# STAT 425 - Case Study #1

#### 2024-10-22

In this case study, our objective is to identify the key qualities of a Halloween candy that make it desirable based on various attributes. We will fit a multiple regression model to explain the desirability of a Halloween candy, as measured by the percentage of votes it receives (winpercent). Key predictor variables include characteristics such as the presence of chocolate, fruity flavors, caramel, peanuts, nougat, and other ingredients. Using this model, we will estimate the desirability of at least two favorite candies and determine the attributes of the ideal Halloween candy.

The significance level that we choose for this case study is alpha = 0.05.

```
df <- read.csv("~/Desktop/uiuc/stat425/Case Study 1/candy-data.csv")
df</pre>
```

##		competitorname	chocolate	fruity	caramel	peanutyalmondy	nougat
##	1	100 Grand	1	0	1	0	0
##	2	3 Musketeers	1	0	0	0	1
##	3	One dime	0	0	0	0	0
##	4	One quarter	0	0	0	0	0
##	5	Air Heads	0	1	0	0	0
##	6	Almond Joy	1	0	0	1	0
##	7	Baby Ruth	1	0	1	1	1
##	8	Boston Baked Beans	0	0	0	1	0
##	9	Candy Corn	0	0	0	0	0
##	10	Caramel Apple Pops	0	1	1	0	0
##	11	Charleston Chew	1	0	0	0	1
##	12	Chewey Lemonhead Fruit Mix	0	1	0	0	0
##	13	Chiclets	0	1	0	0	0
##	14	Dots	0	1	0	0	0
##	15	Dum Dums	0	1	0	0	0
##	16	Fruit Chews	0	1	0	0	0
##	17	Fun Dip	0	1	0	0	0
##	18	Gobstopper	0	1	0	0	0
##	19	Haribo Gold Bears	0	1	0	0	0
##	20	Haribo Happy Cola	0	0	0	0	0
##	21	Haribo Sour Bears	0	1	0	0	0
##	22	Haribo Twin Snakes	0	1	0	0	0
##	23	HersheyÕs Kisses	1	0	0	0	0
##	24	HersheyÕs Krackel	1	0	0	0	0
##	25	HersheyÕs Milk Chocolate	1	0	0	0	0
##	26	HersheyÕs Special Dark	1	0	0	0	0
##	27	Jawbusters	0	1	0	0	0
##	28	Junior Mints	1	0	0	0	0
##	29	Kit Kat	1	0	0	0	0
##	30	Laffy Taffy	0	1	0	0	0
##	31	Lemonhead	0	1	0	0	0

