

MTH282

Two vectors are said to be equal if their ----- are equal.

magnitudes and directions

Two vectors A, B, are said to collinear (linearly dependent) if there are scalar a and b such $aA + bB = 0$ implies -----

a and b are not all zero

Collinear vectors are said be -----

linearly dependent

Find the unit vector in the direction of the vector $3i + 2j + 6k$.

$(3i + 2j + 6k)/7$

The following are true about scalar product of vectors accept -----

$j \cdot j = 1$

Given that $v = 2i + j + 5k$ and $u = 3i - 4j + k$, find $v \cdot u$

7

Find the direction cosines of the vector $3i + 4j$

$3/5, 4/5$

Find sum of direction cosines of the vector $3i + 2j + 6k$.

$1/7$

Given that vector $D = 2i - 3j + 5k$ and $P = 4i + j + 6k$ find $D \cdot P$

35

If vector $OC = 2i + j$ and vector $OB = 6i - 2j$, find the magnitude of vector CB

5

Find the vector product of $A = i + j + k$ and $B = 3i + 3j + 3k$

0

Find the acute angle (to the nearest degree) angle between the vectors $a = -3i + 4j$ and

$b = 5i + 12j$.

59.49°

Find a vector that is of magnitude 6 units and is collinear to the vector $i + j$.

$3\sqrt{2}i + 3\sqrt{2}j$

Given that $A = 2i + j - 3k$, $B = i - 2j + k$ $C = i + j - 4k$. Evaluate $A \cdot (B \times C)$.

10

Find the unit vector perpendicular to the plane of the vectors $A = 3i - 2j + 4k$ and

$B = i + j - 2k$

$$15(2\mathbf{i} + \mathbf{j})$$

An object moves in a straight curve $\mathbf{R} = e^{3t} \mathbf{i} - 3e^{2t} \mathbf{j} + 2\sin 5t \mathbf{k}$, Find its velocity at time $t=1$.

$$5\mathbf{i} + 0.812 \mathbf{j} + 2.837\mathbf{k}$$

If the scalar product of vectors $2\mathbf{i} - \mathbf{j} - 4\mathbf{k}$ and $5\mathbf{i} - 2\mathbf{j} - m\mathbf{k}$ is four, find m .

$$-2$$

Find the angle between the vectors $2\mathbf{i} - 4\mathbf{j} + \mathbf{k}$ and $2\mathbf{i} - 3\mathbf{j} - 3\mathbf{k}$.

$$\cos^{-1}(0.6048)$$

Determine s such that the vectors $s\mathbf{i} + 4\mathbf{j} + 4\mathbf{k}$ and $-2\mathbf{i} + 5\mathbf{j} + s\mathbf{k}$ perpendicular.

$$-10$$

Find the value of a that makes the vectors $5\mathbf{i} - a\mathbf{j} + 2\mathbf{k}$ and $\mathbf{i} + 3\mathbf{j} + 5\mathbf{k}$ perpendicular.

$$5$$

Determine n such that the vectors $5\mathbf{i} + n\mathbf{j} - 5\mathbf{k}$ and $-4\mathbf{i} + n\mathbf{j} + \mathbf{k}$ are perpendicular.

$$5$$

Determine the unit vector parallel to the sum of vectors $3\mathbf{i} + 4\mathbf{j} - 5\mathbf{k}$ and $\mathbf{i} + 8\mathbf{j} + 9\mathbf{k}$

$$12\mathbf{i} + 4\mathbf{j} + 3\mathbf{k} / 13$$

Find the scalar product of the vector $-2\mathbf{i} - \mathbf{j} - 2\mathbf{k}$ and the unit vector parallel to the vector $4\mathbf{i} + 3\mathbf{j} - 12\mathbf{k}$

$$1$$

Find the vector product of $\mathbf{v} = (1, 0, 2)$ and $\mathbf{u} = (2, 4, 3)$.

