Natural Language Processing with Deep Learning



Lecture 6 — Neural language models and learning word embeddings

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www.trusthlt.org

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Ruhr University Bochum & Research Center Trustworthy Data Science and Security





Motivation

I give you a large corpus of plain text data

Can you build a model that will answer any of the 'word analogy' tasks?

- 'Germany to Berlin is like France to?'
- 'Man to king is like woman to?'



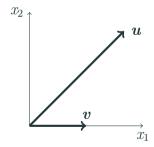
We need to talk about the dot product first

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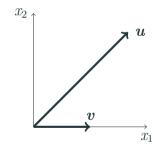
For two n-dimensional vectors ${m u}$ and ${m v}$



For two n-dimensional vectors \boldsymbol{u} and \boldsymbol{v}

Algebraic

$$oldsymbol{u}\cdotoldsymbol{v} = \sum_{i=1}^n oldsymbol{u}_{[i]}oldsymbol{v}_{[i]}$$



For two n-dimensional vectors \boldsymbol{u} and \boldsymbol{v}

Algebraic $oldsymbol{u} \cdot oldsymbol{v} = \sum_{i=1}^n oldsymbol{u}_{[i]} oldsymbol{v}_{[i]}$

u

Geometric

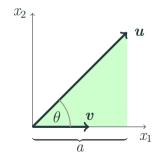
$$\boldsymbol{u} \cdot \boldsymbol{v} = \|\boldsymbol{u}\| \|\boldsymbol{v}\| \cos(\theta)$$

 x_1

For two *n*-dimensional vectors \boldsymbol{u} and \boldsymbol{v}

Algebraic

$$oldsymbol{u}\cdotoldsymbol{v}=\sum_{i=1}^noldsymbol{u}_{[i]}oldsymbol{v}_{[i]}$$



Geometric

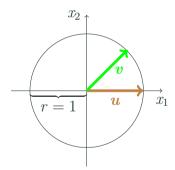
$$\boldsymbol{u} \cdot \boldsymbol{v} = \|\boldsymbol{u}\| \|\boldsymbol{v}\| \cos(\theta)$$

Scalar projection:

$$\implies a = \frac{\boldsymbol{u} \cdot \boldsymbol{v}}{\|\boldsymbol{v}\|}$$

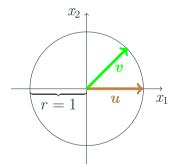


For unit vectors u, v:



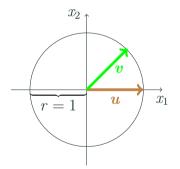
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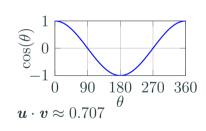


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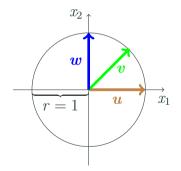


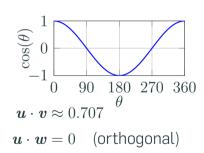
Neural LMs and learning word embeddings



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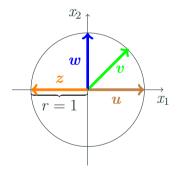
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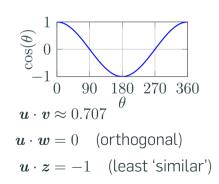


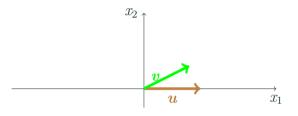


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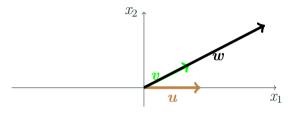
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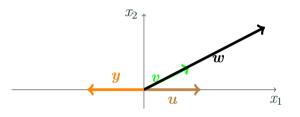




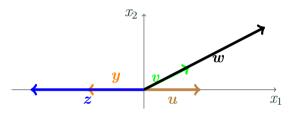
 $\boldsymbol{u} \cdot \boldsymbol{v} > 0$



$$\boldsymbol{u} \cdot \boldsymbol{w} > \boldsymbol{u} \cdot \boldsymbol{v} > 0$$

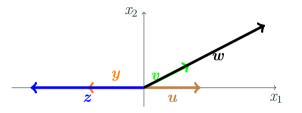


 $\boldsymbol{u} \cdot \boldsymbol{w} > \boldsymbol{u} \cdot \boldsymbol{v} > 0 > \boldsymbol{u} \cdot \boldsymbol{y}$



$$\boldsymbol{u} \cdot \boldsymbol{w} > \boldsymbol{u} \cdot \boldsymbol{v} > 0 > \boldsymbol{u} \cdot \boldsymbol{y} > \boldsymbol{u} \cdot \boldsymbol{z}$$

Dot product ($u \cdot v = ||u|| ||v|| \cos(\theta)$) is unbounded in \mathbb{R}



$$u \cdot w > u \cdot v > 0 > u \cdot y > u \cdot z$$

Isn't it somehow related to Euclidean distance?