					_	_	
##	32	Lifesavers big ring gummies	0	1	0	0	0
##	33	Peanut butter M&MÖs	1	0	0	1	0
##	34	M&MÕs	1	0	0	0	0
##	35	Mike & Ike	0	1	0	0	0
##	36	Milk Duds	1	0	1	0	0
##	37	Milky Way	1	0	1	0	1
##	38	Milky Way Midnight	1	0	1	0	1
##	39		1	0	1	0	0
		Milky Way Simply Caramel					
	40	Mounds	1	0	0	0	0
	41	Mr Good Bar	1	0	0	1	0
	42	Nerds	0	1	0	0	0
##	43	Nestle Butterfinger	1	0	0	1	0
##	44	Nestle Crunch	1	0	0	0	0
##	45	Nik L Nip	0	1	0	0	0
##	46	Now & Later	0	1	0	0	0
##	47	Payday	0	0	0	1	1
##	48	Peanut M&Ms	1	0	0	1	0
##	49	Pixie Sticks	0	0	0	0	0
##	50	Pop Rocks	0	1	0	0	0
##	51	Red vines	0	1	0	0	0
##	52	ReeseÕs Miniatures	1	0	0	1	0
##		ReeseÕs Peanut Butter cup	1	0	0	1	0
##		ReeseÕs pieces	1	0	0	1	0
				0			
		ReeseÕs stuffed with pieces	1		0	1	0
##		Ring pop	0	1	0	0	0
##		Rolo	1	0	1	0	0
	58	Root Beer Barrels	0	0	0	0	0
##	59	Runts	0	1	0	0	0
##	60	Sixlets	1	0	0	0	0
##	61	Skittles original	0	1	0	0	0
##	62	Skittles wildberry	0	1	0	0	0
##	63	Nestle Smarties	1	0	0	0	0
##	64	Smarties candy	0	1	0	0	0
##	65	Snickers	1	0	1	1	1
##	66	Snickers Crisper	1	0	1	1	0
	67	Sour Patch Kids	0	1	0	0	0
##	68	Sour Patch Tricksters	0	1	0	0	0
	69	Starburst	0	1	0	0	0
##		Strawberry bon bons	0	1	0	0	0
	71	Sugar Babies	0	0	1	0	0
	72	9	0	0	1	0	0
		Sugar Daddy					
##		Super Bubble	0	1	0	0	0
	74	Swedish Fish	0	1	0	0	0
	75	Tootsie Pop	1	1	0	0	0
	76	Tootsie Roll Juniors	1	0	0	0	0
	77	Tootsie Roll Midgies	1	0	0	0	0
##	78	Tootsie Roll Snack Bars	1	0	0	0	0
##	79	Trolli Sour Bites	0	1	0	0	0
##	80	Twix	1	0	1	0	0
##	81	Twizzlers	0	1	0	0	0
##	82	Warheads	0	1	0	0	0
##		WelchÕs Fruit Snacks	0	1	0	0	0
##		WertherÕs Original Caramel	0	0	1	0	0
##		Whoppers	1	0	0	0	0
	-	"Hopperb	_	9	· ·	V	J

