

**ENGLISH****Problem 1** [Agents. Answer 1(True) or 0 (False) for each of the following sentences.]

*Note 2020: Several students have pointed out that there sometimes exists reasonable alternative answers to questions about agent environments. On future exams these kinds of questions will be discussion questions where you will explain your answers and what assumptions you make.*

- A. Simple reflex agents often use situation-actions rules for their reasoning.
- B. Simple reflex agents have an internal model of the current state of the world.
- C. An agent's utility function is essentially internalization of the performance measure.
- D. In order to be rational an agent should have a utility function.
- E. In a learning agent the learning element is responsible for selecting the external action to be executed next.
- F. Taxi driving happens in a stochastic, sequential, partially observable, and continuous environment.
- G. Agents need an internal model to cope with partially observable environments.
- H. An agent system has an agent function that selects the next action and a state transition function which computes what the next state of the environment would be when an action is executed.
- I. The action selection in model based agents uses as input the currently sensed data as well as the internal representation of the environment.
- J. In goal-based agents, rationality of the agents is measured based on the utility function.

**Problem 2** [General Questions about Search and Logic. Answer 1(True) or 0 (False) for each.]

- a. Depth-first search is more space efficient than Breadth-first search.
- b. The basic Genetic Algorithm is Stochastic Beam Search supplemented with a crossover operator.
- c. Iterative Deepening search is more space efficient than Breadth-first search?
- d. One of the main reasons why Texas Hold'em poker is harder for AI than chess is that there are 52 cards in a deck, but only 32 pieces on a chessboard.
- e. Simulated Annealing is Best-First search supplemented with a temperature variable.
- f. All of the following are traditionally classified as Informed Search methods: A\*, Iterative Deepening and Hill Climbing.
- g. To use a resolution theorem prover, all logical expressions must first be converted into horn-clause form.
- h. In first-order logic, a sentence is satisfiable if and only if there is at least one interpretation and one variable assignment in which it is true.
- i. PROLOG is a computer language that relies heavily on backward chaining.
- j. Skolemization is an important step of resolution theorem proving in both propositional logic and first-order logic.

**Problem 3**

Assume the following predicates:

- $S(x)$  –  $x$  is a student
- $E(y)$  –  $y$  is an exam
- $Q(x)$  –  $x$  is a question.
- $EQ(x,y)$  –  $y$  is a question on exam  $x$
- $K(x,y)$  –  $x$  knows the answer to question  $y$ .

and the following expressions:

- $\forall x: S(x) \Rightarrow \{ \exists y, z: E(y) \wedge EQ(y,z) \wedge \neg K(x,z) \}$
- $\forall x,y: E(x) \wedge EQ(x,y) \Rightarrow \{ \exists z: S(z) \wedge \neg K(z,y) \}$
- $\forall x,y,z: E(x) \wedge Q(y) \wedge S(z) \Rightarrow \{ K(z,y) \Rightarrow EQ(x,y) \}$

### Part 1:

For each logical expression, select the one natural-language sentence below that best captures its meaning:

- There are some students who miss every question on all exams.
- All exams have at least one question that no student can answer correctly.
- Every student gets everything correct on at least one exam.
- No student is perfect.
- No exam question is correctly answered by every student.
- Students do not know the answers to questions that are not on exams.
- Given any student, question and exam, the student can answer the question if it is on the exam.
- Each exam has a question that every student can answer correctly.

### Part 2:

One of the three logical sentences above yields the following expression when converted to Conjunctive Normal Form (CNF), where  $F$  and  $G$  are skolem functions:

$$\{\neg S(x) \vee E(F(x))\} \wedge \{\neg S(x) \vee EQ(F(x), G(x))\} \wedge \{\neg S(x) \vee \neg K(x, G(x))\}$$

Which one of the three logical sentences is it?

### Part 3:

What is the resolvent clause when the binary resolution rule is applied to the following two clauses (where  $F$  is a skolem function and  $Karen$  is a constant symbol)?

$$\begin{aligned} &\neg S(x) \vee E(F(x)) \vee Q(y) \\ &S(Karen) \end{aligned}$$

## Problem 4

Figure 1 displays a search tree generated by Minimax search. Inside of each leaf node is its evaluation. Child nodes are always generated and evaluated from left to right in the tree.

List all of the leaf nodes that will **NOT** be generated if Minimax is run again, but this time with alphabeta pruning.

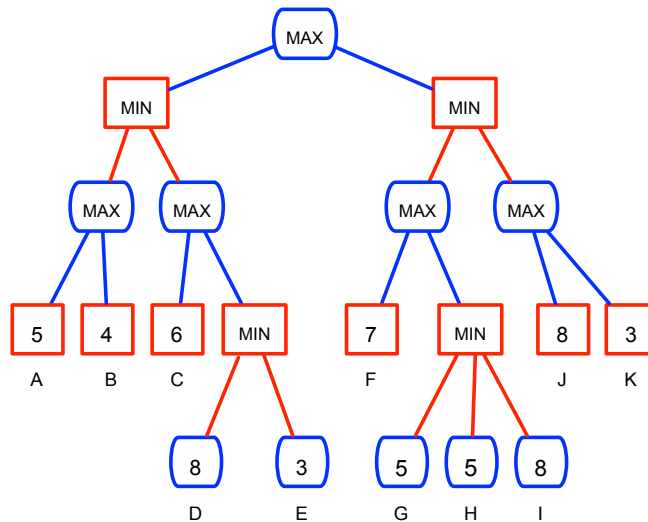


Figure 1: Minimax Search Tree

## Problem 5

Figure 2 shows part of a tree built during A\* search. The task is to rearrange the blocks to achieve the goal state while minimizing the total distance travelled by the blocks, where the width of each block has a distance = 1. The only legal operator is to switch the positions of two blocks. The heuristic is simply the total of the distances of all blocks from their goal locations.

Fill in all missing f, g and h values in the figure.

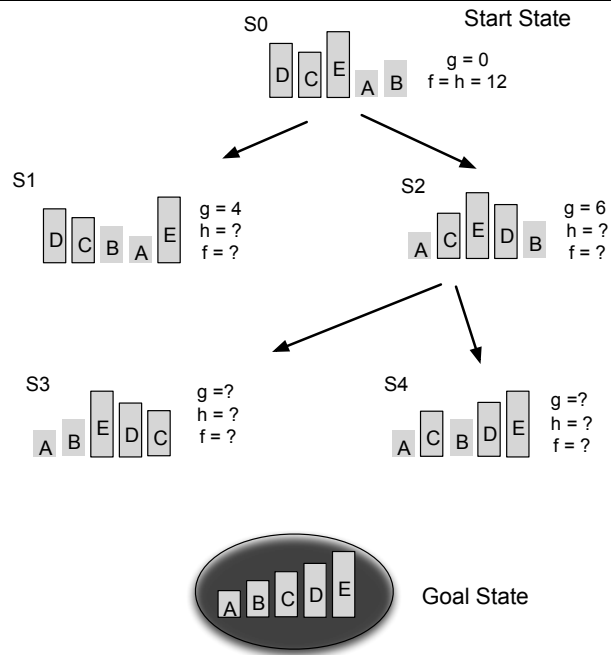


Figure 2: A\* Search Tree

## Problem 6

Figure 3 displays the use of model checking to test whether the following is a **valid** logical expression (using the formal definition of logical validity):

$$\{A \Rightarrow (B \Rightarrow C)\} \Rightarrow \{A \Rightarrow C\}$$

Fill in all missing cells of the table with a 1 (True) or 0 (False).

Next, based on the completed table, tell whether or not the expression is valid.

$$\{A \Rightarrow (B \Rightarrow C)\} \Rightarrow \{A \Rightarrow C\}$$

A	B	C	$B \Rightarrow C$	$A \Rightarrow (B \Rightarrow C)$	$A \Rightarrow C$
0	0	0	1	1	1
0	0	1	1	1	1
0	1	0			
0	1	1	1	1	

1	0	0			
1	0	1			
1	1	0			
1	1	1			

The two starred boxes prove that this is NOT valid.

Figure 3: Model Checking

## Problem 7 [Constraint Satisfaction Problems (CSPs)]

### Part 1:

Figure 4 shows a simple CSP involving 3 integer-valued variables and 3 constraints. The AC-3 (Arc consistency 3) algorithm is applied to the problem, and this involves several calls to the REVISE algorithm. The first 4 of these calls are shown. Fill in the updated domain for the variable listed after each call.

The right of the figure shows one complete solution to the CSP. Are there others? If so, list them.

### Part 2:

Figure 5 shows a second CSP, with 3 integer-valued variables and 3 constraints. The solution method is local search, beginning with the state (3,3,3), and using the MIN-CONFLICTS algorithm to determine the best new value for each randomly-chosen variable. Assuming that the first variable chosen is Z, followed by Y, determine the missing values in the two states (2 and 3) shown in the figure. In this problem, a conflict is a constraint that is violated.

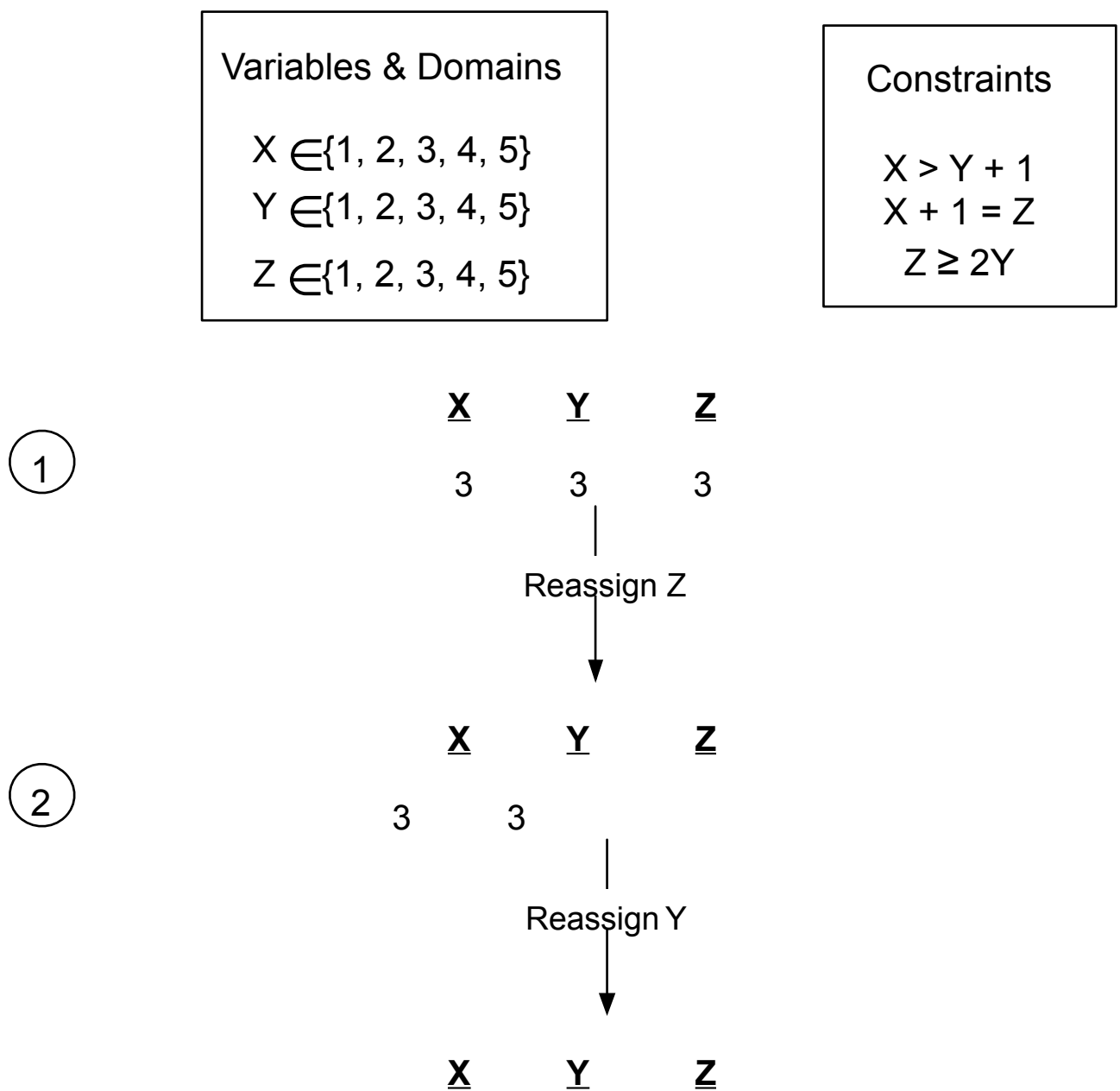
Variables & Domains	Constraints
$X \in \{1, 2, 3, 4, 5\}$ $Y \in \{1, 2, 3, 4, 5\}$ $Z \in \{1, 2, 3, 4, 5\}$	$2Y < X$ $X > 3Z$ $Y < 3Z$

- ① REVISE(X,Y) X
- ② REVISE(Z,X)

- ③ REVISE(Y,Z)
- ④ REVISE(X,Z)

One solution:  $X=4, Y=1, Z=1$

**Figure 4: AC-3 and REVISE**



**Figure 5: MIN-CONFLICTS****Problem 8** [Planning graphs]

Rob and Mary are at home. Rob has to get to work and has two options: either he walks or he uses the car. Mary needs to get to the airport and her only option is to use the car. The car needs fuel before it can be used. For the sake of brevity we will use the following simple string description for the states and actions.

robAtHome	Rob is at home
maryAtHome	Mary is at home
fuel	there is fuel in the car
car	car is at home

The actions to be modelled are:

```

Walk {
    precondition: robAtHome
    add: robAtWork
    del: robAtHome
}

GetFuel {
    precondition:
    add: fuel
    del:
}

DriveAirport{
    precondition: maryAtHome, fuel, car
    |
    add: maryAtAirport
    del: maryAtHome, car
}

DriveWork{
    precondition: robAtHome, fuel, car
    add: robAtWork
    del: robAtHome, car
}

```

**The goal :** robAtWork, maryAtAirport

**The initial condition:** robAtHome, maryAtHome, car

**Figure 6** illustrates the incomplete planning graph. The dashed lines at A0 level show the mutex relations. The gray boxes mean "no operation".

**Part 1:**

Mark the following mutex relationships either "correct" or "wrong" according to whether they are mutex at stage A1 or not, respectively. It is recommended that you find the mutex relations at S1 first. In the following list "robAtHome" and the other literal symbols refer to the persistence actions of the literals.

- A. (Walk, robAtHome)
- B. (Walk, robAtWork)
- C. (DriveAirport, DriveWork)
- D. (DriveAirport, car)
- E. (robAtWork, DriveWork)
- F. (robAtWork,  $\neg$ robAtWork)
- G. (maryAtAirport, car)
- H. ( $\neg$ fuel, DriveWork)
- I. (DriveWork,  $\neg$ robAtHome)
- J. (DriveWork, fuel)

**Part 2:**

Is there a need to expand the graph after S2? Explain why (not) with 1 ( or max 2) sentences.



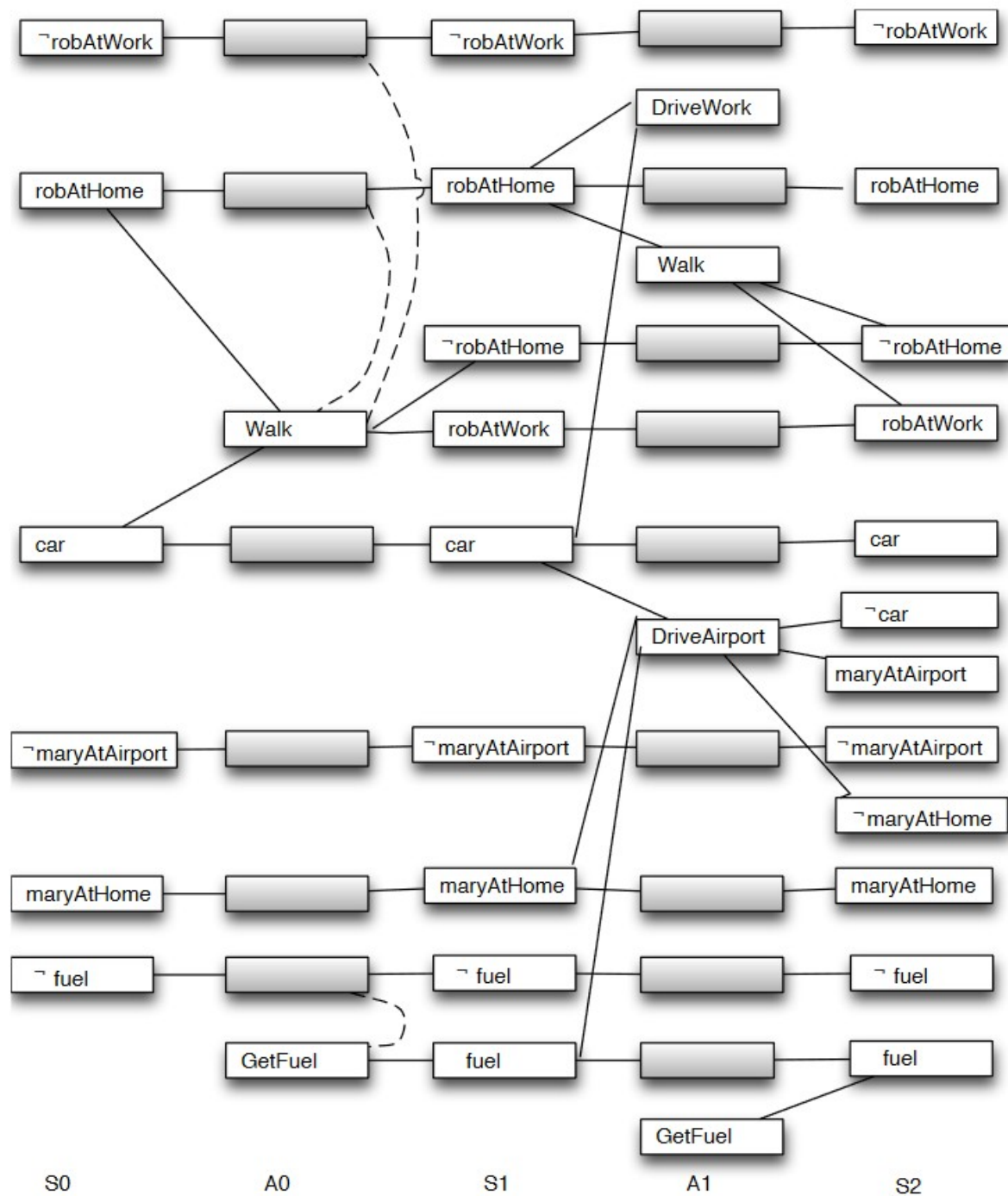
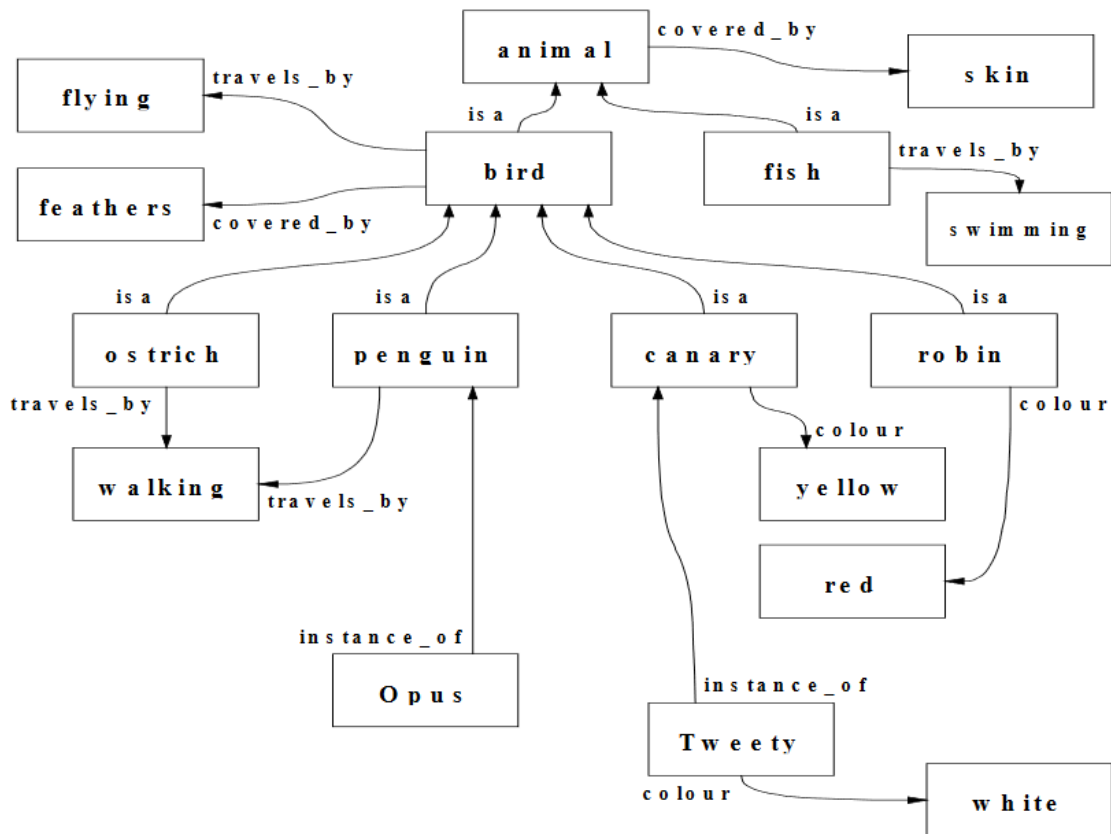


Figure 6 Planning graph for Problem 8

**Problem 9** [Knowledge representation languages.]**Part 1:**

How would a Question Answering system answer the question "What is the color of bird?" if it operates on the semantic network shown in Figure 7?

- A. It is white.
- B. It is yellow.
- C. It is red.
- D. It is red or white or blue.
- E. Don't know .



**Figure 7. Semantic Network for "bird"**

**Part 2:**

Which of the following is (are) true for the knowledge base shown in **Figure 8**? A.

- A. Apple-1 weighs 10 gram.
- B. Apple-1 weighs 50 gram.
- C. Apple-1 weighs 100 gram.
- D. Apple-1 weighs 200 gram.
- E. Apple-1 is green or red.

**Part 3:**

You will represent the sentence “*Jack kidnapped Billy on August 5*” be as an event in a frame-based language. Write down the frame.

