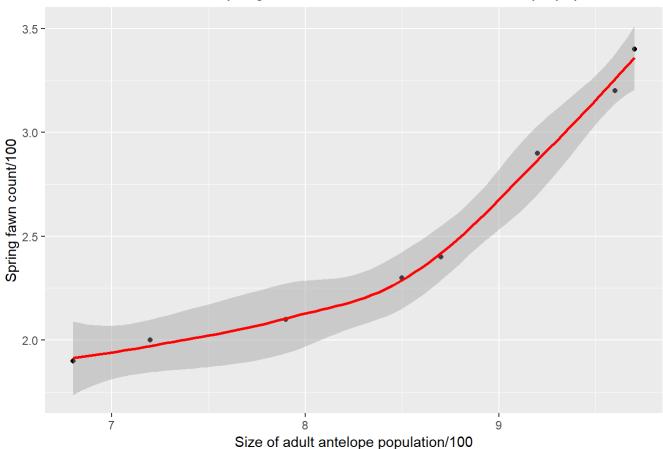
# how they look in ggplot using Lm
ggplot(data = mlr,aes(x=mlr\$antelope\_size,y=mlr\$fawn\_count))+labs(x="Size of adult antelope popu
lation/100",y="Spring fawn count/100",title = "Bivariate Plot between spring fawn count and size
of adult antelope population") + geom\_point() + geom\_smooth(method="lm", color="red",size=1)

#### Bivariate Plot between spring fawn count and size of adult antelope population



# how they look in ggplot using loess
ggplot(data = mlr,aes(x=mlr\$antelope\_size,y=mlr\$fawn\_count))+labs(x="Size of adult antelope popu
lation/100",y="Spring fawn count/100",title = "Bivariate Plot between spring fawn count and size
of adult antelope population") + geom\_point() + geom\_smooth(method="loess", color="red",size=1)

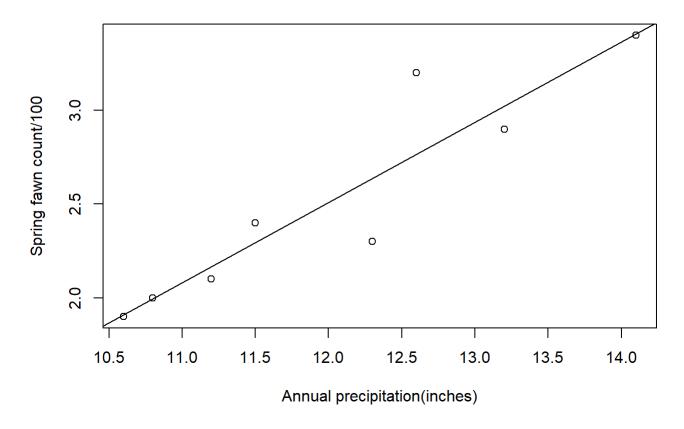
#### Bivariate Plot between spring fawn count and size of adult antelope population



# Let's plot the relationship between Annual precipitation and fawn\_count
lm\_pVsfc <- lm(formula = mlr\$fawn\_count ~ mlr\$annual\_precipitation,data=mlr)</pre>

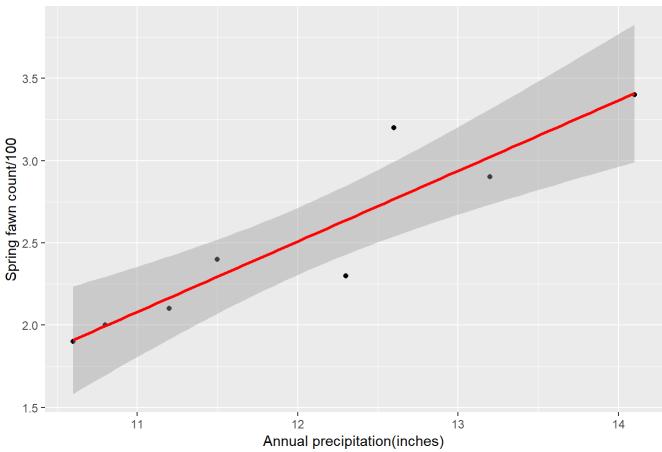
plot(mlr\$annual\_precipitation,mlr\$fawn\_count,main ="Bivariate Plot between spring fawn count and
annual precipitation",xlab = "Annual precipitation(inches)",ylab = "Spring fawn count/100",type
= "p" )
abline(lm\_pVsfc)