##		crispedricewafer	hard	bar	pluribus	sugarpercent	pricepercent	winpercent
##	1	1	0	1	0	0.732	0.860	66.97173
##	2	0	0	1	0	0.604	0.511	67.60294
##	3	0	0	0	0	0.011	0.116	32.26109
##	4	0	0	0	0	0.011	0.511	46.11650
##	5	0	0	0	0	0.906	0.511	52.34146
##	6	0	0	1	0	0.465	0.767	50.34755
##	7	0	0	1	0	0.604	0.767	56.91455
##	8	0	0	0	1	0.313	0.511	23.41782
##	9	0	0	0	1	0.906	0.325	38.01096
##	10	0	0	0	0	0.604	0.325	34.51768
##	11	0	0	1	0	0.604	0.511	38.97504
##	12	0	0	0	1	0.732	0.511	36.01763
##	13	0	0	0	1	0.046	0.325	24.52499
##	14	0	0	0	1	0.732	0.511	42.27208
##	15	0	1	0	0	0.732	0.034	39.46056
##	16	0	0	0	1	0.127	0.034	43.08892
##	17	0	1	0	0	0.732	0.325	39.18550
##	18	0	1	0	1	0.906	0.453	46.78335
##	19	0	0	0	1	0.465	0.465	57.11974
##	20	0	0	0	1	0.465	0.465	34.15896
##	21	0	0	0	1	0.465	0.465	51.41243
##	22	0	0	0	1	0.465	0.465	42.17877
	23	0	0	0	1	0.127	0.093	55.37545
##	24	1	0	1	0	0.430	0.918	62.28448
##	25	0	0	1	0	0.430	0.918	56.49050
##	26	0	0	1	0	0.430	0.918	59.23612
## ##	<ul><li>27</li><li>28</li></ul>	0	1	0	1	0.093	0.511	28.12744
##	29	0	0	1	1 0	0.197 0.313	0.511 0.511	57.21925 76.76860
##	30	0	0	0	0	0.313	0.116	41.38956
##	31	0	1	0	0	0.220	0.116	39.14106
##	32	0	0	0	0	0.040	0.104	52.91139
##	33	0	0	0	1	0.825	0.651	71.46505
##	34	0	0	0	1	0.825	0.651	66.57458
	35	0	0	0	1	0.872	0.325	46.41172
##		0	0	0	1	0.302	0.511	55.06407
	37	0	0	1	0	0.604	0.651	73.09956
	38	0	0	1	0	0.732	0.441	60.80070
##		0	0	1	0	0.965	0.860	64.35334
##		0	0	1	0	0.313	0.860	47.82975
##	41	0	0	1	0	0.313	0.918	54.52645
##	42	0	1	0	1	0.848	0.325	55.35405
##	43	0	0	1	0	0.604	0.767	70.73564
##	44	1	0	1	0	0.313	0.767	66.47068
##	45	0	0	0	1	0.197	0.976	22.44534
##	46	0	0	0	1	0.220	0.325	39.44680
##	47	0	0	1	0	0.465	0.767	46.29660
##	48	0	0	0	1	0.593	0.651	69.48379
##	49	0	0	0	1	0.093	0.023	37.72234
##	50	0	1	0	1	0.604	0.837	41.26551
	51	0	0	0	1	0.581	0.116	37.34852
##	52	0	0	0	0	0.034	0.279	81.86626
##	53	0	0	0	0	0.720	0.651	84.18029