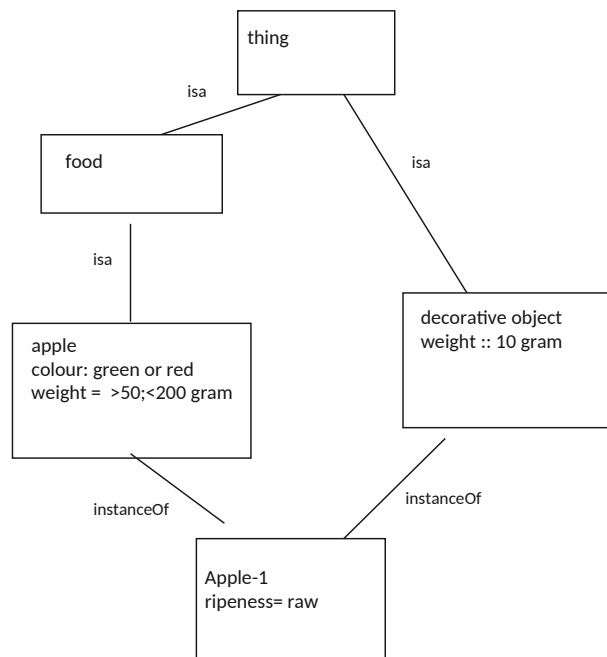


Figure 8 Apple model

**Problem 10** [General, mixture of chapters 10-13 &22 and the “An Overview of Knowledge Acquisition” (Musen) paper].

Fill in the blanks in the following questions:

- A. You are a knowledge engineer and are working on a problem where the system’s reasoning mechanism relies on prototypical objects in the world.  
 ”.....” would be the most appropriate representation language to use for this problem.
- B. Sentiment analysis is a form of text ”.....”.
- C. Knowledge elicitation (as described in Musen’s paper) involves a knowledge engineer and a “.....” expert.

- D. Taste, smell and color of a cake are its "... .." properties while weight and shape are its "... .." properties.
- E. "... .." are both disjoint and exhaustive decomposition of categories.
- F. In natural language processing, information "... .." is the process of acquiring knowledge from text.
- G. "... .." test is the most known scenario for testing the intelligence of an artificial intelligence system.
- H. "... .." is a measure used to evaluate IR systems and measures the proportion of documents in the result set that are actually relevant.
- I. In frame-based languages, default reasoning is facilitated by inheritance of "... .." values.
- J. In rule based systems, a depth first approach can be implemented by using "... .." as the conflict resolution strategy when selecting between the candidate rules that can fire at a certain time point.

END of QUESTIONS

GOOD LUCK!

**ENGLISH** (Oppgaver på bokmål starter på side 8, og nynorsk på side 15)

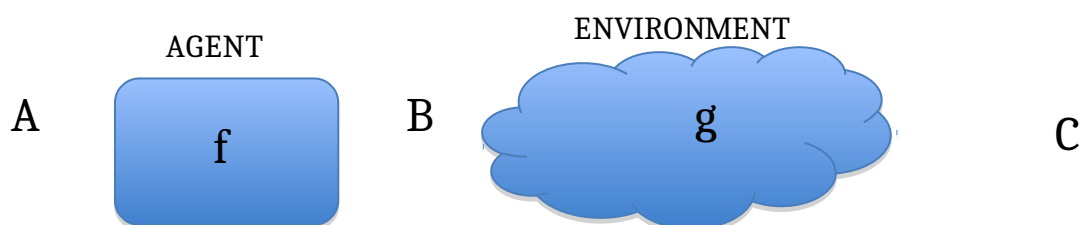
**All problems have equal weight, i.e., 10 points.**

## Problem 1

Answer the following sentences with True or False. A is a special case where you should choose between *a* and *b*. For some of the sentences you are explicitly asked to explain your answer.

- A. Which one of these does a rule-based agent system (like the one on a classical expert system) have in its *agent function*? a) contention scheduling algorithm b) conflict resolution algorithm? Answer with *a* or *b*.
- B. In a rule based system, when there are more than one rules that match the current situation and when the agent wants to explore a new/different (than the one in focus last time) hypothesis, the agent prefers the rule that has in its left side (of the  $a \rightarrow b$ ) elements that are most recently updated in the working memory of the agent. Is this statement True or False? If false, describe why – very briefly.
- C. The first phase of GraphPlan can be used as a heuristic function for forward search in the following way: Given a state *s* and goal *g*, run the graph-construction phases of GraphPlan until all the components are present and not mutex in the last layer. Let *n* be the number of action layers in the graph. We can let *n* be the heuristic value for *s*. This an admissible heuristic. True or false?
- D. Density is an extrinsic property of olive oil. True or false?
- E. Frame-based representation is mainly a declarative representation. True or false?
- F. Spreading activation and inheritance are main mechanisms of inference in rule-based systems. True or False?
- G. Turing test measures the utility of an agent. True or false?
- H. In a rule based system, backward chaining works best when the rules have complex consequent structures. True or False?
- I. N-gram character model is a natural language model. True or False?
- J. *Sufficient* and *necessary* conditions are inference rules for sound reasoning. True or False?

## Problem 2



The above figure illustrates an agent system. The two main components (depicted as a square and a cloud shape respectively in the figure) are the agent and the environment modules.

- A. In the agent terminology what is the generic/abstract names of each of A, B and C in the figure?
- B. What is the  $f$  and the  $g$  function called in the agent terminology? What role does each play in an agent system?
- C. Is there a relationship between A and C? Explain your answer – very briefly.
- D. Assume now that the “AGENT” in the system is purely reactive.
  - a. Draw a figure illustrating how the agent makes its decisions, i.e., illustrate what it takes into consideration and what type of decision(s) it takes?
  - b. Can a purely reactive agent predict the consequences of its action in the environment? If the answer is “yes”, explain how, and if it is “no” explain why not
- E. Assume now that the agent is a goal-based agent and its current task is to achieve a certain goal in the block world ENVIRONMENT . For example, ON(X,Y); move (X,Table) etc, .
  - a. Draw a figure illustrating how the agent makes its decisions, i.e., what it takes into consideration and how it does deliberate (think)?.
  - b. Can a goal-based agent predict the consequences of its action in the environment? If the answer is “yes”, explain how, and if it is “no” explain why not.

### Problem 3

Choose suitable predicates and translate the following sentences into first order predicate logic:

- A. Cats are animals.
- B. Pusur is a cat.
- C. Every dog owner is an animal lover.
- D. No animal lover kills an animal.
- E. Either Ole or Pusur kills Fido
- F. All soccer players either play with Rosenborg, or they are world-class players, or both.
- G. All soccer players either play with Rosenborg, or they are world-class players, but not both.

### Problem 4

Given a set of logical sentences and a set of models for which sentences can be true or false.

- A. What does it mean that a sentence is ‘valid’?

- B. What does it mean that a sentence is 'satisfiable'?
- C. Determine, for example by using a truth table, whether the following sentence is 'satisfiable':

$$(A \Leftrightarrow B) \wedge (\neg A \vee B)$$

Justify your answer.

- D. What does it mean that an inference rule is 'sound'?
- E. Prove whether the following inference rule is sound or not:

$$\frac{P \Rightarrow Q, Q}{P}$$

<i>P</i>	<i>Q</i>	<i>P</i> $\Rightarrow$ <i>Q</i>
T	T	T
T	F	F
F	T	T
F	F	T

## Problem 5

- A. What is a state space? List the most important components of a state space, and describe the role of each component.
- B. Explain the meaning of the following two concepts:
- Heuristic
  - Heuristic search
- C. Given the evaluation function for heuristic search in the form  $f(n) = g(n) + h(n)$ . What do the terms mean?
- C. Define the A\* algorithm

## Problem 6

- A. True or False?: Greedy Best-First search using the heuristic  $h(n) = 0$  for all states  $n$ , is guaranteed to find an optimal solution.
- B. True or False?: If  $h_1$  and  $h_2$  are both admissible heuristics, it is always preferable to use the heuristic  $h_3(n) = \max(h_1(n), h_2(n))$  over the heuristic  $h_4(n) = \min(h_1(n), h_2(n))$ .
- C. True or False?: If  $h_1$  is an admissible heuristic and  $h_2$  is not an admissible

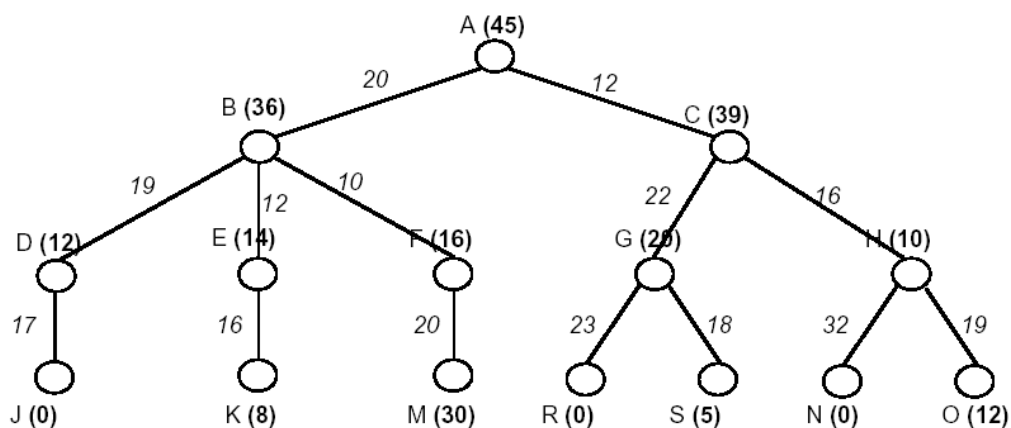
heuristic,  $(h_1 + h_2)/2$  must be an admissible heuristic.

D. Greedy Best-First search using  $h(n) = -\text{depth}(n)$  corresponds to which search method?

E. Say we have a search space that has a large branching factor at most nodes, there may be infinitely long paths in the search space, we have no heuristic function, and all arcs have cost 1. What search method would be good to use in this situation and why?

## Problem 7

A search tree is shown below. Node A is the initial state and the nodes J, R, og N are goal states. Each node is marked (in parenthesis behind the letter) with a number corresponding to the value of the heuristic evaluation function for that node. For example: G(20).



For each of the following search strategies A and B,

- list the nodes in the order that they get expanded
- list the nodes along the final path between the initial state and the goal state:

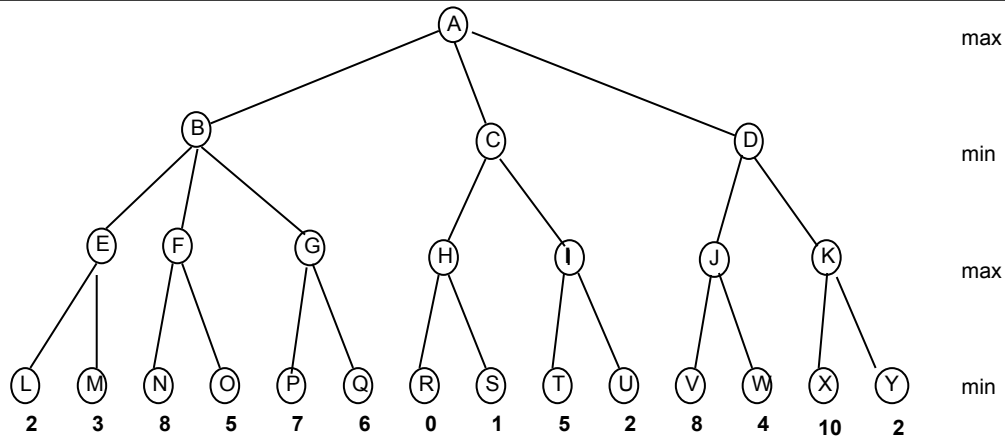
A. Hill climbing

B. A\* search

## Problem 8

Given the game tree below, in which the evaluation function values are given for the leaf nodes. Assume an alpha-beta search strategy, left to right.

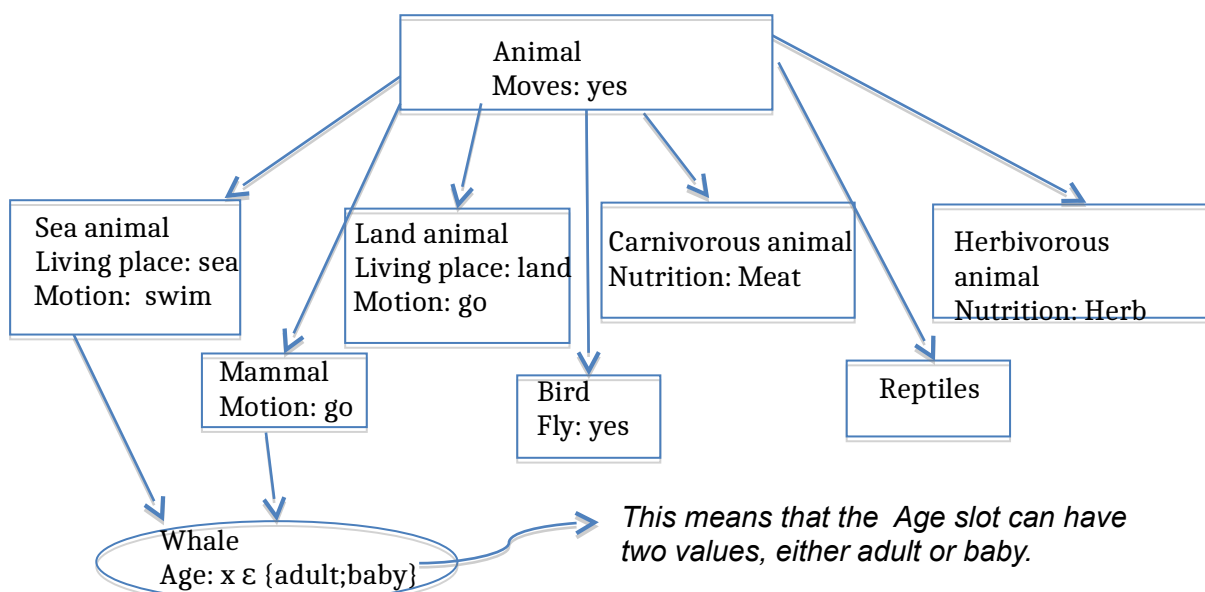




Which nodes will not be expanded? Which move will max choose in state A?

## Problem 9

- What does a partition of a category mean? Give an example.
- Does the **animal** category in the figure below have a partition? If so, write it down; write all partitions of **animal** if there are more than one.
- We want the system to be able to answer the question “How many kg does a particular whale (i.e., my-whale) eat each day?”. How would you update the knowledge base of the agent in order for it to give the correct answer to such a question? In your solution, the system shall have the knowledge that baby whales eat 5 kg food each day while adult whales eat 20 kg. A constraint is that the new knowledge base shall NOT have two additional frames for “baby whale” and “adult whale”.



**Problem 10**

This problem is about planning and consists of two independent questions (A and B).

- A. Suppose you are implementing a planning mechanism for the block-world applications. **Result** is a function which, given action **a** and environmental state **s**, computes the state of the environment after execution of **a**. Assume you have the following two alternatives to define **Result**:

$$\text{Result1}(s, a) = ([s \cup [\text{Add}(a)] - \text{Del}(a)])$$

$$\text{Result2}(s, a) = ([s \cup \text{Del}(a)] - \text{Add}(a))$$

where **Del** and **Add** correspond to what becomes True and False, respectively, as the result of action **a**.

Would a choice between adopting Result1 or Result2 make a difference on the planning result? Choose one of these 3 options: a) No difference between Result1 and Result2, b) Result1 is the correct function, c) Result2 is the correct function.

Motivate your answer by considering the following PDDL for a blocks-world problem:

```
Action MoveToTable(b, x)
PRECOND: On(b, x) ^ Clear(b) ^ Block(b) ^ (b ≠ x)
EFFECT: On(b, Table) ^ Clear(x) ^ ¬ On(b, x)
```

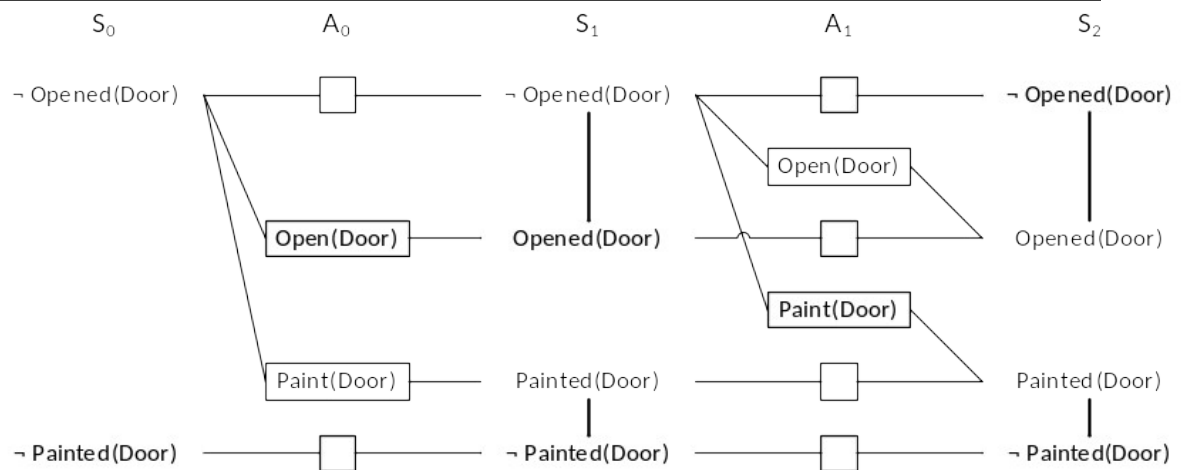
Notice that in the PDDL snippet above, **Add** and **Del** are not separated but are put together as **EFFECT**.

Explain your answer briefly.

- B. For the following planning problem

```
Init(¬Opened(Door) ^ ¬Painted(Door))
Goal(Opened(Door) ^ Painted(Door))
Action(Open(Door))
    Precond: ¬Opened(Door)
    Effect: Opened(Door)
Action(Paint(Door))
    Precond: ¬Opened(Door)
    Effect: Painted(Door)
```

we have the following planning graph where some mutex links are missing:



Find the missing mutex links between state literals and between actions on all levels.

Write down the list of missing mutex links for each level (both state and action levels). For each mutex link, provide an explanation of why they are mutex. Your answer will look like, for example:

S1:

- ¬Opened(Door), Opened(Door) – one negates the other
- ¬Painted(Door), Painted(Door) – one negates the other

S2:

- ¬Opened(Door), Opened(Door) – one negates the other
- ¬Painted(Door), Painted(Door) – one negates the other

You do not need to draw the graph, just list the pairs of the state literals and the actions that have mutex relations between them, with an explanation for each pair as shown in the example above.

END OF QUESTIONS  
GOOD LUCK!

English. Bokmål på side 7, nynorsk på side 11. I tilfelle du er usikker på betydningen av noen av begrepene (noen er ikke så letteå oversette), se på den engelske versjonen.

## Problem 1

10 points total, 1 point each subtask. Answer each question with *True* or *False*.

- (a) Artificial intelligence was born when Alan Turing formulated the Turing Test.
- (b) Early advances in artificial intelligence were met with skepticism and doubt.
- (c) The agent function maps percept sequences to action.
- (d) The real world is fully observable.
- (e) A taxi driving from A to B in traffic operates in a deterministic environment.
- (f) A simple reflex agent has a small but limited short-term memory.
- (g) Goal-based agents often rely on search and planning to find their goal.
- (h) A utility-based agent is better suited in the real world than a learning agent, since it is able to estimate its own utility.
- (i) Learning is necessary for complex agent behaviour to arise in a multi-agent setting.
- (j) Learning helps in a stochastic and continuous environment.

## Problem 2

10 points total, 1 point each subtask. Answer each question with *True* or *False*.

- (a) Intelligent agents are supposed to optimize their performance measure.
- (b) The vacuum world is not a toy problem.
- (c) Redundant paths in a search tree are impossible to avoid.
- (d) GRAPH-SEARCH is the same as TREE-SEARCH, only with history.
- (e) Time complexity and space complexity are the two best ways to evaluate the performance of an algorithm.
- (f) Blind search is also known as heuristic search.
- (g) A graph with branching factor  $b$  and depth  $d$  can be solved in most cases by uninformed search.

- (h) Bidirectional search reduces the time complexity with the square root.
- (i) An heuristic estimates the cheapest cost from one node to the goal node, even if the path is impossible to execute.
- (j) A\* is the best known form of best-first search.

### Problem 3

10 points in total, points indicated for each subtask. Express tasks *a*, *b* and *e* using first-order logic, otherwise follow the instructions.

- (a) (1 point) All lectures are fun.
- (b) (1 point) There exists a lecture that is not fun.
- (c) (2 points) Siblinghood is a symmetric relationship (i.e. write how to express this relationship in first-order logic).
- (d) (2 points) Express that “everyone dislikes vegetables” in two ways, using the “FOR ALL” quantifier in one sentence and “THERE EXISTS” quantifier in the other sentence, and the same predicate in both sentences.
- (e) (4 points) Some siblings have different parents.

### Problem 4

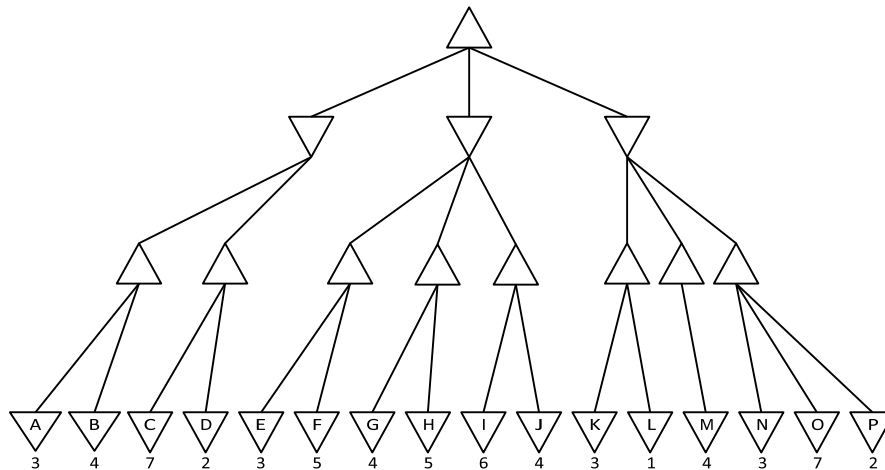
10 points in total, 2 points each subtask.

- (a) What is another word for *unification*?
- (b) What is the purpose of *Universal Instantiation*?
- (c) *Existential Instantiation* is a special case of a more general process. What is the name of this general process?
- (d) What is the best known programming language that builds on backward chaining?
- (e) What is conjunctive normal form, and what is it used for?

### Problem 5

15 points. Points indicated in each subtask.

- (a) (2 points) What is the name of the tree structure in the figure below?

