

FBQ1: Let $G = \{1, -1, i, -i\}$. Then G is a group under usual multiplication of complex numbers, in this group, the order of i is ____.

Answer: 4

FBQ2:

Answer: (4,1)

FBQ3:

Answer: N

FBQ4: The order of (12) in S_n is ____.

Answer: 2

FBQ5: In a permutation, any cycle of length two is called ____.

Answer: Transposition

FBQ6: A field K is called ____ of F if F is a subfield of K , thus Q is a subfield of R and R is a field extension of Q

Answer: Field extension

FBQ7:

Answer: Proper subfield

FBQ8:

Answer: Primitive

FBQ9: We call an integral domain R a ____ if every non zero element of R which is not a unit in R can be uniquely expressed as a product of a finite number of irreducible elements of R

Answer: Unique factorization domain

FBQ10:

Answer: Greatest Common divisor

FBQ11: Given two elements a and b in a ring R , we say that c is a ____ of a and b if $c|a$ and $c|b$.

Answer: Common divisor

FBQ12: We call an integral domain R a ____ if every ideal in R is a principal ideal.

Answer: Principal ideal

FBQ13: ____.

Answer: 2

FBQ14: Let R be an integral domain, an element $a \in R$ is called a unit or an ____ in R if we can find $b \in R$ such that $ab = 1$ i.e if a has a multiplicative inverse

Answer: Invertible element

FBQ15: A domain on which we can define a Euclidean valuation is called ____.

Answer: Euclidean domain

FBQ16:

Answer: Euclidean Evaluation

FBQ17:

Answer: Root of multiplicity m

FBQ18: Let F be a field and $f(x) \in F[x]$ we say that an element $a \in F$ is a ____ (or zero) of $f(x)$ if $f(a) = 0$

Answer: Factor

FBQ19: If S is set, an object $a \in S$ in the collection S is called

an _____ of S

Answer: Element

FBQ20: A set with _____ element in S is called an empty set

Answer: No

FBQ21: _____ method is sometimes used to list the element of a large set

Answer: Roster

FBQ22: The set of rational numbers and the set of real numbers are respectively represented by the symbol _____ and _____.

Answer: Q and R

FBQ23: The symbol _____ denotes _____.

Answer: There exist

FBQ24: If A and B are two subsets of a set S , we can collect the element that are common to both A and B , we call this set the _____ of A and B .

Answer: Intersection

FBQ25: A relation R defined on a set S is said to be _____ if we have

Answer: Reflexive

FBQ26: A relation R defined on a set S is said to be _____ if

Answer: Symmetric

FBQ27: A relation R defined on a set S is said to be _____ if $a R b$ and

Answer: Transitive

FBQ28: A relation R defined on a set S that is reflexive, symmetric and transitive is called _____ relation

Answer: Equivalence

FBQ29: A _____ f from a non- \emptyset empty set A to a non- \emptyset empty set B is a rule which associates with every element of A exactly one element of B

Answer: Function

FBQ30: A function is called _____ if it associates different elements of A with different elements of B

Answer: Injective

FBQ31: A function is called _____ if the range of f is B .

Answer: Onto

FBQ32:

Answer: Projection

FBQ33: A function that is both one to one and onto is called _____

Answer: Bijective

FBQ34: _____ set.

Answer: Finite

FBQ35: A set that is not _____ is called infinite set

Answer: Finite

FBQ36: _____

Answer: Bijective

FBQ37: 1 and p

Answer: Prime

FBQ38: _____ number
Answer: Composite

FBQ39: _____ on A .
Answer: Identity function

FBQ40: _____ on S .
Answer: Binary operation

FBQ41:
Answer: Closed

FBQ42:
Answer: Associative

FBQ43:
Answer: Commutative

FBQ44: _____.
Answer: Distributive over

FBQ45:
Answer: Identity element

FBQ46: The Cayley table is named after the famous mathematician
Answer: Arthur Cayley

FBQ47: _____ system consists of a set with a binary operation which satisfies certain properties is called a group
Answer: Algebraic

FBQ48:
Answer: The integral power

FBQ49: is an equivalence relation, and hence partition Z into disjoint equivalence classes called _____ modulo n .
Answer: Congruence class

FBQ50: If the set X is finite, say $X = \{1, 2, 3, \dots, n\}$ then we denote $S(x)$ by and each of is called a _____ on n symbols
Answer: Permutation

MCQ1: In a principle ideal Domain an element is prime if and only if it is
Answer: Reducible

MCQ2:
Answer: I only

MCQ3:
Answer: $3x+1$

MCQ4:
Answer: II only

MCQ5:
Answer: II only

MCQ6:
Answer:

MCQ7:
Answer: 1

MCQ8:

Answer: $f(a) = 1$

MCQ9: Express $x^4 + x^3 + 5x^2 - x$ as $(x^2 + x + 1) + rx$ in $\mathbb{Q}[x]$

Answer: None of the options

MCQ10: Let F be a field. Let $f(x)$ and $g(x)$ be two polynomials in $F[x]$ with $g(x) \neq 0$. Then I There exist two polynomials $q(x)$ and $r(x)$ in $F[x]$ such that $f(x) = q(x)g(x) + r(x)$, where $\deg(r(x)) < \deg(g(x))$. II The polynomials $q(x)$ and $r(x)$ are unique, which of the following is a properties of Division Algorithm?