##	54	0	0	0	1	0.406	0.651	73.43499
##	55	0	0	0	0	0.988	0.651	72.88790
##	56	0	1	0	0	0.732	0.965	35.29076
##	57	0	0	0	1	0.860	0.860	65.71629
##	58	0	1	0	1	0.732	0.069	29.70369
##	59	0	1	0	1	0.872	0.279	42.84914
##	60	0	0	0	1	0.220	0.081	34.72200
##	61	0	0	0	1	0.941	0.220	63.08514
##	62	0	0	0	1	0.941	0.220	55.10370
##	63	0	0	0	1	0.267	0.976	37.88719
##	64	0	1	0	1	0.267	0.116	45.99583
##	65	0	0	1	0	0.546	0.651	76.67378
##	66	1	0	1	0	0.604	0.651	59.52925
##	67	0	0	0	1	0.069	0.116	59.86400
##	68	0	0	0	1	0.069	0.116	52.82595
##	69	0	0	0	1	0.151	0.220	67.03763
##	70	0	1	0	1	0.569	0.058	34.57899
##	71	0	0	0	1	0.965	0.767	33.43755
##	72	0	0	0	0	0.418	0.325	32.23100
	73	0	0	0	0	0.162	0.116	27.30386
##	74	0	0	0	1	0.604	0.755	54.86111
##	75	0	1	0	0	0.604	0.325	48.98265
##	76	0	0	0	0	0.313	0.511	43.06890
##	77	0	0	0	1	0.174	0.011	45.73675
##	78	0	0	1	0	0.465	0.325	49.65350
	79	0	0	0	1	0.313	0.255	47.17323
	80	1	0	1	0	0.546	0.906	81.64291
	81	0	0	0	0	0.220	0.116	45.46628
	82	0	1	0	0	0.093	0.116	39.01190
	83	0	0	0	1	0.313	0.313	44.37552
	84	0	1	0	0	0.186	0.267	41.90431
##	85	1	0	0	1	0.872	0.848	49.52411

