## Natural Language Processing with Deep Learning



Lecture 7 — Recurrent neural networks and encoder-decoder architectures

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#### **Motivation**

Language data – working with sequences (of tokens, characters, etc.)

MLP – fixed input vector size

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MLP – fixed input vector size

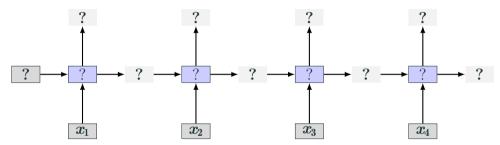
How we dealt with it

- Vector concatenation
- Vector addition/averaging (CBOW)
- Limiting context (e.g., Markov property)

What we want to really work with: Sequence of inputs, fixed-size output(s)



## Our goal would be to build something like this



Example for 4 input tokens

## Recurrent Neural Networks (RNN) abstraction

- 1 Recurrent Neural Networks (RNN) abstraction
- 2 RNN architectures
- 3 Encoder-decoder architectures



#### **RNN** abstraction

We have a sequence of n input vectors  $x_{1:n} = x_1, \ldots, x_n$ 

Each input vector has the same dimension  $d_{in}: oldsymbol{x_i} \in \mathbb{R}^{d_{in}}$ 

What might  $x_i$  contain?

 $lue{}$  Typically a word embedding of token i, but could be any arbitrary input, e.g., one-hot encoding of token i

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We have a single **output**  $d_{out}$ -dimensional vector  $\mathbf{u}_n \in \mathbb{R}^{d_{out}}$ 

RNN is a function from input to output

$$y_n = \text{RNN}(x_{1:n})$$

## RNN in fact returns a sequence of outputs

RNN definition:  $y_n = \text{RNN}(x_{1:n})$ 

Let's have n = 3, so our input sequence is  $x_1, x_2, x_3$ :

$$\mathbf{y_2} = \mathrm{RNN}(\mathbf{\mathit{x}}_1, \mathbf{\mathit{x}}_2, \mathbf{\mathit{x}}_3)$$

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Let's have n=3, so our input sequence is  $x_1, x_2, x_3$ :

$$oldsymbol{y_2} = ext{RNN}(oldsymbol{x_1}, oldsymbol{x_2}, oldsymbol{x_3})$$

But our input sequence also contains  $x_1, x_2$ , so:

$$y_2 = \text{RNN}(x_1, x_2)$$

Which makes RNN outputting a vector  $u_i \in \mathbb{R}^{d_{out}}$  at each position  $i \in (1, \ldots, n)$ 

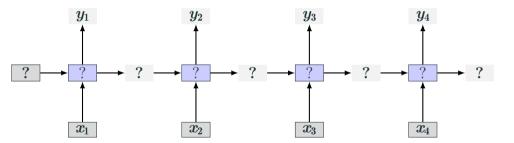
Let's call this sequence-outputting function RNN\*:

$$y_{1:n} = \operatorname{RNN}^*(x_{1:n})$$





## Adding outputs to our sketch



For a sequence of input vectors  $x_{1:i}$ 

$$y_i = \text{RNN}(x_{1:i})$$
  $y_{1:n} = \text{RNN}^*(x_{1:n})$ 

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Without knowing what RNN actually is, what are the advantages?

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Each output  $y_i$  takes into account the entire history  $x_{i,i}$ without Markov property

What to do with  $y_n$  or  $y_{1:n}$ ?

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What to do with  $y_n$  or  $y_{1:n}$ ?

■ Use for further prediction, e.g., plug into softmax, MLP, etc.