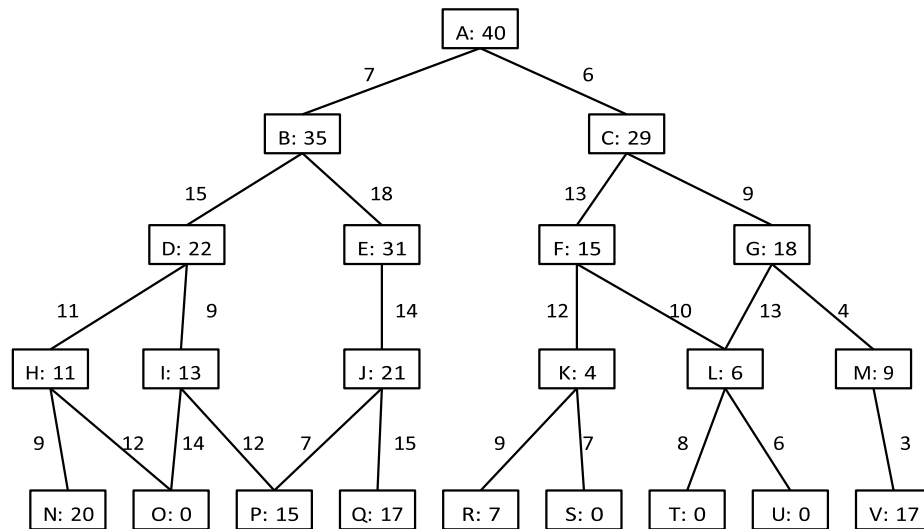


- (b) (2 points) What does it represent?
- (c) (5 points) Write down the node values that are missing in a breadth-first manner.
- (d) (6 points) Apply alpha-beta pruning and write down the leaf nodes that won't get expanded.

## Problem 6

20 points. Points indicated in each subtask.

- (a) (2 points) A\* belongs to which class of search algorithms?
- (b) (2 points) What is the worst-case time complexity of A\*?
- (c) (2 points) What does it mean to use an *admissible heuristic* in A\* search?
- (d) (9 points) In the figure below, each node is labeled with the heuristic function for that node, e.g. node A has heuristic function value 40. Apply A\* search to the tree and write down  $f(n) = g(n) + h(n)$  for each node the algorithm visits (i.e. generates), e.g. the starting node would be written A(40). Assume we visit child nodes from left to right.



- (e) (2 points) List the nodes along the final path between the start state and the end state, using A\* search.
- (f) (3 points) What is the biggest drawback of the A\* algorithm?

## Problem 7

10 points. Points indicated in each subtask.

- (a) (2 points) What are the best known examples of information retrieval systems?
- (b) (3 points) What are the three essential elements in information retrieval?
- (c) (2 points) What separates information extraction from information retrieval?
- (d) (3 points) What is the limiting factor in information extraction?



Faglig kontakt under eksamen: Pinar Øzturk: (91897451 eller 73551019)

## Introduksjon til Kunstig Intelligens (TDT4136)

30th November 2015 Tid:  
09:00 – 13:00

Language: English-Bokmål-Nynorsk  
Aid - Tillatte hjelpemidler:

No printed or hand written material is allowed. Simple calculator is allowed. Ingen trykte eller håndskrevne hjelpemidler tillatt. Bestemt, enkel kalkulator tillatt.

If you think some necessary information is missing from a question please explain what assumptions you find it necessary to make.

### **Problem 1** (20 pts, 2pts each question)

Answer the following questions with TRUE or FALSE.

- a) Knitting is a fully observable, episodic, stochastic, static and exciting agent environment.
- b) Procedural attachment is used in semantic networks.
- c) Ontology is not a key component in simple-reflex agents.
- d) *Recall* is an evaluation metric used in information retrieval that measures the proportion of returned documents that are truly relevant



- e) Simulated annealing is a local search method.
- f) Term Frequency (TF) defines the count of a term  $t$  in a collection of documents..
- g) A common heuristic function for 8-puzzle game is Manhattan distance which is the sum of the distances of the tiles to their goal positions.
- h) If both  $H_1$  and  $H_2$  are admissible heuristics for a problem and  $H_2 < H_1$ , then  $H_2$  is a better heuristic.
- i) An agent must think like a human in order to pass the Turing test..
- j) Iterative deepening search is optimal if step-costs is a constant, the search-space is finite and a goal exists.

**Problem 2** (15 pts, 3 pts each question)

Choose the correct answers (one for each question) to the questions below.

- a) Suppose the following action schema in a planning system for 8-puzzle.

*Action*( $Slide(t, s_1, s_2)$ ,

PRECOND:  $On(t, s_1) \wedge Tile(t) \wedge Blank(s_2) \wedge Adjacent(s_1, s_2)$

EFFECT:  $On(t, s_2) \wedge Blank(s_1) \wedge \neg On(t, s_1) \wedge \neg Blank(s_2)$ )

Which of the following needs to be removed from the action schema in order to get "number-of-misplaced-tiles" heuristic?

- A.  $Blank(s_1)$
  - B.  $Blank(s_2)$
  - C.  $Adjacent(s_1, s_2)$
  - D.  $Blank(s_2) \wedge Adjacent(s_1, s_2)$
  - E. None of the above
- b) We look at a Constraint Satisfaction Problem (CSP) with the three variables  $X$ ,  $Y$  and  $Z$ . Let the domain for each of these variables be the set of integers from 1 to 3:

$$D_x = D_y = D_z = \{1, 2, 3\}$$

Let the following binary constraint  $C_{XY}$  apply between  $X$  and  $Y$ , and  $C_{YZ}$  between  $Y$  and  $Z$ :

$$C_{XY} = [(1, 1), (2, 1), (2, 2), (3, 1), (3, 2), (3, 3)]$$

$C_{YZ} = [(2,1), (3,1), (3,2)]$

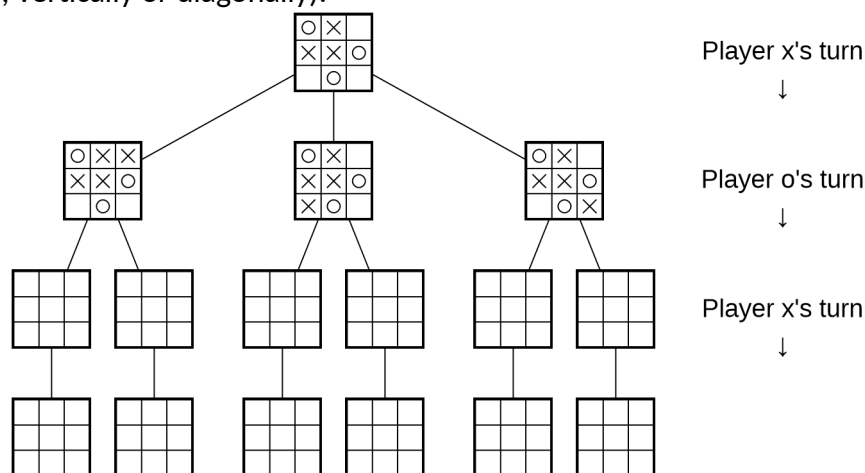
After running AC-3, what is the domain of  $X$ ?

- A. {1,2,3}    D. {1,2}    G. {3}  
 B. {2,3}    E. {1}  
 C. {1,3}    F. {2}    H. {}

c)  $Z$  is then set to 2 in the CSP from the previous question, and AC-3 is run again. What is now the domain of  $X$ ?

- A. {1,2,3}    D. {1,2}    G. {3}  
 B. {2,3}    E. {1}  
 C. {1,3}    F. {2}    H. {}

d) Consider the following (incomplete) game tree for tic-tac-toe. Tic-tac-toe is a two-player game where players "x" and "o" take alternating turns to place their respective symbols in an empty cell on the 3 x 3 game board, with the goal of getting three in a row (horizontally, vertically or diagonally):



Which one of the following statements is true?

- A. Player x is guaranteed to win  
 B. Player o is guaranteed to win  
 C. Player x can win, but only if player o plays suboptimally  
 D. Player o can win, but only if player x plays suboptimally  
 E. Either player can win, if the other player plays suboptimally  
 F. Neither/none of the players can win

e) Which of the following may be most useful in generation of a semantic network automatically from documents?

- A. Information retrieval
- B. Sentiment analysis
- C. Syntactic parsing
- D. Information extraction
- E. none of the above.

**Problem 3** (15 points)

a) (2 points) For the following sentence in English, is the accompanying sentence in first-order logic a good translation? If yes, answer yes. If no, explain why not.

No two NTNU students have the same ID number.

$$\neg \exists x, y, z (NTNUStudent(x) \wedge NTNUStudent(y) \wedge \neg (x = y)) \Rightarrow (IDNum(x, z) \wedge IDNum(y, z))$$

b) (2 points) For the following sentence in English, is the accompanying sentence in first-order logic a good translation? If yes, answer yes. If no, explain why not.

All mammals except whales are similar to humans.

$$\forall x, y Mammal(x) \wedge \neg Whale(x) \Rightarrow Mammal(y) \wedge Human(y) \wedge Similar(x, y)$$

c) (2 points) Consider the following knowledge base containing four sentences in propositional logic:

$$A \Rightarrow (B \vee C)$$

$$\neg A \Rightarrow (B \vee C)$$

$$\neg C$$

$$(B \vee D) \Rightarrow E$$

Can these four sentences be converted to a set of Horn clauses? If yes, write them down; if not, explain why not.

- d) (2 points) Consider the following knowledge base containing four sentences in propositional logic:  $A \Rightarrow (B \vee C)$ ,  $\neg A \Rightarrow (B \vee C)$ ,  $\neg C$ ,  $(B \vee D) \Rightarrow E$

Convert the four sentences above into conjunctive normal form(CNF) and show the result as a set of clauses.

- e) (3 points) Is the following sentence (1) the correct skolemization (i.e., elimination of existential quantifier) of the sentence  $\forall x \text{Person}(x) \iff \exists y \text{Heart}(y) \wedge \text{Has}(x,y)$ ?

(1)  $\forall x \text{Person}(x) \Rightarrow \text{Heart}(H1) \wedge \text{Has}(x,H1)$ .

Why not? Write down the correct one.

- f) (4 points) Suppose the following facts are in the knowledge base:

- Pia works in a restaurant  $R(\text{Pia})$
- Georg works in a restaurant  $R(\text{Georg})$
- Anyone who works in a restaurant and makes a big mistake is fired  
 $\forall x R(x) \wedge M(x) \Rightarrow F(x)$
- The restaurant owner is happy with anyone who doesn't make a big mistake  
 $\forall y \neg M(y) \Rightarrow H(\text{owner}, y)$
- Anyone who is happy with Pia is unhappy with Georg  
 $\forall w H(w, \text{Pia}) \Rightarrow \neg H(w, \text{Georg})$

Using resolution refutation, prove that "there exists someone who makes a big mistake and is fired". Show your proof on a tree starting from the boxes in the figure below. Copy the boxes into your answer sheet and fill in the last box. Apply resolution and clearly indicate the clauses being resolved in each step. Show also the binding of variables in each step/link.

#### Problem 4 (10 points)

NOTE: There is a correction in the points of the sub-questions. (a) should be 4 points and (b) is 2 points.

We changed the rules of the wumpus world. First of all, we are dealing only with wumpuses, not with gold, breeze, stench, etc. There may be more than one wumpus in the grid and they may be in any square. In the beginning of the game all squares are blank and the agent does not know which square(s) contains a wumpus. When the agent clicks on a square with a wumpus, she loses the game. If the square that the agent clicked on does not contain a wumpus, a number will appear on that square indicating the number of wumpuses adjacent to the square. Adjacency here means the four squares to the immediate left, right, top and bottom, excluding the diagonals. The goal of the game is to click on all squares which do not have wumpuses. Suppose you are playing the game in the following figure showing the current state of the grid. In the figure, squares marked *a*, *b*, *c*, and *d* are not clicked on yet. You may refer to these squares by these variables. The upper-left square is labeled 1, meaning that it is adjacent to exactly one wumpus. The other squares show the number of wumpuses in their adjacent squares.

1	a
b	2
d	c

- a) (4 points) Represent the current state of the grid using propositional logic. Use the predicate  $W(s)$  to express that square  $s$  contains a wumpus, and  $\neg W(s)$   $s$  not having a wumpus.
  - b) (2 points) Suppose you click on the lower-left square (which is a  $d$  in the beginning, see the figure) and number two (2) is revealed. This means that there is no wumpus in that square but two of squares adjacent to it have wumpuses. Represent this situation of the grid using propositional logic.
  - c) (4 points) Prove  $\neg W(a)$ , that is, the square labeled  $a$  does not contain a wumpus. For this use the combination of initial knowledge base and the new knowledge obtained by clicking on  $d$ . Show your proof by resolution refutation on a drawing.
- a) Both  $b$  and  $c$  should have a wumpus. Therefore we can write

$$W(b) \wedge W(c)$$

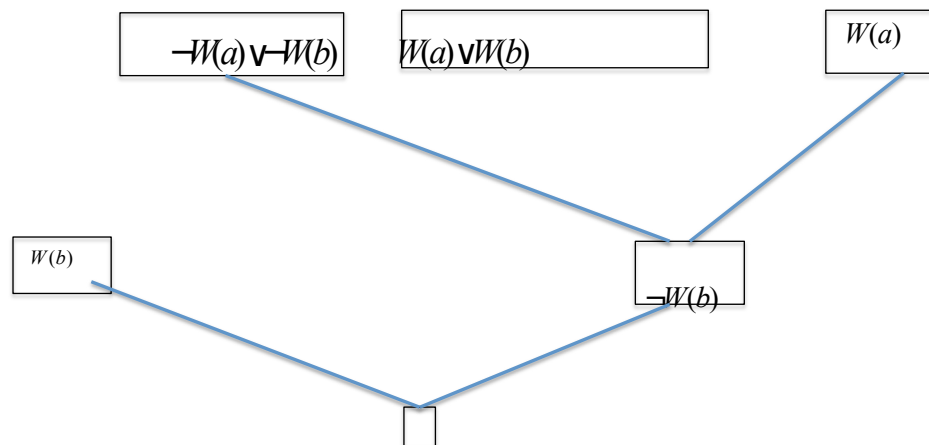
- b) First convert the KB into CNF form. E.g.,

$$(W(a) \vee W(b)) \wedge (\neg W(a) \vee W(b))$$

In CNF form:  $(W(a) \vee W(b)) \wedge (\neg W(a) \vee \neg W(b))$  etc.

To prove, add the contradiction (i.e.  $W(a)$ ) of the query to the KB. Then resolve  $W(a)$  with  $(\neg W(a) \vee \neg W(b))$  to conclude  $\neg W(b)$ .

Apply AND-elimination on  $W(b) \wedge W(c)$  to get  $W(b)$ . Resolve this with  $\neg W(b)$  obtained above to get the contradiction.



### Problem 5 (10 points)

This is a planning problem to be solved using GraphPlan algorithm. The initial state is represented as  $\{R, H, Q\}$ . The goal state is  $\{D, P, \neg R\}$ . There are four actions (Cx, Wx, Tx, and Vx) of which preconditions and effects (in terms of add and delete) are shown in the following figure.

Action	Precond	Add	Delete
Cx	{H}	{D}	{}

Wx	{Q}	{P}	{}
Tx	{}	{}	{H, R}
Vx	{}	{}	{Q, R}

- a) (1 point) Under which conditions does a plan graph level off (i.e., stops expanding)?
- b) (3 points) Starting from state level zero (i.e.,  $S_0$ ) draw the graph of the plan (i.e., the state and the action levels with mutex relations) applying the GraphPlan algorithm. Expand the graph as long as it is necessary for obtaining a plan. Use "NOP" for the persistence (no operation/maintenance) actions.
- c) (3 points) Is it possible to find a plan for this problem at state level  $S_1$ ? In case it is possible, write down the plan. In case it is not possible, justify your answer by writing down the mutex relation(s) that hinders the extraction of a plan from the graph. Write down each mutex relation (both those between the states and between the actions) and explain why it is mutex.
- d) (3 points) Are the following plans in (1) and (2) below valid plans, according to your answers above? Explain why or why not.
1.  $Cx \Rightarrow Wx \Rightarrow Tx$
  2.  $Wx \Rightarrow Cx \Rightarrow Tx$

**Problem 6** (10 pts, 2 pts each question)

Choose the correct answers (one for each question) to the questions below.

- a) What is the primary drawback of hill-climbing search?
- A. The search can get stuck in a local maximum
  - B. The algorithm requires a lot of memory
  - C. The search can get stuck in a global maximum
  - D. The result depends strongly on the temperature schedule

- b) When we illustrate the Minimax algorithm, we use the symbols 4 and 5 for nodes in the search tree. A variation of the Minimax algorithm additionally uses the symbol  $\frac{1}{2}$  for some of the nodes. What does this symbol represent?
- A. A second opponent in a multiplayer game
  - B. A game rule has been broken
  - C. An element of chance in the game
  - D. An estimated score, due to cutoff
  - E. A tie between the players
- c) Which of the following researchers did not participate in the Dartmouth conference where the name "artificial intelligence" was coined?
- A. John McCarthy
  - B. Marvin Minsky
  - C. Herbert Simon
  - D. Allen Newell
  - E. Alan Turing
- d) Which of the following is the main inference mechanism in semantic networks?
- A. Resolution refutation
  - B. Generalized modus ponens
  - C. Inheritance
  - D. Skolemization
  - E. De Morgan's law
- e) Which of the following would you choose as the unifier for  $UNIFY (Loves(Per,x),Loves(y,z))$ ? Explain why. No points will be given without correct explanation.
- A.  $(y/Per, x/z)$
  - B.  $(y/Per, x/Per, z/Per)$

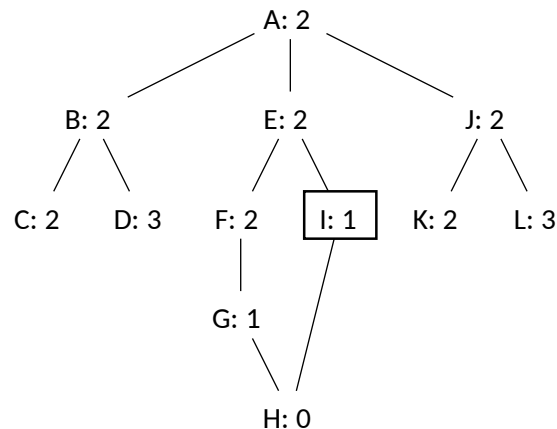


C. (y/Per, x/z, z/Siri)

D. none of the above are suitable unifiers.

**Problem 7** (10 points)

Consider the following search problem:

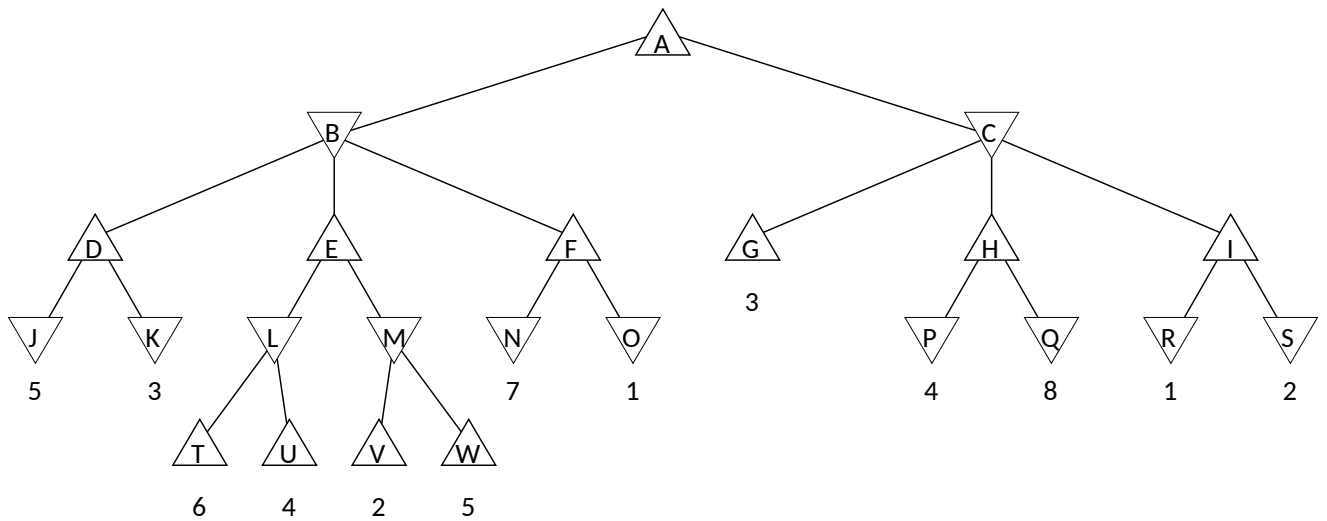


The initial node is A and the goal node is H. All step costs are 1, and a heuristic value is given for each node in the figure (for example, the heuristic value for node D is given as 3). Assume that there is a goal-test function which will be called by the search algorithm every time it needs to determine whether a node is a goal node.

- a) (2 points) Using breadth-first search (BFS): What is the sequence of nodes for which the goal-test function will be called? Write the letters for each node, and in the correct order.
  - b) (1 point) Using breadth-first search (BFS): What will be returned as the shortest path to the goal?
  - c) (6 points) Using A\*: What is the sequence of nodes for which the goal-test function will be called? Whenever several nodes have the same estimated cost, always choose the node that comes first alphabetically.
- a) (1 point) Using A\*: What will be returned as the shortest path to the goal?

**Problem 8** (10 points)

Consider the following Minimax tree:



The leaf nodes have their final utility values given as numbers below them.

- (2 points) What is the final value in node A, after running Minimax?
- (3 points) What is the final value of the rest of the internal nodes, after running Minimax? Write the values for the nodes in alphabetical order, and do not include the root node or the leaf nodes. In other words, write the numbers in the order B, C, D, E, F, H, I, L, M.
- (5 points) Which nodes will be pruned when using alpha-beta pruning on this tree (assuming nodes are evaluated from left to right)? Give the answer as a list of the nodes' letters in alphabetical order, and include *all* of the nodes in the branches that are pruned.

GOOD LUCK!

Department of Computer and Information Science

## **Examination paper for (course code) (course title)**

### **TDT4136 - Introduction to Artificial Intelligence**

**Academic contact during examination:** Odd Erik Gundersen

**Phone:** +47 47637075

**Examination date:** 19/12/2016

**Examination time (from-to):** 09:00 – 13:00

**Permitted examination support material:** D No  
printed or handwritten material is permitted.  
Calculator is permitted.

**Other information:**

Results: 19 January 2017

If you believe that some information is missing in the formulation of a problem, briefly describe the necessary assumptions you made.

**Language:** English

**Number of pages (front page excluded):** 6

**Number of pages enclosed:** 7

**Checked by:**

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Date

Signature

*Students will find the examination results in Studentweb. Please contact the department if you have questions about your results. The Examinations Office will not be able to answer this.*

**(NOTE: All the answers need to be written down into answer sheets, not into the question list.)**

## **TASK 1: Task Environment (10p)**

Specify the task environment of the following four agents.

*Note 2020: Several students have pointed out that there sometimes exists reasonable alternative answers to questions about agent environments. On future exams these kinds of questions will be discussion questions where you will explain your answers and what assumptions you make.*

Possible answers:

Observable: Fully (F) or partially (P).

Agents: Single (S) or Multi (M)

Deterministic: Deterministic (D) or stochastic (S).

Episodic: Episodic (E) or sequential (S)

Static: Static (S), semi (I) or dynamic (D)

Discrete: Discrete (D) or continuous (C)

Agent 1: Deep Blue

Deep Blue is a chess playing agent that played and won against Garry Kasparov in 1997. Consider one game against Garry using a clock.

Agent 2: Roomba

Roomba is a vacuum-cleaning robot that drives around and vacuums the floors in all the rooms of a home.