## Bivariate Plot between spring fawn count and annual precipitation



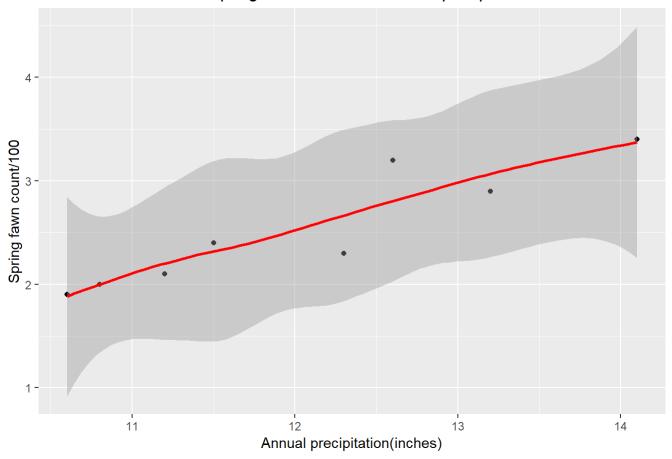
# how they look in ggplot using Lm
ggplot(data = mlr,aes(x=mlr\$annual\_precipitation,y=mlr\$fawn\_count))+labs(x="Annual precipitation
(inches)",y="Spring fawn count/100",title = "Bivariate Plot between spring fawn count and Annual
precipitation") + geom\_point() + geom\_smooth(method="lm", color="red",size=1)

## Bivariate Plot between spring fawn count and Annual precipitation



# how they look in ggplot using loess
ggplot(data = mlr,aes(x=mlr\$annual\_precipitation,y=mlr\$fawn\_count))+labs(x="Annual precipitation
(inches)",y="Spring fawn count/100",title = "Bivariate Plot between spring fawn count and Annual
precipitation") + geom\_point() + geom\_smooth(method="loess", color="red",size=1)

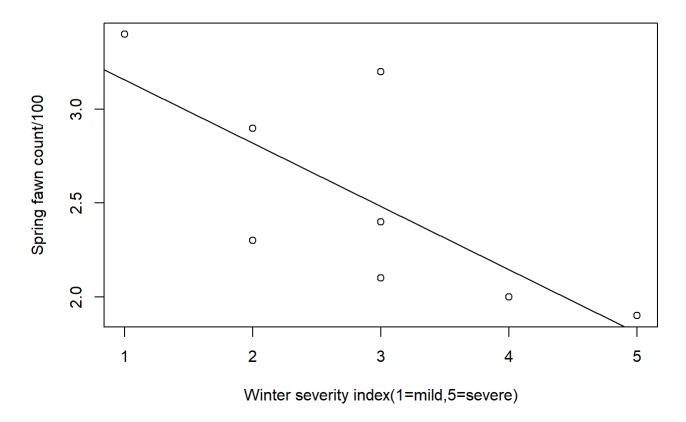
#### Bivariate Plot between spring fawn count and Annual precipitation



# Let's plot the relationship between winter severity index(1=mild,5=severe) and fawn\_count
lm\_wiVsfc <- lm(formula = mlr\$fawn\_count ~ mlr\$winter\_severity,data=mlr)</pre>