Dot product vs. Euclidean distance $\|m{u}-m{v}\|_2 = \sqrt{\sum_{i=1}^n ig(m{u}_{[i]}-m{v}_{[i]}ig)^2}$

Let's take the square of the Euclidean distance

$$\left(\left\|oldsymbol{u}-oldsymbol{v}
ight\|_{2}
ight)^{2}=\sum_{i=1}^{n}\left(oldsymbol{u}_{[i]}-oldsymbol{v}_{[i]}
ight)^{2}=\sum_{i=1}^{n}\left(oldsymbol{u}_{[i]}-oldsymbol{v}_{[i]}
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Dot product vs. Euclidean distance $\|m{u}-m{v}\|_2 = \sqrt{\sum_{i=1}^n ig(m{u}_{[i]}-m{v}_{[i]}ig)^2}$

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Dot product vs. Euclidean distance $\|m{u}-m{v}\|_2 = \sqrt{\sum_{i=1}^n ig(m{u}_{[i]}-m{v}_{[i]}ig)^2}$ Conceptual difference: if the

Let's take the square of the Euclidean distance

$$= \sum_{i=1}^{n} \left(\boldsymbol{u}_{[i]} \boldsymbol{u}_{[i]} + \boldsymbol{v}_{[i]} \boldsymbol{v}_{[i]} - 2 \boldsymbol{u}_{[i]} \boldsymbol{v}_{[i]} \right)$$

$$= \sum_{i=1}^{n} \boldsymbol{u}_{[i]} \boldsymbol{u}_{[i]} + \sum_{i=1}^{n} \boldsymbol{v}_{[i]} \boldsymbol{v}_{[i]} - 2 \sum_{i=1}^{n} \boldsymbol{u}_{[i]} \boldsymbol{v}_{[i]}$$

$$= \boldsymbol{u} \cdot \boldsymbol{u} + \boldsymbol{v} \cdot \boldsymbol{v} - 2 \boldsymbol{u} \cdot \boldsymbol{v} \qquad (= 2 - 2 \boldsymbol{u} \cdot \boldsymbol{v} \text{ for unit vectors})$$

$$\rightarrow \text{Minimizing (square) euclidean distance is proportional to$$

 $\left(\left\|oldsymbol{u}-oldsymbol{v}
ight\|_{2}
ight)^{2}=\sum_{i}^{n}\left(oldsymbol{u}_{[i]}-oldsymbol{v}_{[i]}
ight)^{2}=\sum_{i}^{n}\left(oldsymbol{u}_{[i]}-oldsymbol{v}_{[i]}
ight)\left(oldsymbol{u}_{[i]}-oldsymbol{v}_{[i]}
ight)$

changes, but the distances remains the same

origin shifts, the dot product

→ Minimizing (square) euclidean distance is proportional to maximizing cosine similarity (equivalent for unit vectors)



Language modeling revisited

- Language modeling revisited



Recap: What was the task of a language model again?

LM as a conditional probability predictor

Given a sequence of k words, return a probability distribution over V (the vocabulary) for the next possible word

In detail, compute

$$\Pr(W_{k+1} = v \mid W_1, W_2, \dots, W_k)$$

for all possible words v from vocabulary V



Example

So I was at this party at Joe's place last night, but man I was so tired, so like at about midnight I said, Joe, I am

$$\Pr(W_{k+1} = v \mid W_1 = \text{`So'}, W_2 = \text{'I'}, \dots, W_k = \text{`am'})$$

Higher Pr:

- leaving
- out
- calling (it a night)
- qonna (head home)

Lower Pri

- hungry
- in (love)
- . . .



LM looks like... a text classification task?!