## **Underlying mechanism of RNNs — states**

For "passing information" from one position to the next, i.e. from

$$y_i = \text{RNN}(x_{1:i})$$

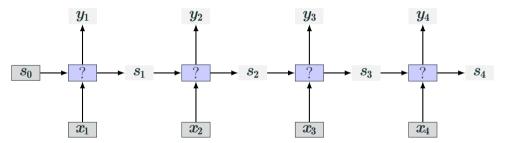
to

$$y_{i+1} = \text{RNN}(x_{1:i+1})$$

we use a "state" vector

$$oldsymbol{s_i} \in \mathbb{R}^{d_{state}}$$

## **Adding state vectors**



## Define RNN recursively — Computing current state

At each step  $i \in (1, ..., n)$  we have

- $\blacksquare$  Current input vector  $x_i$
- Vector of the previous state  $s_{i-1}^1$

and compute

Current state  $s_i$ 

$$s_i = R(s_{i-1}, x_i)$$
 (we will specify  $R$  later)

Initial state vector  $s_0$  — often omitted, assumed to be zero-filled

## Define RNN recursively — Computing current output

At each step  $i \in (1, ..., n)$  we have

- $\blacksquare$  Current input vector  $x_i$
- Vector of the previous state  $s_{i-1}$

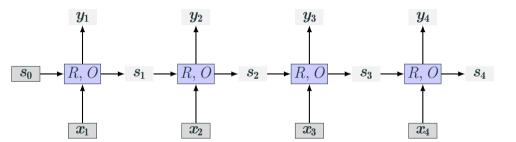
#### and compute

- $\blacksquare$  Current state  $s_i = R(s_{i-1}, x_i)$
- $\blacksquare$  Current output  $y_i$

$$y_i = O(s_i)$$
 (we will specify  $O$  later)

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## Adding R and O



## Summary

At each step  $i \in (1, ..., n)$  we have

 $\blacksquare$  Current input  $x_i$  and previous state  $s_{i-1}$ 

and compute

$$lacksquare s_i = R(s_{i-1}, x_i) ext{ and } y_i = O(s_i)$$

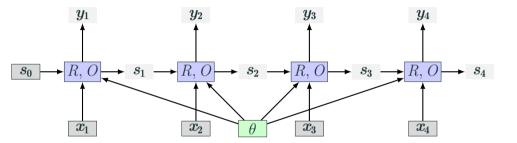
The functions R and O are the same for each position i

#### **RNN**

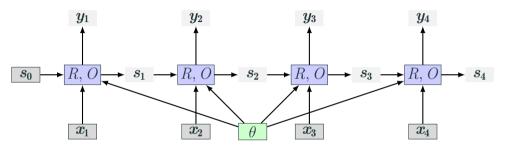
$$y_{1:n} = \text{RNN}^*(x_{1:n}, s_0)$$
  $s_i = R(s_{i-1}, x_i)$   $y_i = O(s_i)$ 

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## **Graphical visualization of abstract RNN (unrolled)**

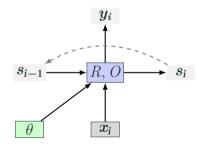


## **Graphical visualization of abstract RNN (unrolled)**



Note that  $\theta$  (parameters) are "shared" (the same) for all positions

## **Graphical visualization of abstract RNN (recursive)**

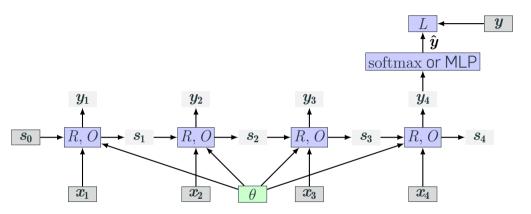




## Recurrent Neural Networks (RNN) abstraction

RNN as 'acceptor' or 'encoder'

## Supervision on the last output

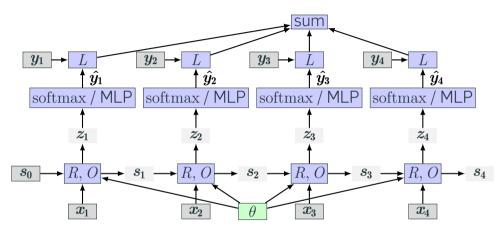


The loss is computed on the final output (e.g., directly on  $y_n$ or by putting  $y_n$  through MLP)

# Recurrent Neural Networks (RNN) abstraction

RNN as 'transducer'

## Supervision on each output



For sequence tagging — loss on each position, overall network's loss simply as a sum of losses



#### Bi-directional RNNs

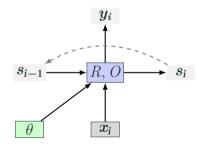
Simple idea: Run one RNN from left-to-right (forward, f) and another RNN from right-to-left (backward, b), and concatenate

$$\mathrm{biRNN}(\boldsymbol{x_{1:i}},i) = \boldsymbol{y_i} = [\mathrm{RNN}(\boldsymbol{x_{1:i}}); \mathrm{RNN}_b(\boldsymbol{x_{n:i}})]$$

Both for encoder (concatenate the last outputs) and transducer (concatenate each step's output)

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## But what is happening 'inside' R and O?