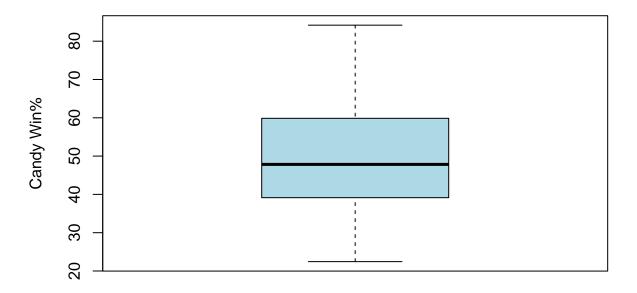
### unique(df\$competitorname)

```
## [1] "100 Grand"
                                       "3 Musketeers"
##
  [3] "One dime"
                                       "One quarter"
  [5] "Air Heads"
                                       "Almond Joy"
  [7] "Baby Ruth"
                                       "Boston Baked Beans"
##
##
  [9] "Candy Corn"
                                       "Caramel Apple Pops"
## [11] "Charleston Chew"
                                       "Chewey Lemonhead Fruit Mix"
                                       "Dots"
## [13] "Chiclets"
## [15] "Dum Dums"
                                       "Fruit Chews"
## [17] "Fun Dip"
                                       "Gobstopper"
## [19] "Haribo Gold Bears"
                                       "Haribo Happy Cola"
## [21] "Haribo Sour Bears"
                                       "Haribo Twin Snakes"
## [23] "HersheyÕs Kisses"
                                       "HersheyÕs Krackel"
## [25] "HersheyÕs Milk Chocolate"
                                       "HersheyÕs Special Dark"
## [27] "Jawbusters"
                                       "Junior Mints"
## [29] "Kit Kat"
                                       "Laffy Taffy"
                                       "Lifesavers big ring gummies"
## [31] "Lemonhead"
## [33] "Peanut butter M&MÕs"
                                       "M&MÕs"
## [35] "Mike & Ike"
                                       "Milk Duds"
## [37] "Milky Way"
                                       "Milky Way Midnight"
```

```
## [39] "Milky Way Simply Caramel"
                                        "Mounds"
## [41] "Mr Good Bar"
                                        "Nerds"
## [43] "Nestle Butterfinger"
                                        "Nestle Crunch"
## [45] "Nik L Nip"
                                        "Now & Later"
##
  [47]
        "Payday"
                                        "Peanut M&Ms"
       "Pixie Sticks"
## [49]
                                        "Pop Rocks"
## [51] "Red vines"
                                        "ReeseÕs Miniatures"
                                       "ReeseÕs pieces"
## [53] "ReeseÕs Peanut Butter cup"
##
   [55]
        "ReeseÕs stuffed with pieces"
                                       "Ring pop"
  [57]
        "Rolo"
                                        "Root Beer Barrels"
##
## [59] "Runts"
                                        "Sixlets"
                                        "Skittles wildberry"
## [61] "Skittles original"
       "Nestle Smarties"
                                        "Smarties candy"
   [63]
## [65]
       "Snickers"
                                        "Snickers Crisper"
## [67]
        "Sour Patch Kids"
                                        "Sour Patch Tricksters"
## [69]
        "Starburst"
                                        "Strawberry bon bons"
   [71]
        "Sugar Babies"
                                        "Sugar Daddy"
##
       "Super Bubble"
                                        "Swedish Fish"
   [73]
  [75] "Tootsie Pop"
                                        "Tootsie Roll Juniors"
                                        "Tootsie Roll Snack Bars"
  [77] "Tootsie Roll Midgies"
## [79]
       "Trolli Sour Bites"
                                        "Twix"
## [81] "Twizzlers"
                                        "Warheads"
## [83] "WelchÕs Fruit Snacks"
                                        "WertherÕs Original Caramel"
## [85] "Whoppers"
```

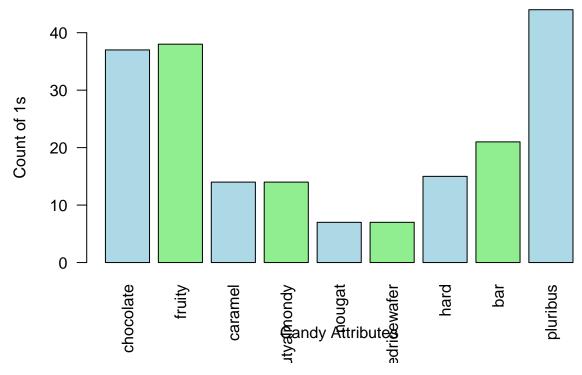
We have chosen to display the five-number summary alongside a box and whisker plot to analyze the distribution and variance of the winpercent variable. This provides a clearer understanding of the range and spread of the data, which will be useful as we proceed with the multiple linear regression (MLR) model.