Text classification

Given a text,* predict its label from a set of arbitrarily ordered items (classes such as {sports, politics, travel}). We model cond. probability for each label (a probability distribution over all the classes), for example by softmax.

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LM looks like... a text classification task?!

Text classification

Given a text,* predict its label from a set of arbitrarily ordered items (classes such as {sports, politics, travel}). We model cond. probability for each label (a probability distribution over all the classes), for example by softmax.

* We already know how to turn text into a feature vector, e.g., by bag of words

LM

Given a text,* predict the next word from a set of arbitrarily ordered items (the vocabulary). We model cond. probability for each word (a probability distribution over the entire vocabulary), for example by softmax.

Neural LMs and learning word embeddings

Language modeling revisited

Neural language models

Neural LMs

LM as 'text classification' again

Given a text,* predict **the next word** from a set of arbitrarily ordered items (**the vocabulary**). We model cond. probability for each **word** (a probability distribution over **the entire vocabulary**), for example by softmax.

Let's build a neural network to solve this task

Neural LMs

LM as 'text classification' again

Given a text,* predict the next word from a set of arbitrarily ordered items (the vocabulary). We model cond. probability for each word (a probability distribution over the entire vocabulary), for example by softmax.

Let's build a neural network to solve this task

- Input: a k-gram of words $w_{1:k}$
- Desired output: a conditional probability distribution over the vocabulary V for the next word w_{k+1}



Embedding layer

If the input are symbolic categorical features

e.g., words from a closed vocabulary

it is common to associate each possible feature value

i.e., each word in the vocabulary

with a d-dimensional vector for some d

These vectors are also parameters of the model, and are trained jointly with the other parameters

Embedding layer: Lookup operation

Mapping from a symbolic feature such as word-number-48 to d-dimensional vectors is performed by an embedding layer (a lookup layer)

The parameters in an embedding layer is a matrix $E^{|V| \times d}$. each row corresponds to a different word in the vocabulary

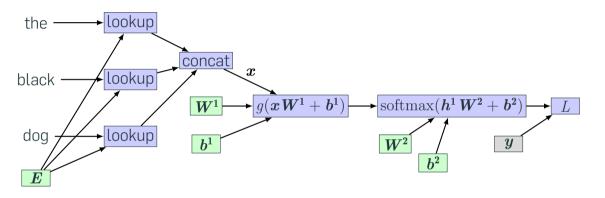
The lookup operation is then indexing v(w), e.g.,

$$v(w) = v_{48} = \mathbf{E}_{[48,:]}$$

If the symbolic feature is a one-hot vector x, the lookup operation can be implemented as the multiplication xE

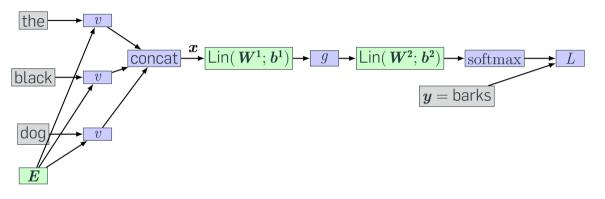


Network concatenating 3 words as embeddings ($d_w = 50$)



Each word $\in \mathbb{R}^{|V|}$ (one hot), $\boldsymbol{E} \in \mathbb{R}^{|V| \times 50}$, each lookup output $\mathbf{x} \in \mathbb{R}^{50}$, concat output $\mathbf{x} \in \mathbb{R}^{150}$

Simplify notation: Lookup as v, linear layer with params



the, black, dog, $oldsymbol{y}$ = one-hot encoding, $\mathbb{R}^{|V|}$

Loss L and gold label y — only for training



Training neural LMs

Where to get training examples?

Training examples are simply word k-grams from an unlabeled corpus

- Identities of the first k-1 words are used as features.
- The last word is used as the target label for the classification

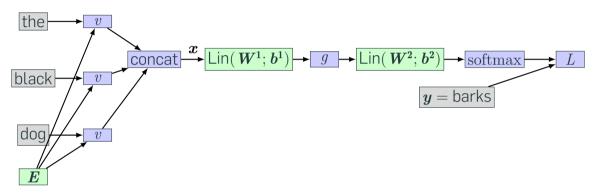
The model is trained using cross-entropy loss

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Some advantages of neural LMs

 \approx linear increase in parameters with k+1 (better than 'classical' LMs)

Learned word representations as a by-product



Each row of *E* learns a word representation



Learning word embeddings

- Learning word embeddings



Learning word embeddings

Distributional hypothesis

Recall: One-hot encoding of words

Major drawbacks?

