



Berner Fachhochschule  
Haute école spécialisée bernoise  
Bern University of Applied Sciences

Introduction to Computer Vision:

# Point Operations

Marcus Hudritsch (hsm4)

# Image Processing: Point Operations

<div>Output</div> <div>Input</div>	Image	Description
Image	Image Processing	Image Analysis
Description	Image Synthesis (Computer Graphics)	All other IT

# Image Processing vs. Image Analysis

## Image Processing

- Contrast & brightness manipulation
- Color space manipulation
- Gray level reduction
- Sharpening
- Noise reduction
- Edge extraction
- Image algebra
- Geometric operations

## Image Analysis

- Segmentation
- Region Representation
- Feature Extraction
- Classification
- Tracking

# Image Operators

## Point Operators

- Binarisation
- Gray level reduction
- Contrast & Brightness manipulations
- Histogram Equalization
- Arithmetic Operations
- Logic Operations

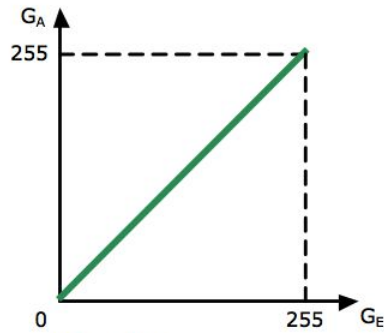
## Global Operators

- Discrete Fourier Transform
- Wavelet Transform
- Hough Transform
- Principal Component Analysis

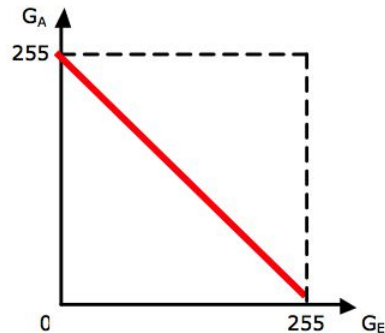
## Local Operators

- Filters
  - Low Pass Filter
    - Gauss & Box Filter
  - High Pass Filter
    - Sobel Filter
    - Laplace Filter
- Morphological Operators
  - Erosion & Dilation
  - Opening & Closing
- Rank Order Operators
  - Min. & Max. Filter
  - Median Filter

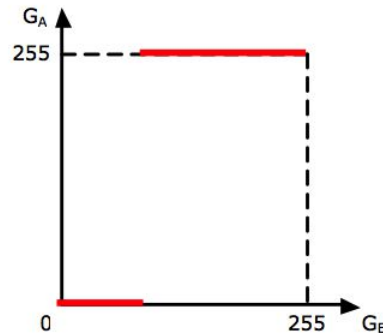
# Point Operation: Mapping Function



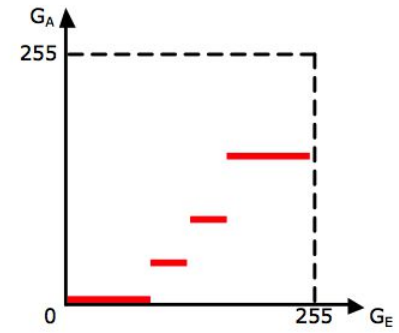
Identität



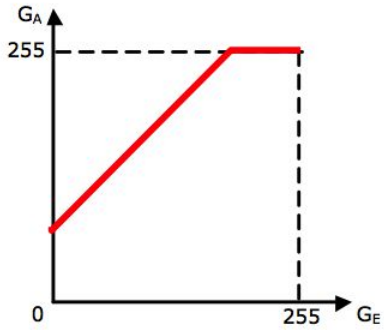
Invertierung



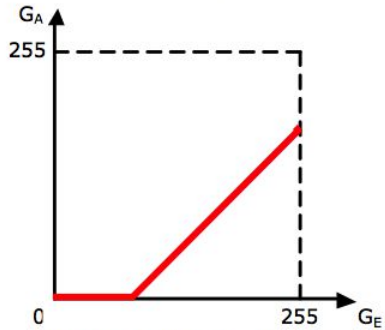
Binärisierung



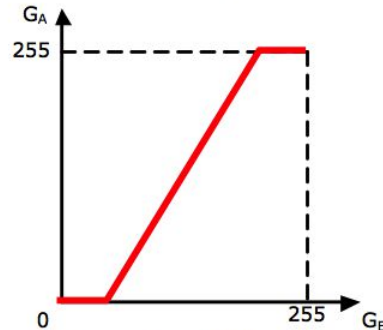
Grauwertreduktion



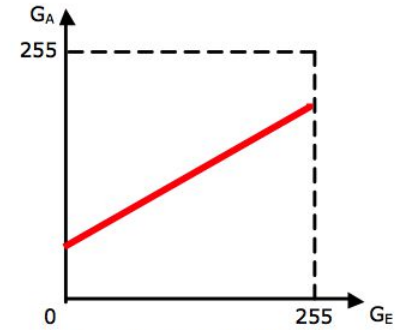
Helligkeit erhöhen



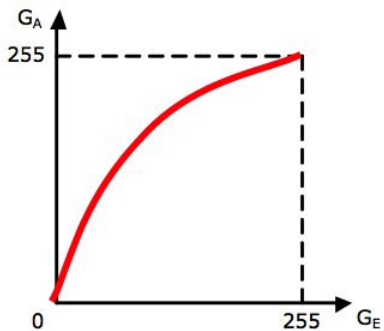
Helligkeit reduzieren



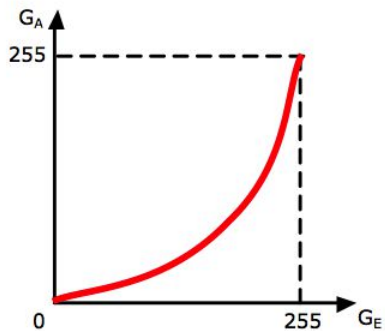
Kontrast erhöhen  
Histogrammstreckung



Kontrast reduzieren  
Histogrammstauchung

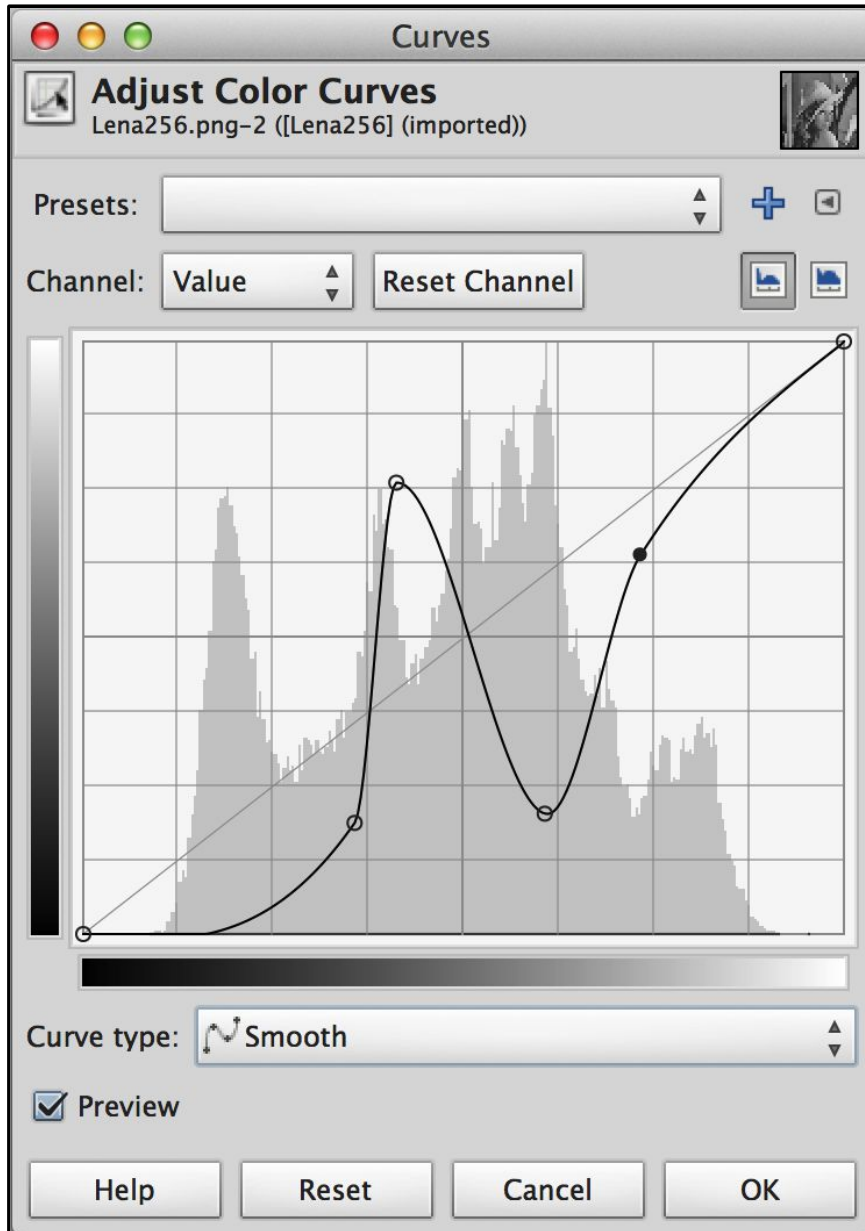


Helligkeit erhöhen  
(Gammakorrektur)



Helligkeit reduzieren  
(Gammakorrektur)

# Point Operation: Mapping Function in Gimp



# Point Operation: Mapping Function

- Mapping functions are first applied to a **lookup table**:

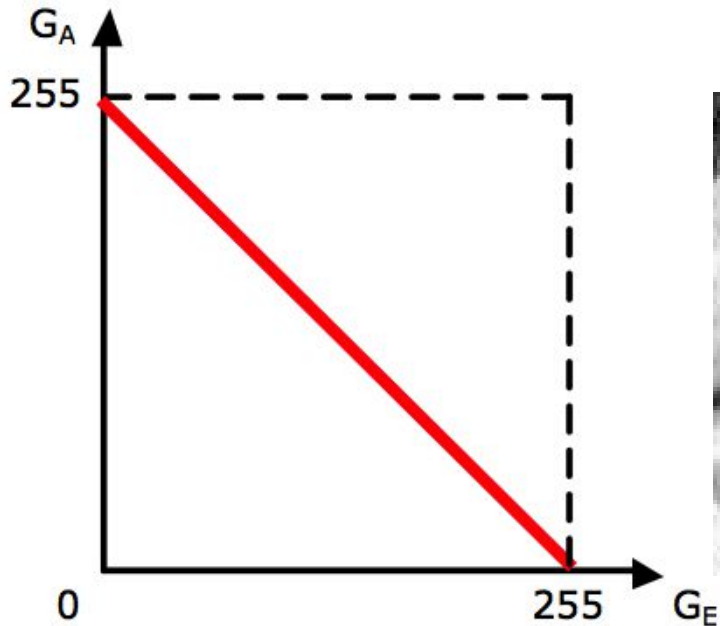
Input	0	1	2	3	4	5	6	7	...	250	251	252	253	254	255
Output	255	254	253	252	251	250	249	248	...	5	4	3	2	1	0

- The point operation is then a **simple and fast lookup operation**.

