

# Git hub website project

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## Fundamental Theorem of Calculus

If  $f : [a, b] \rightarrow \mathbf{R}$  is integrable, and  $F : [a, b] \rightarrow \mathbf{R}$  satisfies  $F'(x) = f(x)$  for all  $x \in [a, b]$ , then  $\int_a^b f = F(b) - F(a)$ .  
(ii) Let  $g : [a, b] \rightarrow \mathbf{R}$  be integrable, and define  $G(x) = \int_a^x g$  for all  $x \in [a, b]$ . Then,  $G$  is continuous on  $[a, b]$ . If  $g$  is continuous at some point  $c \in [a, b]$  then  $G$  is differentiable at  $c$   $G'(c) = g(c)$ .

## Gauss bonnet theorem

Suppose  $M$  is a compact two dimensional Riemannian manifold with boundary  $\partial M$ . Let  $K$  be the Gaussian Curvature of  $M$ , and let  $k_g$  be the geodesic curvature of  $\partial M$ . Then  $\int_M K dA + \int_{\partial M} k_g ds = 2\pi\chi(M)$  where  $dA$  is the area element of the surface and  $ds$  is the line element along the boundary of  $M$ . Here,  $\chi(M)$  is the Euler characteristic of  $M$ .