■ No 'semantic' similarity, all words are equally 'similar'

Example (see Lecture 3 for more)

$$V = \begin{pmatrix} \mathsf{a}_1 & \mathsf{abandon}_2 & \dots & \mathsf{zone}_{2,999} & \mathsf{zoo}_{3,000} \end{pmatrix}$$

nice =
$$\begin{pmatrix} 0_1 & \dots & 1_{1,852} & \dots & 0_{2,999} & 0_{3,000} \end{pmatrix}$$

pleasant = $\begin{pmatrix} 0_1 & \dots & 1_{2,012} & \dots & 0_{2,999} & 0_{3,000} \end{pmatrix}$

horrible =
$$\begin{pmatrix} 0_1 & \dots & 1_{696} & \dots & 0_{2,999} & 0_{3,000} \end{pmatrix}$$

Distributional hypothesis

The distributional hypothesis stating that words are similar if they appear in similar contexts

Example

Intuitively, when we encounter a sentence with an unknown word such as the word **wampinuk** in

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Example

Intuitively, when we encounter a sentence with an unknown word such as the word wampinuk in

Marco saw a hairy little wampinuk crouching behind a tree

We infer the meaning of the word based on the context in which it occurs

From neural LMs to training word embeddings

- From neural LMs to training word embeddings





From neural language models to training word embeddings

(Neural) language model's goal: Predict probability distribution over $|{\it V}|$ for the next word conditioned on the previous words

Side product: Can learn useful word embeddings

From neural language models to training word embeddings

(Neural) language model's goal: Predict probability distribution over |V| for the next word conditioned on the previous words

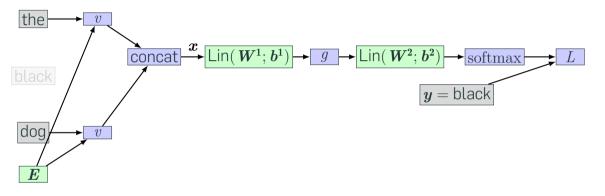
Side product: Can learn useful word embeddings

What if we don't need probability distribution but just want to learn word embeddings?

- We can relax our Markov assumption of 'look at kprevious words only'
- We can get rid of the costly normalization in softmax



Simplification 1: Ditch the Markov property — look into the future!



For example, instead of modeling $Pr(w_3|w_1, w_2, \square)$, we model $\Pr(w_2|w_1, \square, w_3)$

Simplification 2: Give up the costly probability distribution

Instead of predicting probability distribution over the entire vocabulary, we just want to predict some score of context and target word

What could such a score be?

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Instead of predicting probability distribution over the entire vocabulary, we just want to predict some score of context and target word

What could such a score be?

Prefer words in their true contexts (high score)

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Simplification 2: Give up the costly probability distribution

Instead of predicting probability distribution over the entire vocabulary, we just want to predict some score of context and target word

What could such a score be?

- Prefer words in their true contexts (high score)
- Penalize words in their 'untrue' contexts (low score)

Negative sampling

Instead of predicting probability distribution for the target word, we **create an artificial binary task** by choosing either the correct or a random incorrect target word

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Instead of predicting probability distribution for the target word, we **create an artificial binary task** by choosing either the correct or a random incorrect target word

$$y = \begin{cases} 1 & \text{if } (w, c_{1:k}) \text{ is a positive example from the corpus} \\ 0 & \text{if } (w', c_{1:k}) \text{ is a negative example from the corpus} \end{cases}$$

Negative sampling

Instead of predicting probability distribution for the target word, we **create an artificial binary task** by choosing either the correct or a random incorrect target word

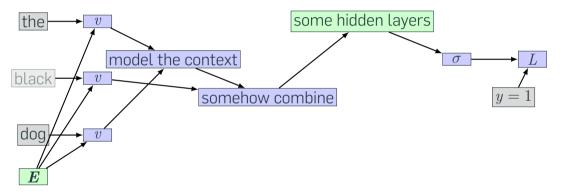
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Which distribution for sampling w' from V?