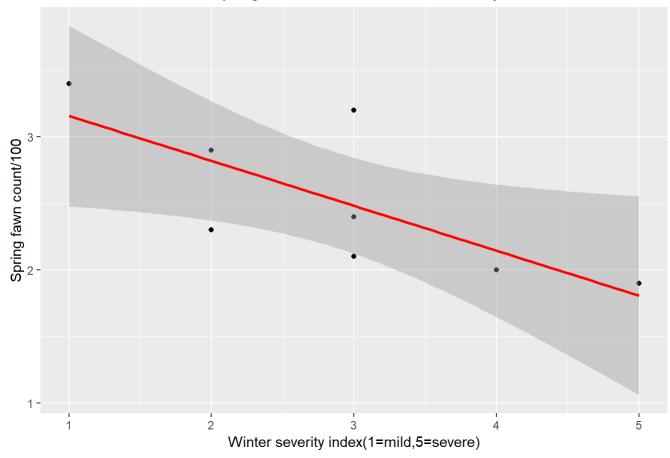
plot(mlr\$winter\_severity,mlr\$fawn\_count,main ="Bivariate Plot between spring fawn count and wint
er severity index",xlab = "Winter severity index(1=mild,5=severe)",ylab = "Spring fawn count/10
0",type = "p" )
abline(lm\_wiVsfc)

## Bivariate Plot between spring fawn count and winter severity index



# how they look in ggplot using lm
ggplot(data = mlr,aes(x=mlr\$winter\_severity,y=mlr\$fawn\_count))+labs(x="Winter severity index(1=m
ild,5=severe)",y="Spring fawn count/100",title = "Bivariate Plot between spring fawn count and W
inter severity index") + geom\_point() + geom\_smooth(method="lm", color="red",size=1)

#### Bivariate Plot between spring fawn count and Winter severity index



# how they look in ggplot using loess
ggplot(data = mlr,aes(x=mlr\$winter\_severity,y=mlr\$fawn\_count))+labs(x="Winter severity index(1=m
ild,5=severe)",y="Spring fawn count/100",title = "Bivariate Plot between spring fawn count and W
inter severity index") + geom\_point() + geom\_smooth(method="loess", color="red",size=1)

```
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : pseudoinverse used at 0.98
```

```
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : neighborhood radius 2.02
```

```
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : reciprocal condition number 2.3712e-017
```

```
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : There are other near singularities as well. 1
```

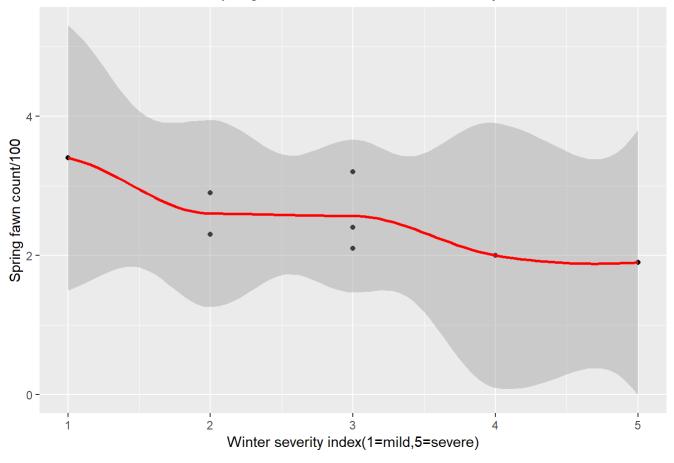
```
## Warning in predLoess(object$y, object$x, newx = if
## (is.null(newdata)) object$x else if (is.data.frame(newdata))
## as.matrix(model.frame(delete.response(terms(object)), : pseudoinverse used
## at 0.98
```

```
## Warning in predLoess(object$y, object$x, newx = if
## (is.null(newdata)) object$x else if (is.data.frame(newdata))
## as.matrix(model.frame(delete.response(terms(object)), : neighborhood radius
## 2.02
```

```
## Warning in predLoess(object$y, object$x, newx = if
## (is.null(newdata)) object$x else if (is.data.frame(newdata))
## as.matrix(model.frame(delete.response(terms(object)), : reciprocal
## condition number 2.3712e-017
```

```
## Warning in predLoess(object$y, object$x, newx = if
## (is.null(newdata)) object$x else if (is.data.frame(newdata))
## as.matrix(model.frame(delete.response(terms(object)), : There are other
## near singularities as well. 1
```