## **Box & Whisker Plot of Candy Win%**



We created this model to visualize the frequency of each candy attribute, which helps in understanding the distribution of key variables. By examining the count of each attribute (chocolate, fruity, caramel, etc.), we can determine which attributes are more common in candies, giving us an idea of the factors that may influence the win percentage. This stacked bar plot serves as a useful descriptive statistic visualization, allowing us to compare the prevalence of different variables side by side. Additionally, it highlights potential predictors of win percentage in the MLR model, guiding us toward identifying which variables might have a stronger effect on candy success.

## **Stacked Bar Plot of Candy Variables**



The correlation matrix is a valuable tool in regression analysis because it helps us identify relationships between independent variables and the dependent variable, as well as correlations between independent variables themselves. In the context of an MLR (Multiple Linear Regression) model, it is important to understand the relationships between variables to avoid multicollinearity, which occurs when independent variables are highly correlated with one another. Multicollinearity can make it difficult to interpret the coefficients of the regression model and may inflate standard errors. By reviewing this correlation matrix, we can also identify which predictors have strong correlations with the dependent variable (winpercent in this case) and prioritize those in our model, thereby improving model performance and interpretability.

```
binary_vars <- df[, c("chocolate", "fruity", "caramel", "peanutyalmondy", "nougat", "crispedricewafer",
cor_matrix <- cor(binary_vars)
cor_matrix</pre>
```

```
##
                     chocolate
                                    fruity
                                                caramel peanutyalmondy
                                                                             nougat
## chocolate
                     1.0000000 -0.74172106
                                            0.24987535
                                                            0.37782357
                                                                        0.25489183
## fruity
                    -0.7417211
                                1.00000000 -0.33548538
                                                           -0.39928014 -0.26936712
                     0.2498753 -0.33548538
                                             1.00000000
  caramel
                                                            0.05935614
                                                                        0.32849280
  peanutyalmondy
                     0.3778236 -0.39928014
                                             0.05935614
                                                            1.00000000
                                                                        0.21311310
## nougat
                     0.2548918 -0.26936712
                                             0.32849280
                                                            0.21311310
                                                                        1.00000000
## crispedricewafer
                     0.3412098 -0.26936712
                                             0.21311310
                                                           -0.01764631 -0.08974359
## hard
                    -0.3441769 0.39067750 -0.12235513
                                                           -0.20555661 -0.13867505
## bar
                     0.5974211 -0.51506558
                                            0.33396002
                                                            0.26041960
                                                                        0.52297636
## pluribus
                    -0.3396752 0.29972522 -0.26958501
                                                           -0.20610932 -0.31033884
## sugarpercent
                     0.1041691 -0.03439296
                                            0.22193335
                                                            0.08788927
                                                                        0.12308135
## pricepercent
                     0.5046754 -0.43096853
                                            0.25432709
                                                            0.30915323 0.15319643
```

```
0.40619220 0.19937530
## winpercent
                   0.6365167 -0.38093814 0.21341630
##
                                                           pluribus
                  crispedricewafer
                                        hard
                                                    bar
                       0.34120978 -0.34417691 0.59742114 -0.33967519
## chocolate
                       ## fruity
## caramel
                       ## peanutyalmondy
                       -0.01764631 -0.20555661 0.26041960 -0.20610932
## nougat
                       -0.08974359 -0.13867505 0.52297636 -0.31033884
## crispedricewafer
                       1.00000000 -0.13867505 0.42375093 -0.22469338
## hard
                       -0.13867505 1.00000000 -0.26516504 0.01453172
## bar
                       0.42375093 -0.26516504 1.00000000 -0.59340892
## pluribus
                       ## sugarpercent
                        0.06994969 0.09180975 0.09998516
                                                        0.04552282
## pricepercent
                        0.32826539 -0.24436534 0.51840654 -0.22079363
## winpercent
                        0.32467965 -0.31038158 0.42992933 -0.24744787
##
                  sugarpercent pricepercent winpercent
## chocolate
                    0.10416906
                                 0.5046754 0.6365167
                                -0.4309685 -0.3809381
## fruity
                   -0.03439296
## caramel
                    0.22193335
                                 0.2543271 0.2134163
## peanutyalmondy
                                 0.3091532 0.4061922
                    0.08788927
## nougat
                    0.12308135
                                 0.1531964 0.1993753
## crispedricewafer
                    0.06994969 0.3282654 0.3246797
## hard
                    0.09180975 -0.2443653 -0.3103816
## bar
                    ## pluribus
                    0.04552282 -0.2207936 -0.2474479
## sugarpercent
                    1.00000000
                                 0.3297064 0.2291507
## pricepercent
                    0.32970639
                                 1.0000000 0.3453254
## winpercent
                    0.22915066
                                 0.3453254 1.0000000
df_clean <- df[, -which(names(df) == "competitorname")]</pre>
full_model <- lm(winpercent ~ ., data = df_clean)</pre>
summary(full model)
##
## Call:
## lm(formula = winpercent ~ ., data = df_clean)
##
## Residuals:
##
                     Median
       Min
                1Q
                                 3Q
                                        Max
                     0.1986
## -20.2244 -6.6247
                             6.8420 23.8680
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   34.5340
                              4.3199
                                      7.994 1.44e-11 ***
## chocolate
                   19.7481
                              3.8987
                                      5.065 2.96e-06 ***
                    9.4223
                              3.7630
                                      2.504 0.01452 *
## fruity
## caramel
                    2.2245
                              3.6574
                                      0.608 0.54493
## peanutyalmondy
                   10.0707
                              3.6158
                                      2.785 0.00681 **
## nougat
                    0.8043
                              5.7164
                                      0.141
                                            0.88849
## crispedricewafer
                    8.9190
                              5.2679
                                      1.693 0.09470 .
## hard
                   -6.1653
                              3.4551 -1.784
                                             0.07852 .
## bar
                    0.4415
                              5.0611
                                      0.087 0.93072
## pluribus
                   -0.8545
                              3.0401 -0.281 0.77945
## sugarpercent
                    9.0868
                              4.6595
                                      1.950 0.05500 .
```

```
## pricepercent -5.9284 5.5132 -1.075 0.28578
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.7 on 73 degrees of freedom
## Multiple R-squared: 0.5402, Adjusted R-squared: 0.4709
## F-statistic: 7.797 on 11 and 73 DF, p-value: 9.504e-09
```