Agent 3: A Tesla factory paint-robot.

A paint robot on the Tesla factory paints one and one car. The cars are transported by a transport robot to and from the paint robot. The paint robot uses a spray-painting robot arm to paint the cars.

Agent 4: Stats Monkey the robot journalist

Stats Monkey collects box scores and play-by-play data to spit out credible accounts of college baseball games while the games are being played.

*Answer to be written down into answer sheet following the given table:*

Task Environment	Observable P/F	Agents S/M	Deterministic D/S	Episodic E/S	Static S/D/I	Discrete D/C
Deep Blue						
Roomba						

*Students will find the examination results in Studentweb. Please contact the department if you have questions about your results. The Examinations Office will not be able to answer this.*

Paint robot						
Stats Monkey						

## TASK 2: Propositional and first-order logic (20p)

- a) (4p) What are the advantages and disadvantages of the propositional logic ? What is the difference between implication and entailment in propositional logic ? (*The answer should be shorter than one page*).
- b) (4p) Convert the following formula to CNF (conjunctive normal form)  

$$(A \wedge B) \Rightarrow (\neg A \Leftrightarrow B)$$
- c) (2p) Multiple choice  
 The formula  $\forall x \exists y P(x,y) \rightarrow \exists q P(q,q)$  would be treated as a validity
- Under all possible circumstances
  - By an inference engine that implements occurs check as Skolem functions
  - By an inference engine that implements occurs check as Skolem constants
  - Under no possible circumstances
- d) (3p) True or False (*correct answer= 1p; wrong answer= -1/2p; total score will be 0-3p*)
- Universal Instantiation is built on Skolemization.
  - The Backward Chaining Algorithm can be described as follows:
    - Pose the original query as a goal.
    - Find every clause in the knowledge base whose right-hand side unifies with the goal under some substitution.
    - Prove in turn every conjunct on the left-hand sides of each of these clauses, keeping track of the accumulated substitutions.
  - There exists a sentence S in First Order Logic such that S cannot be converted into an inferentially equivalent sentence in Conjunctive Normal Form.
- e) The statement “Every Russian school boy knows a game”<sup>1</sup> has two interpretations:  
 A. There exists a game such that every Russian school boy knows this game.  
 B. For each Russian school boy, there exists a game so that the boy knows this game.
- Questions:
- (2p) Formulate each of these two interpretations in first order logic.
  - (2p) Convert the formulas into clausal form.
  - (3p) Use either a resolution proof or the Tableaux method to show that the logical formulation of interpretation A implies the logical formulation of interpretation B.

<sup>1</sup> The saying “Every Russian schoolboy knows ...” (that you must recapture with the pawn!) is attributed to the Soviet chess Grandmaster David Bronstein who used it to imply how little Western chess players (in the 1950s) understood of the game compared to any Russian. However, Bronstein never met Magnus Carlsen 🐼

*Students will find the examination results in Studentweb. Please contact the department if you have questions about your results. The Examinations Office will not be able to answer this.*

### TASK 3: Search (20p)

You are going to evaluate search algorithms that can find the shortest indoor walking paths. Figure 2 illustrates seven rooms and the actual walking distances between them. Table 1 specifies the straight-line distances between room 127D and all the other rooms. The evaluation function  $f(n)$  evaluates node  $n$ . When we evaluate the algorithms, we start our path search in room 181 and we want to find the shortest path to room 127D, which is our end node.

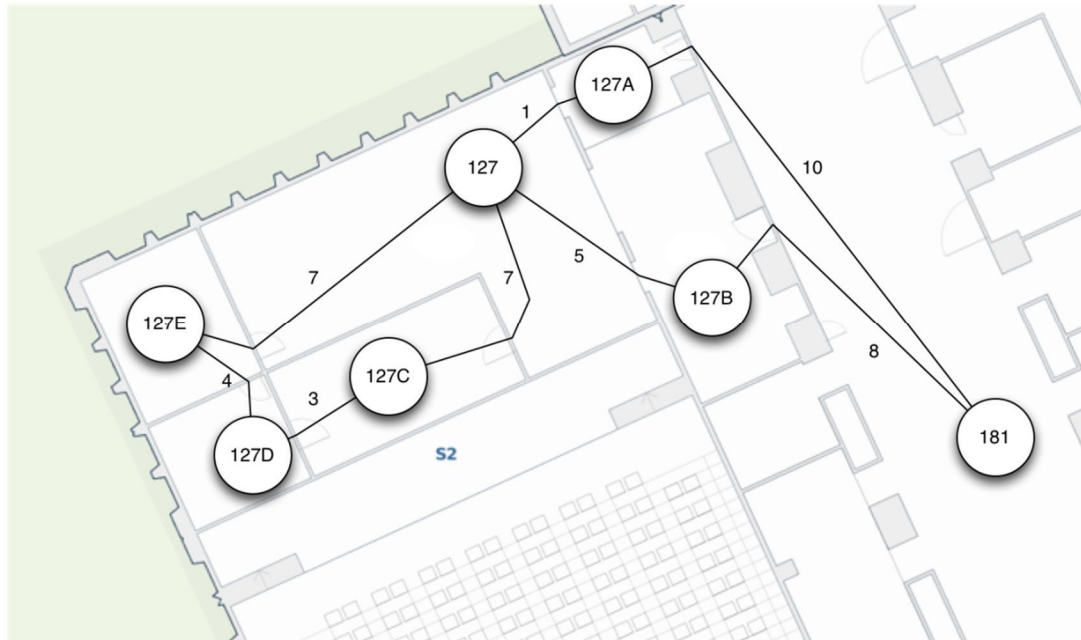


Figure 1: The graph represents the possible walking paths between the seven rooms 127D, 127E, 127C, 127, 127A, 127B and 181. The numbers close to the paths indicate the actual walking distances between the connected rooms.

Table 1: Straight line distance between the rooms and 127D

Room	SLD from 127D
127	7
127A	10
127B	9
127C	3
127E	2
181	14

- Greedy best-first search (3p): What is the evaluation function  $f(n)$  for greedy best-first search? Write the function and describe the term(s) on the right hand side.
- A\* (3p): What is the evaluation function for A\*? Write the function and describe the term(s) on the right hand side.

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- c) Greedy best first search (3p): For each step in the search, write the evaluation function for the node that is selected for expansion.
- d) A\* (3p): For each step in the search, write the evaluation function including all the terms and their values for the node that is selected for expansion.
- e) Admissible heuristics (4p): Explain what an admissible heuristics is in one sentence only. Give two examples of admissible heuristics for the 8-puzzle where the objective is to slide tiles horizontally or vertically into the open space until the goal state is reached.
- f) Optimality of A\* for graph search (1p): Must the heuristics be both admissible and consistent in order for the Russel and Norvig version of A\* to be optimal when applied to graph search? Alternatives: Yes or No.
- g) Search algorithms (3p): Which of the search algorithms 1) A\*, 2) genetic algorithms, 3) minimax, 4) constraint propagation should be chosen for the following search problems:
  - 1. Search for a schedule of flights that has some restrictions.
  - 2. Search for best action in backgammon.
  - 3. Find the best design of a car.
  - 4. Find the shortest route for a self-diving car.

## **TASK 4: Constraint satisfaction (20p)**

Figure 2 shows the water regions in Norway, which there are eleven of, and these are Finnmark (F), Troms (T), Norland (N), Sør-Trøndelag (ST), Møre og Romsdal (MR), Østfold (Ø), Sogn of Fjordane (SF), Hordaland (H), Buskerud (B), Rogaland (R) and Vest-Agder (VA).

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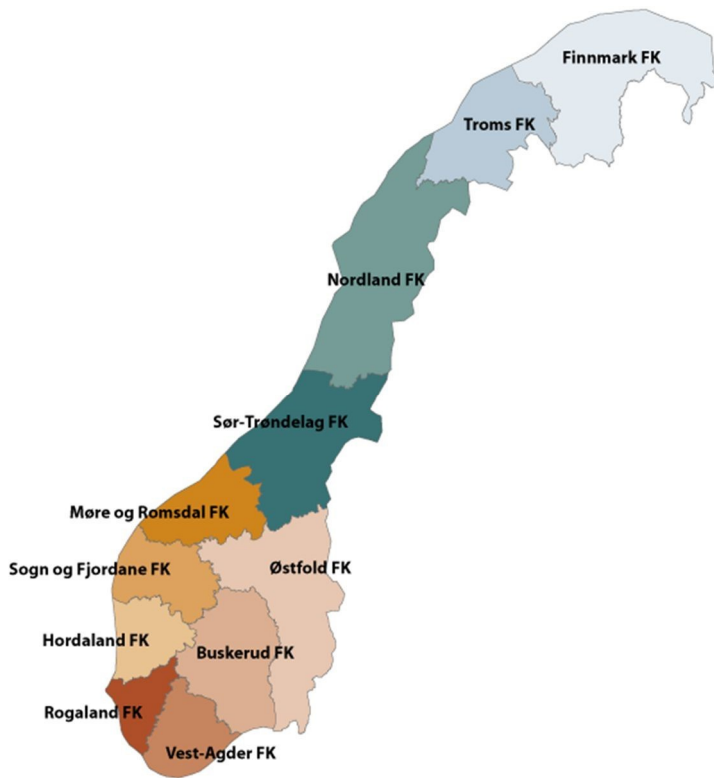
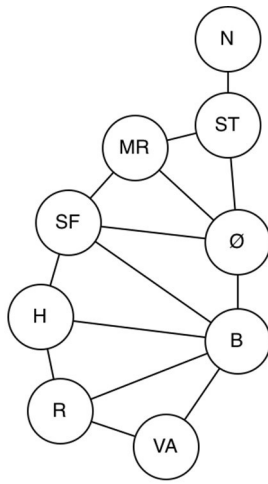


Figure 2: Water regions of Norway.

You are going to color the map. Unlike the artist that has colored the map of figure 2, you can use three colors only (red, green and blue), but no neighboring regions can have the same color. To solve this problem, you have to use your knowledge of constraint satisfaction. You will use the full constraint graph for b, and the reduced constraint graph for d and e. The reduced constraint graph only includes the regions south of Møre og Romsdal (that is we are not including Møre and Romsdal in the reduced constraint graph).

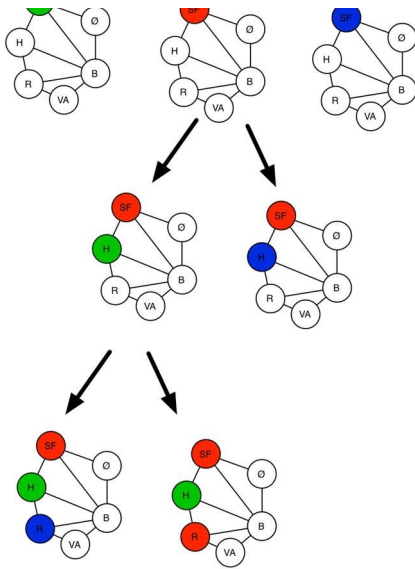
- a) Constraint satisfaction problems (3p): Specify 1) the variables, 2) the domain and 3) give at least three examples of constraints.
- b) Graph (3p): Draw the full constraint graph illustrating the water regions of Norway. Use the abbreviations in your graph: F, T, N and so on.

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- c) Description (3p): Which of the following terms describe the domain and the constraints of the specified problem?
1. Discrete domain,
  2. Continuous domain,
  3. Finite domain,
  4. Infinite domain,
  5. Linear constraints
  6. Nonlinear constraints,
  7. Unary constraints,
  8. Binary constraints,
  9. N-ary constraints.
- d) Backtracking search (4p): Illustrate the first three levels of the search tree of backtracking search using the constraint graph. Each node in the tree should list all the assignments made by that point in the search. Use the reduced constraint graph. You should assign values to nodes in the following order:  $SF$ ,  $H$ ,  $R$ ,  $VA$ ,  $\emptyset$ .

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- e) Forward checking (4p): Illustrate forward checking with a table. Each variable should have a column in the table, showing the remaining domain for that variable at each point in the search (represented by rows). Show three steps. Use the reduced constraint graph.
- f) Heuristics (3p): Of the three heuristics minimum-remaining-values (MRV), degree (D) and least-constraining-value (LCV):
- Which heuristic should be used to choose which region to color next?
  - Which heuristic should be used to decide the order to examine values?

## TASK 5: Planning (10p)

- a) Characterizing planning (5p): How can a planning (problem) be characterized? Name two situations when planning is useful. (*The answer should be shorter than one page.*)
- b) Plan representation (5p): Explain how a plan can be represented? Give an example of withdrawing cash from an ATM in either STRIPS or PDDL. (*The answer should be shorter than one page.*)

## TASK 6: Natural Language Processing (20p)

- a) (6p) True or False (*correct answer= 1p; wrong answer= -1/2p; total score will be 0-6p*)
- Sentiment analysis is a text classification application.

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- The purpose of smoothing is to avoid dramatic effects of low-frequency counts.
  - The bag of words model can be seen as a simple language model.
  - ‘Freeze’, ‘halt’, ‘cease’ and ‘finish’ are examples of stop words.
  - The task of Information Retrieval is to return the answer to a user query.
  - Information Extraction systems are often based on templates
- b) (2p) What are the main features of human languages that make parsing of these different from the parsing of programming languages?
- c) (2p) Sentiment analysis of Twitter messages (tweets) faces several challenges. Give examples of at least four problems that need to be addressed.
- d) (4p) The documents in a collection that were returned respectively not returned by an Information Retrieval system in response to a given query were analysed for relevance and shown to be distributed as follows:

	Returned	Not returned
Relevant	60	40
Not relevant	20	180

1. What was the system’s precision?
  2. What was the system’s recall?
  3. What is  $F_1$  score?
  4. Calculate the  $F_1$  score of the system.
- e) (6p) Suppose you have access to the following knowledge sources:
- Dictionaries of basic word forms (lemmas) for English and Norwegian,
  - Morphological inflection rules for the same two languages,
  - A large set of English e-mails already classified as spam,
  - A large set of Norwegian e-mails already classified as spam,
  - A large set of English e-mails already classified as not being spam,
  - A large set of Norwegian e-mails already classified as not being spam,
  - A huge set of unclassified e-mails written in a wide range of human languages, and
  - A stream of incoming messages, each of the length of no more than one sentence.

Describe how you would go about building a system which would analyze each incoming message and produce one of the following outputs:

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1. The message is not written in a human language.
2. The message is written in a human language which is neither English nor Norwegian.
3. The message is written in English and is spam.
4. The message is written in Norwegian and is spam.
5. The message is written in English and is not spam.
6. The message is written in Norwegian and is not spam.

You do not need to produce a complete solution, but rather sketch the steps that would have to be taken.

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**NOTE:** All the answers need to be written down into answer sheets, not into the question sheet.

**Problem 1** (10 points, 2.5 pts each question))

You are a map-coloring robot assigned to the task of coloring the following map (see Figure 1 ). Each region must be colored one of Red (R), Green(G) or Blue(B). Adjacent regions must be a different color. The map (left) and the constraint graph (right) are shown below.

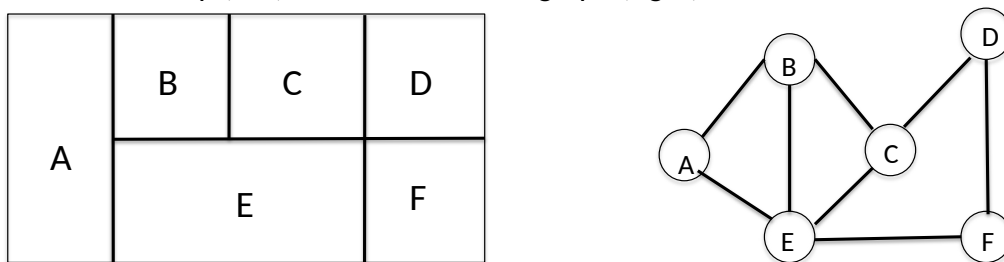


Figure 1: Map coloring problem

- a) Consider the partial assignment in Figure 2 below where variable A and E have been assigned values as shown in the figure. Cross out all values that should be eliminated by Arc Consistency (using AC-3 in the textbook.)

Regions in the map					
A	B	E	C	D	F
Blue	R G B	RED	R G B	R G B	R G B

Figure 2: Partial assignment for Region A= Blue and E= Red

- b) Minimum Remaining Values Heuristics. Consider the partial assignment in Figure 4 where B is assigned value Green and constraint propagation has been done. Write down all unassigned variables (just the letters that correspond to these variables) that might be selected by Minimum Remaining Values Heuristic (MRV)

*Region in the map*

*Regions in the map*

A	B	E	C	D	F
R B	Green	R B	R B	R G B	R G B

Figure 4: Partial assignment for Region B= Green

- c) Degree Heuristic. Consider the partial assignment in Figure 4 where B is assigned Green and constraint propagation has been done. Write down all unassigned variables that might be selected by the Degree Heuristics
- d) Consider the following complete but inconsistent assignment in Figure 6. E has been selected to be assigned a value during local search for a complete and consistent assignment. What new value would be chosen for E by the MINIMUM-CONFLICT heuristic?

*Regions in the map*

A	B	E	C	D	F
R B	Green	R B	R B	R G B	R G B

Figure 5: Partial assignment for Region B= Green

*Regions in the map*

A	B	E	C	D	F
B	G	?	G	G	G

Figure 6: Complete assignment where the value of Region E needs to be changed, and to be found.

**Problem 2** (10 points)

Assume the following knowledge base KB:

$$\forall x \text{ allergies}(x) \Rightarrow \text{sneeze}(x)$$

$$\forall x \forall y \text{ cat}(y) \wedge \text{allergicToCats}(x) \Rightarrow \text{allergies}(x)$$

$$\text{cat}(\text{Felix})$$

$$\text{allergicToCats}(\text{Mary})$$

The Goal/Query: Does Mary sneeze?, i.e.,  $\text{sneeze}(\text{Mary})$ ?

Perform Resolution Refutation (RR) and find out if the query has a positive (True) or negative (False) answer for this KB? Answer the question with True (Yes) or False (No), and show how you derived this answer through RR. Show also unifications if any. T/F answers without the poof/refutation of the query will not be given any point. Partial points will be given to the proof.

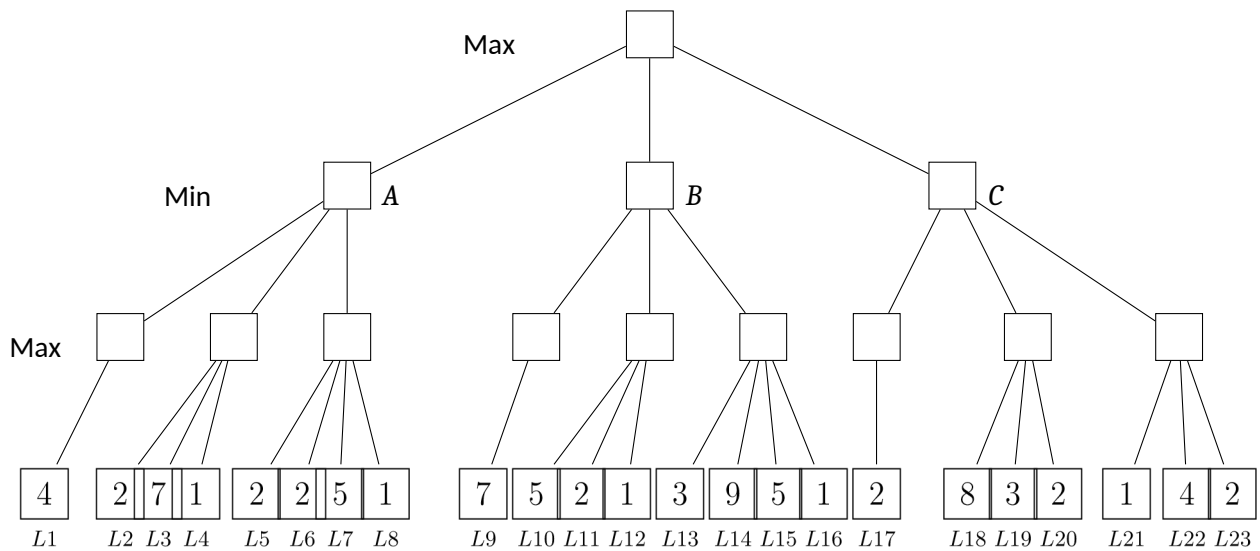
$$\neg \text{allergies}(w) \vee \text{sneeze}(w) \quad \neg \text{cat}(y) \vee \neg \text{allergicToCats}(z) \vee \text{allergies}(z)$$



**Problem 3** (10 points, division: 3-3-4 pts)

In the following adversarial game (see Figure 8) it is MAX's turn to play. The numbers at each leaf node is the estimated score of that position. Check nodes from left to right order.

- Perform mini-max search and label each branch node with its value. Draw the figure on your answer sheet and fill the squares above the leaf nodes. You don't need to draw the nodes at the leaf level.
- What is Max's best move, i.e., which node it is and which utility does it give?



- Write down all leaf nodes that the alpha-beta algorithm would prune. Your answer will be a list of  $L_i$  labels .

**Problem 4** (15 points total, 4 points for each of the first questions. The sum will not be negative for this problem.)

This is a mixture of multiple choice (b), Classical "writing the answer" (a and c), and True/False type of tasks.

- Assume the following problem represented as a graph (see Figure 10) where the numbers on the edges represent the cost of traveling between the nodes connected by the edge. You

will apply A\* graph search algorithm and the nodes in the graph have the following h-values:

$$h(S) = 7$$

$$h(A) = 6$$

$$h(B) = 2$$

$$h(C) = 1$$

$$h(G) = 0$$

Write down the to-be expanded node and the content of the priority queue at each step. Ties break alphabetically. Write down the generated solution path - you will not get any points if you don't show how the solution is generated (i.e., the queue and the currently expanding node). Is this an optimal solution? Why or why not, explain very briefly.

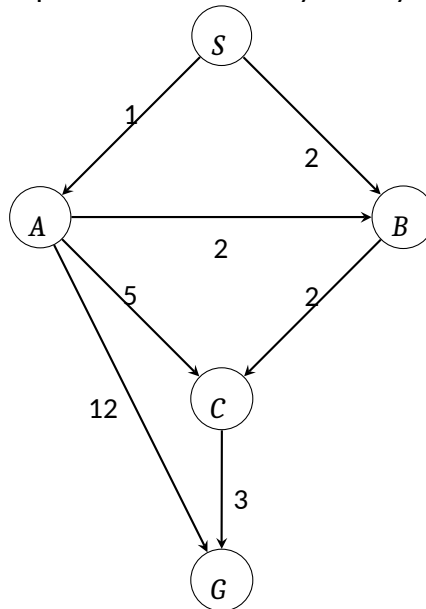


Figure 10: A\* Problem

b) Which of the following set of heuristic values provide a consistent heuristic for this problem (Figure 10)? Choose one of the options below.

$$1. \{h(S) = 7, h(A) = 6, h(B) = 2, h(C) = 1, h(G) = 0\}$$

$$2. \{h(S) = 7, h(A) = 6, h(B) = 2, h(C) = 2, h(G) = 0\}$$

3.  $\{h(S) = 7, h(A) = 6, h(B) = 4, h(C) = 2, h(G) = 0\}$
  4.  $\{h(S) = 7, h(A) = 4, h(B) = 4, h(C) = 4, h(G) = 0\}$
  5. None of the above. IMPORTANT: Note that for consistency, every pair of adjacent nodes (node that have direct connection) should be checked. Not only between S→A or A→B but all pairs, and all nodes must be used in these pairs (including G, which is also "a node". Those answers which make part of the Figure consistent but not the entire one will not be accepted as correct.
- c) Write down a consistent heuristic set and apply A\* graph search with it on the same graph (Figure 10). What is the solution path with this heuristic set? You don't get any points by writing only the optimal solution if it is not accompanied with a consistent set of heuristics.
- d) Uniform cost Search is a special case of A-star. True or False?
- e) Simulated annealing is a stochastic optimization method. True or False?