## **RNN** architectures

- RNN architectures

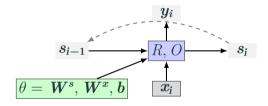
RNNs and encoder-decoder architectures



## **RNN** architectures

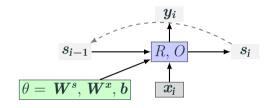
Simple RNN

## Elman Network or Simple-RNN (S-RNN)



$$s_i = R(x_i, s_{i-1}) = g(s_{i-1} W^s + x_i W^x + b)$$
  
 $y_i = O(s_i) = s_i$ 

## Elman Network or Simple-RNN (S-RNN)

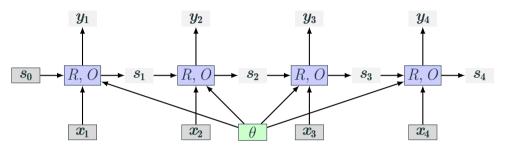


$$s_i = R(x_i, s_{i-1}) = g(s_{i-1} W^s + x_i W^x + b)$$
  
 $y_i = O(s_i) = s_i$ 

$$oldsymbol{s_i, y_i} \in \mathbb{R}^d_s \quad oldsymbol{x_i} \in \mathbb{R}^d_{in} \quad oldsymbol{W^x} \in \mathbb{R}^{d_{in} imes d_s} \quad oldsymbol{W^s} \in \mathbb{R}^{d_s imes d_s} \quad oldsymbol{b} \in \mathbb{R}^{d_s}$$

 $g-{\sf commonly}$  tanh or ReLU

## Elman Network and vanishing gradient



Gradients might vanish  $(\rightarrow 0)$  as they propagate back through the computation graph

- Severe in deeper nets, especially in recurrent networks
- Hard for the S-RNN to capture long-range dependencies



## **RNN** architectures

**Gated architectures** 

## RNN as a general purpose computing device

State  $s_i$  represents a finite memory

#### Recall: Simple RNN

 $s_i = R(x_i, s_{i-1}) = g(s_{i-1} W^s + x_i W^x + b)$ 

# RNN as a general purpose computing device

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#### Recall: Simple RNN

$$s_i = R(x_i, s_{i-1}) = g(s_{i-1} W^s + x_i W^x + b)$$

Each application of function R

- Reads the current memory  $s_{i-1}$
- Reads the current input  $x_i$
- Operates on them in some way

RNNs and encoder-decoder architectures

■ Writes the result to the memory  $s_i$ 

# RNN as a general purpose computing device

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- Operates on them in some way
- Writes the result to the memory  $s_i$

Memory access not controlled: At each step, entire memory state is read, and entire memory state is written

Memory vector  $\boldsymbol{s} \in \mathbb{R}^d$  and input vector  $\boldsymbol{x} \in \mathbb{R}^d$ 

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Let's have a binary vector ("gate")  $\mathbf{g} \in \{0, 1\}^d$ 

Memory vector  $\boldsymbol{s} \in \mathbb{R}^d$  and input vector  $\boldsymbol{x} \in \mathbb{R}^d$ 

Let's have a binary vector ("gate")  $\mathbf{q} \in \{0,1\}^d$ 

#### Hadamard-product $z=u\odot v$

Fancy name for element-wise multiplication  $z_{[i]} = u_{[i]} \cdot v_{[i]}$ 

$$s' \leftarrow g \odot x + (1+g) \odot s$$

Memory vector  $oldsymbol{s} \in \mathbb{R}^d$  and input vector  $oldsymbol{x} \in \mathbb{R}^d$ 

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Reads the entries in x corresponding to ones in the gate, writes them to the memory

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$$s' \leftarrow g \odot x + (1+g) \odot s$$