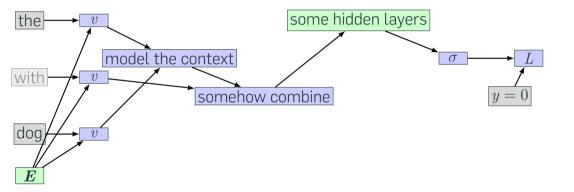
- Corpus-based frequency: $\frac{\#(v)}{\sum_{v' \in V} \#(v')}$ (pr. of each word v)
 Re-weighted: $\frac{\#(v)^{0.75}}{\sum_{v' \in V} \#(v')^{0.75}}$ (more weight on less
- frequent words done in word2vec)



Turn the problem into binary classification (positive example)



Turn the problem into binary classification (negative example)



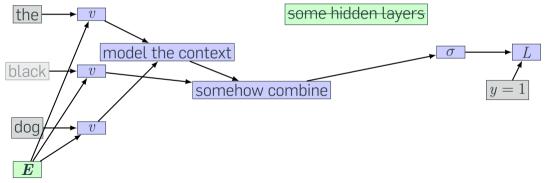
word2vec

- word2vec



word2vec

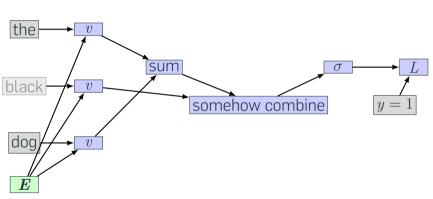
word2vec simplifies the neural LM by removing the hidden layer (so turning it into a log-linear model!)



word2vec — how to model the context?



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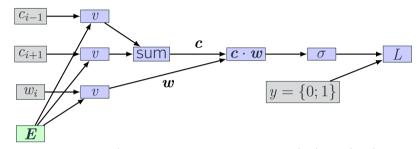


T. Mikolov, K. Chen, G. Corrado, and J. Dean (2013). "Efficient estimation of word representations in vector space". In: 1st International Conference on Learning Representations ICLR, Workshop Track Proceedings. Ed. by Y. Bengio and Y. LeCun, pp. 1–12

Variant 1: Continuous bag of words (CBOW) $oldsymbol{c} = \sum_{i=1}^k v(c_i)$



Final CBOW word2vec — similarity score is the dot product



 w_i — target word, c_{i-1} , c_{i+1} — context words (one-hot)

y=1 for correct word-context pairs, y=0 for random w_i

The only learnable parameter is the embedding matrix $m{E}$

What is $\sigma(\mathbf{c} \cdot \mathbf{w})$ doing?

word2vec: Learning useful word embeddings

Train the network to distinguish 'good' word-context pairs from 'had' ones

Create a set D of correct word-context pairs and set \bar{D} of incorrect word-context pairs

The goal of the algorithm is to estimate the probability $Pr(D=1\mid w,c)$ that the word-context pair w, c comes from the correct set D

This should be high $(\to 1)$ for pairs from D and low $(\to 0)$ for pairs from \bar{D}

Advantages and limitations of words embeddings

- Advantages and limitations of words embeddings



Using word embeddings

Pre-trained embeddings: 'Semantic' input to any neural network instead of one-hot word encoding

■ Instance of transfer learning — pre-trained (self-trained) on an auxiliary task, plugged into a more complex model as pre-trained weights

Example: Represent a document as an average of its words' embeddings (average bag-of-words through embeddings) for text classification

Side note: word2vec and word embeddings → part of the deep-learning revolution in NLP around 2015





Semantic similarity, short document similarity, query expansion

"Using Word2Vec's CBOW embedding approach, applied over the entire corpus on which search is performed, we select terms that are semantically related to the query."

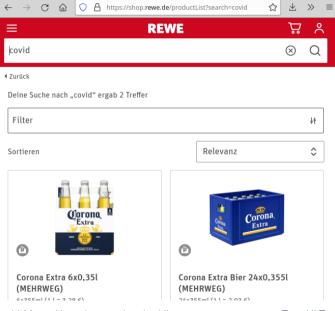
S. Kuzi, A. Shtok, and O. Kurland (2016). "Query Expansion Using Word Embeddings". In: Proceedings of the 25th ACM International on Conference on Information and Knowledge Management, ACM, pp. 1929-1932

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"Using Word2Vec's CBOW embedding approach, applied over the entire corpus on which search is performed, we select terms that are semantically related to the query."