**Problem 5** (15 points. Division: 3-2-2-3-2-3, and -1 for each wrong answer. Sum of the points will not be negative for the whole problem.)

This is a combination of multiple-choice and True/False types of task. Choose the correct answer for each question.

- a) "Men and women are welcome to apply." is equivalent to

$$\forall(x) [(M(x) \wedge W(x)) \Rightarrow \text{Apply}(x)]$$

- b) Which of the following represents the sentence "Some person plays every game"?

1.  $\exists x \forall y [Person(x) \wedge Game(y) \rightarrow Plays(x, y)]$
2.  $\exists x \forall y [Person(x) \wedge Game(y) \wedge Plays(x, y)]$
3.  $\forall x \forall y [Person(x) \wedge [Game(y) \rightarrow Plays(x, y)]]$
4.  $\exists x \forall y [Person(x) \wedge [Game(y) \rightarrow Plays(x, y)]]$
5. None of the above.

- c) Which of the following is the Skolemized version of this sentence:

$$\forall x [(\neg P(x) \wedge Q(x)) \vee \exists y (R(x, y) \wedge T(y))]$$

1.  $\forall x[\neg P(x) \wedge Q(x) \vee (R(f(x),y) \wedge T(y))]$
2.  $\forall x[P(x) \wedge \neg Q(x) \vee (R(x,f(x)) \wedge T(f(x)))]$
3.  $\forall x[\neg P(x) \wedge Q(x) \vee (R(x,f(x)) \wedge T(f(x)))]$
4.  $\forall x[\neg P(x) \wedge Q(x) \vee (R(x,x) \wedge T(x))]$
5. None of the above.

d) For the sentence below, write V=valid if the sentence is valid, U=unsatisfiable if the sentence is unsatisfiable and S=satisfiable if the sentence is satisfiable but not valid.

1.  $\forall x[[Student(x) \wedge \neg Student(x)] \rightarrow BornOn(x,Moon)]$

e) Apply one step resolution to the following clauses:  $p \vee q$  and  $\neg p \vee \neg q$ . Which of the below is the correct result of the resolution step.

1.  $\{p \vee \neg p\}$  and  $\{q \vee \neg q\}$
2.  $\{\}$

f) You will convert the following sentence into Conjunctive Normal form.

$$(A \wedge B) \vee (C \wedge D) \vee (E \Rightarrow F)$$

Which one is the resultant CNF?

1.  $(A \vee C) \wedge (B \vee C) \wedge (A \vee D) \wedge (B \vee D \vee \neg E \vee F)$
2.  $(A \vee C) \vee (B \vee C) \vee (A \vee D) \wedge (B \vee D \vee \neg E \vee F)$
3.  $(A \vee C) \wedge (B \vee C) \wedge (A \vee D) \wedge (B \vee D \vee E \vee F)$
4.  $(A \vee C \vee \neg E \vee F) \wedge (A \vee D \vee \neg E \vee F) \wedge (B \vee D \vee E \vee F) \wedge (B \vee C \vee E \vee F)$
5. none of the above

**Problem 6** (20 points. Each question is 2 points. -1 for each wrong answer but the total points will not be negative.)

True/False type of questions. Answer with either True(T) or False(F)

- a) Randomized behaviour may be rational in competitive multi-agent environments.
- b) There exists a task environment in which every agent is rational.
- c) Philosopher John Searle suggests that any physical symbol system has necessary and sufficient means for general intelligent action. True or False?
- d) If  $h$  is a consistent heuristic, then  $h$  is also an admissible heuristic. True or False?
- e) Purely reactive agents use semantic networks for planning. True or False?
- f) Backgammon is a fully observable, sequential, deterministic, static, discrete and multiagent environment. True or False?
- g) Circumscription allows the entailed sentences to be removed after new sentences added to the knowledge base.
- h) "Multiple inheritance" is one of the reasons that leads to undecidability problem in first order logic. True or False?
- i) "Closed world assumption" is the assumption that atomic sentences not known to be true are in fact false.
- j) Two agents participate in a game which is defined as follows:

Agents. {Agent-i, Agent-j}

Actions: {0,100,200,300} - these actions can be thought as giving bid in an auction for example.

		Agent j			
		0	100	200	300
Agent i	0	300,0	200,0	0,100	0,0
	100	200,0	200,0	200,100	0,300
	200	0,0	0,200	0,0	0,0
	300	-100,0	-100,0	-100,0	-100,0

Figure 12: Game theory question

The Payoff matrix is shown in Figure 12 .

Which of the options below is the strongly dominant equilibrium in this game? Each option shows the pair of actions, (action of agent-i, action of agent-j):

1. (0, 100)
2. (200, 200)

3. (300,0)
4. (300,100)
5. None of the above

**Problem 7** (20pts- division of points: 3-3-3-3-2-2-2. Minus point: -1 for each wrong answer)

Multiple Choice or True/False type of tasks.

a) In situation calculus, something true in one situation may not be true in another situation. True or False?

b) The following plan describes the process of withdrawing money from an ATM. Which of the representations is written in STRIPS?

1. Action (withdraw(cash),  
 PRECOND: At(ATM)  $\wedge$  Sells(ATM, cash, person)  $\wedge$  hasMoneyOnAccount(person)  
 DELETE-LIST: hasMoneyOnAccount(person)  
 ADD-LIST: have(cash))

2. Action (withdraw(cash),  
 PRECOND: At(ATM)  $\wedge$  Sells(ATM, cash, person)  $\wedge$  hasMoneyOnAccount(person)  
 EFFECT:  $\neg$  hasMoneyOnAccount(person)  $\wedge$  have(cash))

c) Which statements about partial order planning are true?

1. Search in plan space and use least commitment when possible.
2. Make only choices that are relevant to solving the current part of the problem.
3. Both of the above.
4. None of the above.

d) Progression planners reason from the goal state, trying to find the actions that will lead to the start state. True or False?

e) In Medieval Europe, Latin worked as the Lingua Franca. Today English has taken over that role, obviously giving an advantage to persons who have it as mother tongue. There have been attempts to create artificial human languages (e.g., Esperanto and Interlingua) that would not give anybody such an advantage, but those languages have not been very successful. Suppose you were given the task of creating such a language. Which of the following would say would be most important to try to restrict:

1. The lexicon.
  2. The grammar.
  3. Ambiguity.
  4. Redundancy
- f) Two search engines were evaluated on a web search query. Engine A returned 27 web pages, 18 of which were deemed relevant to the query. Engine B returned 9 pages, all of which were relevant to the query. Which of the following statements is definitely correct?
1. System A had a higher recall than system B.
  2. System B had a higher precision than system A.
  3. System B had a higher F1-score than system A.
  4. System A had a better performance than system B.
- g) When performing sentiment analysis, it is normally important to find out:
1. Who the opinion holder is.
  2. What object the opinion is expressed on.
  3. If the opinion is positive, negative or neutral.
  4. All of the above.
- h) Which of the following statements is not correct?
1. The distributional hypothesis assumes that words with similar usage have similar meanings.
  2. The bag of words model ignores the grammatical structure of the language.
  3. An n-gram model is an example of a language model.
  4. Grounding means that a speaker defines the basis for a dialogue.

LYKKE TIL!

## EXAM TDT4136 HØST-2018 ORDINARY.

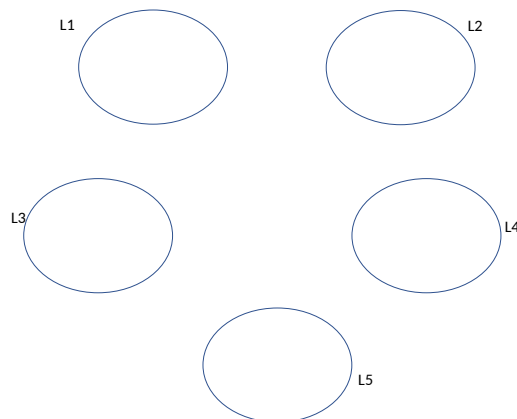
### QUESTIONS and ANSWERS (at the very end) Problem 1: CSP (10 POINTS)

In a 2-days seminar, there are 5 lectures to be allocated to 3 professors. Each professor can teach at most 1 lecture on a day. Each professor has knowledge to teach only a subset of the lectures. The following table shows which professor has the knowledge to teach which lectures where “L” means “lecture”:

Prof. Arne	L1, L2, L3
Prof. Berit	L1, L2, L5
Prof. Carl	L2, L4, L5

There are some constraints about the sequence that the lectures can be given:  $\text{Day}(L1) < \text{Day}(L2)$ , i.e., Lecture 1 must be taught the day before the day of Lecture 2, and  $\text{Day}(L3) < \text{Day}(L5)$ . Each lecture will be assigned to a professor and to a day.

- 1) Complete the following drawing to a constraint graph that represents this problem. Nodes represent the lectures that are the Variables in this Constraint Satisfaction Problem. You will draw the links between the nodes in the graph.



2. Write down the domains of the variables. Each value in the domain of a variable shows the combination of a professor that can teach the course and the time it can be taught. Instead of the whole name of a professor use only the first letter of his/her name, i.e., A, B, C shows the three professors. A domain value, hence looks like this: A2 (i.e., Arne on Day=2), B1 (i.e., Berit on Day=1. You can write the domain values by filling in the curly brackets for each variable ( L1,...., L5).

L1: { ..... }



L2: {        }

L3: {        }

L4: {        }

L5: {        }

- 2) Write down all the constraints, as implicit constraints, for this problem. Hint: You can use n-ary Alldiff to represent one type of the constraints you need.
- 3) Is this initial constraint graph arc-consistent? If not, apply AC-3 arc consistency algorithm and find the reduced domains. Write these domains for each variable in the form:

L1: { ..... }

L2: {        }

L3: {        }

L4: {        }

L5: {        }

- 5) Apply Backtracking on this arc-consistent graph without forward checking. Use Minimum Remaining Value for variable ordering (tie breaking in numerical order), and Least Constraining Value for value ordering (tie breaking alphanumerically). What order are the variables are assigned and what are their values? Your answer will look like this:

The 1. assigned variable is ....., and its value is .....

The 2. assigned variable is ....., and its value is .....

The 3. assigned variable is ....., and its value is .....

The 4. assigned variable is ....., and its value is .....

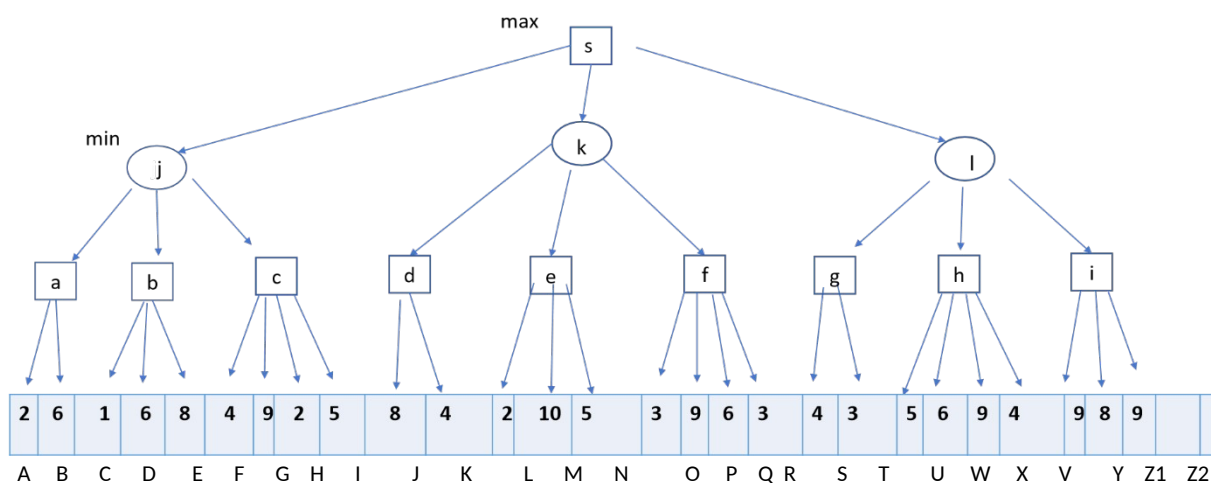
The 5. assigned variable is ....., and its value is .....

In this question you should calculate the Least Constraining Value by counting how many values in the domains of the neighboring variables in the constraint graph no longer satisfy the constraint between

themselves and the variable being assigned to. You should also count no longer valid answers in the domains of already assigned variables.

## Problem 2: Adversarial Search (10 POINTS)

- 1) Write the minimax values in the nodes (s, j, k, l, ..., h, i) at different layers of the search tree above the leaf nodes.



- 2) Apply alpha-beta pruning algorithm to prune the parts of the tree that don't need to be examined.

For each pruned part (i.e., one or more leaf nodes) of the tree write down which nodes are pruned and why, referring to V and Alpha/Beta values, in the following format:

PRUNE <The letter(s) that represent the pruned leaf nodes> BECAUSE : <Reason>

The "reason" is either

$V = \text{<value>} < \text{Alpha} = \text{<value>}$  or

$V = \text{<value>} > \text{Beta} = \text{<value>}$

Example (not necessarily correct, just to show the requested format):

Prune A,B,C because:  $v=4 < \text{Alpha}=7$

So, if there are more than one leaf nodes next to each other write them at once and together as in the example above.

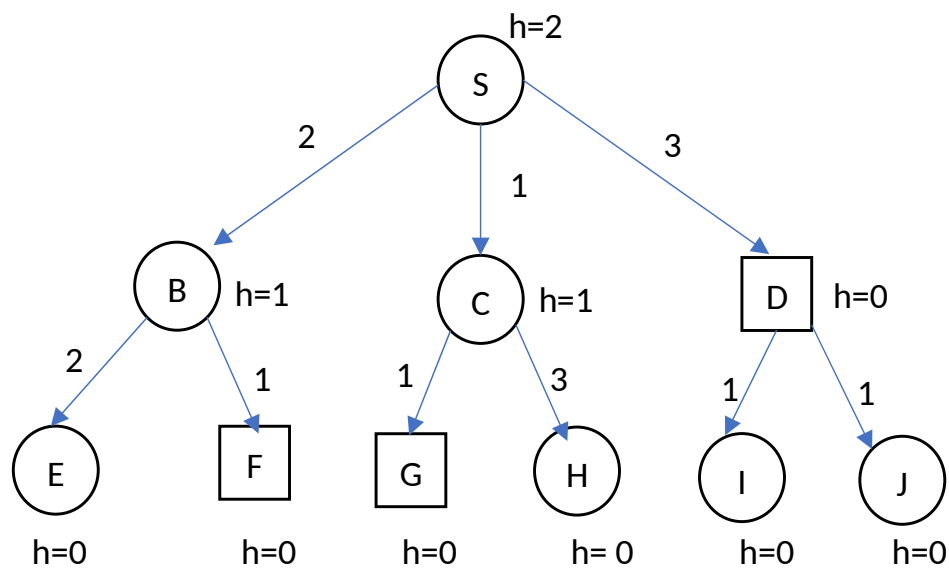
**PROBLEM 3 True/False Questions (2 points for each correct answer, -1 point for each wrong answer, 0 for each unanswered question.  
Total score between 0-20 points)**

1. Reactive agents typically use partial planning.
2. This is procedural knowledge about two cities in Norway: bigger (Oslo, Trondheim)
3. Expectimax is better suited for a deterministic environment than minimax.
4. In simulating annealing search the states represent a complete solution.
5. Principal of rationality (due to Allen Newell) maintains that the agent chooses actions in order to achieve its goal using the knowledge it has the knowledge it might gather.
6. Shortcoming of hill climbing algorithms are local maximas and plateaus.
7. Consider a block world problem where  $\text{On}(A,B)$ ,  $\text{On}(B,C)$  is the goal, and the KB Consists of these sentences:  $\text{On}(C,A)$ ,  $\text{On}(B,\text{Table})$ ,  $\text{On}(A,\text{Table})$ ,  $\text{Clear}(C)$ ,  $\text{Clear}(B)$ ,  $\text{Block}(A)$ ,  $\text{Block}(B)$ ,  $\text{Block}(C)$ . Suppose a planner that, given subgoals  $G_1, \dots, G_n$ , solves each subgoal consecutively (i.e., first one goal, and then the next one,...). If we use such a planner to solve the planning problem above and solve the goals in the given order (i.e.,  $\text{On}(A,B)$ ,  $\text{On}(B,C)$ ) the planning will obtain an optimal plan.
8. "Frames" as knowledge representation language combines declarative and procedural knowledge through their resolution mechanism.
9. Semantic networks allow multiple inheritance on the basis of specificity in the hierarchy.

10. Precision measures an NLP system's ability not to exclude a relevant document from the list of retrieved documents

#### PROBLEM 4 (Search Algorithms) (10 POINT)

In the following tree, the goals are shown by squares - there are three goals. Heuristic values and the step costs are as shown in the figure.



For each of the following algorithms, write the list of expanded nodes, and the path found. Ties are broken alphabetically.

1. Depth-first search

Expanded nodes:

The final path:

2. Breadth first search

Expanded nodes:

The final path:

3. Uniform Cost search

Expanded nodes:

The final path:

4. Greedy Best First search

Expanded nodes:

The final path:

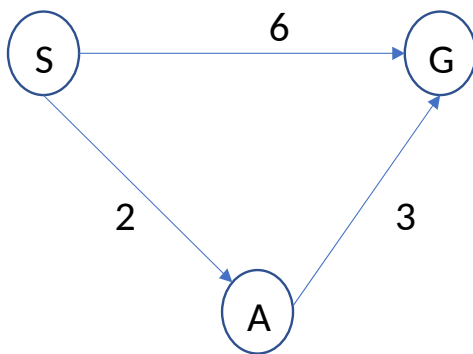
5. A\* search

Expanded nodes:

The final path:

## PROBLEM 5 (A\* heuristics) (10 POINTS)

Consider A\* search for the following search graph where S is the starting and G is the goal node. There are 4 different heuristic functions (H1-H4) of which values for the S, G, A nodes are shown in the table on the right of the graph.



Heuristic	$h(S)$	$h(A)$	$h(G)$
H1	4	1	0
H2	5	4	0
H3	4	3	0
H4	5	2	0

- 1) For each heuristic function fill in the following table with Y/N for admissibility and consistency for the search graph above. Explain your answer for each Yes or No.

Heuristic	Admissible (Yes/No)	Consistency (Yes/No)
H1		
H2		
H3		
H4		

- 2) Dominance of Heuristics. Remember that domination has a special meaning in the context of heuristic functions. What does it mean that a heuristic function dominates another one? Write the definition of dominance of heuristics.

Now your task is to investigate the dominance relationship between H1 – H4.

- 3) Do heuristic functions H3 and H4 have a dominance relationship?  
 4) Is there a dominance relationship between Heuristic function H4 and H1?

## PROBLEM 6 (Propositional Logic) 10 POINTS

Four bunny rabbits played together in the forest. Each bunny is either brown or white.

However, none of them could see each other very clearly, and their views were obscured by bushes.

Bunny 1 says, "One of bunnies 2 & 3 is brown and one is white, but I can't tell which."

Bunny 2 says, "One of bunnies 3 & 4 is brown and one is white, but I can't tell which."

Bunny 3 says, "Bunny 4 is brown."

Bunny 4 says, "It is not the case that both Bunny 1 and Bunny 4 are brown."

Bunny 1 asks, "Is it true that I am a white bunny rabbit?"

Converting these statements into propositional logic and using resolution refutation, can we answer the question of Bunny 1? Use  $B_i$  for "Bunny  $i$  is brown", e.g.,  $B_2$ : Bunny 2 is brown.

Show all the steps you have taken to prove/answer this question.

## PROBLEM 7 (GAME THEORY) (10 POINTS)

This problem is about watering rice farms in Sumatra. Two farms are located in the riverside, upstream and downstream farms. Water is not sufficient---meaning if both farmers water their rice crops at the same time the upward one gets enough water but the downstream one is not watered sufficiently. However, if they don't water their crops at the same time, both farms will suffer from a pest problem.

The game is about the timing of watering. Assume two possible times for watering, A and B.

Let  $x$  represent the utility loss for the farmer who gets reduced water and let  $y$  represent the loss in utility due to pests. Assume that when there is no crop loss due to lack of water or a pest problem, then the payoff is equal to 1.

1. Draw the payoff matrix using A and B as actions. Use  $x$  and  $y$  to define the payoffs for the upward and downward farms.
2. Under which conditions does a strongly dominant strategy equilibrium arise?

## PROBLEM 8 SHORT QUESTIONS

1. In some environments randomized behaviour can be rational. Describe what type of environments and give an example.

2. Entailment for first-order logic is semidecidable. What does this mean? Explain very briefly.
3. Convert this sentence into Conjunctive normal form and show all the steps in this process:  
 $\forall Y (\forall X \text{ taller}(Y,X) \vee \text{wise}(X)) \Rightarrow \text{wise}(Y)$

5 Fill in the blank so that the sentence becomes correct.

A entails B if and only if ( . . . . . ) is unsatisfiable.

## PROBLEM 9 (LOGIC) (10 points, 2 point each)

Translation from English to Logic.

- 1) There is a mouse that every cat chases.
- 2) For every flavor, there is some person who likes that flavor.
- 3) "There was no student who scored 100 on every quiz."
- 4) There is a barber who shaves all men in town who do not shave themselves.
- 5) There exists a lawyer all of whose clients are doctors



**OPPGAVE 1 (True/False questions) (20 pts, 2 pts for each correct answer, -1 for each wrong answer. Total points will not be less than zero)** *Mark each of the following sentences either as True or False*

1. True or False: Greedy best-first search algorithm is guaranteed to find an optimal path.
2. True or False: Uniform Cost algorithm is guaranteed to find the optimal solution when all step costs are greater than zero and the branching factor is finite.
3. True or False: Let  $b$  be the branching factor of a search,  $d$  the depth of the solution, and  $m$  the maximum depth of the search space. Then the complexity of breadth-first search is  $b^m$ .
4. True or false:  $(A \iff B) \models (\neg A \vee B)$
5. Linear planning is incomplete.
6. Simple “hill climbing” algorithm is perfect to solve constraint satisfaction problems.
7. A sound logical reasoning process is not necessary in order to pass the Turing test.
8. Depth-first tree search algorithm always expands at least as many nodes as an A\* tree search algorithm with admissible heuristic does.
9. The set consisting of “mammal” and “non-mammal” categories is both a disjunctive and an exhaustive decomposition of the category “animal”.
10. Explainability is an ethical problem in AI which domain knowledge may help to solve.

