

## NATIONAL OPEN UNIVERSITY OF NIGERIA 14-16 AHMADU BELLO WAY, VICTORIA ISLAND, LAGOS SCHOOL OF SCIENCE & TECHNOLOGY JANUARY/FEBRUARY 2013 EXAMINATION

## **CIT 425 - OPERATIONS RESEARCH**

Instruction: Answer Any Five Questions

Time Allowed: 3 Hours

1a. List fourbasic facts of Operations Research as a concept *4 marks* 

b. Why is Operations Research an adaptation of scientific approach? 3 marks

c. State the seven stages of Operations Research 7
marks

2. Solve the following linear programming problem bysimplex method.

Maximise 
$$Z = 10X1 + 20X2$$
  
Subject to the following constraints  
 $3X1 + 2X2 < 1200$   
 $2X1 + 6X2 < 1500$   
 $X1 < 350$   
 $X2 < 200$   
 $X1 \cdot X2 > 0$ 

14 marks

A calculator company produces a scientific calculator and a graphing calculator. Long-term projections indicate an expected demand of at least 100 scientific and 80 graphing calculators each day. Because of limitations on production capacity, no more than 200 scientific and 170 graphing calculators can be made daily. To satisfy a shipping contract, a total of at least 200 calculators much be shipped each day.

If each scientific calculator sold results in a N2 loss, but each graphing calculator produces a N5 profit, how many of each type should be made daily to maximize net profits? 14 marks

4. A convalescent hospital wishes to provide at a minimum cost, a diet that has a minimum of 200g of carbohydrates, 100g of protein and 120g of fats per day. These requirements can be met with two foods:

Food	Carbohydrates	Protein	Fats
Α	10 <i>g</i>	2 <i>g</i>	3 <i>g</i>
В	5 <i>g</i>	5 <i>g</i>	4 g

If food A cost  $^{29\,k}$  per ounce and food B cost  $^{15\,k}$  per ounce, how many ounces of each food should be purchased for each patient per day in order to meet the minimum requirements at the lowest cost? You are required to formulate the above as a well documented LP model.  $^{14\,marks}$ 

The sales manager of Turnover Limited maintains he could increase the sales turnover (in units) of any of the company's product by  $^{50}$  percent if he was authorized to give a  $^{10}\%$  price discount and place appropriate additional advertising matterWhat is the maximum additional advertising expense they can incur in respect of any given product without the manager's proposal resulting in a smaller profit?

## 14marks

- 6. Big Bros. Inc. is an investment company doing an analysis of the pension fund for a certain company. A maximum of  $^{i10}$  million is available to invest in two places. No more than  $^{i8}$  million can be invested in stocks yielding  $^{12}$ % and at least  $^{i2}$  million can be invested in long-term bonds yielding  $^{8}$ %. The stock-to-bond investment ratio cannot be more than  $^{1}$  to  $^{3}$ . How should Big Bros. advise their client so that the pension fund will receive the maximum yearly return on investment? You are required to formulate the required LP model  $^{14}$  marks.
- 7. A farmer has 100 acres on which to plant two crops: corn or wheat. To produce these crops, there are certain expenses as shown in the table.

Item	Cost per Acre
	<i>i</i> ( <i>i</i> )
Corn	
Seed	12
Fertilizer	58
Planting/care/ harvesting	50
Total	120
Wheat	
Seed	40

Fertilizer	80
Planting/care/ harvesting	90
Total	210

After the harvest, the farmer must store the crops awaiting proper market conditions. Each acre yields an average of  $^{110}$  bushels of corn or  $^{30}$  bushels of wheat. The limitations of resources are as follows:

Available capital: 615,000 .

Available storage facilities: 4,000 bushels.

If net profit (the profit after all expenses have been subtracted) per bushel of corn is  $i^{1.30}$  and for wheat is  $i^{2.00}$ , how should the farmer plant the  $i^{100}$  acres to maximize the profits? 14 marks

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