- Reads the entries in x corresponding to ones in the gate, writes them to the memory
- Remaining locations are copied from the memory
- Note that the operation + here is modulo 2

### Gate example

Updating memory position 2

$$\begin{pmatrix} 8 \\ 11 \\ 3 \end{pmatrix} \leftarrow \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \odot \begin{pmatrix} 10 \\ 11 \\ 12 \end{pmatrix} + \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \odot \begin{pmatrix} 8 \\ 9 \\ 3 \end{pmatrix}$$

$$s' \leftarrow g \odot \qquad x + (1+g) \odot \qquad s$$

### Gate example

Updating memory position 2

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s' \leftarrow g \odot \qquad x + (1 + g) \odot \qquad s$$

Could be used for gates in RNNs! But:

- Our gates are not learnable
- Our hard-gates are not differentiable

Solution: Replace with 'soft' gates

### **RNN** architectures

**LSTM** 

Designed to solve the vanishing gradients problem, first to introduce the gating mechanism



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LSTM splits the state vector  $s_i$  exactly in two halves

- One half is treated as 'memory cells'
- The other half is 'working memory'

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### Memory cells

- Designed to preserve the memory, and also the error aradients, across time
- Controlled through differentiable gating components smooth functions that simulate logical gates





The state at time j is composed of two vectors:

- $\mathbf{c}_{j}$  the memory component
- lacksquare  $h_j$  the hidden state component

The state at time i is composed of two vectors:

- $c_i$  the memory component
- $h_i$  the hidden state component

At each input state i, a gate decides how much of the new input should be written to the memory cell, and how much of the memory cell should be forgotten

The state at time i is composed of two vectors:

- $c_i$  the memory component
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There are three gates

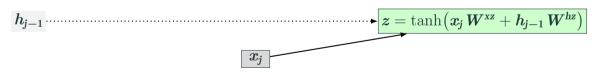
- *i* input gate
- **f** − forget gate
- o output gate

 $c_{j-1}$ 

 $h_{j-1}$ 

 $x_j$ 

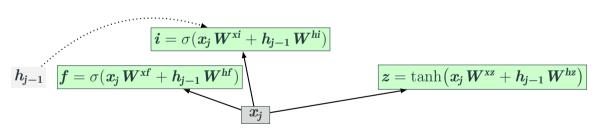
 $c_{i-1}$ 



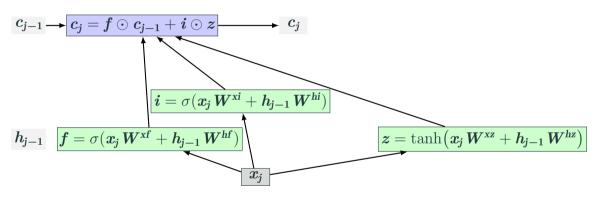
 $c_{j-1}$ 

$$h_{j-1} ildar f = \sigma(x_j W^{xf} + h_{j-1} W^{hf})$$
  $z = anh(x_j W^{xz} + h_{j-1} W^{hz})$ 