What can possibly go wrong?



Searched for **covid** (test), returned the closest items with **corona** in the title (because their embeddings learned that covid \approx corona).

Query expansion with word embeddings might be tricky



Mining word analogies with word2vec

'Germany to Berlin is France to?'

Solved by v(Berlin) - v(Germany) + v(France), outputs vector \boldsymbol{x} which is closest to Paris in the embeddings space (the closest row in \boldsymbol{E})

Find the queen

 $v(\text{king}) - v(\text{man}) + v(\text{woman}) \approx v(\text{queen})$

Limitations of word embeddings (1)

Definition of similarity

Completely operational: words are similar if used in similar contexts

Antonyms

Words opposite of each other (buy—sell, hot—cold) tend to appear in similar contexts (things that can be hot can also be cold, things that are bought are often sold)

Models might tend to judge antonyms as very similar to each other

Limitations of word embeddings (2)

Biases

Distributional methods reflect the usage patterns in the corpora on which they are based

The corpora reflect human biases in the real world (cultural or otherwise)

Neural LMs and learning word embeddings

"Word embeddings encode not only stereotyped biases but also other knowledge [..] are problematic as toward race or gender, or even simply veridical, reflecting the status auo distribution of gender with respect to careers or first names."

A. Caliskan, J. J. Bryson, and A. Narayanan (Apr. 2017), "Semantics derived automatically from language corpora contain human-like biases". In: Science 356 (6334), pp. 183-186

Limitations of word embeddings (3)

Polysemy, context independent representation

Some words have obvious multiple senses

Neural LMs and learning word embeddings

A bank may refer to a financial institution or to the side of a river, a star may be an abstract shape, a celebrity, an astronomical entity

Using a single vector for all forms is problematic



Recap



Take aways

- Neural language models
- Self-supervised training of word embeddings
- word2vec trained with negative sampling
- CBOW for context modeling

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Credits

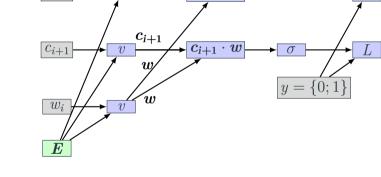
Ivan Habernal

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Skip-Gram in word2vec

Skip-Gram — even more relaxed context notion



 c_{i-1}

For k-element context $c_{1:k}$, treat as k different independent contexts (w_i, c_i)

46 Neural LMs and learning word embeddings

Choosing the context

Sliding window approach — CBOW

Auxiliary tasks are created by taking a sequence of 2m+1 words

- The middle word is the target (focus) word
- \blacksquare The m words to each side is the context

Sliding window approach — Skip-Gram

2m distinct tasks are created, each pairing the focus word with a different context word

Skip-gram-based approaches shown to be robust and efficient to train

FastText embeddings: Sub-word embeddings

FastText embeddings

Popular word embedding models ignore the morphology of words, by assigning a distinct vector to each word.

 Limitation, especially for languages with large vocabularies and many rare words

FastText embeddings

Popular word embedding models ignore the morphology of words, by assigning a distinct vector to each word.

- Limitation, especially for languages with large vocabularies and many rare words
- \rightarrow Model each word as a bag of character n-grams
 - Each character *n*-gram has own embedding
 - Word is represented as a sum of *n*-gram embeddings

P. Bojanowski, E. Grave, A. Joulin, and T. Mikolov (2017). "Enriching Word Vectors with Subword Information". In: Transactions of the ACL 5, pp. 135–146

FastText embeddings example

Extract all the character n-grams for $3 \le n \le 6$

Example

$$v(\text{eating}) = \sum_{g \in G_w} v(G_w)$$

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Train with skip-gram and negative sampling (same as word2vec)

50 Neural LMs and learning word embeddings

Generating text with language models

We can generate ("sample") random sentences from the model according to their probability

- Predict a probability distribution over the vocabulary conditioned on the start symbol <s>
- 2 Draw a word from the predicted distribution
- 3 Predict a probability distribution over the vocabulary conditioned on the start symbol and the first generated word
- Draw a word from the predicted distribution
- 5 Repeat until generated *end-of-sentence* symbol </s>
 (or <EOS>)
- 51 Neural LMs and learning word embeddings