In the full model, we include all potential predictor variables from the dataset to assess their relationships with the response variable, winpercent. This model is necessary as it allows us to observe the statistical significance of each variable, measured by their p-values, which indicate whether or not each predictor is contributing meaningful information to explain variations in winpercent.

From the model output, we can see which variables have significant p-values (below a threshold, typically 0.05) and which do not. In this case, chocolate, fruity, and peanutyalmondy are statistically significant with p-values well below 0.05. Other variables like nougat, bar, pluribus, and others have much higher p-values, meaning they are not significant predictors in this model.

Once we identify the statistically insignificant variables, we can exclude them from the model, creating a reduced model that only includes the significant variables. This process of variable selection is important because it simplifies the model, making it more interpretable, reduces multicollinearity, and improves generalizability by focusing only on the predictors that have a meaningful relationship with the response variable.

```
reduced_model <- lm(winpercent ~ chocolate + fruity + peanutyalmondy, data = df_clean)
summary(reduced_model)</pre>
```

```
##
## lm(formula = winpercent ~ chocolate + fruity + peanutyalmondy,
##
       data = df clean)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
  -23.0497
            -7.3084
                      -0.4523
                                7.9446
                                         23.8712
##
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    35.788
                                3.237
                                        11.057 < 2e-16 ***
## chocolate
                    21.983
                                3.599
                                         6.108 3.34e-08 ***
## fruity
                     7.753
                                3.625
                                         2.139
                                                 0.0354 *
## peanutyalmondy
                     9.066
                                3.520
                                         2.576
                                                 0.0118 *
##
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 10.94 on 81 degrees of freedom
## Multiple R-squared: 0.4673, Adjusted R-squared: 0.4475
## F-statistic: 23.68 on 3 and 81 DF, p-value: 4.209e-11
candy row nums <- which(df$competitorname %in% c("ReeseOs Peanut Butter cup", "Snickers", "Almond Joy",
actual_values <- df$winpercent[candy_row_nums]</pre>
```

```
predictions <- predict(reduced_model, newdata = df[candy_row_nums,])
residual_error <- abs(actual_values - predictions)</pre>
```

```
results <- data.frame(
   Candy = df$competitorname[candy_row_nums],
   Predicted = round(predictions,2),
   Actual = round(actual_values,2),
   Residual = round(residual_error,2)
)
print(results)</pre>
```

```
##
                          Candy Predicted Actual Residual
## 6
                     Almond Joy
                                     66.84
                                            50.35
                                                     16.49
## 9
                     Candy Corn
                                     35.79
                                            38.01
                                                      2.22
## 53 ReeseÕs Peanut Butter cup
                                     66.84
                                            84.18
                                                     17.34
## 65
                                            76.67
                                                      9.84
                       Snickers
                                     66.84
```

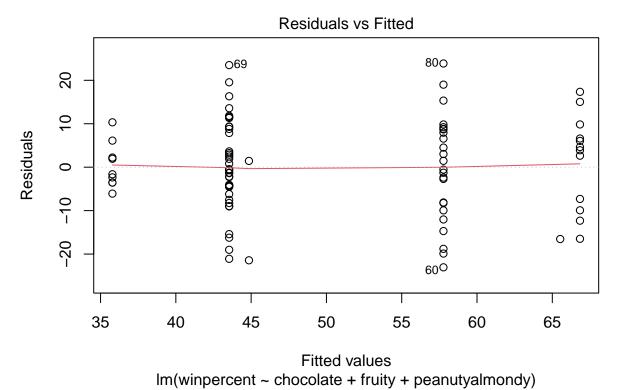
The predictions for the win percentages of Reese's Peanut Butter Cup, Snickers, and Almond Joy were all around 66.84%, with Candy Corn having a prediction of 35.78%. However, the actual win percentages varied for each candy:

Reese's Peanut Butter Cup had an actual win percentage of 84.18%. Snickers had an actual win percentage of 76.67%. Almond Joy had an actual win percentage of 50.35%. Candy Corn had an actual win percentage of 38.01%. The residuals, which represent the difference between the actual values and the predicted values, are as follows:

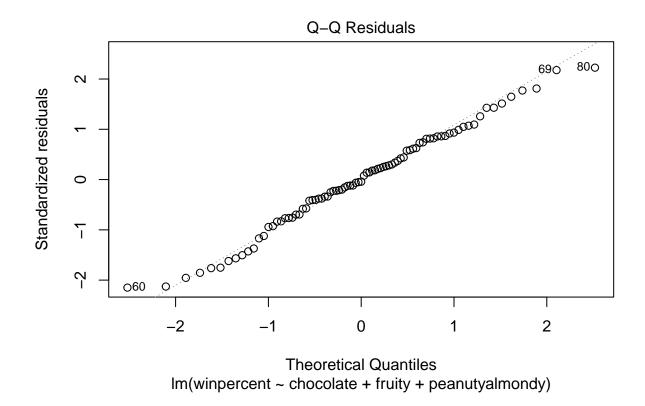
Reese's Peanut Butter Cup: 17.34 Snickers: 9.84 Almond Joy: 17.34 Candy Corn: 2.22

These residuals indicate that the model under-predicted the win percentages for all candies, particularly for Reese's Peanut Butter Cup and Almond Joy, where the predicted values were considerably lower than the actual values. Candy Corn had the smallest residual error, meaning the model's prediction was closer to its actual value.