$$(-8, 1, 4)$$

Find the gradient of the scalar field $\phi(x, y, z) = x^3yz^2$ at the point $(1, 1, 1)$

$$3\mathbf{i} + \mathbf{j} + 2\mathbf{k}$$

If that $\phi = x^4y + z^2$, find the Laplacian of ϕ

$$2(6x^2 + 1)$$

Given that $\mathbf{R} = xz\mathbf{i} - y^2\mathbf{j} + 2x^2y\mathbf{k}$, find $\nabla \cdot (\nabla \times \mathbf{R})$

$$0$$

Given that $\mathbf{R} = xz\mathbf{i} - y^2\mathbf{j} + 2x^2y\mathbf{k}$, find the divergence of \mathbf{R}

$$z - 2y$$

Given that $\phi = 3y^2x + x^2z^2$, find $\nabla \phi$

$$(3y^2 + 2xz^2)\mathbf{i} + 6yx\mathbf{j} + 2zx^2\mathbf{k}$$

If $\phi = 3y^2x + x^2z^2$, find $\nabla^2\phi$.

$$2z^2 + 6x + 2x^2$$

Given that $\vec{A} = yx\mathbf{i} + yx^2\mathbf{j} + 2zy\mathbf{k}$, find $(\nabla \times \vec{A})$

$$2z\mathbf{i} + x(2y-1)\mathbf{k}$$

Given that $\vec{T} = y^2x^2\mathbf{i} + x^2z^2\mathbf{j} + y^2z^2\mathbf{k}$, find curl of \vec{T} .

$$2z(yz - x^2)\mathbf{i} + 2x(z^2 - yx)\mathbf{k}$$

Given that $\vec{T} = y^2x^2\mathbf{i} + x^2z^2\mathbf{j} + y^2z^2\mathbf{k}$, find curl of \vec{T} at point $(1, -1, 1)$

$$-4\mathbf{i} + 4\mathbf{k}$$

The scalar product of vectors \vec{a} and \vec{b} , where θ is the angle between them, is

$$|\vec{a}| |\vec{b}| \cos \theta$$

If that $\phi = x^2z - yz^2$, find the Laplacian of ϕ

$$2z - 2y$$

If that $\phi = x^2y^2z^2$, find the Laplacian of ϕ .

$$2(y^2z^2 + x^2z^2 + x^2y^2)$$

Given that $\vec{A} = yx\mathbf{i} + yx^2\mathbf{j} + 2zy\mathbf{k}$, find $\nabla \cdot (\nabla \times \vec{A})$

$$2xi - (2y-3)j$$

Let $\vec{E} = yx\mathbf{i} + xz\mathbf{j} + zy\mathbf{k}$, find $\nabla \cdot (\nabla \times \vec{E})$.

$$-2j$$

Find the Jacobian of the transformation $x = R\sin\theta\cos\phi$, $y = R\sin\theta\sin\phi$ and $z = R\cos\theta$ with respect to R , θ and ϕ

$$-R^2\sin\theta$$

Determine the Jacobian of $x = u+v$, $y = 2v$ with respect to u and v

$$2$$

Given that $u = x+2y$ and $v = x - y$, find the Jacobian of the transformation x and y with respect to u , and v

$$-1/3$$

Find the Jacobian of $x = u+v + s$, $y = 2v - s$ and $z = u - v$ with respect to u , v and s

$$-5$$

Given that $x = 2s - w$, $y = v + s + 2w$ and $z = 2v - s - w$ find the Jacobian of the transformation x and y with respect to v , s and w

$$13$$

Let $\frac{\partial x}{\partial u}$, $\frac{\partial y}{\partial u}$, $\frac{\partial z}{\partial u}$ be the Jacobian of the transformation x and y with respect to u and v , then $\frac{\partial x}{\partial v}$, $\frac{\partial y}{\partial v}$, $\frac{\partial z}{\partial v}$ is equal to -----

$$-\frac{\partial y}{\partial v}, \quad x\frac{\partial x}{\partial u}, \quad v$$

Expand $1-i+1+i^4$

1

Let $F(z) = 7 - z^1 - z^2$ and $z = 1+2i$. Find $F(z)$.

$1+i/2$

Given that $R = y^2z^2i + xj - y^4z^3k$, find $\nabla \cdot R$.