**OPPGAVE 2 (First Order Logic) (15pts – 7-3-5)**

The Knowledge base has the following sentences for which FOL representations are given below.

Everyone who loves all animals is loved by someone.

Anyone who kills an animal is loved by no one.

Sofie loves all animals.

Either Sofie or CarAccident killed the cat, who is named Kismet.

*FOL representations:*

1.  $\forall x [\forall y [\text{Animal}(y) \Rightarrow \text{Loves}(x,y)]] \Rightarrow [\exists z \text{Loves}(z,x)]$
2.  $\forall x [\exists y (\text{Animal}(y) \wedge \text{Kills}(x,y)) \Rightarrow \neg(\exists z \text{Loves}(z,x))]$
3.  $\forall x [\text{Animal}(x) \Rightarrow \text{Loves}(\text{Sofie}, x)]$
4.  $\text{Kills}(\text{Sofie}, \text{Kismet}) \vee \text{Kills}(\text{CarAccident}, \text{Kismet})$
5.  $\text{Cat}(\text{Kismet})$

*Query:* Did CarAccident kill the cat?

You are going to answer the above query by using resolution by refutation.

1. First convert all FOL sentences into conjunctive normal form (CNF). Show every step in this process.
2. Write down any background knowledge that is needed to solve the problem
3. Apply resolution by refutation and show how the query is answered. Show each and every unification.

### **OPPGAVE 3 - A\* search algorithm (13 pts, 1-4-4-4)**

1. Apply A\* algorithm for graphs on the graph in the following figure (Figure 1). Write down the nodes in the order they are expanded. A is the start node, and G is the goal node.
2. What is the returned path? Is it optimal? explain your answer on an example from the given graph in the figure.
3. Modify the pseudocode in the figure (Figure 2) for A\* algorithm for graph search so that it guarantees to find the optimal solution with heuristic values given in Figure 1. Write down the pseudocode in a separate paper starting from the sentence just before your modification starts, and ending with the sentence right after your last change. That is, you don't need to write the whole pseudocode, only the part you modified, plus a single/one original sentence before and one after your modified sentences.
4. Assume that a search tree has heuristic values which enable the A\* algorithm presented in the pseudocode (the unmodified version in figure 2) to find an optimal path to the goal. Would the A\* algorithm still be guaranteed to find the minimal path to the goal if there are negative transition costs? This question is general, not about the problem presented in Figure 1.

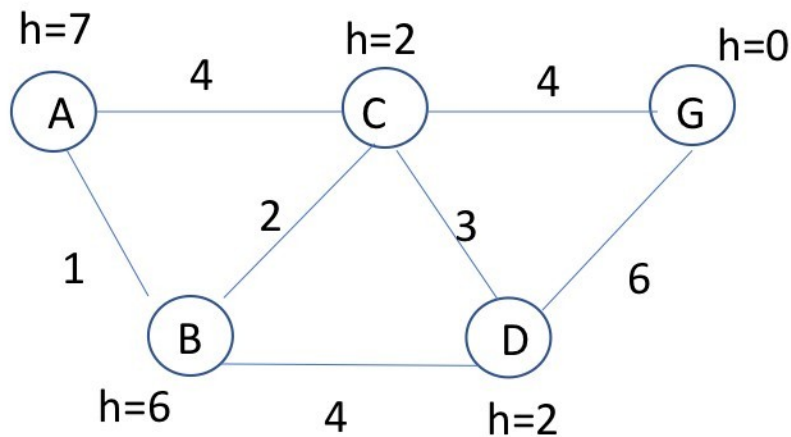


Figure 1 Graph for the question. A is the start node, and G is the goal node.

- ```

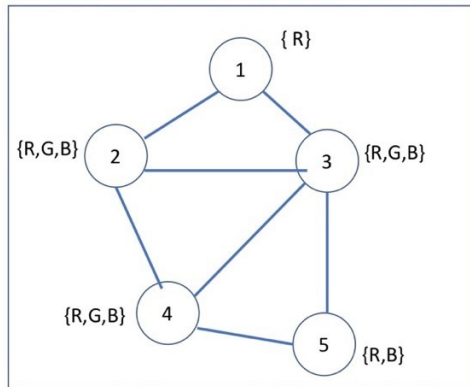
5.  WHILE FRONTIER is not empty
6.      N = FRONTIER.popLowestF()
7.      IF state of N= GOAL RETURN N
8.      add N to CLOSED
9.      FOR all children M of N not in CLOSED:
10.         M.parent = N
11.         M.g = N.g + cost(N,M)
12.         M.h = heuristic(M)
13.         add M to FRONTIER
14.     ENDFOR
15.  ENDWHILE
  
```

Figure 2 .Pseudocode for A\* algorithm.

## OPPGAVE 4 - CONSTRAINT SATISFACTION (12 pts, 2-4-2-4)

Consider the following constraint graph (in the figure) for a graph coloring problem where the constraints mean that the connected nodes cannot have the

same color. The variables are shown inside the nodes while the domains are shown next to each variable node.



1. What are the domains after a full constraint propagation using an arc consistency algorithm?
2. Show the sequence of variable assignments during a pure backtracking search (don't assume that propagation above has been done). Assume that the variables are examined in numerical order and the values are assigned in the order shown next to each node. Show assignments by writing the variable number and the letter for the value, e.g, 5R, 2G.
3. Describe how forward checking works.
4. This time you'll apply backtracking search with forward checking. Use the same ordering convention for variables and values as above. Show the sequence of variable assignments during backward search with forward checking. Again, show assignments by writing the number of variables followed by the letter for the value.

## OPPGAVE 5 – Game Theory (10 pts, equal points for each question))

Consider the game for which the payoff matrix is shown in the following figure.

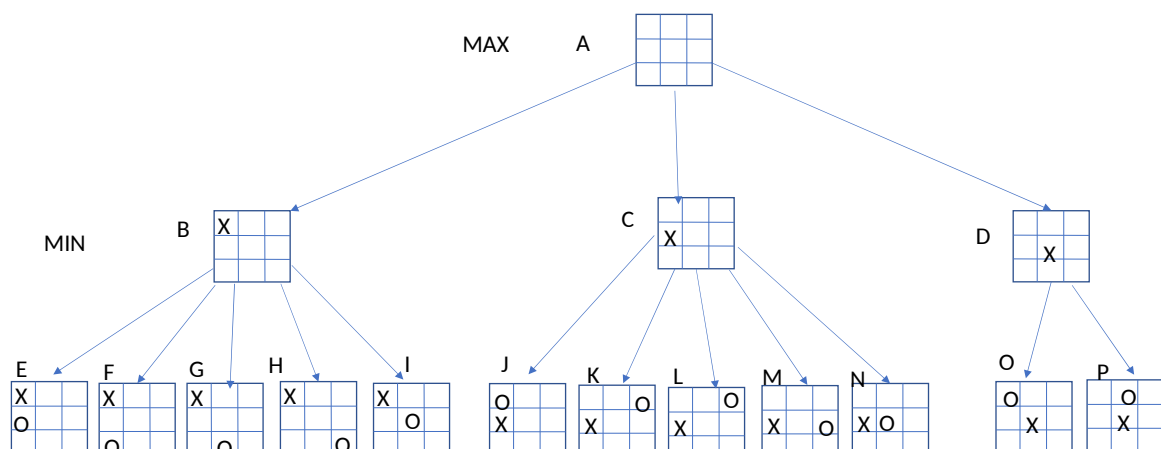
|               |    |               |      |
|---------------|----|---------------|------|
|               |    | <i>agent2</i> |      |
|               |    | G             | NG   |
| <i>agent1</i> | H  | 8, 0          | 3, 1 |
|               | NH | 4, 4          | 2, 3 |

Figure 3 Payoff Matrix.

1. Identify any *dominated* strategy. Explain your answer.
2. Find the *Nash equilibrium*. What are the equilibrium payoffs, i.e., values for each agent?
3. Are there any *pareto optimal* joint actions? If any exists, what are they?
4. Explain (in general, not for this particular problem) why a *social welfare maximizing* joint action profile is also pareto optimal.

## OPPGAVE 6 - ADVERSARIAL SEARCH (10 pts, 3-3-4)

Consider a tic-tac-toe game on a 3x3 grid (see the figure below) where players MAX and MIN take turns marking the spaces in a 3×3 grid by placing their X's and O's, respectively. The player who succeeds in placing three of their marks in a horizontal, vertical, or diagonal row is the winner.



The values of the terminal nodes have not been provided. You will compute these values using an evaluation function  $e$ . Function  $e$  uses a heuristic that estimates the value of each terminal node according to the following formula:

$e(\text{node}) = E1 - E2$  where

$E1$  = sum of the number of rows, columns and diagonals that are possible winning situations for Max and,

$E2$  = sum of the number of rows, columns and diagonals that are possible winning situations for Min.

The following figure shows examples for computing the values of some hypothetical nodes:

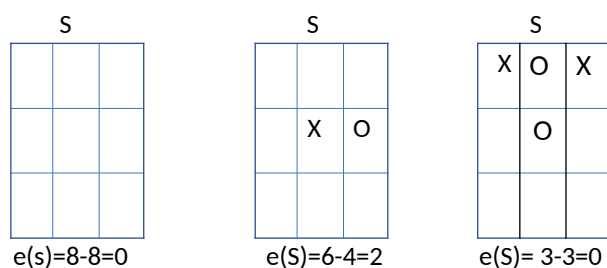


Figure : Example on estimation the values of terminal nodes

1. Compute and write down the values of each terminal node node, i.e. of E, ..., P.
2. Using the *Minimax* algorithm find and write down the values of the remaining nodes(A,...D) in the search tree. Which action will Max play in this game, the action whose outcome is B, C or D?
3. Is it possible to prune any nodes using the *Alpha-Beta pruning* algorithm? If there are any, write down the prunable node(s) - i.e., write the letter for the node.

## OPPGAVE 7 - SHORT QUESTIONS (20 pts, 2 pts for each question. Plus 2 points for correct answer to the “bonus”/voluntary question.)

1. How is the goal information represented in simple reflex agents?

2. Is the PL sentence  $((P \rightarrow Q) \wedge Q) \rightarrow P$  valid, unsatisfiable or satisfiable? Justify your answer.
3. Translate the following sentence into predicate logic:  
“Any person who has an umbrella is not wet”
4. Translate the following sentence into predicate logic:  
“John has at least two daughters.”
5. Assume a Hill Climbing algorithm that aims to find the best state according to a heuristic cost function. Does it try to find the global minimum or the global maximum?
6. It has been suggested that the first phase of *GraphPlan* be used as a heuristic function for forward search in the following way: Given a state  $s$  and goal  $g$ , run the graph-construction phases of *GraphPlan* until all the components are represented and not mutex in the last layer. Let  $n$  be the number of action layers in the graph. We will let  $n$  be the heuristic value for  $s$ . Is this an admissible heuristic? Explain your answer.
7. If *GraphPlan* terminates with a successful, 3-action plan in the first iteration, what constraints are there on the order in which the actions must be executed?
8. Does *Regression Planning* work in a forward or backward manner?
9. You will represent the concept of “student” using a *frame-based* knowledge representation language. You want the age of a student to be computed on the basis of her birth year and the current year. How would you represent this in a slot of “student” frame?

10. Assume a version of the original vacuum cleaner agent in the textbook. 10% of the time the SUCK action of this one does not clean the floor if it is dirty and even may deposit dirt on the floor if the floor is clean. Classify this environment with respect to each of the following dimensions:  
Sequential/Episodic, deterministic/stochastic, and dynamic versus static.
11. BONUS QUESTION: Assume that *Simulated Annealing* search algorithm starts from a state  $S_0$  in the middle of a large plateau. That is, the values of all states on the plateau are exactly the same. Assume also that in the first step the random neighbor we picked is  $S_1$ , which has the same value as  $S_0$ . Will Simulated annealing move to  $S_1$ ? Explain your answer mathematically (i.e. using a formula). No points will be given otherwise.



**NOTE:** The workload in this exam was too high and I did some adaptations/adjustments in grading so that the final grades were comparable with the previous years' grades. Pinar, November 2021

## **QUESTION – SEARCH** (25 points)

In the year 2100 humanity has branched out to many star systems in the Milky Way Galaxy. The decennial (10-yearly) human conference is being held soon, and you have been chosen as the ambassador of your star system. You are in star system S and have to travel to star system G, where the meeting is being held (strangely, we still haven't figured out how to remotely attend meetings despite being an interstellar species). The map of the nearby star systems are shown in Figure 1.

a) This task is about problem formulation. You are expected to formulate the problems described in the task using the “Well-defined problems and solutions” approach described in Chapter 3 in Russell and Norvig. Note that you are NOT expected to find a solution to the problem in a), you only need to write up the problem formulation.

Represent the following problem using the aforementioned method:

This is your first time representing your planet as an ambassador and you don't want to show up late, so you need to find the fastest route to get there, i.e the one taking the shortest amount of time. You therefore formulate the task as a search problem. Fill out the rest of the problem formulation by specifying the States, Actions, Path cost, Initial State, Transition model and Goal test such that the problem formulation can be used with A\* to find the quickest path.

- Initial\_state:
- States:
- Actions:
- Path\_cost:
- Transition\_model:
- Goal\_test:

b) A\* algorithm: Given the heuristic values presented in Figure 1, find the least costly path to star system G using the graph version of the A\* algorithm. Tie breaks are solved in alphabetical order. Show the Frontier and Explored list in each step, as a table. Note that this question does not depend on your answer to a).

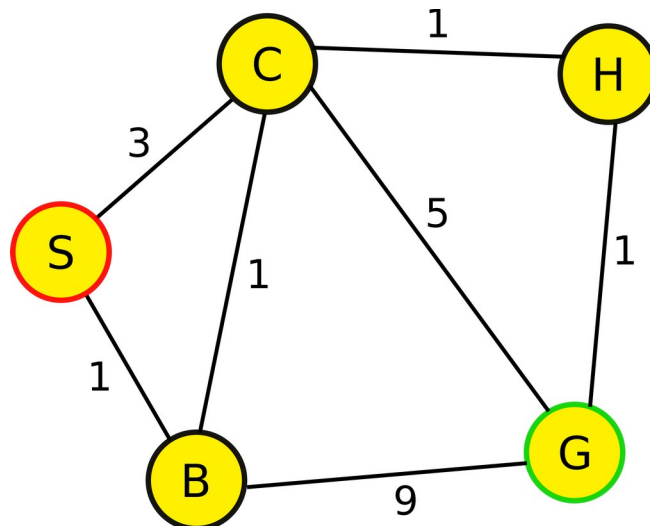


Figure 1. Figure for A\*

$$H(s) = 5$$

$$H(b) = 4$$

$$H(c) = 1$$

$$H(h) = 1$$

$$H(g) = 0$$

- c) A\* algorithm: Is the path you found above the optimal route to star system G? If it is not optimal can you make it optimal by changing one or more heuristic values? If it is not possible explain why, if it is possible show how.

- d) Minimax algorithm: When you arrive at star system G you take out your speech to look it over one last time, but then an unknown life form grabs your speech and runs off with it. You chase after the life form. Fortunately, one of the organizers saw what happened and helps you. Eventually, you are able to corner the life form in a room as shown in Figure 2. The organizer knows that this particular type of alien loves “bluuurgh”, a spiky type of food. In the figure, Y is you, O is the organizer, the green thing is the life form, and the blue one is food.

Now a turn-based game will be played that has the following rules:

1. The life form moves either Left, Right, Up or Down.
2. You move either Up or Right
3. The organizer moves either Down or Left.
4. Everyone must make a move.

If the alien life form enters the square with the bluuurgh in it, it gets a reward of +10. If either you or the organizer enters the same square as the alien life form you will then catch it and get the speech, giving the alien life form a reward of -30. The game ends when you’ve either caught the alien life form or everyone (i.e., each of you, organiser and the life form) has made one move. Construct a minimax tree for the situation described with this order of players: Alien Life form, You, and

Organizer. The alien life form is the maximizer and you and the organizer are both minimizers.

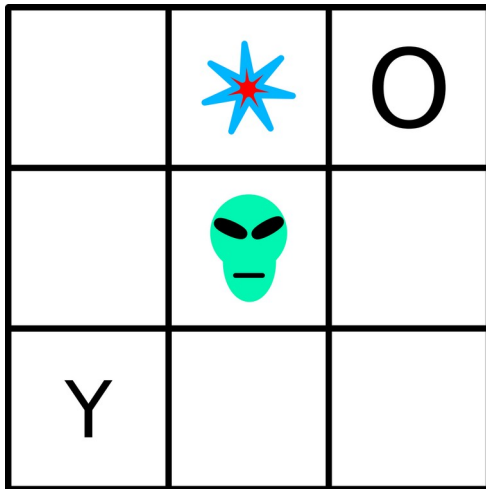


Figure 2. Figure for Minimax alg

e) Alpha-Beta pruning: Use minimax algorithm with alpha-beta pruning on the tree given in Figure 3. Successor nodes are examined from left to right.

- Which nodes, if any, are pruned?
- Which move ordering prunes the most nodes?

**Def:** Move ordering is the order that successor nodes are examined.  
Changing the move ordering does *not* change the parent-child relationships between any nodes.

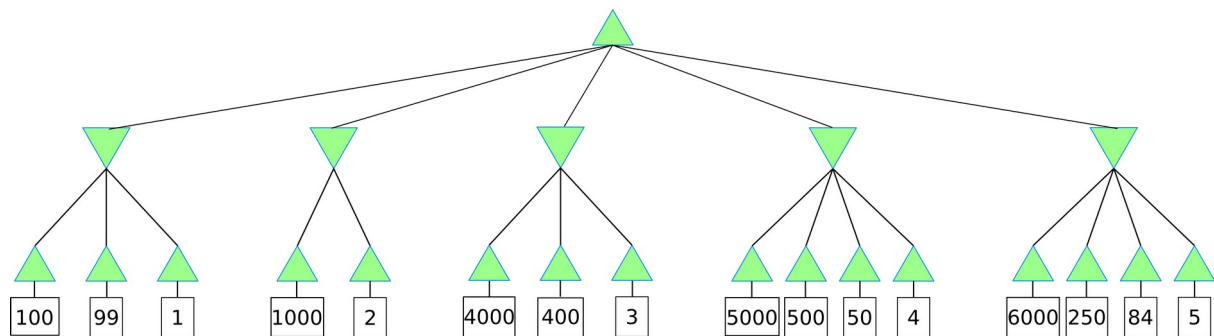


Figure 3. Figure for Alpha-Beta pruning

f) Breadth-first search: Having arrived in the meeting star system you must now find the planet where the meeting is being held. Use breadth first graph search to find a path from the starting planet S to the meeting planet G and show the node

expansion order. Tie breaks are solved alphabetically. Write down the path found by breadth first graph search. Is this the optimal path?

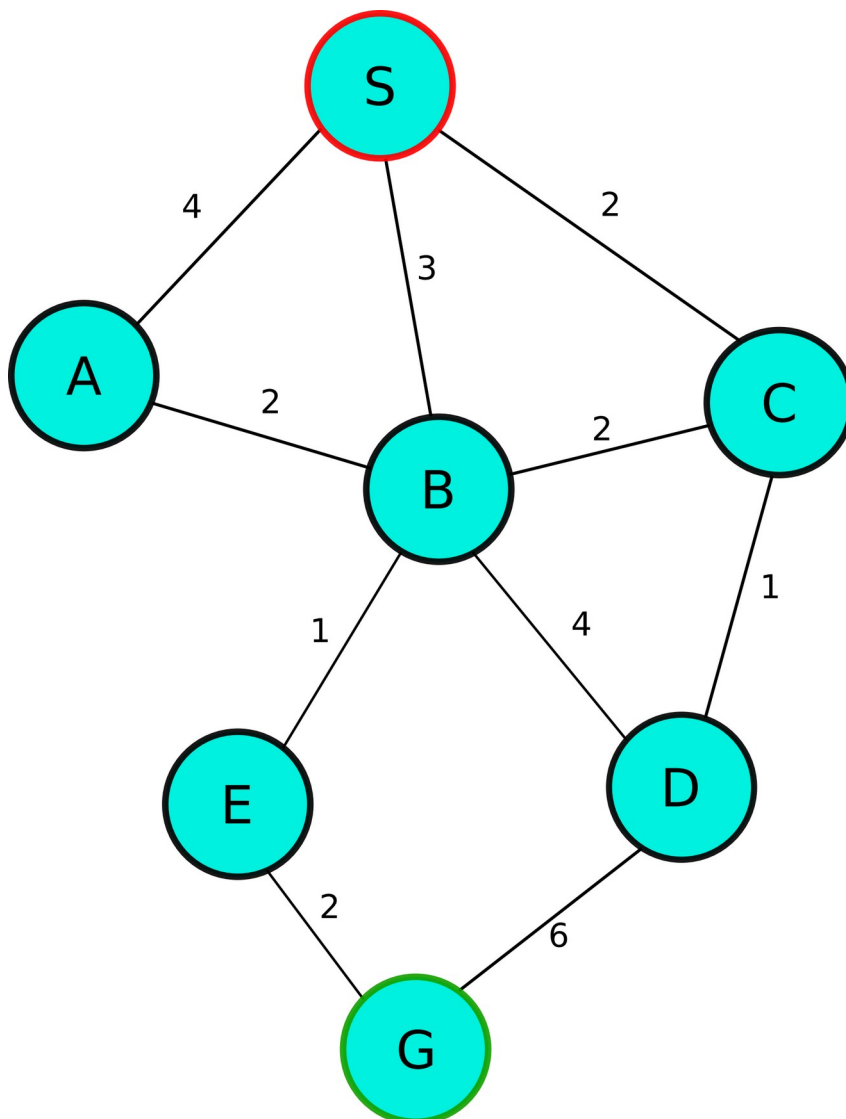


Figure 4. Figure for Breadth-first search

## QUESTION – LOGIC (total 25 points)

In this exercise you will be solving tasks related to a Cave Spelunking game on a 2D board, shown in Figure 5. In this game every square on the 2D board can contain Lava, Diamonds, one and only one Player, Sparkles, and Red Glow or nothing. To win the game the player must find every diamond on the board by moving to every Diamond square. If you move into any lava square you lose the game. Every square that is vertically or horizontally

adjacent to a lava square has a Red Glow, while every square that is vertically or horizontally adjacent to a diamond square Sparkles. The Player starts at a specific location in each instance of the game.

Please note that although these problems are thematically similar they can all be solved independently of each other, that is, the answer to one question never depends on the answer to another question.

- a) Your first task is to represent the following board state in either propositional or predicate logic. You should pick whichever logic you prefer and comment on your choice, explaining why you prefer one logic over the other for this use case – the question is not looking for a specific answer, but rather for you to show that you are able to reflect and justify your decision. Please specify the semantic meaning of the symbols you use.