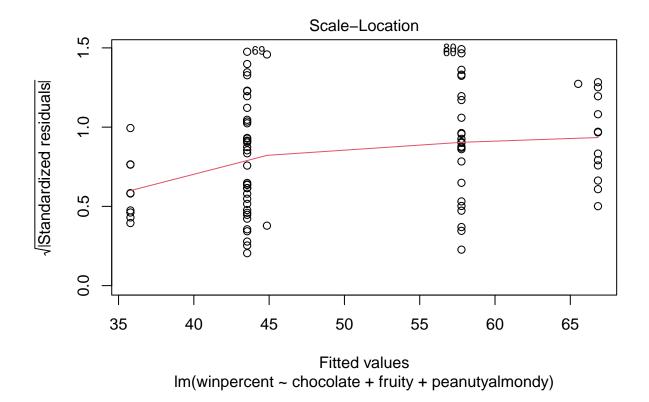
```
plot(reduced_model, which = 1)
```



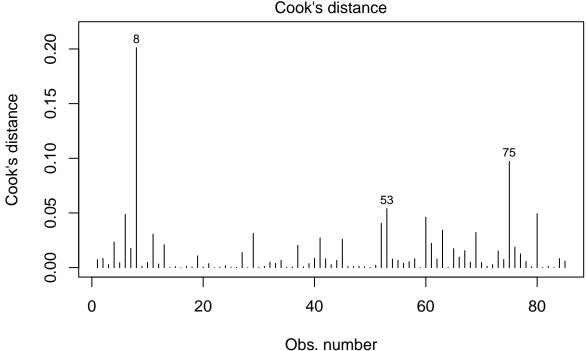
plot(reduced\_model, which = 2)



plot(reduced\_model, which = 3)



plot(reduced\_model, which = 4)



Im(winpercent ~ chocolate + fruity + peanutyalmondy)

vif(reduced\_model)

## chocolate fruity peanutyalmondy ## 2.262878 2.307766 1.211022

The VIF values in the output assess the level of multicollinearity in the reduced model. Specifically:

Chocolate: 2.262878 Fruity: 2.307766 Peanutyalmondy: 1.211022

In our model, we calculated the Variance Inflation Factor (VIF) for the variables chocolate, fruity, and peanutyalmondy. The VIF values we found are all below 5, which is the generally accepted threshold for multicollinearity. This means that while there may be some correlation between these variables and others in the model, it is low enough that it doesn't pose a problem.

Because the VIF values are low (with values of around 2 for chocolate and fruity, and 1.2 for peanutyalmondy), we can confidently say that multicollinearity is not a concern in our model. In other words, the variables are relatively independent of each other, which means they won't cause inflated standard errors or distort the results. This allows us to trust the estimates of the regression coefficients for these variables without worrying that they're being affected by strong correlations with other predictors.

 $\label{eq:bolden} \mbox{Ho: B\_chocolate} = \mbox{B\_fruity} = \mbox{B\_peanutyalmondy} = 0 \mbox{ Ha: B\_chocolate} \mbox{!= B\_fruity} \mbox{!= B\_peanutyalmondy} \\ \mbox{!= 0}$ 

Conclusion: Since the p-values for chocolate (3.34e-08), fruity (0.0354), and peanutyalmondy (0.0118) are all less than the significance level of 0.05, we reject the null hypothesis. This means that all three predictors are significantly related to the winpercent of candy.

Interpretation of the p-value: The p-values for each variable indicate the probability of observing the data, or something more extreme, assuming the null hypothesis is true. For chocolate, the p-value is extremely small (3.34e-08), indicating very strong evidence against the null hypothesis and suggesting that chocolate has a significant positive effect on the winpercent. The p-values for fruity (0.0354) and peanutyalmondy (0.0118) are also below the 0.05 threshold, indicating that these variables also significantly impact the winpercent, though with slightly less strength than chocolate. Therefore, at the 5% significance level, we conclude that these predictors have a statistically significant effect on the winpercent.