$2xy^2zi + y^4x^3k$

Given that $u = x+4y$ and $v = x-3y$, find the Jacobian of the transformation x and y with respect to u , and v

-2

Given that $u = x+2y$ and $v = x - y$, find the Jacobian of the transformation x and y with respect to u and v

-1/7

Given that $\vec{r} = x\vec{i} + y\vec{j} + z\vec{k}$, find $\nabla \times (\nabla \times \vec{A})$

$2\vec{k}$

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Find the unit vector in the direction of the vector $3\vec{i} + 2\vec{j} + 6\vec{k}$.

$(3\vec{i} + 2\vec{j} + 6\vec{k})/7$

The following are true about scalar product of vectors except -----

$\vec{j} \cdot \vec{j} = 1$

Given that $\vec{v} = 2\vec{i} + \vec{j} + 5\vec{k}$ and $\vec{u} = 3\vec{i} - 4\vec{j} + \vec{k}$, find $\vec{v} \cdot \vec{u}$

7

Find the direction cosines of the vector $3\vec{i} + 4\vec{j}$

$3/5, 4/5$

Find sum of direction cosines of the vector $3\vec{i} + 2\vec{j} + 6\vec{k}$.

1/7

Given that vector $\vec{D} = 2\vec{i} - 3\vec{j} + 5\vec{k}$ and $\vec{P} = 4\vec{i} + \vec{j} + 6\vec{k}$ find $\vec{D} \cdot \vec{P}$

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If vector $OC = 2i + j$ and vector $OB = 6i - 2j$, find the magnitude of vector CB

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Find the vector product of $A = i + j + k$ and $B = 3i + 3j + 3k$

0

Find the acute angle (to the nearest degree) angle between the vectors $a = -3i + 4j$ and $b = 5i + 12j$.

59.49°

Find a vector that is of magnitude 6 units and is collinear to the vector $i + j$.

$32i + 32j$

Given that $A = 2i + j - 3k$, $B = i - 2j + k$, $C = i + j - 4k$. Evaluate $A \cdot (B \times C)$.

10

Find the unit vector perpendicular to the plane of the vectors $A = 3i - 2j + 4k$ and

$B = i + j - 2k$

$15(2i + j)$

$5i + 0.812j + 2.837k$

If the scalar product of vectors $2i - j - 4k$ and $5i - 2j - mk$ is four, find m .

-2

Find the angle between the vectors $2i - 4j + k$ and $2i - 3j - 3k$.

$\cos^{-1}(0.6048)$

Determine s such that the vectors $s i + 4 j + 4k$ and $-2 i + 5 j + sk$ perpendicular.

-10

Find the value of a that makes the vectors $5 i - a j + 2k$ and $i + 3 j + 5k$ perpendicular.

5

Determine n such that the vectors $5i + n j - 5k$ and $-4 i + n j + k$ are perpendicular.

5

Determine the unit vector parallel to the sum of vectors $3i + 4 j - 5k$ and $i + 8 j + 9$

$12i + 4j + 3k$

Find the scalar product of the vector $-2i - j - 2k$ and the unit vector parallel to the vector $4i + 3j - 12k$

1

Find the vector product of $v = (1, 0, 2)$ and $u = (2, 4, 3)$.

$$(-8, 1, 4)$$

Find the gradient of the scalar field ϕ $x, y, z = x^3yz^2$ at the point $(1, 1, 1)$

$$3i + j + 2k$$

If that $\phi = x^4y + z^2$, find the Laplacian of ϕ

$$2(6x^2 + 1)$$

Given that $R = xzi - y^2j + 2x^2yk$, find $\nabla \cdot (\nabla \times R)$

$$0$$

Given that $R = xzi - y^2j + 2x^2yk$, find the divergence of R

$$z - 2y$$

Given that $\phi = 3y^2x + x^2z^2$, find $\nabla \phi$

$$(3y^2 + 2xz^2)i + 6yxj + 2zx^2k$$

If $\phi = 3y^2x + x^2z^2$, find $\nabla^2 \phi$.

$$2z^2 + 6x + 2x^2$$

Given that $A = yxi + yx^2j + 2zyk$, find $(\nabla \times A)$

$$2zi + x(2y - 1)k$$

Given that $T = y^2x^2i + x^2z^2j + y^2z^2k$. find curl of T .