# Point Operation: Invert

- Invert all gray values:  $g_A(x, y) = 255 - g_E(x, y)$

■

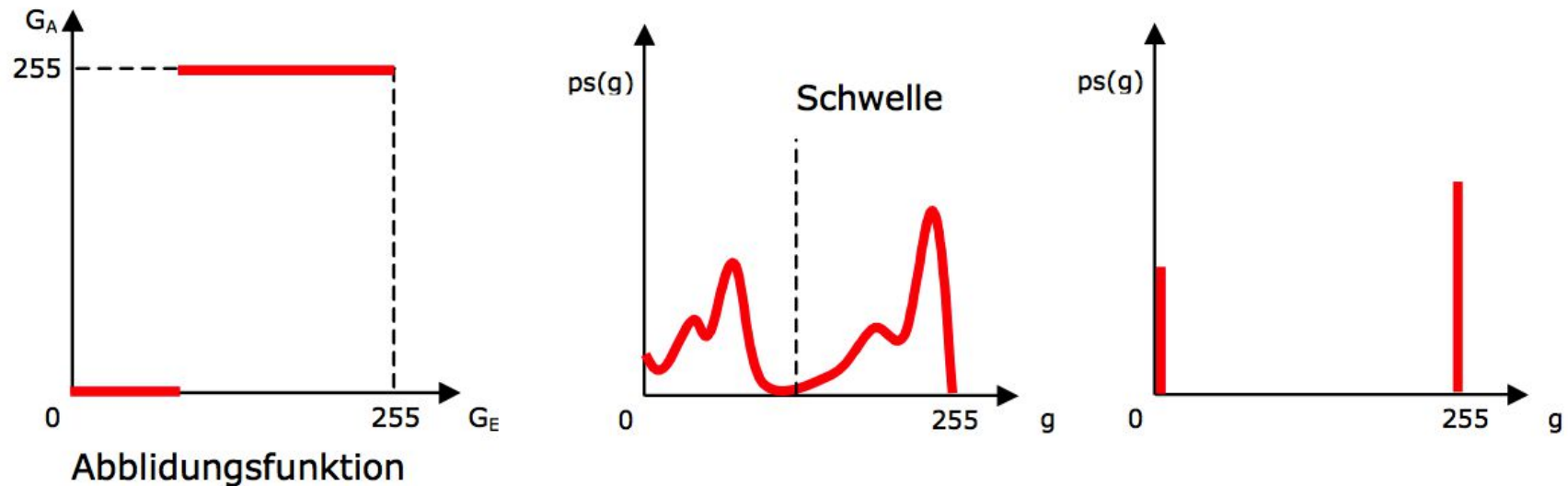




# Point Operation: Binarisation

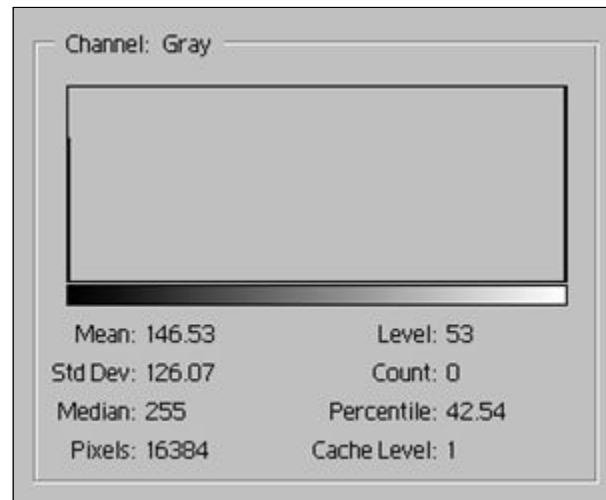
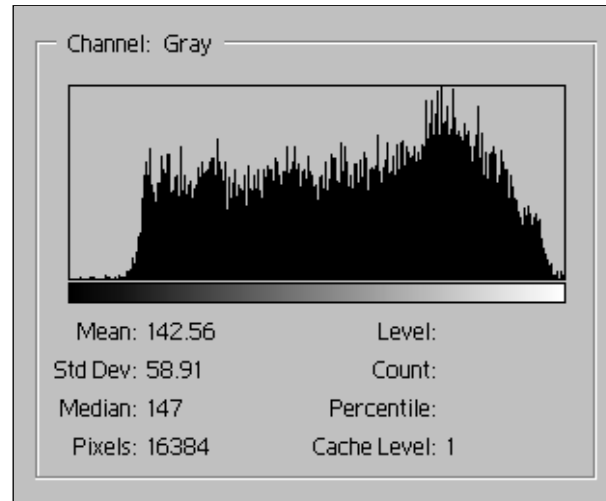
- All gray values below **threshold  $t$**  become black and all other become white:

$$g_A(x, y) = \begin{cases} g_1 : g_E(x, y) < t \\ g_2 : g_E(x, y) \geq t \end{cases}$$



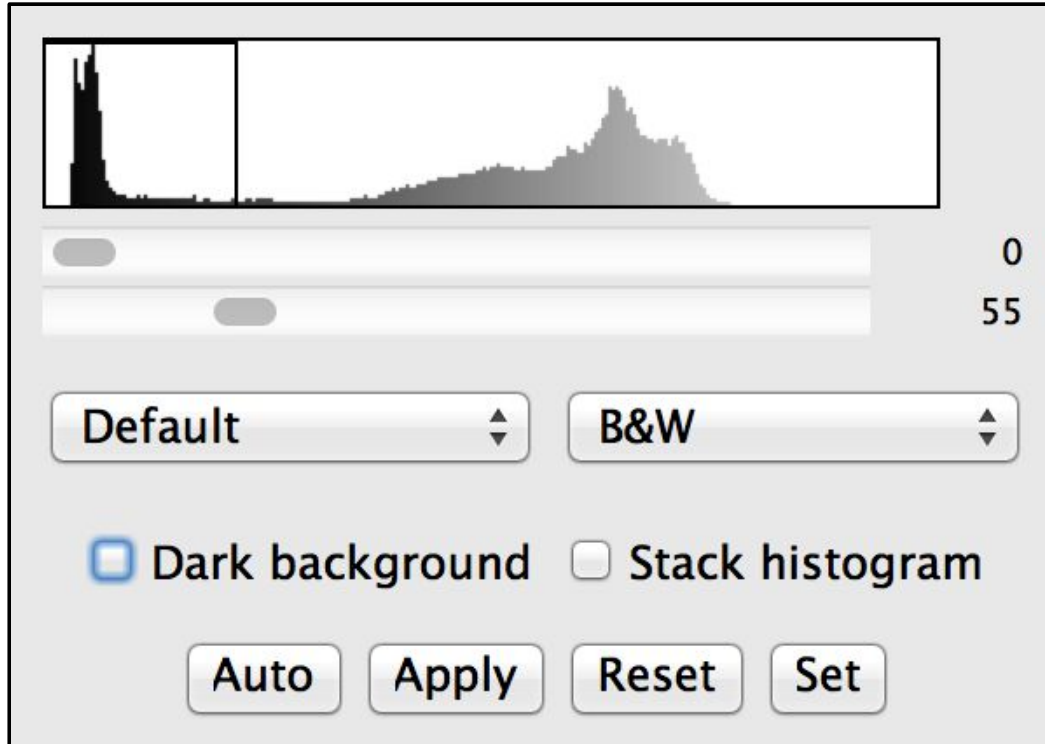
- Calculating the **threshold  $t$  automatically** is not always possible.
- Sometimes there is **no global threshold** and an **adaptive threshold** must be calculated.

# Point Operation: Binarisation



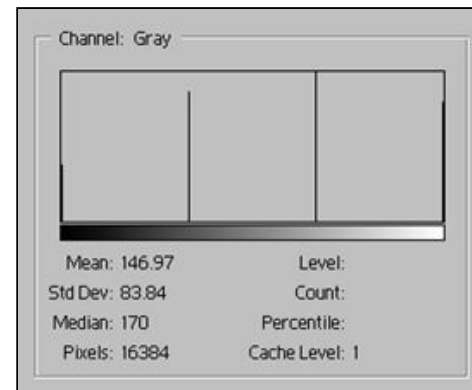
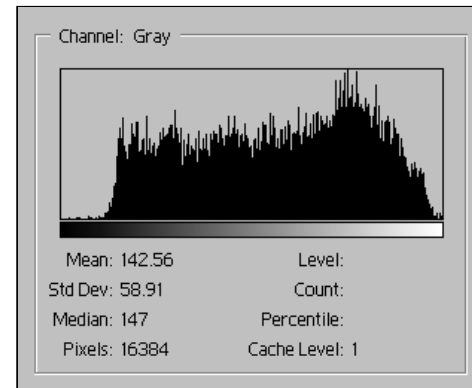
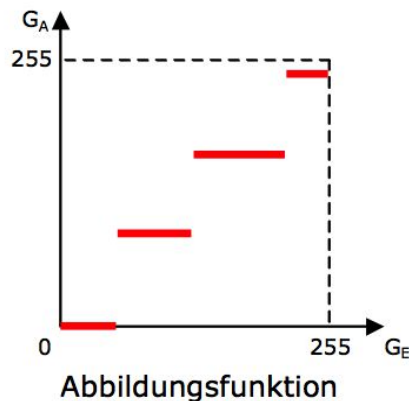
# Point Operation: Binarisation

- Manual setting threshold in **ImageJ**: Image > Adjust > Threshold



# Point Operation: Gray Level Reduction

- Reducing the NO. of gray levels is also known as gray level slicing.
- It is often a prestep for edge detection.
- The Reduction is mostly done with a **lookup table**.
- Well known algorithm: **Median Cut Algorithm** from Paul Heckbert
- Used for bit depth reduction for image formats (e.g. BMP, PNG & GIF)