Answer: I only

MCQ11: Which of the following polynomial ring is free from zero divisor

Answer: $\mathbb{Z}_6[x]$

MCQ12: . Let R be a ring and $f(x)$ and $g(x)$ be two non zero element of $R[x]$. Then $\deg(f(x)g(x)) = \deg f(x) + \deg g(x)$ with equality if

Answer: R does not have a zero divisor

MCQ13: If $p(x), q(x) \in \mathbb{Z}[x]$ then the $\deg(p(x).q(x))$ is

Answer: $\max(\deg p(x), \deg q(x))$

MCQ14: If $f(x) = a_0 + a_1x + \dots + a_nx^n$ and $g(x) = b_0 + b_1x + \dots + b_mx^m$ are two polynomials in $\mathbb{R}[x]$, we define their product $f(x).g(x) = c_0 + c_1x + \dots + c_{m+n}x^{m+n}$ where c_i is

Answer: $a_i b_j$ where $i + j = i, i \in \{0, 1, \dots, m+n\}$

MCQ15: Consider the two polynomials $p(x), q(x)$ in $\mathbb{Z}[x]$ by $p(x) = 1 + 2x + 3x^2$, $q(x) = 4 + 5x + 7x^3$. Then $p(x) + q(x)$ is

Answer: $5 + 7x + 3x^2 + 7x^3$

MCQ16: Determine the degree and the leading coefficient of the polynomial

$1 + x^3 + x^4 + 0.5x^5$ is

Answer: $(3, 1)$

MCQ17: The Degree of a polynomial written in this form $\sum_{i=0}^n a_i x^i$ if $a_n \neq 0$ is

Answer: n

MCQ18: Let R be a domain and $x \in R$ be nilpotent then $x^n = 0$ for some $n \in \mathbb{N}$. Since R has no zero divisors this implies that

Answer: $x = 0$

MCQ19: An ideal m of \mathbb{Z} is maximal if and only if m is

Answer: An even number

MCQ20: Every maximal ideal of a ring with identity is

Answer: A prime ideal

MCQ21: Let R be a ring with identity. An ideal M in R is Maximal if and only if R/M is

Answer: A field

MCQ22: An ideal p of a ring R with identity is a prime ideal of R if and only if the quotient ring is

Answer: An integral domain

MCQ23: The characteristic of a field is either

Answer: None of the options

MCQ24: \mathbb{Z}_n is a field if and only if

Answer: n is a prime number

MCQ25: Which of the following is an axioms of a field

Answer: Is commutative

MCQ26: Let R be a ring, the least positive integer n such that $nx = 0 \forall x \in R$ is called

Answer: The order of R

MCQ27: Which of the following is not a property of an integral domain

Answer: Is a commutative ring

MCQ28: A non zero element in a ring R is called zero divisor in R if there exist a non zero element b in R such that

Answer: $ab = 0$

MCQ29: If H is a subgroup of a group G and $a, b \in G$ then which of the following statement is true

Answer: $Ha = H$ iff $a \in H$

MCQ30: Let G be a group and $a \in G$ such that $O(a) = n$, then $a^n = e$, if and only if

Answer: None of the options

MCQ31: Which of these does not hold for \sim distributive over \cap and \cup

Answer: $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$

MCQ32: The symmetric difference of two given sets A and B , denoted by $A \oplus B$ is defined by

Answer: $A \oplus B = (A \setminus B) \cup (B \setminus A)$

MCQ33: The (relative) complement (or difference) of a set A with respect to a set B denoted by $B \setminus A$ (or $B \setminus A$) is the set

Answer: $B \setminus A = \{x \in B : x \notin A\}$

MCQ34: Which of the following is of the operations and

Answer: Associative $A(BC) = (AB)C$ and $A(BC) = (AB)C$ for three sets A, B, C

MCQ35: The intersection of two sets A and B written as AB is

Answer: The set $AB = \{x : x \in A \text{ and } x \in B\}$

MCQ36: A set X of n elements has

Answer: 2^n subsets

MCQ37: If G is a finite group such that $O(G)$ is neither 1 nor a prime, then G has

Answer: Non trivial proper subgroup

MCQ38: Which of the following is not the definition of Euler Phi function

MCQ39: Every group of prime order is

Answer: Non abelian

MCQ40: An element is of infinite order if and only if all its power are

Answer: Real

MCQ41: Consider the following set of 2×2 matrices over \mathbb{C} . $S = \{I, A, B, C\}$ where $I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$, $A = \begin{pmatrix} i & 0 \\ 0 & -i \end{pmatrix}$, $B = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$, $C = \begin{pmatrix} 0 & i \\ i & 0 \end{pmatrix}$ and $i = -1$. If $H = \langle S \rangle$ is a subgroup, how many distinct right cosets does it have in S_4

Answer: 8

MCQ42: Let $H = 4\mathbb{Z}$. How many distinct right coset of H in \mathbb{Z} do we have?

Answer: 2

MCQ43: A function $f : A \rightarrow B$ is called one to one if and only if different element of A map to different element of B . some time is called

Answer: Injective

MCQ44: Let G be a group, $a \in G$ and $m, n \in \mathbb{Z}$. which of the following does not

hold

Answer: $(gm)n = gmn$

MCQ45: Let G be a group. If there exist $g \in G$ has the form $x = gn$ for some $n \in \mathbb{Z}$ then G is

Answer: A cyclic group

MCQ46: Let $H = \{I, (1, 2)\}$ be a subgroup of S_3 . The distinct left cosets of H in S_3 are

Answer: $H, (123)H, (12)H$

MCQ47: The order of $\sqrt{2}$ in \mathbb{Q}^\times is

Answer: 4

MCQ48: The order of (12) in S_3 is

Answer: 2

MCQ49: A group generated by g is given by $\langle g \rangle = \{e, g, g^2, \dots, g^{m-1}\}$ the order of g is

Answer: m

MCQ50: Let H be a subgroup of a finite group G . We call the number of distinct cosets of H in G _____.

Answer: index