 $c_{j-1}$ 

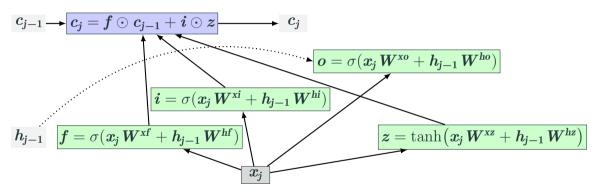






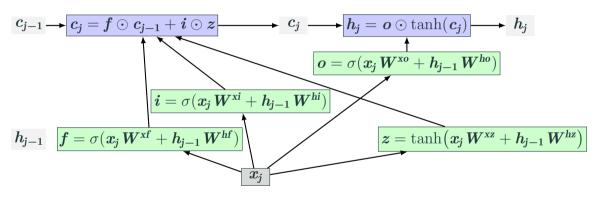




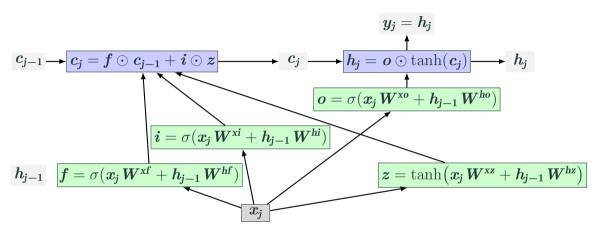














## LSTM parameters and dimensions

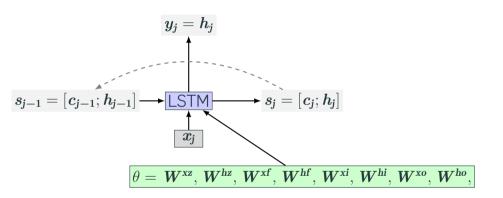
RNNs and encoder-decoder architectures

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$$egin{aligned} x_j \in \mathbb{R}^{d_{in}} & c_j, h_j, y_j, i, f, o, z \in \mathbb{R}^{d_h} & W^{x\star} \in \mathbb{R}^{d_{in} imes d_h} & W^{h\star} \in \mathbb{R}^{d_h imes d_h} \ d_h - ext{dimensionality of LSTM ('hidden' layer)} & y_j = h_j \ & & & & & & & & \\ \hline c_{j-1} & & & & & & & & \\ \hline c_{j-1} & & & & & & & \\ \hline c_j & & & & & & & \\ \hline c_j & & & & & & \\ \hline c_j & & & & & & \\ \hline c_j & & & \\ c_j & & & \\ \hline c_j & & & \\ c_j & & & \\ \hline c_j & & & \\ c_j & & & \\ \hline c_j & & & \\ c_j & & & \\ \hline c_j & & &$$

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### LSTM as a 'layer'



We also ignored bias terms for each gate

# Recap

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### **Encoder-decoder architectures**

- Encoder-decoder architectures



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We also have a **sequence** of  $d_{out}$ -dimensional vector  $y_{1:\hat{n}} \in \mathbb{R}^{\hat{n} \times d_{out}}$  outputs

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RNNs produce a sequence of outputs

RNNs and encoder-decoder architectures

$$y_{1:n} = \text{RNN}(x_{1:n})$$

What are we missing?

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What are we missing?

The input and output sequence: rarely of same length

**Translate to German**: I like attending deep learning lectures

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**Output**: Ich besuche gerne Deep-Learning-Vorlesungen



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Current approach:

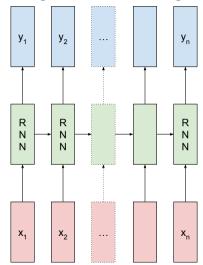
- Tokenize input sequence
- 2 Obtain a word embedding (e.g. word2vec) for each token
- 3 Use a RNN (e.g. LSTM) to encode sequence of tokens
- 4 Generate token sequence in target language

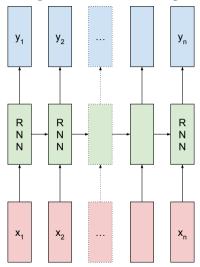
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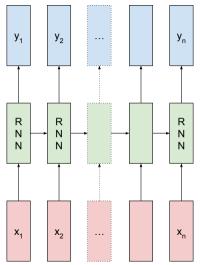
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- 4 Generate token sequence in target language
  - Multi-class classification over target vocabulary



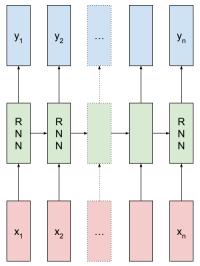


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- We don't have to stop generating after the last input
- 2 We can only consider outputs up to a special "end token"

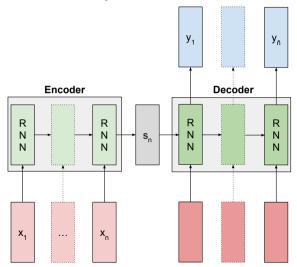


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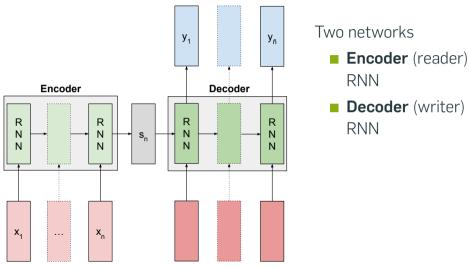
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Neither ideal