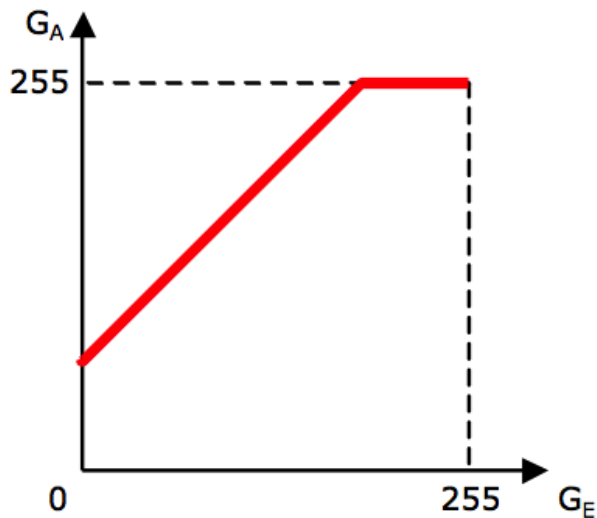


# Point Operation: Linear Brightness Correction

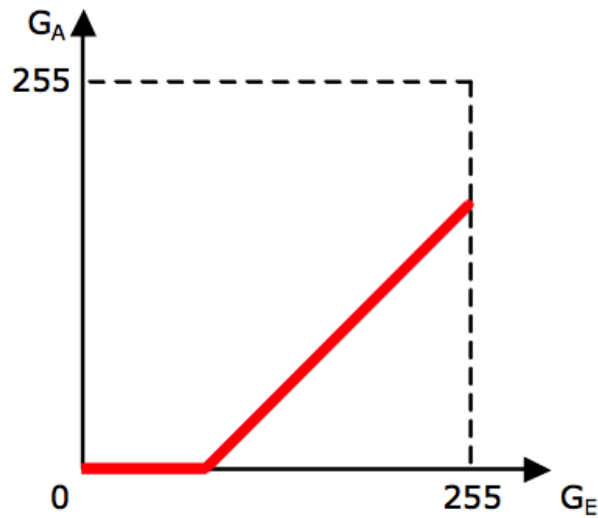
- Linear brightness correction can be expressed in the line equation:

$$g_A(x, y) = c \cdot g_E(x, y) + b$$

where  $c$  changes the contrast and  **$b$  the brightness**.



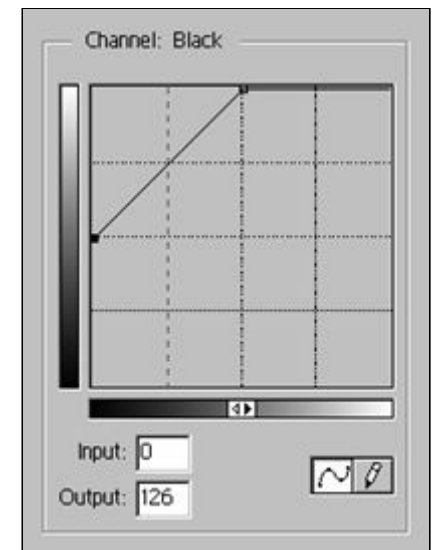
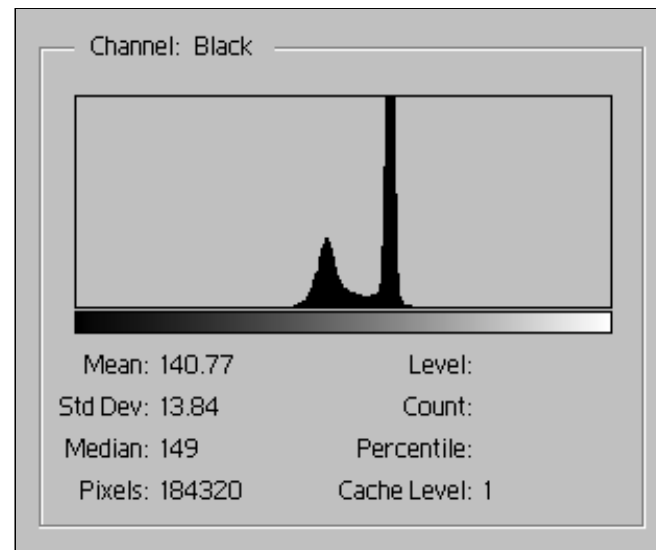
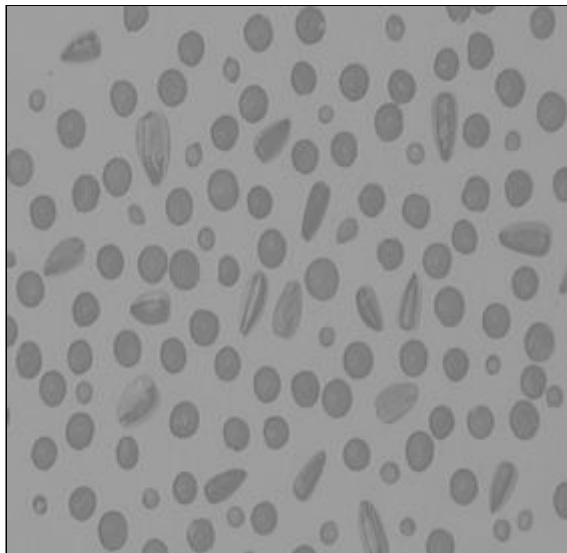
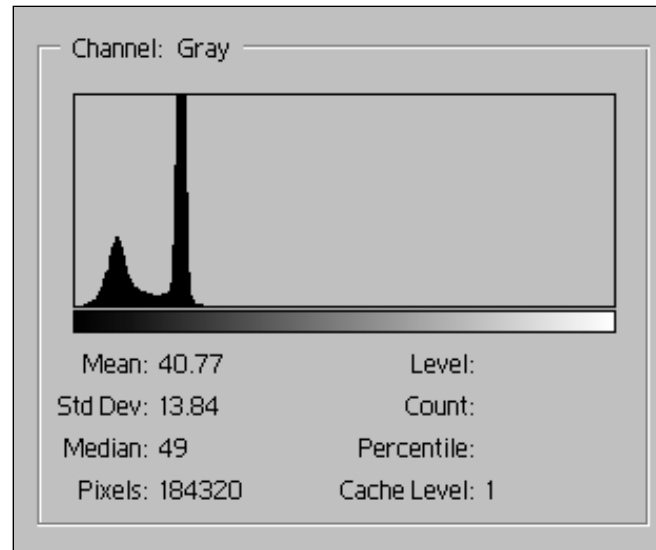
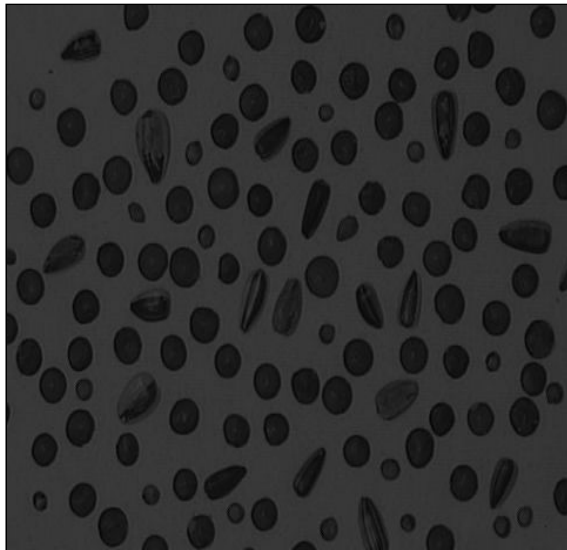
Abbildungsfunktion  
Helligkeit erhöhen



Abbildungsfunktion  
Helligkeit reduzieren

# Point Operation: Linear Brightness Correction

- The histogram is shifted:

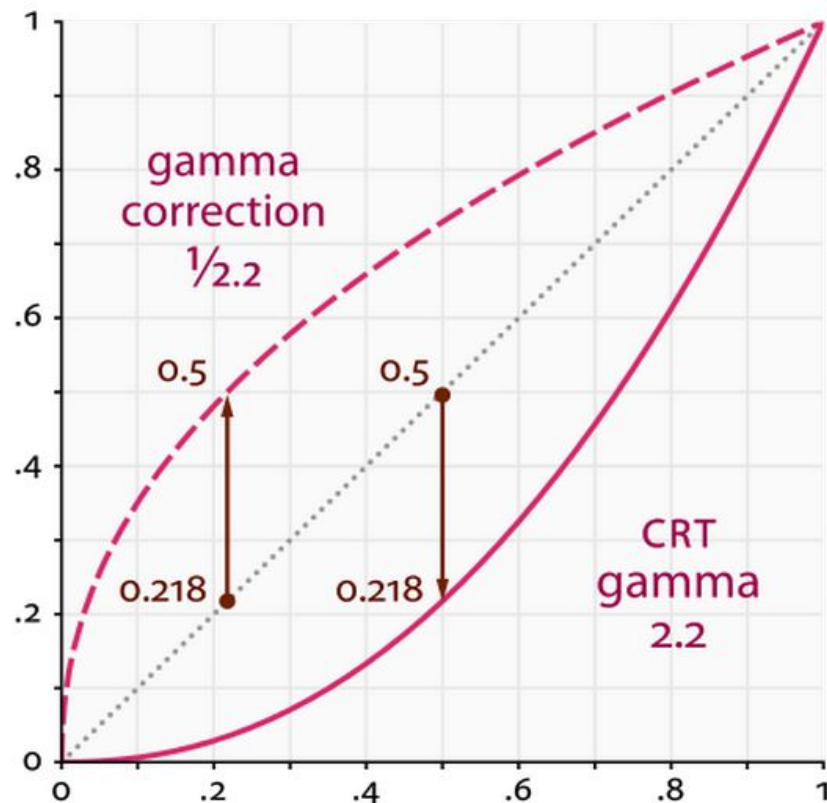


# Point Operation: Gamma Correction

- The **gamma correction** is a **non linear** brightness correction:

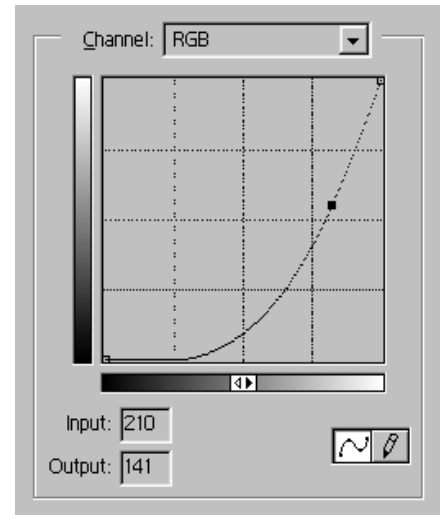
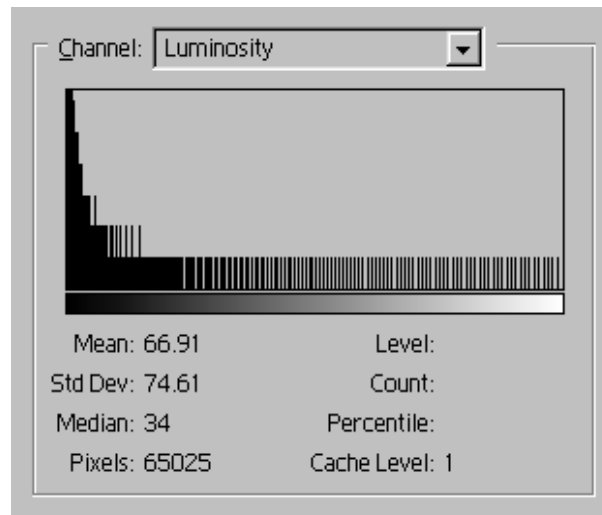
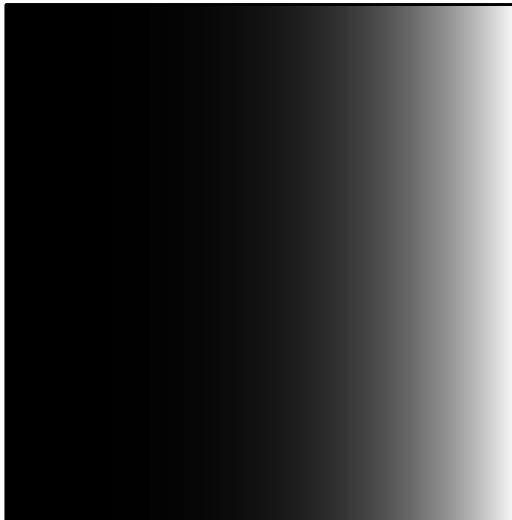
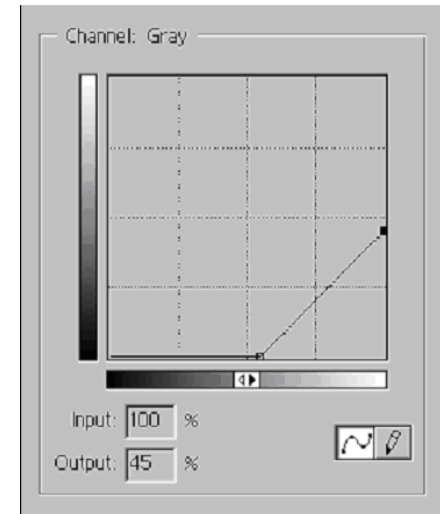
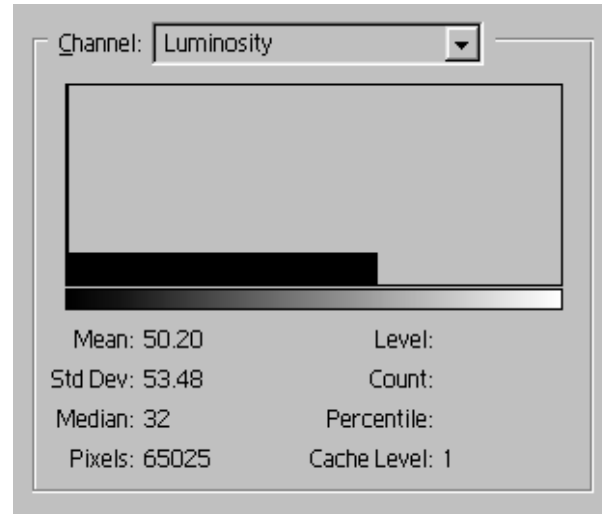
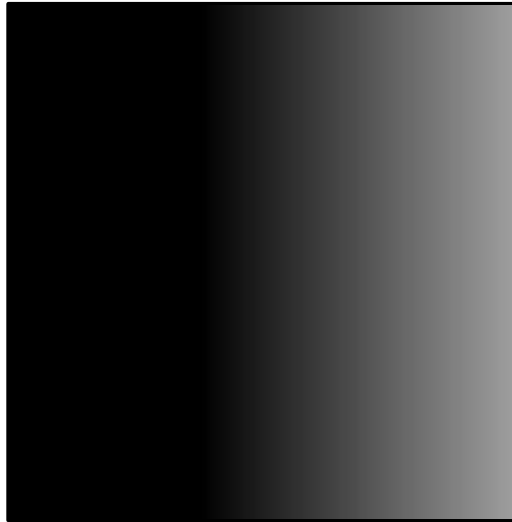
$$g_A(x, y) = 255 \cdot \left( \frac{g_E(x, y)}{255} \right)^\gamma$$

where  $\gamma < 1$  **increases** and  $\gamma > 1$  **decreases** the brightness:



# Point Operation: Gamma Correction

- The gamma correction **preserves information** in the dark & bright areas.





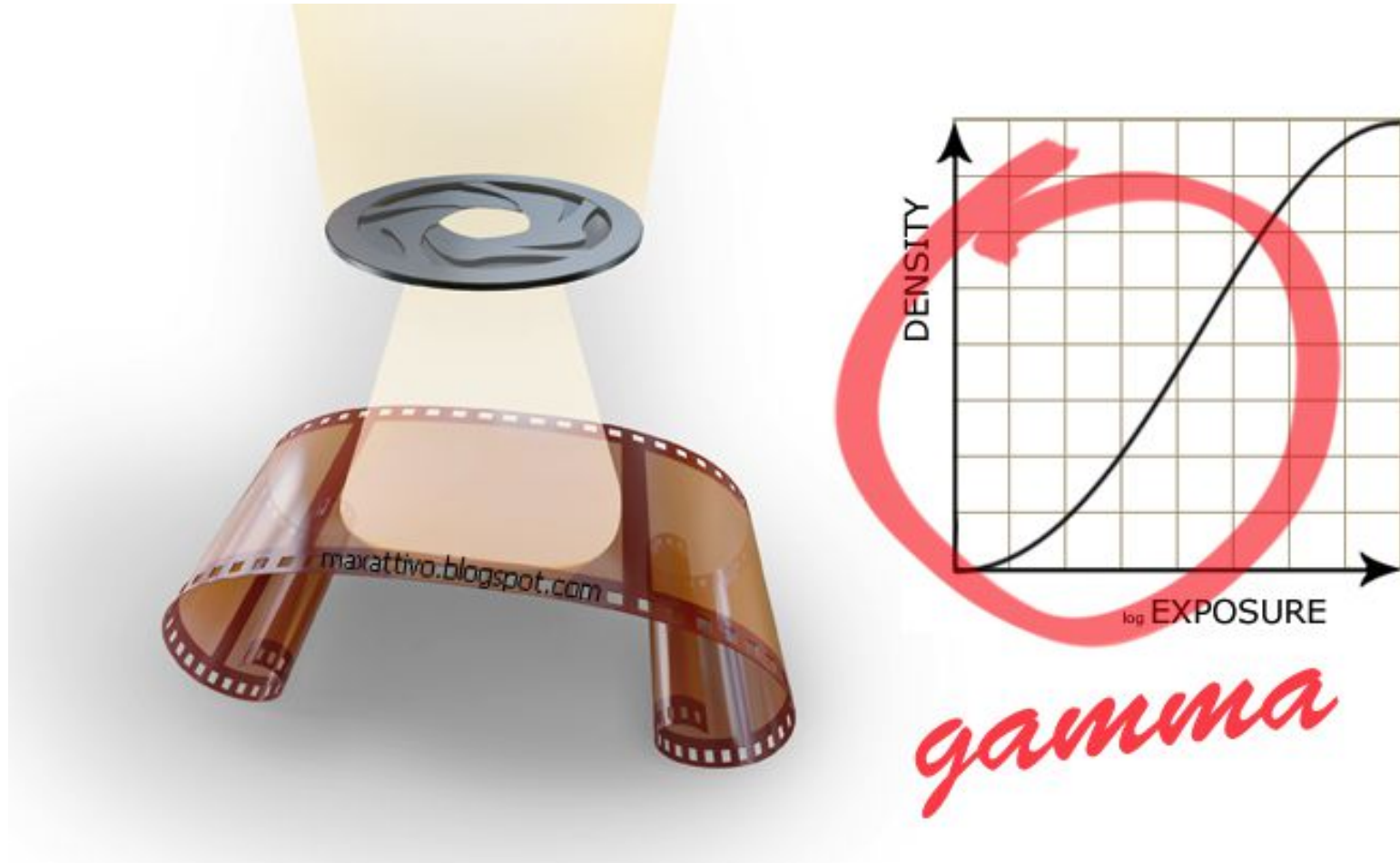
# Point Operation: Gamma Correction



Image: [en.wikipedia.org/wiki/Gamma\\_correction](https://en.wikipedia.org/wiki/Gamma_correction)

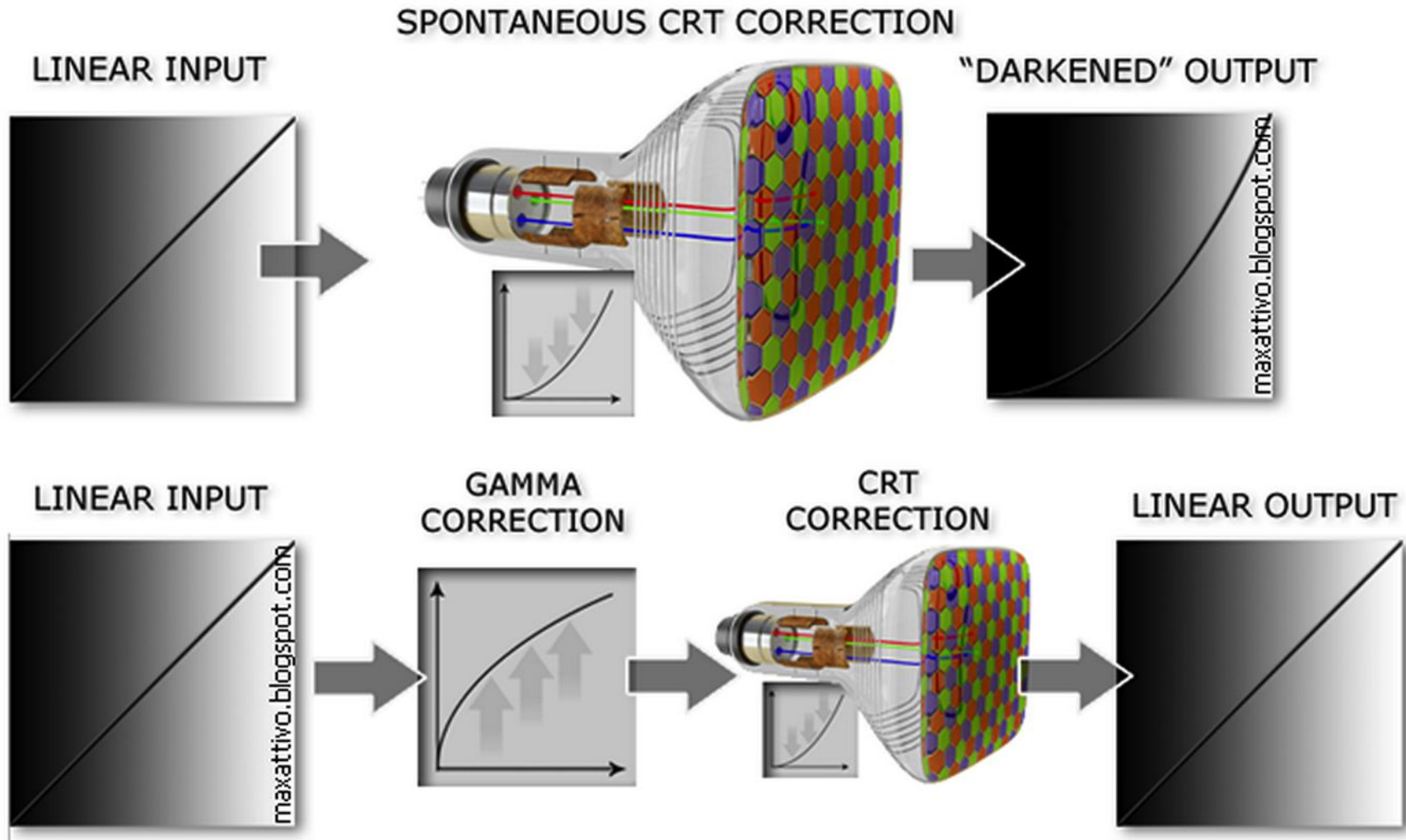
# Point Operation: Gamma Correction

- Gamma correction is important because **analog devices have non linear sensitivity**.
- E.g. analog **film material** has a **non linear sensitivity**:



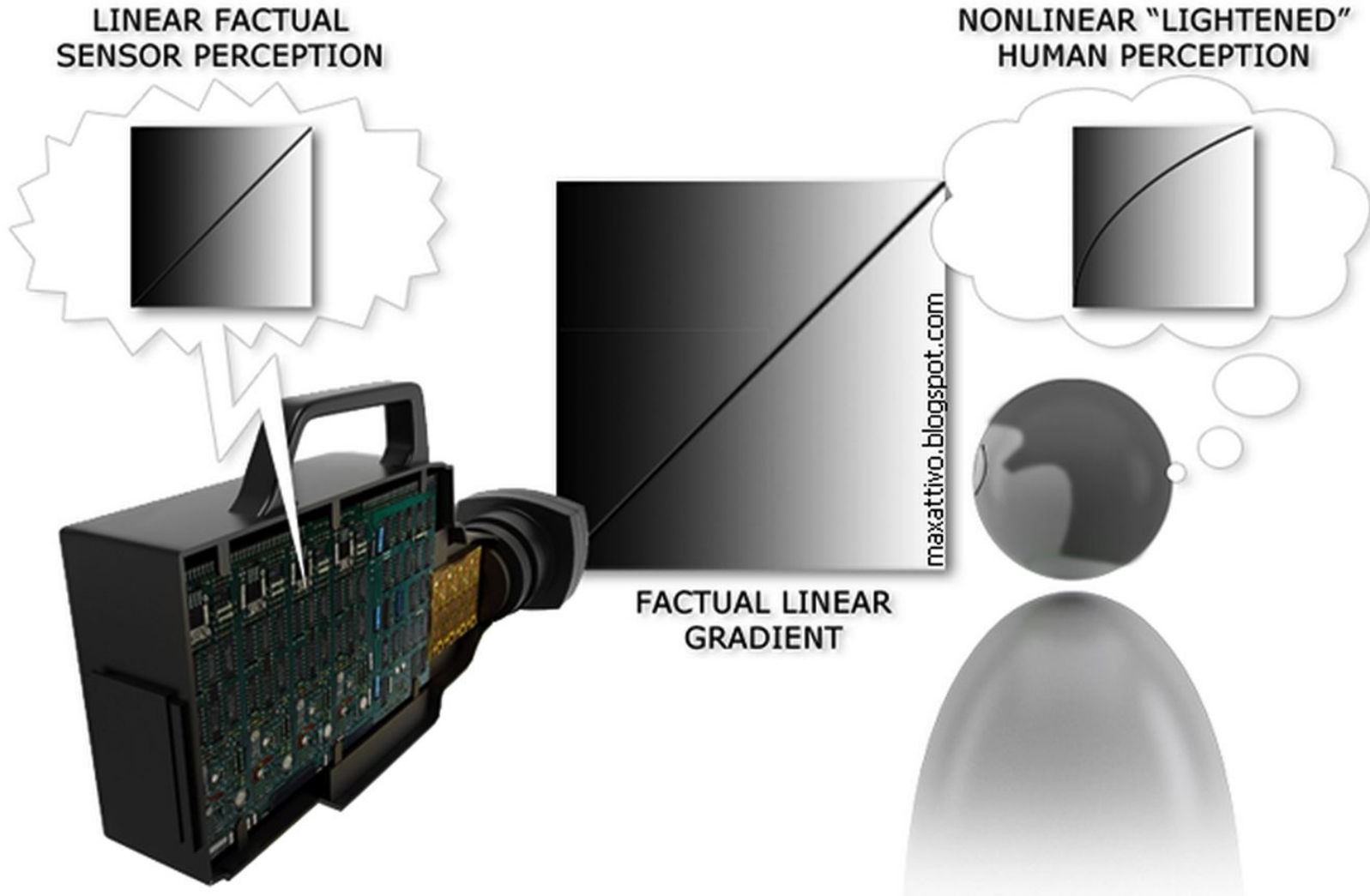
# Point Operation: Gamma Correction

- **CRT Monitors** display power is **not linear**:



# Point Operation: Gamma Correction

- The **human light perception** is also **not linear**:



# Point Operation: Gamma Correction

- Gamma Correction is important in the **digital workflow**:

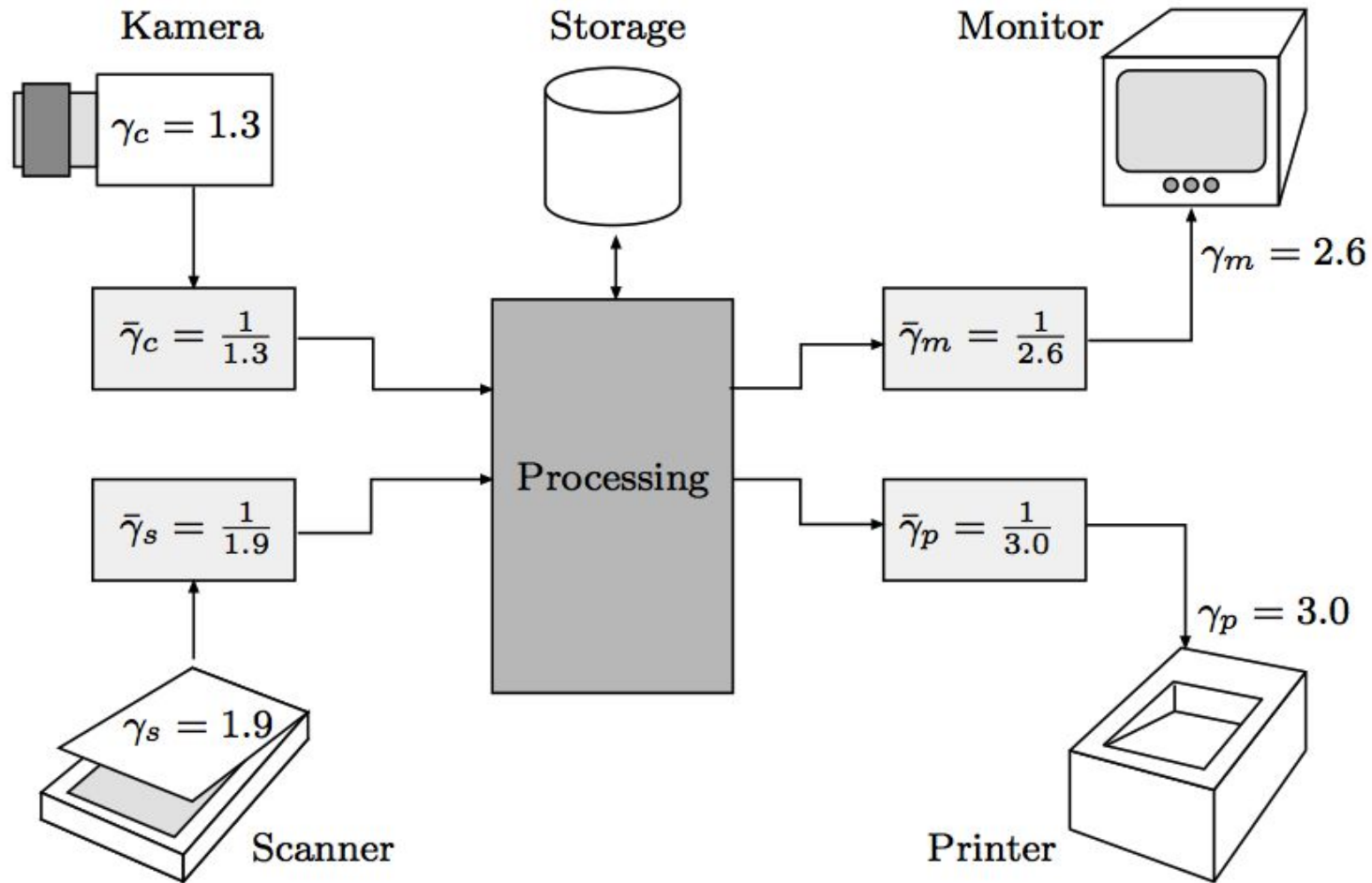


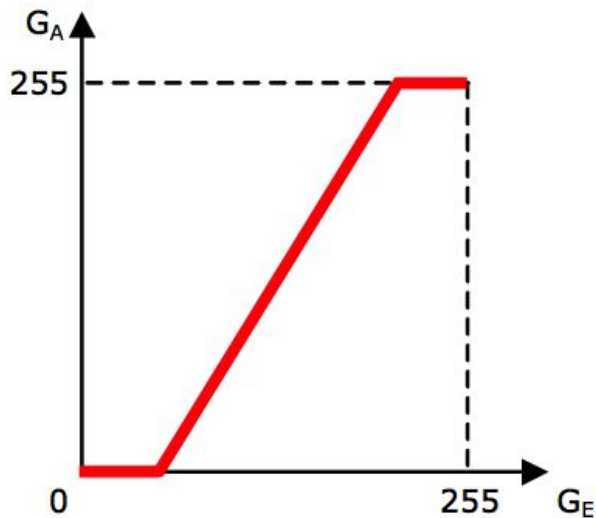
Image: W. Burger: [imagingbook.com](http://imagingbook.com)

# Point Operation: Linear Contrast Correction

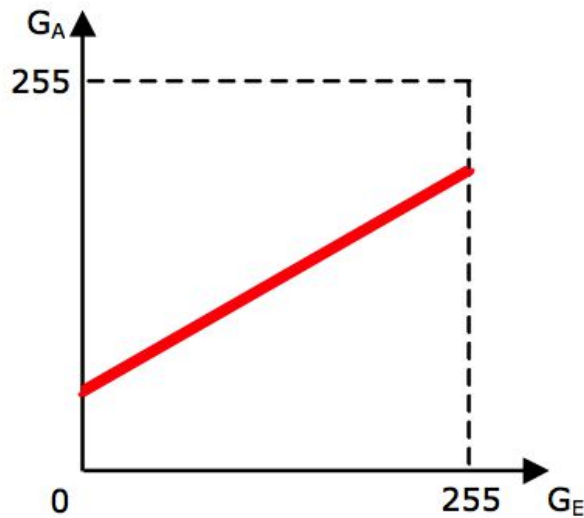
- Linear contrast correction can be expressed in the line equation:

$$g_A(x, y) = c \cdot g_E(x, y) + b$$

where **c** changes the contrast and *b* the brightness.