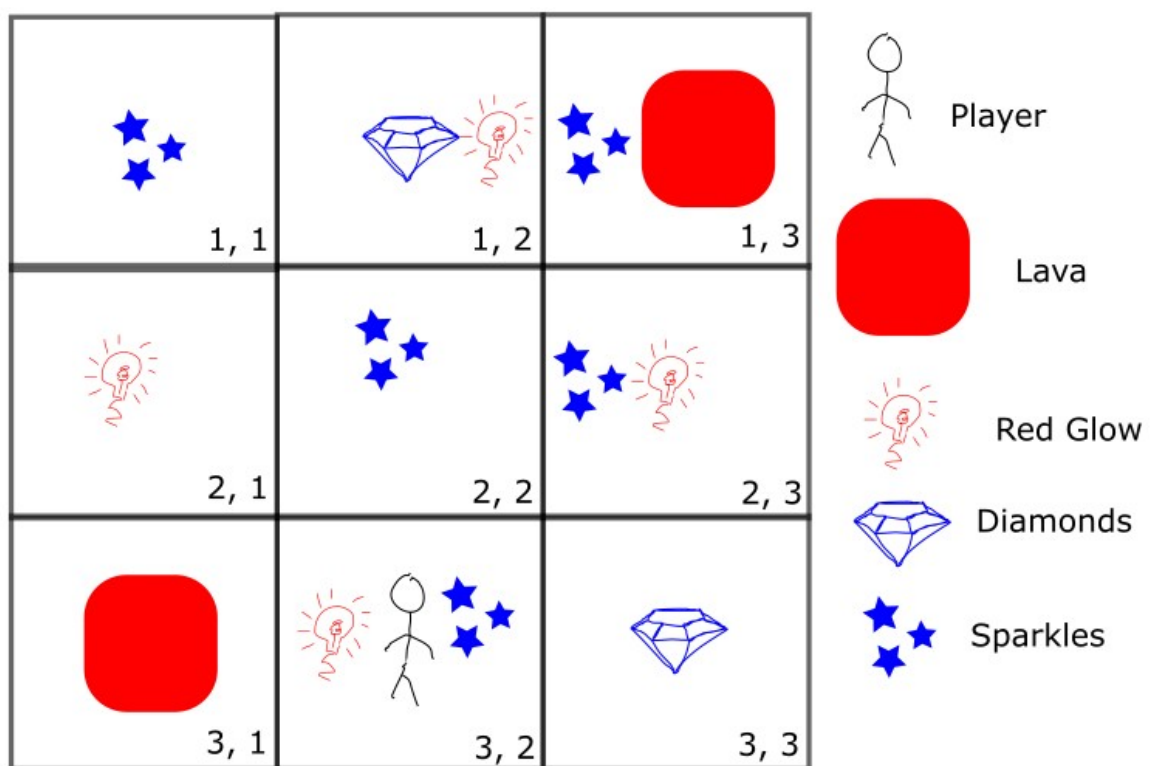


Figure 5. Figure for Logic quest (first task)

- b) The following is an (incomplete) set of rules for the Cave Spelunking game expressed in natural language. Express them using predicate logic and explain the semantic meaning of the symbols you use if it is not obvious (i.e. if you called something *Cactus(x)* you would have to explain what this means). You do not need to consider temporality; the question wants you to represent the sentences in predicate logic and not in a logic where they may be applied sequentially.

1. Every square adjacent to a diamond sparkles
  2. Every square adjacent to lava has a red glow
  3. If the player is in the same square as lava the game is over
  4. If the player finds every diamond in the game the player wins – that is, there is no squares left with any diamonds
  5. If the player is in the same square as a diamond the player has the diamond
  6. The player can only move to a square adjacent to a square that has Red Glow if the square is also adjacent to a square that has Sparkles.
  7. The player can only move to squares adjacent to the square the player is currently in.
- c) Given the rules of the Cave Spelunking game as specified in (b), is it possible for the player to win given the board Figure 6. Explain why/why not. You may assume the player always takes the best action it is allowed to given that they have to follow the rules in (b). Please also ignore the fact that propositional logic is not a temporal logic and that it is a monotonic logic.

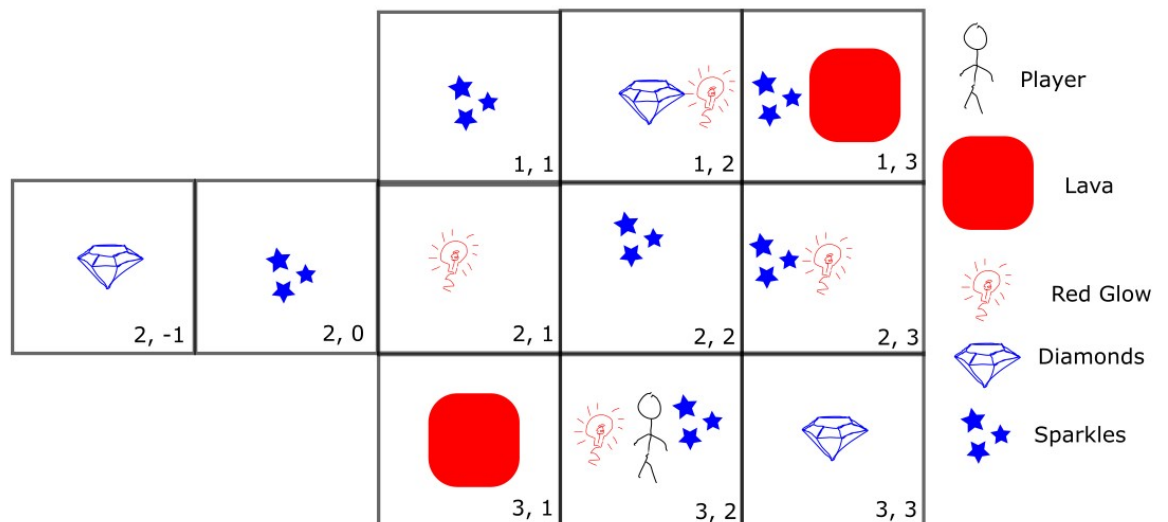


Figure 6. Figure for Logic Quest, Task c.

- d) The following problem does not use any rules mentioned earlier. Given the following sentences in propositional logic, translate the sentences to CNF and use resolution refutation to prove the sentence “Richard does not mine diamonds”. When you convert the sentences to CNF explain every step you do.

Rules:

- a.  $Afraid(Richard, Lava)$
- b.  $Person(Richard)$
- c.  $\forall x \forall y (Person(x) \wedge Afraid(x, y) \Rightarrow \neg Close(x, y))$
- d.  $Close(Diamonds, Lava)$
- e.  $\forall x \forall y \forall z (Close(x, y) \wedge Close(y, z) \Rightarrow Close(x, z))$
- f.  $\forall x \forall y (Close(x, y) \Rightarrow Close(y, x))$

$$g. \quad \forall x (CanMine(x, Diamonds) \Rightarrow Close(x, Diamonds))$$

Intended interpretation:

Richard= A name of a human

Lava= Very hot rock, deadly

Diamonds= Precious gemstone

Afraid(x, y)= x is afraid of y

Close(x, y)= x is close to y

CanMine(x, y)= x can mine y

Person(x)= x is person

- e) For each of the following sentences, write whether the sentence is valid, satisfiable, or neither. Comment/explain on your answer with one sentence (you do not need a detailed explanation, just make it clear how you reasoned).
- $RG$
  - $RG \wedge \neg RG$
  - $RG \vee \neg RG$
  - $RG \Rightarrow RG$
  - $RG \Leftrightarrow D$
  - $\neg(RG \Leftrightarrow D)$
  - $((RG \vee D) \wedge \neg(RG \wedge D)) \Rightarrow RG$

## QUESTION - CONSTRAINT SATISFACTION

Assume five classmates, Rudolf, Anette, Peter, Daisy and Femke, from NTNU has moved to Oslo and as part of their house decoration each bought a plant. It is also known that the plants are either in the Philodendron or the Calathea category. You also know that the plants the classmates own are one of these: Phil1 or Phil2 from the Philodendron category, or Calat1, Calat2, or Calat3 in the Calathea category. We also know that the colour of the leaves of the plants can be light green(LG), dark green(DG), yellow(Y), blue(B), and variegated(i.e., more than one colour,V).

**Each person has a different colour and a different plant than all the other 4 friends.** For example if one has a LG coloured plant, none of the others can have a LG coloured plant. Similarly. if one has a Calat2 plant, then none of the others can have a Calat2.

**The CSP problem: You want to find out which person may have what kind of plant, i.e., which plant and its colour.**

You know somethings about the favorites of these people, which is shown in Table 1, which you must take into consideration when solving some of the following tasks.

Table 1. CSP problem, domains

| Person               | Peter                   | Anette          | Rudolf                  | Daisy           | Femke                               |
|----------------------|-------------------------|-----------------|-------------------------|-----------------|-------------------------------------|
| Preferred clour      | LG                      | V, B, DG        | V, B                    | V, B            | V, DG, Y                            |
| Preferred plant type | Calat1, Calat2<br>Phil1 | Phil2<br>Calat3 | Phil1, Phil2,<br>Calat1 | Calat1<br>Phil2 | Phil1<br>Calat1<br>Calat3<br>Calat2 |

In addition, you know that:

- Those persons who have Blue as favourite color and Phil2 as their favourite plant do not want any other blue coloured plant or any Phil2 with any other colour.
- Daisy and Peter have a plant in the same plant category (i.e, both have either Philodendron or Calathea)
- Anette and Femke also have a plant in the same plant category.

1. After learning that “Those persons who have Blue as their favourite color and Phil2 as their favourite plant don’t want any other blue coloured plant and any Phil2 with other colour”, you can reduce the domains of some people immediately. Write down the domains for all variables taking into consideration this information. Use the notation where a value in a domain is a pair of color and plant type (eg. LG-Calat1).
2. Draw the **search tree** (complete the one below) that results from applying **backtracking search with forward checking**. Don’t do&show the complete search tree but only for the assignment of LG-Calat1 and LG-calat2 for Peter. Use the reduced domains you made in task 1 and assign the variables in the order shown in the tree below (i.e., Peter, Anette, Rudolf, Daisy, Femke). For each variable assign the values like this: first color and first plant type (i.e., pair of colour and the plant type) , then the first colour and the second plant type, etc. where the order of the colours is **LG, V, B, DG, Y**, and the order of plants is Calat1, Calat2, Calat3, Phil1, Phil2. Complete the search tree in the figure 7.
3. Draw the search tree that results from applying **backtracking search with forward checking and propagating the check through domains that are reduced to singleton domains**. That is, if a domain with a single value appears during the consistency



check after assignment of a variable, then the check propagates along this domain for all unassigned variables. Use the domains found above, in 1. Draw the search tree STARTING WITH FIGURE BELOW Figure 7.

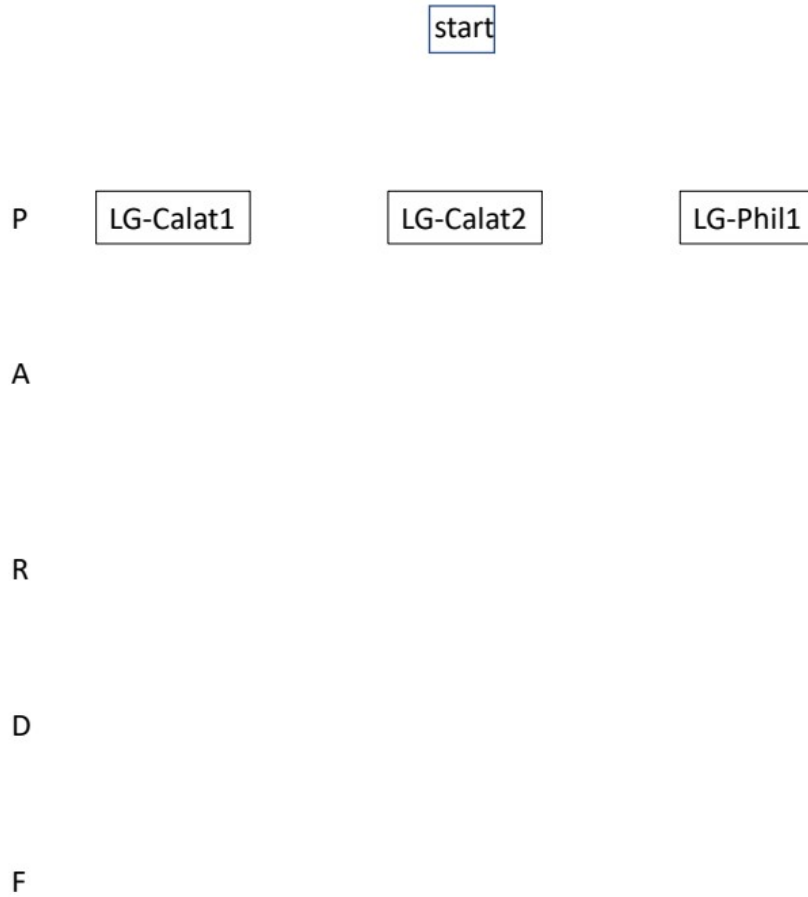


Figure 7. CSP problem. Complete this search tree

## QUESTION –PLANNING

1. An agent has a task of painting two chairs, A and B, and stacking A on top of B. A Chair is “free” ( i.e.,  $\text{Free}(A)$ ) if there is nothing on it preventing it being painted

(e.g., nothing is on top of it). The agent has three types of actions, *sand*, *paint*, and *putOn*:

*sand* (x)

precondition: *Free*(x)

postcondition: *Smooth*(x)

*paint*(x)

precondition: *Smooth*(x), *Free*(x)

postcondition: *Painted*(x)

*putOn*(x,y)

precondition: *Free*(x), *Free*(y)

postcondition: *On*(x,y),  $\neg \text{Free}(x)$ ,  $\neg \text{Free}(y)$

In Figure 8 you see a partially-ordered plan that is not correct because it has some problems/flaws.

- Give at least 3 reasons why it is not correct. In case an action is the cause of more than one flaw, write each one as a separate flaw and number them as Flaw 1, Flaw 2, ..... in a list
- For each flaw write the plan operation that is needed to resolve the flaw.
- Write down the final plan a semicolon between the actions in the plan where the action on the left of a semicolon will be executed before the one on its right. When the order of two actions are not important, write them within a parenthesis with an "AND" between them, e.g., (action-x AND action-y). Hence a plan may look like this:

action-z ; (action-x AND action-y) ; action-m.

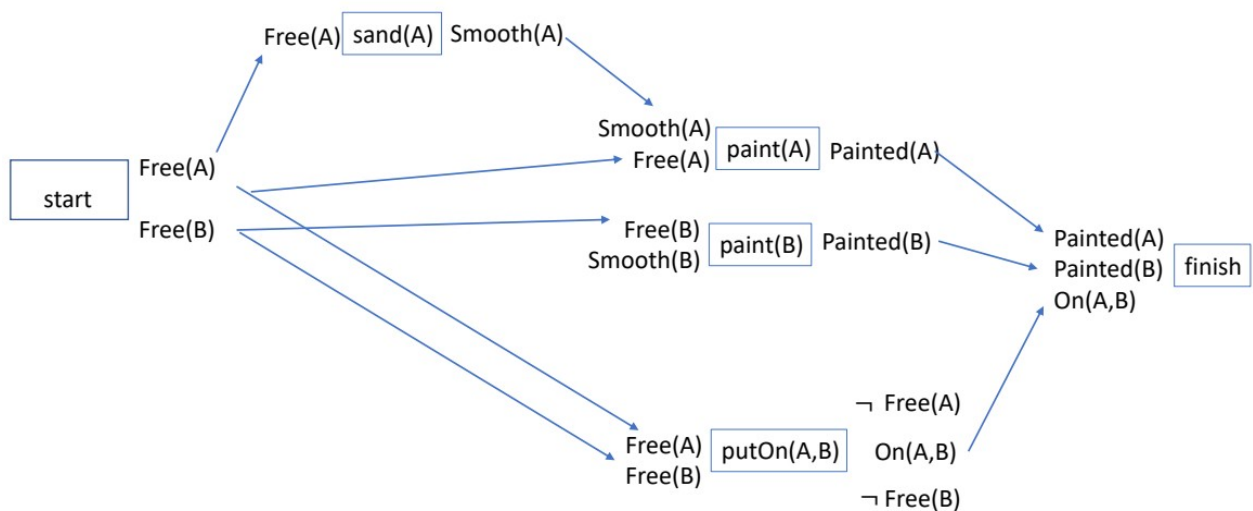


Figure 8. Figure for planning

2. This question is independent from the preceding one. Assume that the GraphPlan algorithm successfully generates a plan in one action layer only, and there are 3 actions in that plan. What kind of constraints may be there regarding the order of the execution of these actions?
3. This is a planning problem and is domain independent. In the given planning problem the goal is:  $C \wedge D$   
There are two action schemas, specified below.

Action: tik

Precondition: none

Postcondition: C, D

Action: tak

Precondition: none

Postcondition:  $D, \neg A$

- a) Find the solution that Partial-order planner returns, and write it down. If there are more than one solution write down each as an alternative plan. Show the planning process on a figure.
- b) Find the solution that the GraphPlan algorithm would return, and write it down. If there are more than one solutions write down each as an “alternative plan”. Show the planning process on a figure.
- c) What is the main reason for the two planning methods’ behaving differently in this particular planning problem/case.

## QUESTION - GAME THEORY

- 1) Fifty students taking TDT4136 are asked to choose an integer between zero and hundred. They will play a game where the payoffs are calculated like this: If a

number  $0 \leq k \leq 100$  is chosen strictly more times than all other numbers, then the students who chose  $k$  will get a Freia Milk Chocolate plate while others get nothing. If no number was chosen strictly more times than any other number, nobody gets chocolate.

- a) How will you represent this story in Game Theory? Since you cannot show the payoffs in a matrix, use a function to represent utilities.
- b) What is the Nash equilibrium (of equilibria if more than one) of this game if there is any? Explain your answer/reasoning.

2) A game with two agents has the payoff matrix shown in Figure 9.

|         |   | Agent 2 |       |
|---------|---|---------|-------|
|         |   | A       | B     |
| Agent 1 | A | 9, 9    | 12, 7 |
|         | B | 0, 20   | 8, 8  |

Figure 9. GT. Task 2, Find pareto etc

- a) Find the pareto optimal strategy of the game. Write down all if there are more than one.
- b) Write down the social optimum strategy. Write down all if there are more than one.

3) Two agents are playing a game where the payoff matrix is shown in Figure 10:

|        |   | Agent2 |       |       |
|--------|---|--------|-------|-------|
|        |   | S      | T     | R     |
| Agent1 | a | 0 , 1  | 1 , 5 | 2 , 2 |
|        | b | 2 , 5  | 5 , 4 | 4 , 9 |
|        | c | 3 , 0  | 7 , 4 | 8 , 3 |

Figure 10. GT. Fig for Elimination of dominated strategies

Find the solution of the game through eliminating dominated strategies. Describe every step of elimination.

## QUESTION - SHORT QUESTIONS

### 1. Local search

The goal of the 6-queen problem is to place 6 queens on a chessboard such that no queen attacks any other. A queen attacks any piece in the same row, column or diagonal. We define the rules of this puzzle as follows:

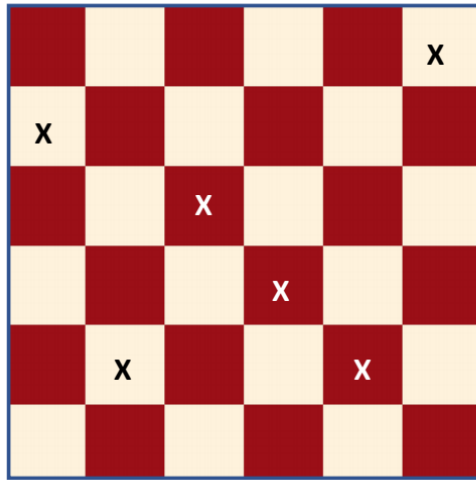
A state consists of a queen in each column. A queen can be moved to another square in the same row. The evaluation function is

$\text{Eval}(s) = 1 - \# \text{ attacking pairs in state } s.$

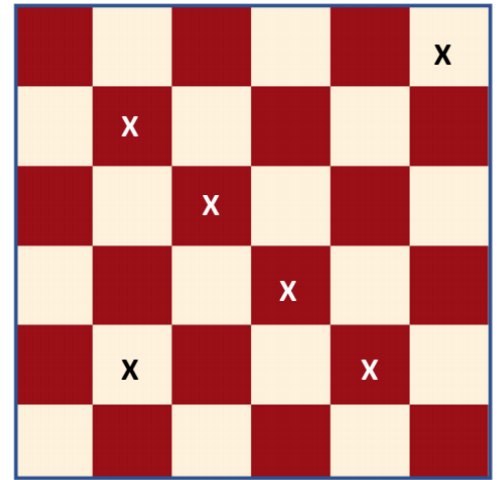
The following figure illustrates two states: the current state (a in Figure 11), and a state that the basic Simulated Annealing algorithm generates randomly as a candidate next state. You need to find out what the algorithm will decide regarding to move or not to the next randomly generated state (b in the figure) from the current state (a in the figure).

- Which values will the Eval function return in the current situation shown in (a) in the figure, and the next state candidate in (b) – i.e.,  $\text{Eval}(a)$  and  $\text{Eval}(b)$ ? Explain how you found the numbers.

- b) With which probability will the SA algorithm accept this move to (b)? Explain your answer and provide a number for the probability, between 0 and 1. Assume the temperature  $T=4$ .



(a) Current state  
(with 5 attacking pairs)



(b) Randomly generated possible next state

6-Queens problem

Figure 11. Figure for local search

## 2. Ethical Issues

One of the approaches to ethics we have seen is the consequentialist approach. How can you connect this approaches to the rest of the syllabus in this course? Explain your reasoning.

## 3. PEAS and Characteristics of the Environment

Consider a problem domain where an autonomous boat is dropping stone blocks into the water to safely detonate hidden mines. Give a PEAS description of this task environment and characterize it in terms of the properties of task environments as defined in Chapter 2 in Russel and Norvig.

## 4. Translation from Semantic Networks to Logic

Translate the semantic network representations shown in Figure 12 to logic representations. Note that an instance is like a member. For example, Clyde is-a (or a member-of) Elephant class/category.