#### Sequence-to-sequence models

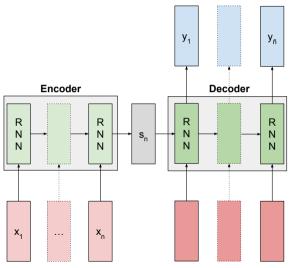


#### Sequence-to-sequence models





#### Sequence-to-sequence models



Two networks

- Encoder (reader) RNN
- **Decoder** (writer) RNN

#### Note:

Encoder and decoder haveseparate params





1 How to **initialize** decoder hidden **state**?



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  - $lackbox{$\blacksquare$} h_0^{dec} = h_n^{enc}$ : simply copy the last encoder state
  - lacksquare  $h_0^{dec} = \mathsf{NN}_{\theta}(h_n^{enc})$ : transform the last encoder state

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- **2** When do we **stop generating** with the decoder?

- 1 How to **initialize** decoder hidden **state**?

  - $h_0^{dec} = NN_\theta(h_n^{enc})$ : transform the last encoder state
- 2 When do we **stop generating** with the decoder?
  - We use a **special token** (<EOS>, \n) to indicate the end-of-sequence
  - When the **maximum generation length** is exceeded

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- 2 When do we **stop generating** with the decoder?
  - We use a **special token** (<EOS>, \n) to indicate the end-of-sequence
  - When the maximum generation length is exceeded
- **3** What are the **inputs** of the decoder?

- 1 How to **initialize** decoder hidden **state**?

  - $h_0^{dec} = NN_\theta(h_n^{enc})$ : transform the last encoder state
- 2 When do we **stop generating** with the decoder?
  - We use a **special token** (<EOS>, \n) to indicate the end-of-sequence
  - When the **maximum generation length** is exceeded
- **3** What are the **inputs** of the decoder?
  - The **previous output** of the decoder
    - Teacher forcing (with probability p): use the **correct output**



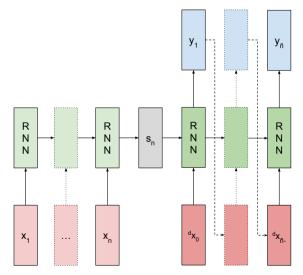
- 1 How to **initialize** decoder hidden **state**?
  - $lackbox{ } h_0^{dec} = h_n^{enc}$ : simply copy the last encoder state
  - $\blacksquare h_0^{dec} = \mathsf{NN}_{\theta}(h_n^{enc})$ : transform the last encoder state
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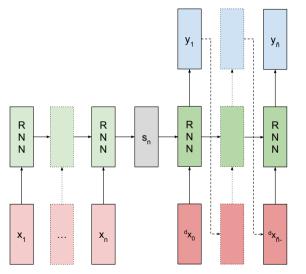
- How to **initialize** decoder hidden **state**?
  - $h_0^{dec} = h_n^{enc}$ : simply copy the last encoder state
  - $h_{\theta}^{dec} = NN_{\theta}(h_{\eta}^{enc})$ : transform the last encoder state
- 2 When do we **stop generating** with the decoder?
  - We use a **special token** (<EOS>, \n) to indicate the end-of-sequence
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- 3 What are the **inputs** of the decoder?
  - The **previous output** of the decoder
    - $\blacksquare$  Teacher forcing (with probability p): use the **correct** output
  - What is the **initial input**  $x_0^{dec}$ ?
    - A beginning-of-sequence **special token** (<BOS>)



#### The encoder-decoder architecture



#### The encoder-decoder architecture



Decoder inputs

- $x_0^{dec} = < BOS >$
- $x_i^{dec} = y_i^{dec}$  if no teacher forcing
- $\mathbf{x}_i^{dec} = \hat{y}_i$  if we use teacher forcing

#### Take aways

- RNNs for arbitrary long input
- Encoding the entire sequence and/or each step
- Modeling freedom with bi-directional RNNs
- Vanishing gradients in deep nets gating mechanism. memory cells
- LSTM a particularly powerful RNN
- Encoder-decoder RNNs for text-to-text tasks



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