Abbildungsfunktion  
Kontrasterhöhung

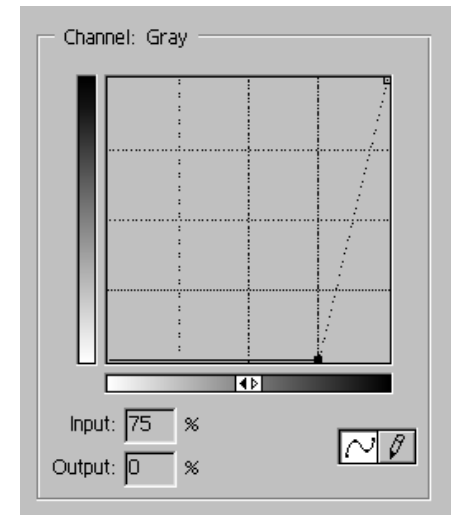
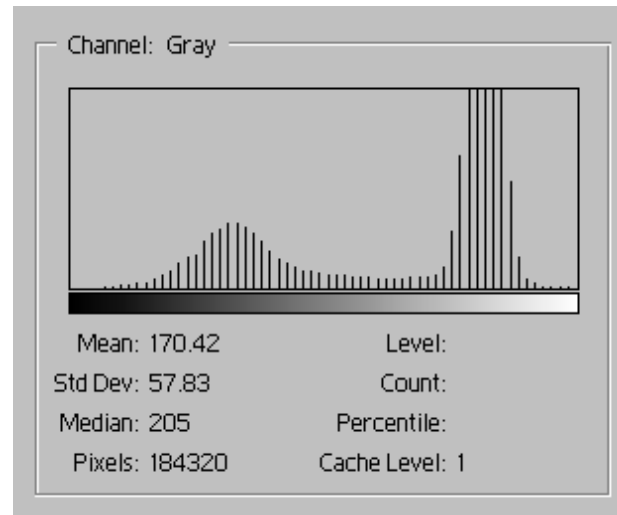
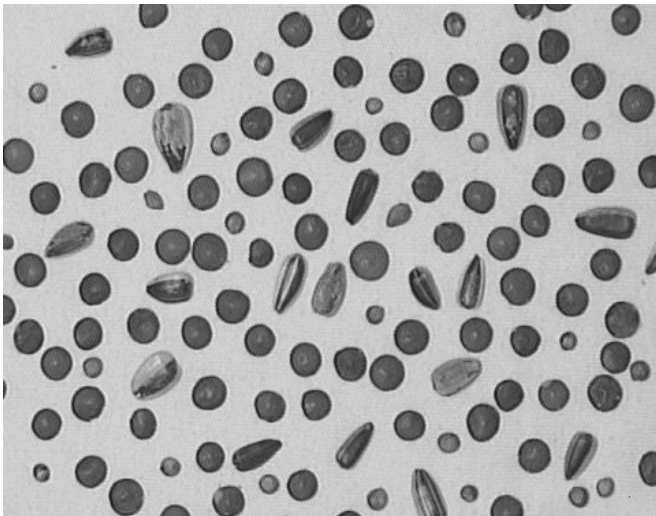
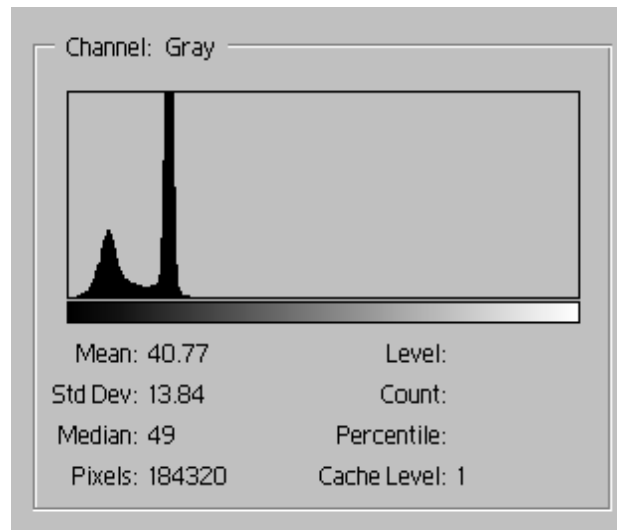
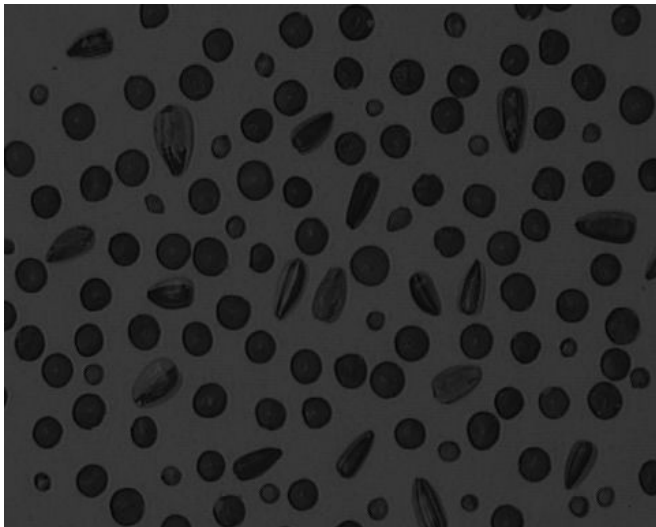


Abbildungsfunktion  
Kontrastverminderung



# Point Operation: Linear Contrast Correction

- The histogram is spread:



# Point Operation: Linear Contrast Correction

- For **automatic contrast correction** the formula is:

$$g_A(x, y) = (g_E(x, y) - g_{\min}) \cdot \frac{255}{g_{\max} - g_{\min}}$$

- If  $g_{\min} = 0$  and  $g_{\max} = 255$  we cut off a percentage of the brightest and darkest:

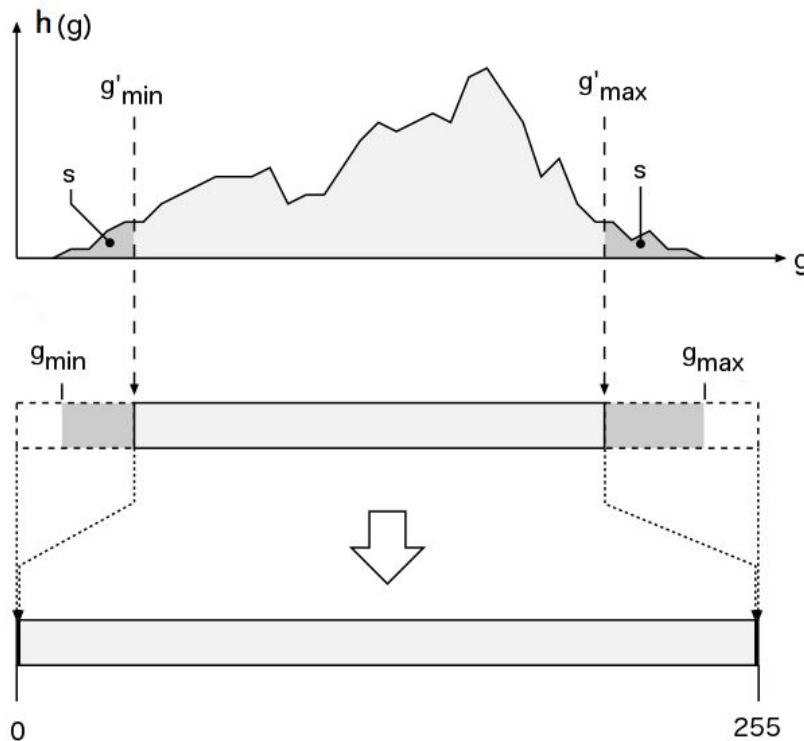


Image: W. Burger: [imagingbook.com](http://imagingbook.com)



# Point Operation: Histogram Equalization

- Another automatic contrast correction is the **equalization of the histogram**.
- The algorithm uses the **cummulative histogram**:

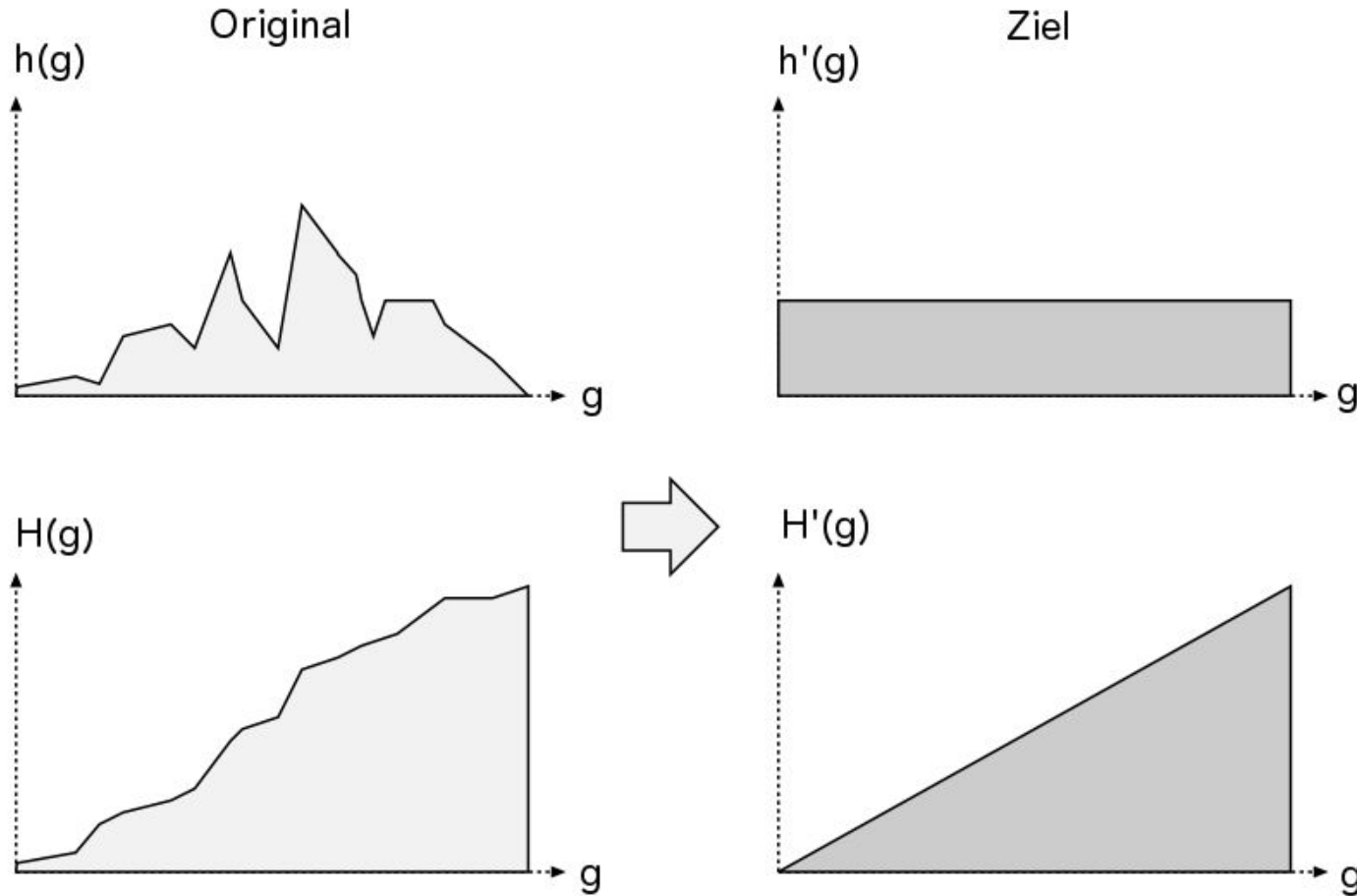
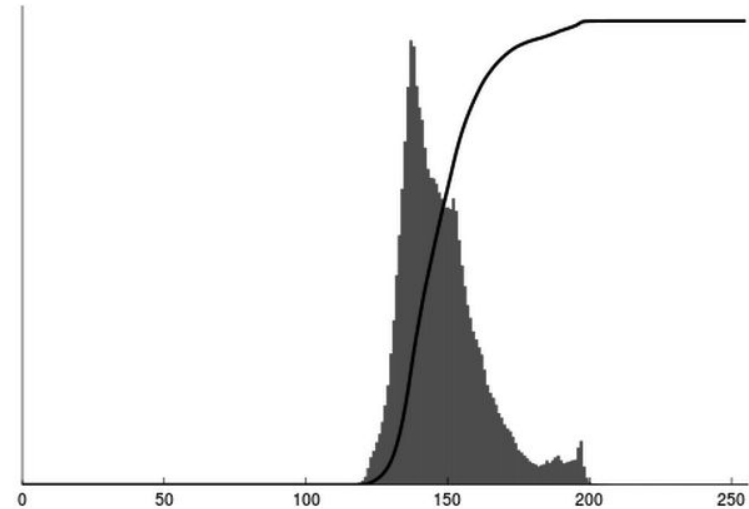


Image: W. Burger: [imagingbook.com](http://imagingbook.com)

# Point Operation: Histogram Equalization

- We can use the cumulative histogram as a LUT.
- Gray levels with lots of pixels get spread apart.

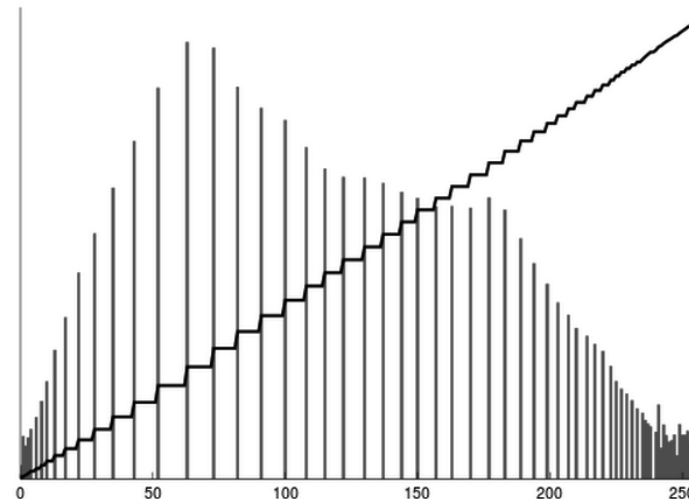
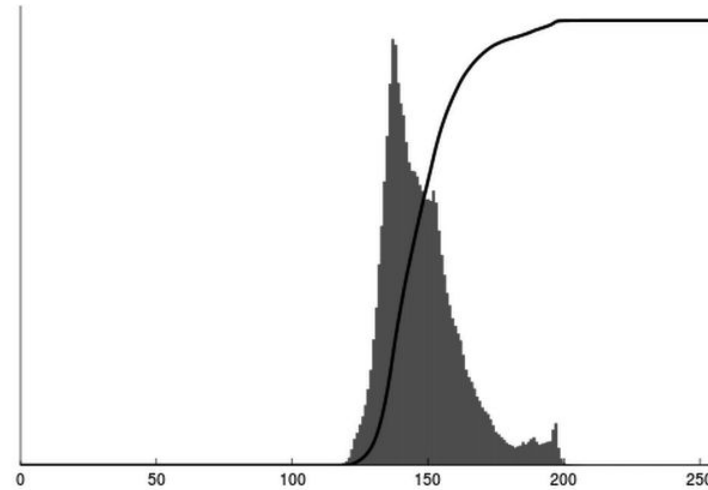


- The scaled cumulative histogram is used as mapping function:

$$f_{eq}(g) = H(g) \cdot \frac{(K-1)}{N}$$

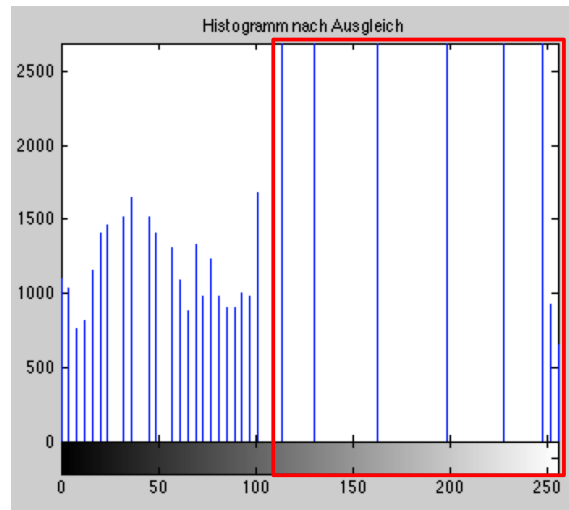
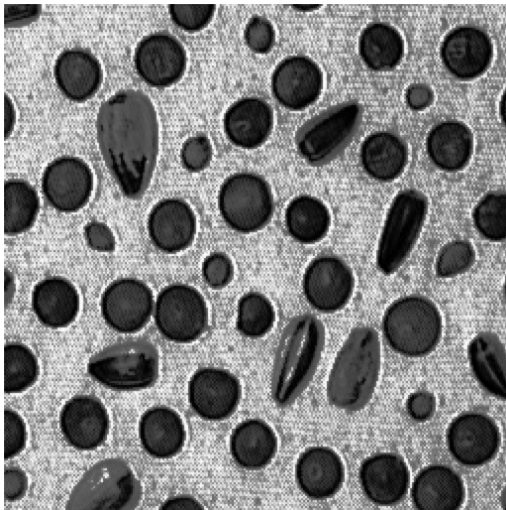
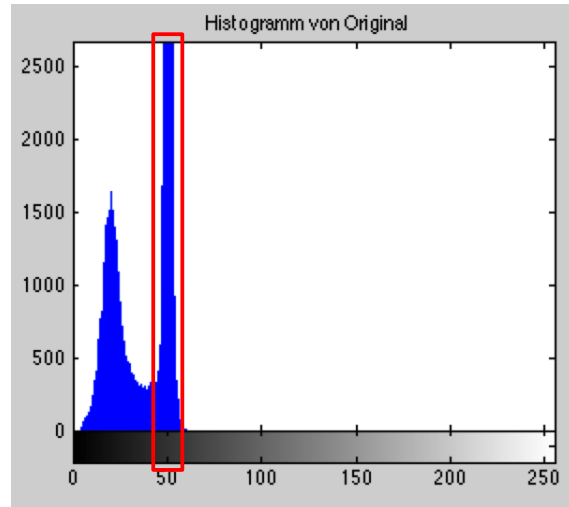
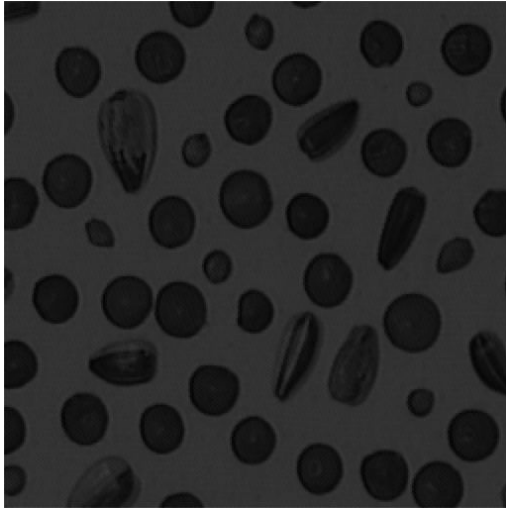
# Point Operation: Histogram Equalization

- After the histogram equalization we have equal or less gray levels.
- We often loose information even that the contrast is strong.