#### Bivariate Plot between spring fawn count and Winter severity index



```
# Regression Model, predict the number of fawns from Antelope Size
sum.lm_apVsfc <- summary(lm_apVsfc)
paste("p values:")</pre>
```

```
## [1] "p values:"
```

```
sum.lm_apVsfc$coef[,4]
```

```
##
         (Intercept) mlr$antelope_size
        0.0381522675
                          0.0005471422
##
paste("Adjusted R squared: " ,sum.lm_apVsfc$adj.r.squared)
## [1] "Adjusted R squared: 0.861563784952523"
                        predict the number of fawns
# Regression Model,
                                                         from
                                                                  Annual Precipitation
sum.lm_pVsfc <- summary(lm_pVsfc)</pre>
paste("p values:")
## [1] "p values:"
sum.lm_pVsfc$coef[,4]
##
                (Intercept) mlr$annual_precipitation
##
                0.023840288
                                          0.001039425
paste("Adjusted R squared: " ,sum.lm_pVsfc$adj.r.squared)
## [1] "Adjusted R squared: 0.829212576293043"
# Regression Model,
                        predict the number of fawns from Winter Severity Index
sum.lm_wiVsfc <- summary(lm_wiVsfc)</pre>
paste("p values:")
## [1] "p values:"
sum.lm wiVsfc$coef[,4]
##
           (Intercept) mlr$winter_severity
##
           0.000108158
                               0.036263036
paste("Adjusted R squared: " ,sum.lm_wiVsfc$adj.r.squared)
## [1] "Adjusted R squared: 0.47020333641798"
# Let's predict fawn count from two variables antelope_size and annual_precipitation
lm_ap.pVsfc <- lm(formula = mlr$fawn_count ~ mlr$antelope_size + mlr$annual_precipitation,data=m</pre>
lr)
sum.lm_ap.pVsfc <- summary(lm_ap.pVsfc)</pre>
paste("p values:")
```

```
## [1] "p values:"
sum.lm_ap.pVsfc$coef[,4]
##
                (Intercept)
                                    mlr$antelope size mlr$annual precipitation
##
                 0.02846521
                                           0.12406648
                                                                     0.23548196
paste("Adjusted R squared: " ,sum.lm_ap.pVsfc$adj.r.squared)
## [1] "Adjusted R squared: 0.878160928538559"
# Addition of one more variable to annual_precipitation has increased the model accuracy from 8
6% to 87% from the original model with just antelope size
# Let's predict fawn count from two variables antelope size and winter index
lm_wi.pVsfc <- lm(formula = mlr$fawn_count ~ mlr$antelope_size + mlr$winter_severity,data=mlr)</pre>
sum.lm wi.pVsfc <- summary(lm wi.pVsfc)</pre>
paste("p values:")
## [1] "p values:"
sum.lm wi.pVsfc$coef[,4]
##
           (Intercept)
                          mlr$antelope_size mlr$winter_severity
            0.16977988
                                 0.01118699
##
                                                     0.59557987
paste("Adjusted R squared: " ,sum.lm_wi.pVsfc$adj.r.squared)
## [1] "Adjusted R squared: 0.84389367311556"
# Addition of winter index to annual precipitation has dropped the model accuracy from 86% to 8
4% from the original model with just antelope size
# Let's predict fawn count from two variables annual_precipitation and winter_index
lm_wi.apVsfc <- lm(formula = mlr$fawn_count ~ mlr$annual_precipitation + mlr$winter_severity,dat</pre>
a=mlr)
sum.lm_wi.apVsfc <- summary(lm_wi.apVsfc)</pre>
paste("p values:")
## [1] "p values:"
```