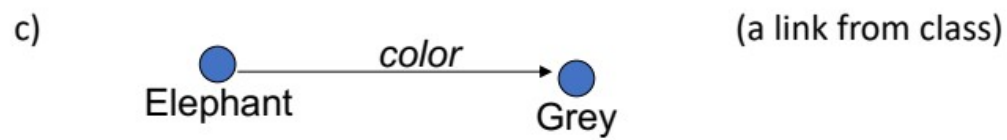
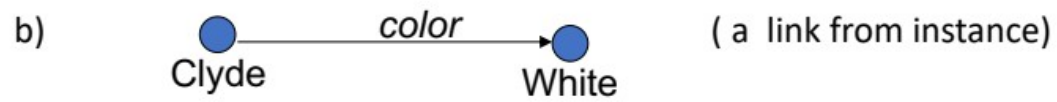
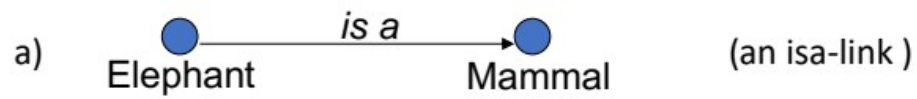


Figure 12. Translation from SN to Logic

## KONT EKSAMEN AUGUST 2021--- QUESTIONS

**Weighting:** There are 5 questions in this exam. The weights are as following: Q1:25 points, Q2:25 pts, Q3: 25pts, Q4: 10pts, and and Q5 15 pts each

### PROBLEM 1 - LOGIC

Given the following three sentences, you will prove  $\neg S$  is true.

$$P \wedge Q \quad (1)$$

$$P \rightarrow \neg(Q \wedge R) \quad (2)$$

$$S \rightarrow R \quad (3)$$

- Show  $\neg S$  is true by using the inference and the re-writing rules.
- Show that  $\neg S$  is true by enumeration method on a Truth Table.
- Show that  $\neg S$  is true by resolution refutation.
- Use resolution refutation to prove  $\text{Green}(\text{Sophie})$  given the information below. You must first convert each(all) sentence into CNF. Clearly show Skolemizations. Show only the applications of the resolution rule that lead to the desired conclusion. For each application of the resolution rule, show the unification bindings,  $\theta$ .
  - $\text{Electric}(\text{Tesla})$
  - $\text{Drives}(\text{Sophie}, \text{Tesla})$
  - $\forall x \text{Green}(x) \leftrightarrow \text{Bikes}(x) \vee [\exists y : \text{Drives}(x, y) \wedge \text{Electric}(y)]$

### PROBLEM 2 --INFORMED AND UNINFORMED SEARCH

You are given the following graph in the figure where S is the start node and there are three goal nodes, G1, G2 and G3. You are asked to use some search algorithms on this graph (algorithms a-d listed below.) You will use tree search versions of these algorithms that avoid re-expanding the nodes that are already expanded. In case of a tie, break will be done in alphabetical order. In all the algorithms, you don't need to continue after finding a goal, i.e, you don't need to search for more than one goal.

For each of the asked algorithms,

- write down the expanded nodes in the order of expansion,
- write down the solution path and its cost.
- Is the found path optimal? Discuss the optimality of the algorithm.



The algorithms are:

- a) Uniform cost search
- b) Breadth first search
- c) Depth first search
- d) A\* search. The heuristic values are as follows:

$h(S)=5$

$h(A)=7$

$h(B)=3$

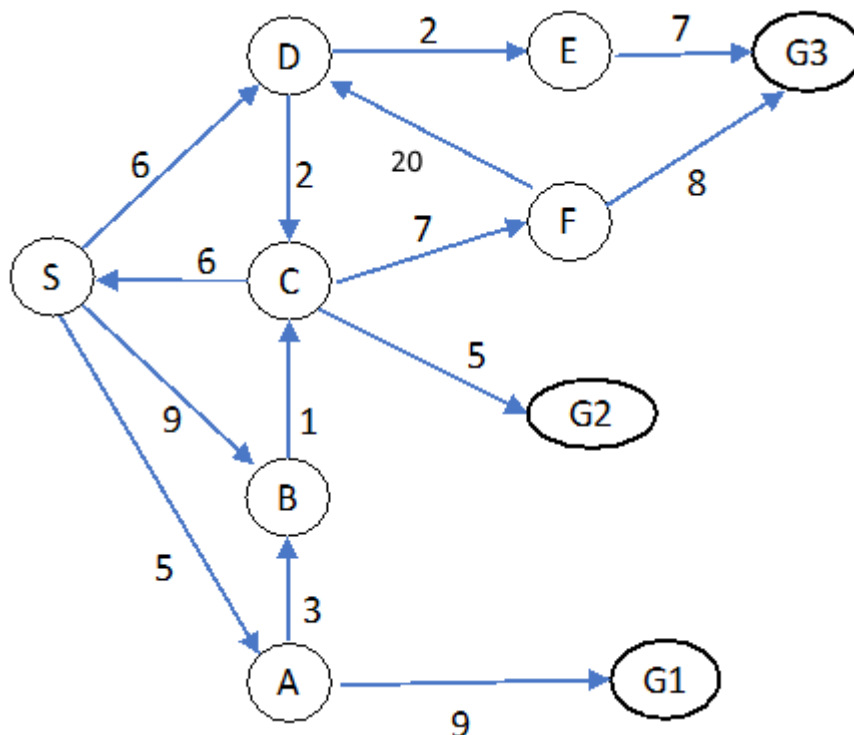
$h(C)=4$

$h(D)=6$

$h(E)=5$

$h(F)=6$

$h(G1)=h(G2)=h(G3)=0$



### PROBLEM 3 ---CSP CROSS WORD PUZZLE

A **crossword puzzle**, is a popular type of [puzzle](#) that uses [words](#).

A crossword is made up of a black/blue and white squares, called a grid. Next to the grid is a list of clues. The answer to each clue is a word. The place in the grid where the answer to

each clue should go is shown by a number and the direction in which the answer appears, for example "1 Across", or "4 Down".

You are given the 4x5 grid on the top of the page. Unlike traditional crossword puzzles, you are not given clues but a list of words to choose from to fill in the grid.

Here is the list of words: *astar, happy, hello, hoses, live, load, loom, peal, peel, save, talk, anon, nerd, tine, ant, oak, old, ten, run.*

There are 4 areas in the grid/puzzle with consecutive white squares where the words will be placed: 1-across (i.e., from left to write), 2-down (write from top to downward), 3-down and 4-across. Blue squares are blocked out meaning that characters cannot be placed on them.

"Instructions" on the grid, e.g., 2-down, indicate the position where a word starts and the direction it will continue until it hits a blue square or the edge of the grid. Note that the number in an instruction does not indicate the length of the word. The length of the word is determined by the number of consecutive white squares in the given direction. For example, the word starting at 1-across is five character long. A solution is a grid with correctly placed words -and no empty white squares. Each word will be used only once.

Consider this as a constraint satisfaction problem and:

- Write down the variables (V1, V2, ..) and describe what they correspond to in the grid shown in the figure. Draw the constraint graph.
- How many constraints are there in this problem and what are they?
- For each variable write down the domain satisfying the node consistency
- Apply arc consistency algorithm AC-3. Write down the domains of the variables after AC. Write down the domains of the variables after AC-3. When applying AC-3, assume a queue (FIFO) of edges of the constraint graph initially sorted in the ascending order, starting from V1, i.e. V1V2, V1V3,.... In order to show your work, fill in the table (similar to the one) in the figure on left.
- If AC-3 finds a solution, what is it? Provide the filled-out crossword puzzle. If it does not find any solution, explain why

|          |          |        |  |        |
|----------|----------|--------|--|--------|
| 1-across |          | 2-down |  | 3-down |
|          |          |        |  |        |
|          | 4-across |        |  |        |
|          |          |        |  |        |

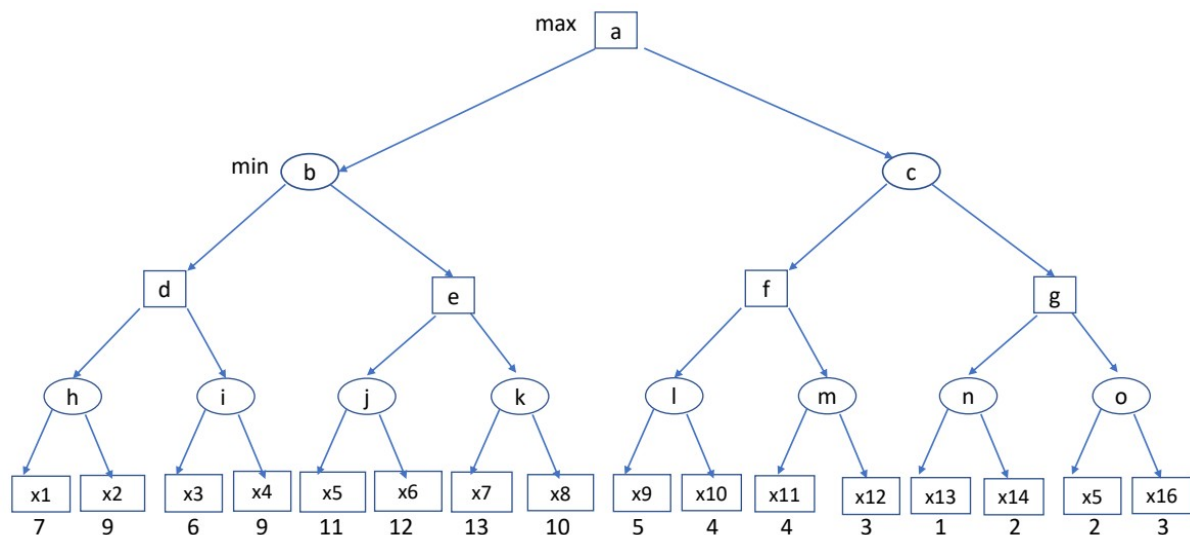
Consider this as a constraint satisfaction problem and:

- Write down the variables (V1, V2, ...), what each corresponds to on the grid shown in Figure xxxxxx, and draw the constraint graph.



## PROBLEM 4 ---- ADVERSARIAL SEARCH

The following figure shows a game tree.



- Apply Minimax algorithm and find the values of all the nodes above the leaf nodes. What is the value of the solution for the agent *max*?
- Apply alpha-beta pruning algorithm to find which nodes can be pruned. Write down the names of the nodes (the letters in the square and ellipses), either leaves or the nodes of which all children are pruned. For example if 11 and 12 are pruned then it is sufficient to write node *j* only.

## PROBLEM 5--- GAME THEORY

In an auction two agents are competing to obtain a porcelain vase. This is a type of auction where **all** bidders simultaneously submit **sealed bids** to the auctioneer so that **no** bidder knows how much the **other** auction participants have **bid**.

The allowed bids are \$0, \$10, \$20, \$30, \$40, \$50.

The porcelain is worth \$40 to the agent A1 and \$30 to the agent A2. The highest bidder wins the porcelain. In case of a tie, A1 gets the vase.

According to the rules of this auction, the winner pays a price  $p$  which is whatever the other agent bids. So, if the value of the porcelain for agent  $i$  is  $x$  and agent  $i$  wins the vase her payoff is  $x-p$ . If she does not win the vase her payoff is zero.

Answer the following questions:

- a. Write down the payoffs of the agents as a matrix – illustrating agents, actions(bids), and the payoffs
- b. Is there a strictly dominant strategy equilibrium of this game? Explain.
- c. Is there a weakly dominant strategy equilibrium of this game? Explain.
- d. What are the action profiles that survive Iterated Elimination of Strictly Dominated Actions? Explain how do the eliminations take place.
- e. What are the action profiles that survive Iterated Elimination of Weakly Dominated Actions? Explain how do the eliminations take place.
- f. What is the solution if the game is solvable using the ‘dominance’ concept. (i.e., dominance solvable). Explain your answer.

# QUESTIONS

## 1) LOGIC (25 pts)

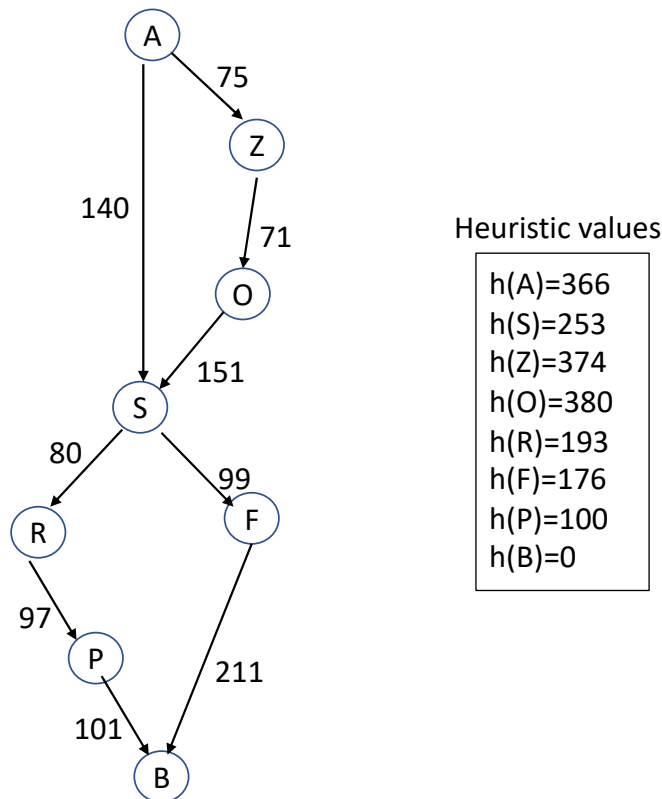
1. Show, using a truth table, that  $\neg a \rightarrow (b \rightarrow c)$  and  $b \rightarrow (a \vee c)$  are logically equivalent. Is  $\neg a \rightarrow (b \rightarrow c)$  valid or satisfiable?
2. Prove that  $A \Leftrightarrow B$  is logically equivalent to  $A \vee B \Rightarrow A \wedge B$ . Use Standard logical equivalence rules here, not the truth table method.
3. Translate the following English sentences into logical representations
  - i. A niece is a sibling's daughter
  - ii. Anette has at most two umbrellas.
  - iii. At least one professor teaches both "Experts in Team" course and an AI course.
4. Convert the following sentence into Conjunctive normal form (CNF). Show every step of the process and write the name of the operation used in the step, e.g., "Eliminate existential quantification".
  - i.  $\forall x (R(x) \rightarrow (\forall y (R(y) \rightarrow R(f(x,y)))) \wedge \neg \forall y (S(x,y) \rightarrow P(y)))$
5. Given the following sentences:
  - 1)  $\forall x,y ( \text{Father}(x,y) \rightarrow \neg \text{Woman}(x) )$
  - 2)  $\forall x,y ( \text{Mother}(x,y) \rightarrow \text{Woman}(x) )$
  - 3)  $\text{Mother}(\text{Sophie}, \text{April})$

Find out if Sophie is not the father of Edgar, using proof by contradiction (resolution refutation). That is, the question is: Is  $\neg \text{Father}(\text{Sophie}, \text{Edgar})$  true?

The first resolution shall be done on the first and second sentences above. Any other solution that does not start with resolving 1 and 2 will not be given any points. Show every operation you have done on/with the sentences, skolemization, standardizing apart, substitution/unification, and the like you may need to do.

## 2) SEARCH (25 pts)

A search problem is represented in the following figure where A is the start and B is the goal node. Costs are shown on the edges while heuristic values for the nodes are shown in the box to the right. In this question solve ties by using left to right ordering, e.g., if there is a tie between R and F in the graph in the figure, then choose R.



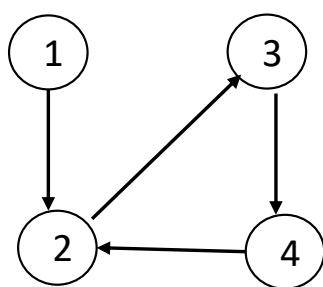
- 1) Write down the expanded nodes in the order they are expanded when Breadth First search algorithm for graph search is applied. Write down the nodes in the frontier at each step. What is the returned solution? Is the solution optimal? Is that expected? Very briefly explain your answer.
- 2) Write down the expanded nodes in the order they are expanded when Depth First search algorithm for graph search is applied. Write down the nodes in the frontier at each step. What is the returned solution? Is it optimal? Is this expected? Very briefly explain your answer.
- 3) Write down the expanded nodes in the order they are expanded when uniform cost search algorithm for graph search is applied. Write down the nodes in the frontier at each step. What is the returned solution? Is it optimal? Is this expected? Explain very briefly your answer.
- 4) A\* graph search algorithm:
  - a) What is the condition to guarantee that A\* search algorithm returns a cost-optimal solution for graph search.
  - b) Is  $h(n)$  for all nodes  $n$  in the graph admissible? If not, write which are not.
  - c) What would the A\* algorithm for graph search return as solution? Write down the nodes in the frontier at each step. Write down the expanded nodes in the order they are expanded. Is the solution cost-optimal? Briefly explain your answer.

- d) What would the same A\* algorithm return for  $h(R) = 227$  instead of 193? Is  $h(R)$  admissible now? What is the returned solution? Is it cost-optimal?
- e) Is your answer in 4 d) inconsistent/contradicts with your answer in 4 a)? Elaborate on your answer and provide a description of the relationship between admissibility and cost-optimality for A\* search algorithm that covers and explains the situation above.

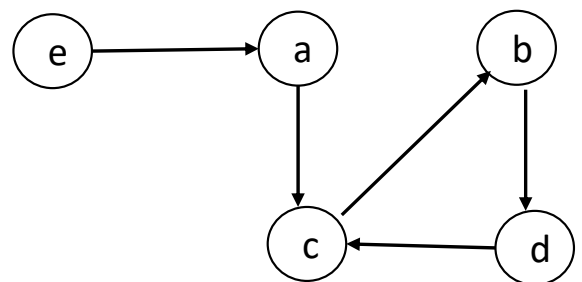
### 3) CSP (10 pts)

Your task is to compare two given graphs and decide whether one contains a copy of the other. Two graphs G1 (where nodes are named using integer numbers) and G2 (where nodes are referred to in terms of the letters of the alphabet), shown in the figure, are given. You will solve this as a constraint satisfaction problem (CSP) and find out if there is a copy of graph G1 in graph G2. «Copy» here means that the same number of nodes with the same connections between them. In other words, you will match these two graphs.

You can use the node-names of G1 (shown in the figure as 1,2,3,4) in the variable names, i.e.,  $x_1, \dots, x_4$ . Regarding the constraints, there is one global “all different”, i.e., AllDiff, constraint expressing that all the variables will have a different value, and four local constraints, each representing the constraints on an edge(arc) in G1, e.g., between node 1 and node 2.



G1



G2

- 1) Write down the variables (i.e.,  $X = \{x_1, x_2, x_3, x_4\}$ ) and the domain of each variable (e.g.,  $D(x_1) = \{\dots\}$ )
- 2) Write down the constraints required for the mapping between the two graphs. Represent the constraints as explicit lists of allowed values for edges in the form of  $\{(x_i - v, x_j - v'), \dots\}$  where the entry  $(x_i - v, x_j - v')$  means that



$(x_i, x_j)$  is an edge in  $G_1$ , and there is an edge  $(v, v')$  in  $G_2$ . That is, it is legal that variable  $x_i$  in  $G_1$  has value  $v$  (from  $G_2$ ) when variable  $x_j$  in  $G_1$  has label  $v'$  (From  $G_2$ ) whenever  $(x_i, x_j)$  is an edge in  $G_1$  and  $(v, v')$  is an edge in  $G_2$ .

- 3) Use backtracking search with forward checking to solve this CSP problem. Draw the search tree. The order of variable assignment is in numerical order, i.e., 1,2,3,4 while the assignment of values is in opposite/reverse alphabetical order. That is, you start with the assignment  $x_1$  = the last letter in alphabetical order in the domain of  $x_1$ .

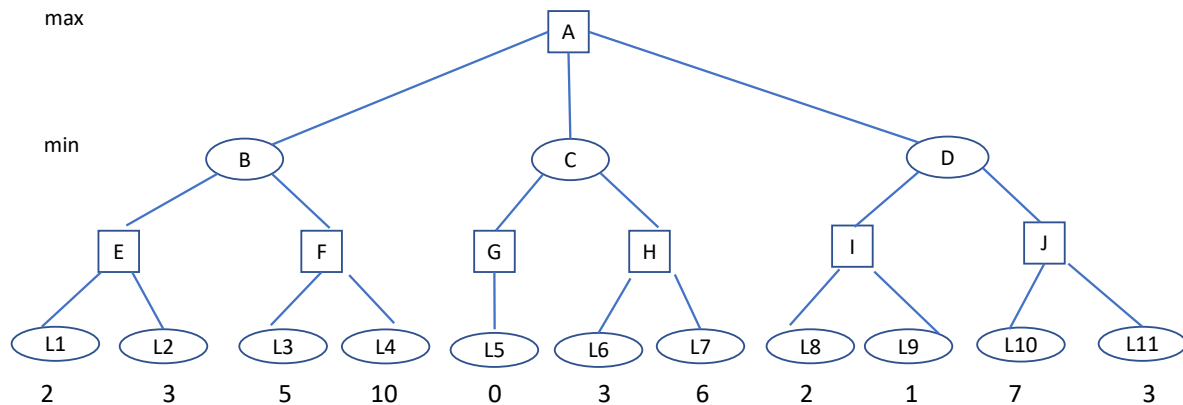
#### 4) PLANNING (10 pts)

- 1) In what way are Partial Order Planning (PoP) process and the resulting plans different from the ones in the progressive and regressive planning? In what situations is it suitable and attractive to use PoP?
- 2) Assume you are going to a Christmas party tonight and you want to put on some jewellery, more specifically a gold ring on each of your pointing finger. It is cold outside and you need to put on gloves as well. Naturally, you need to put on the rings before you put on gloves. You will use a partial order planner to make a plan. You have these action: RightGlove (means put on a glove on your right hand), LeftGlove, RightRing (put on a ring on your right hand), and LeftRing. You will use partial order planning to generate a plan.
  - a. Write the required action schemas in the PDDL language.
  - b. Draw the partial plan with the dependencies between the actions.
  - c. Write down the plan. Use this notation: Action-1; (Action2, Action 3)... which means that Action-1 is followed by either Action2 or Action3 in the plan.

#### 5) ADVERSARIAL SEARCH (10 pts)

.....

- 1) Apply minimax algorithm on the tree in the given figure and find the values of all the nodes above the leaf nodes. Write down the values of nodes A-J. What is the value of the solution for the agent *max*?



- 2) Apply alpha-beta pruning algorithm to find nodes can be pruned. Write down the names of the nodes (i.e., the letters in the squares and ellipses), either leaves or the nodes of which all children are pruned. For example if  $L3$  and  $L4$  are both pruned then it is sufficient to write node  $F$  only. Give the reason why each pruned node is pruned, by referring to alpha and beta values

## 6) SHORT-QUESTIONS (20 pts)

- 1) Game theory: Does the payoff matrix in the given figure represent an instance of the Prisoner Dilemma game? Explain your answer - why is it, or why is it not.

|        | Coop | Defect |
|--------|------|--------|
| Coop   | 4,4  | -1,8   |
| Defect | 8,-1 | 2,2    |

- 2) Knowledge Representation

- a. What are the three ways to represent states and transitions between them? Describe each of them very briefly and describe what kinds of tasks (e.g., planning, or classical search task) we used each of them in this course.

- b. What are semantic networks capable of representing? What kind of reasoning mechanism/methods do they rely on?
- 3) AI-Ethics: What kind of connection can you make between P of PEAS (in Chapter 2) and ethical issues in AI? This is an open question which needs you to support your answer with arguments. In other words, explain your answer – concisely.
- 4) Environment type: Assume a human agent is collecting beautiful, rare orchids in the rain forest. They suddenly notice that some birds are following them and pick the orchids just when the agent reaches to the orchids. Is this a deterministic, stochastic or strategic environment? Explain your answer.