



**NATIONAL OPEN UNIVERSITY OF NIGERIA**  
**14-16 AHMADU BELLO WAY, VICTORIA ISLAND LAGOS**  
**MARCH/APRIL 2016 EXAMINATION**

**SCHOOL OF SCIENCE AND TECHNOLOGY**

**COURSE CODE:** FMT309  
**COURSE TITLE:** MATHEMATICAL PROGRAMMING I  
**TIME ALLOWED** (3 HRS)  
**INSTRUCTION:** Answer any 3 questions.

1. A company manufactures two products A and B. These products are processed in the same machine. It takes 10 minutes to process one unit of product A and 2 minutes for each unit of product B and the machine operates for a maximum of 35 hours in a week. Product A requires 1kg and B 0.5kg of raw material per unit, the supply of which is 600kg per week. Market constraints on product B is known to be minimum of 800 units every week. Product A costs N 5 per unit and sold at N 10. Product B costs N 6 per unit and can be sold in the market at a unit price of N 8. Determine the number of units of A and B per week to maximize the profit. 23marks

2. State the steps or Procedures involved for solving LPP by graphical method. 23marks

3. Solve the following LPP by graphical method.

$$\begin{aligned} \text{Minimize } z &= 20x_1 + 10x_2 \\ \text{Subject to. } x_1 + 2x_2 &\leq 40 \\ 3x_1 + x_2 &\geq 30 \\ 4x_1 + 3x_2 &\geq 60 \end{aligned}$$

with  $x_1, x_2 \geq 0$

23marks

4. Use the simplex method to solve the linear programming problem.

$$\begin{aligned} \text{Minimize } z &= 2x_1 - x_2 + 2x_3 \\ \text{Subject to. } 2x_1 + x_2 &\leq 10 \\ x_1 + 2x_2 - 2x_3 &\leq 20 \\ x_2 + 2x_3 &\leq 5 \end{aligned}$$

with  $x_1, x_2, x_3 \geq 0$

23marks

5. A small petroleum company owns two refineries. Refinery 1 costs N 20,000 per day to operate, and it can produce 400 barrels of high-grade oil, 300 barrels of medium-grade oil,

and 200 barrels of low-grade oil each day. Refinery 2 is newer and more modern. It costs N 25,000 per day to operate, and it can produce 300 barrels of high-grade oil, 400 barrels of medium-grade oil, and 500 barrels of low-grade oil each day. The company has orders totaling 25,000 barrels of high-grade oil, 27,000 barrels of medium grade oil, and 30,000 barrels of low-grade oil. How many days should it run each refinery to minimize its costs and still refine enough oil to meet its orders?

23marks.