$$2z(yz - x^2)i + 2x(z^2 - yx)k$$

Given that $T = y^2x^2i + x^2z^2j + y^2z^2k$. find curl of T at point $(1, -1, 1)$

$$-4i + 4k$$

The scalar product of vectors a and b , where θ is the angle between them, is

$$|a||b| \cos \theta$$

If that $\phi = x^2z - yz^2$, find the Laplacian of ϕ

$$2z - 2y$$

If that $\phi = x^2y^2z^2$, find the Laplacian of ϕ .

$$2(y^2z^2 + x^2z^2 + x^2y^2)$$

Given that $A = yxi + yx^2j + 2zyk$, find $\nabla \times (\nabla \times A)$

$$2xi - (2y - 3)j$$

Let $E = yxi + xzj + zyk$, find $\nabla \times (\nabla \times E)$.

$$-2j$$

Find the Jacobian of the transformation $x = R \sin \theta \cos \phi$, $y = R \sin \theta \sin \phi$ and $z = R \cos \theta$ with respect to R , θ and ϕ

$$-R^2 \sin \theta$$

Determine the Jacobian of $x=u+v$, $y=2v$ with respect to u and v

$$2$$

Given that $u = x+2y$ and $v=x - y$, find the Jacobian of the transformation x and y with respect to u , and v

$$-1/3$$

Find the Jacobian of $x=u+v +s$, $y=2v-s$ and $z=u-v$ with respect to u , v and s

$$-5$$

Given that $x=2s - w$, $y=v+s+2w$ and $z = 2v-s -w$ find the Jacobian of the transformation x and y with respect to v , s and w

$$13$$

Let $\partial x, \partial y, \partial v$ be the Jacobian of the transformation x and y with respect to u and v , then $\partial x, \partial y, \partial v$ is equal to -----

$$-\partial y, \partial x, \partial v$$

Expand $1-i+i^4$

$$1$$

Let $F(z)= 7-z^1-z^2$ and $z =1+2i$. Find $F(z)$.

$$1+i/2$$

Given that $R =y^2zx^2i+xj-y^4zx^3k$, find $\nabla.R$.

$$2xy^2zi+y^4x^3k$$

Given that $u =x+4y$ and $v=x-3y$, find the Jacobian of the transformation x and y with respect to u , and v

$$-2$$

Given that $u =x+2y$ and $v=x - y$, find the Jacobian of the transformation x and y with respect to u and v

$$-1/7$$

Given that $A =zxi+zyj+yxk$, find $\nabla \times (\nabla \times A)$

$$2k$$

A vector V with a unit vector a and magnitude k is written as $V =$ -----

$$*ka*$$

The unit vector in the direction of the resultant of vectors $2i -j + k$ and

$i + j + 2k$ is.....

$$*i + k*$$

If the scalar product of vectors $i - j -k$ and $3i -2j -ak$ is eight, find a .

3

If $A \cdot B = 0$ then the angle between vectors is -----

90

If $A \times B = 0$ and A and B are not null vectors, then A and B are -----

Parallel

Find the acute angle between the vectors $a = -4i - 3j$ and $b = 5i - 12j$ to nearest degree.

58

The vector product of $a = 2i + j + k$ and $b = i + 3j - 2k$ is -----

(17)-i+5j+5k

Determine the acute angle between the vectors $2i + 4j$ and $5i - 4j$ to the nearest degree.

78°

Let $\phi(x, y, z) = \text{constant } c$ be an equation of a surface then, $\nabla\phi$ is -----to this surface.

Normal

If $\phi(x, y, z) = x^4y^6z^4 + xy$. determine $\nabla\phi$

Zero

Let $\phi(x, y, z) = x^3y^2z^4$. determine curl of $\nabla\phi$

0

Find the gradient of the scalar field $\phi(x, y, z) = x^3y^2z^4$ at the point (1,1,1)

3i+2j+4k

Let $\partial x, \partial y, \partial z$ be the Jacobian of the transformation x and y with respect to u and v. Then $\partial x, \partial y, \partial z$ is equal to -----

0

Let $\partial x, \partial y, \partial z$ be the Jacobian of the transformation x and y with respect to u and v. Then $\partial x, \partial y, \partial z$ (where k is constant) is equal to -----

0

Determine the vector product of the vectors $u = 3i - j + k$ and $v = 4i + 2j - k$.