sum.lm\_wi.apVsfc\$coef[,4] ## (Intercept) mlr\$annual\_precipitation mlr\$winter severity ## 0.047647946 0.008431877 0.188417206 paste("Adjusted R squared: " ,sum.lm\_wi.apVsfc\$adj.r.squared) ## [1] "Adjusted R squared: 0.859962754071404" # Addition of winter index to annual precipitation has dropped the model accuracy from 86% to 8 4% from the original model with just antelope size # Let's predict fawn count from three variables antelope size , annual precipitation and winter index lm ap.p.wiVsfc <- lm(formula = mlr\$fawn count ~ mlr\$antelope size + mlr\$annual precipitation + m</pre> lr\$winter severity,data=mlr) summary(lm ap.p.wiVsfc) ## ## Call: ## lm(formula = mlr\$fawn\_count ~ mlr\$antelope\_size + mlr\$annual\_precipitation + mlr\$winter severity, data = mlr) ## ## ## Residuals: ## 3 ## ## Coefficients: Estimate Std. Error t value Pr(>|t|) ## ## (Intercept) -5.92201 1.25562 -4.716 0.0092 \*\* ## mlr\$antelope size 0.33822 0.09947 3.400 0.0273 \* 0.0217 \* ## mlr\$annual\_precipitation 0.40150 0.10990 3.653 ## mlr\$winter severity 0.26295 0.08514 3.089 0.0366 \* ## ---## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.05 '.' 0.1 ' ' 1 ## ## Residual standard error: 0.1209 on 4 degrees of freedom ## Multiple R-squared: 0.9743, Adjusted R-squared: 0.955 ## F-statistic: 50.52 on 3 and 4 DF, p-value: 0.001229 sum.lm\_ap.p.wiVsfc <- summary(lm\_ap.p.wiVsfc)</pre>

```
## [1] "p values:"
```

```
sum.lm_ap.p.wiVsfc$coef[,4]
```

paste("p values:")

```
## (Intercept) mlr$antelope_size mlr$annual_precipitation
## 0.009196072 0.027272444 0.021707219
## mlr$winter_severity
## 0.036626174
```

```
paste("Adjusted R squared: " ,sum.lm_ap.p.wiVsfc$adj.r.squared)
```

```
## [1] "Adjusted R squared: 0.955004704934087"
```

# After we added the winter index to the model, accuracy has increased from 87% to 95% from the original model with just antelope size and annual\_precipitation

#Compare all the models

cat(paste("One Variable Prediction ", "Adjusted R squared for Antelope Size : ",sum.lm\_apVsfc\$ad j.r.squared, "Adjusted R squared for Annual Precipitation: ",sum.lm\_pVsfc\$adj.r.squared, "Adjusted R squared for Winter Index: ",sum.lm\_wiVsfc\$adj.r.squared, "Two Variable Prediction ", "Adjusted R squared for Antelope Size and Annual Precipitation : ",sum.lm\_ap.pVsfc\$adj.r.squared, "Adjusted R squared for Antelope Size and Winter Index : ",sum.lm\_wi.pVsfc\$adj.r.squared, "Adjusted R squared for Annual Precipitation and Winter Index : ",sum.lm\_wi.apVsfc\$adj.r.squared, "Three Variable Prediction ", "Adjusted R squared for Antelope Size, Annual Precipitation and Winter Index : ",sum.lm ap.p.wiVsfc\$adj.r.squared,sep='\n' ))

```
## One Variable Prediction
## Adjusted R squared for Antelope Size :
## 0.861563784952523
## Adjusted R squared for Annual Precipitation:
## 0.829212576293043
## Adjusted R squared for Winter Index:
## 0.47020333641798
## Two Variable Prediction
## Adjusted R squared for Antelope Size and Annual Precipitation :
## 0.878160928538559
## Adjusted R squared for Antelope Size and Winter Index :
## 0.84389367311556
## Adjusted R squared for Annual Precipitaion and Winter Index :
## 0.859962754071404
## Three Variable Prediction
## Adjusted R squared for Antelope Size, Annual Precipitation and Winter Index :
## 0.955004704934087
```

# The best predction with fewer variable is given by the model using Antelope Size and Annual Precipitation