-i+7j+10k

Determine the scalar product of the vectors $A = 4i + 2j - 6k$ and $B = i + 6j + k$

10

Given that $A = 2i + j - 3k$, $B = i - j + 2k$, $C = i + 3j - k$. Evaluate $A \cdot (B \times C)$

-19

Find the vector perpendicular to the plane of the vectors $A = i - j + k$ and $B = i + j - 2k$

-i+3j+2k

Given that $A = 2i + j - 3k$, $B = i - j + 2k$, $C = i + 3j - k$. Evaluate $C \cdot (A \times B)$

-19

An object moves in a straight curve $G = (t^3 + 2t^2 + 2t)i + 3e(t-1)j + 2tk$. Find its acceleration at time $t = 1$.

10i + 3j

Find the unit vector in the direction of the sum of the vectors $i + 6j$ and $2i - 2j$.

3i/5+4j/5

An object moves in a straight curve $R = (3t^2 + t)i + 3e(t-2)j + 2k$ Find its velocity at

time $t=2$.

13i +3j

Find the gradient of the scalar field ϕ $x, y, z=4xzy^2$ at the point $(1, 1, 2)$

8i +16j +4k

Given that $E=xzi-y^2j+2x^2yk$, find $\nabla \cdot E$

4xy

Given that $R=x+zi-y^2j+2x^2yk$, find $\nabla \cdot \nabla \times R$

0

Given that $T=y^2i+z^2j+x^2k$. find curl of T .

2zi+2xj-2ky

Given that $P=y^2i+z^2j+x^2k$.. find curl of P at point $(2, 2, 2)$

4i+4j+4k

Let the scalar product of vectors $x\mathbf{i} + 3\mathbf{j} - 5\mathbf{k}$ and $x\mathbf{i} + \mathbf{j} - 2\mathbf{k}$ be thirty eight. Find x .

5

The scalar product of vectors $2\mathbf{i} + c\mathbf{j} + 6\mathbf{k}$ and $3\mathbf{i} + 5\mathbf{j} - 6\mathbf{k}$ is five, find c .

7

If that $\phi=x^2y^2z^2$, find the Laplacian of ϕ at $(1, -1, -1)$.

6

Given that $A=yx\mathbf{i}+yx^2\mathbf{j}+2zy\mathbf{k}$, find curl curl A at $(3, -1, 5)$

6i+5j

Let $E=yx\mathbf{i}+xz\mathbf{j}+zy\mathbf{k}$, find magnitude of curl E

2

Find the Jacobian of the transformation $x=(r+2)\sin\theta$, $y=(r+2)\cos\theta$ with respect to r and θ

* -(r+2)*

Determine the Jacobian of $x=v\cos\theta$, $y=v\sin\theta$ with respect to v and θ

v

Determine the Jacobian of $x=3u+2v$, $y=v$ with respect to u and v

3

Find the Jacobian of $x=u-v+s$, $y=2u+v-s$ and $z=v+s$ with respect to u , v and s

6

If A^- is the conjugate of the complex number A , determine $A^- + A$

* $\sum_{i=1}^n 2\operatorname{Re}(z)$ *

Evaluate $1-i+in$ where n is a positive even positive integer.

1

Evaluate $1-i+in$ where n is a positive odd positive integer.

-i

Given that $F(z)=2-z^{1-z}$ and $z=1+i$, find $F(z)$

-1+2i

Given that $F(z)=4+z^{1-z}$ and $z=1-i$, find $F(z)$

-1+5i

Expand $(1+2i)(1+i)(1-i)$.

2+4i

Find the real part of the complex number $4+i4-i2$

15/17

If $z=2(\cos\pi/6+i\sin\pi/6)$, find z^6

-64

Evaluate $1+i1-i8$

1

Evaluate $1-i1+i^n$ where n is a positive odd positive integer.

-1

Given that $u = 3x+y$ and $v=x -2y$, find the Jacobian of the transformation x and y with respect to u , and v

1

Evaluate $1-i1+i^n$ where n is a positive even positive integer.

1

Given that $u = x+y$ and $v=2x-y$, find the Jacobian of the transformation x and y with respect to u , and v

-1/3

Evaluate $1-i1+i^n$ where n is a positive even positive integer.

1