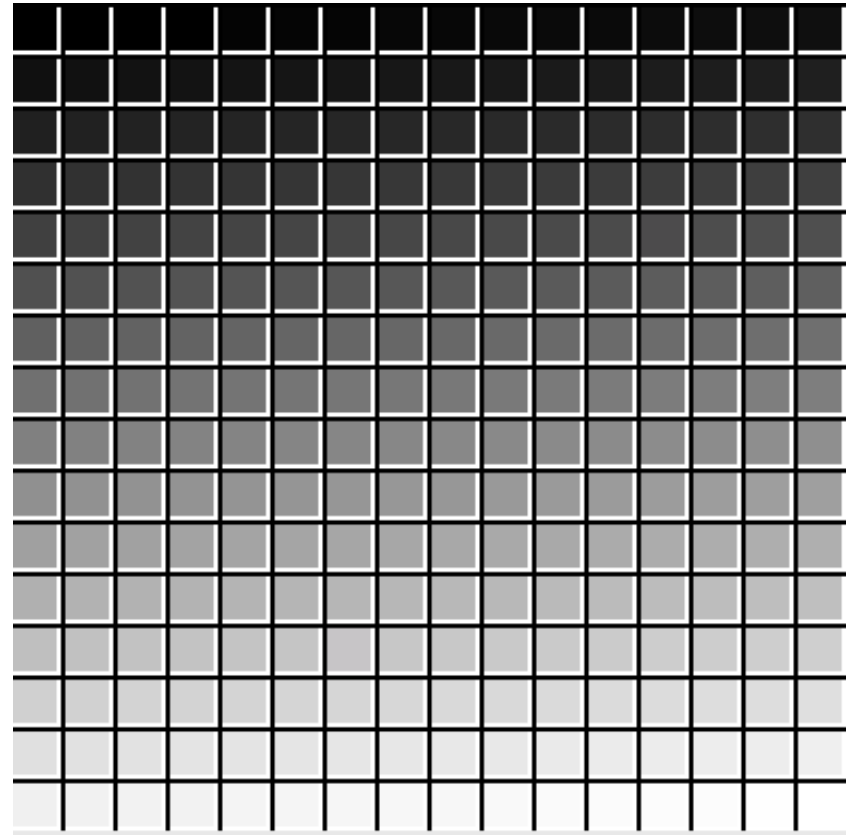
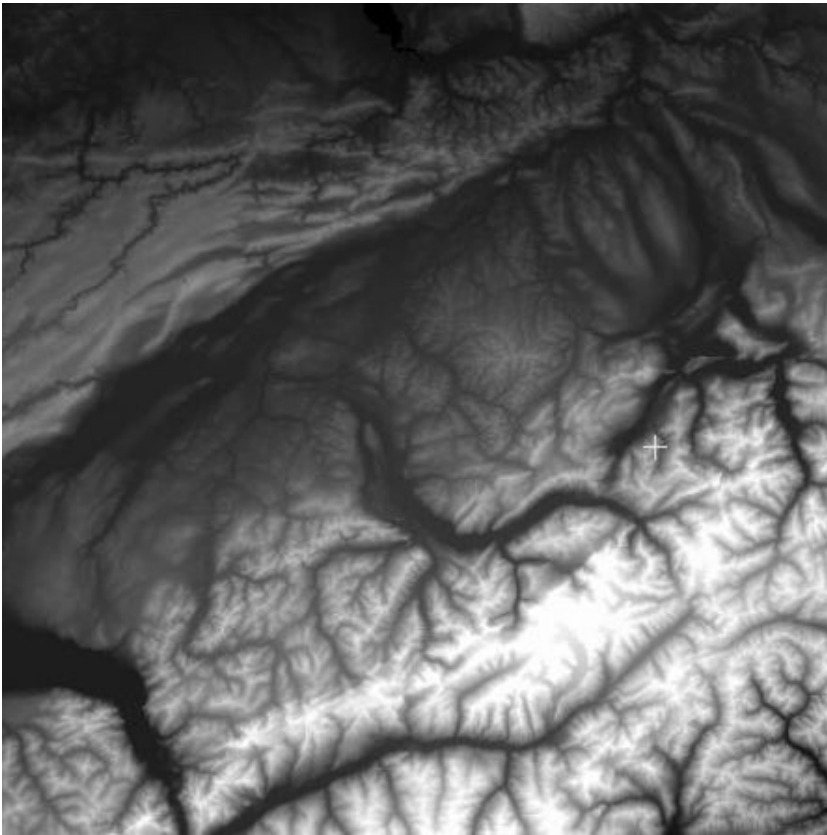
# Point Operation: Histogram Equalization

- Histogram Equalization can lead to noise in homogenous regions.
- A few gray levels with lots of pixels get torn apart:



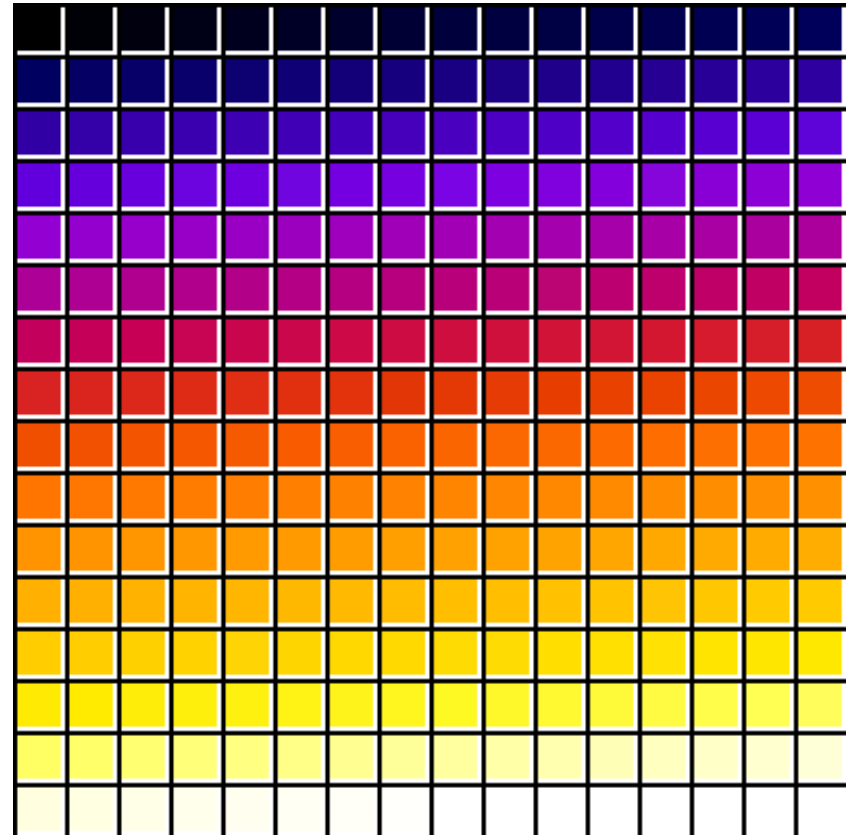
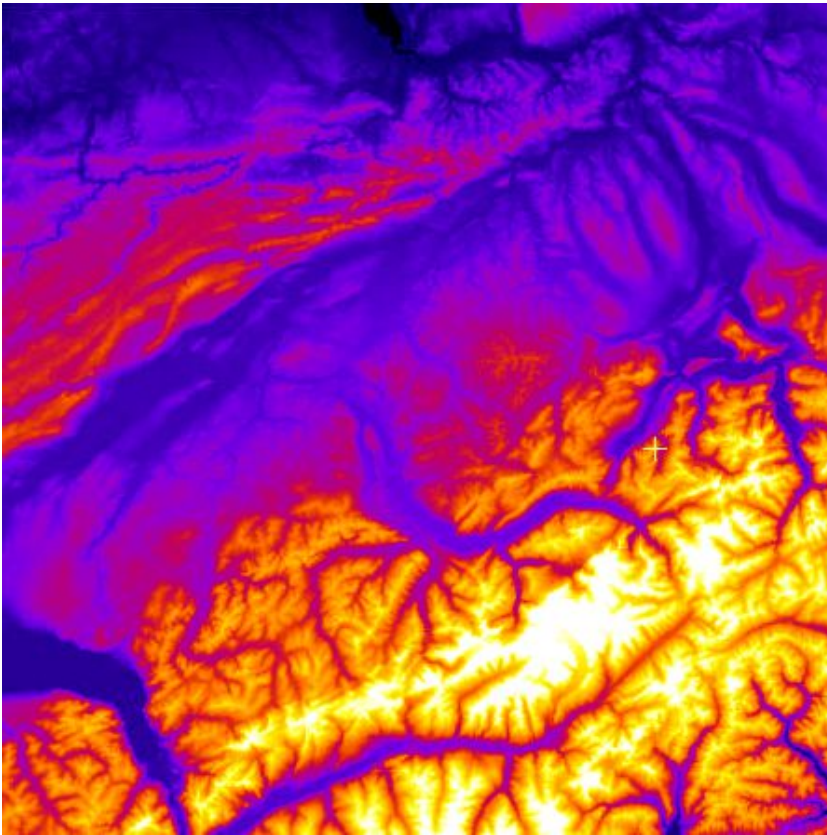
# Point Operation: Increase Contrast with Colors

- The human eye can **distinct only 60 gray levels**.
- With **color lookup tables** we can visualize **more information**.
- Height map of Switzerland with 256 gray scales:



# Point Operation: Increase Contrast with Colors

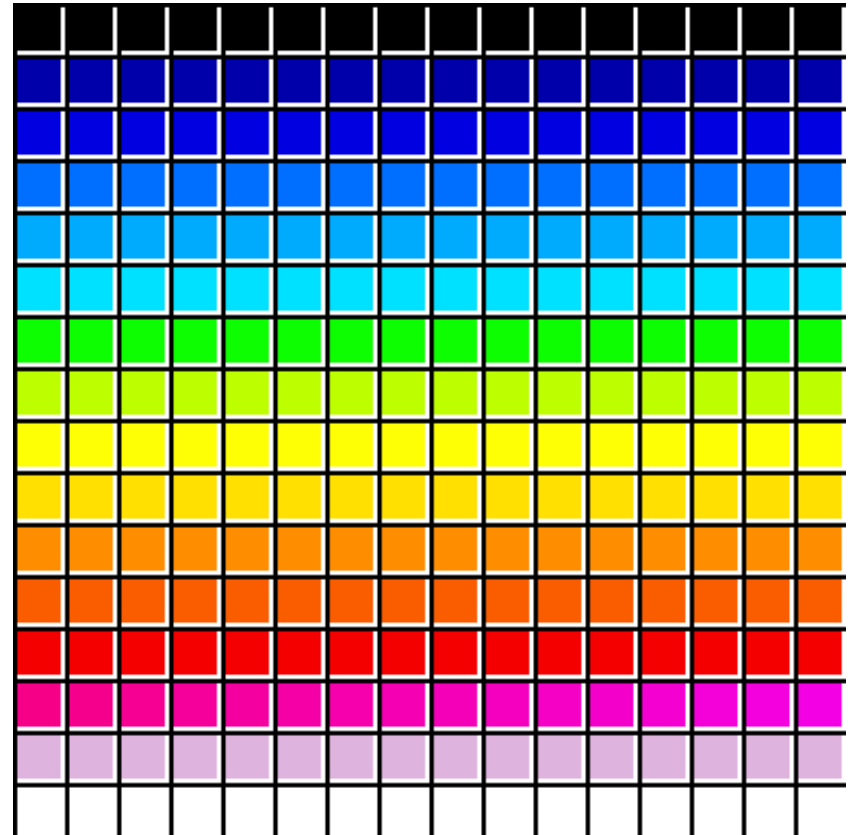
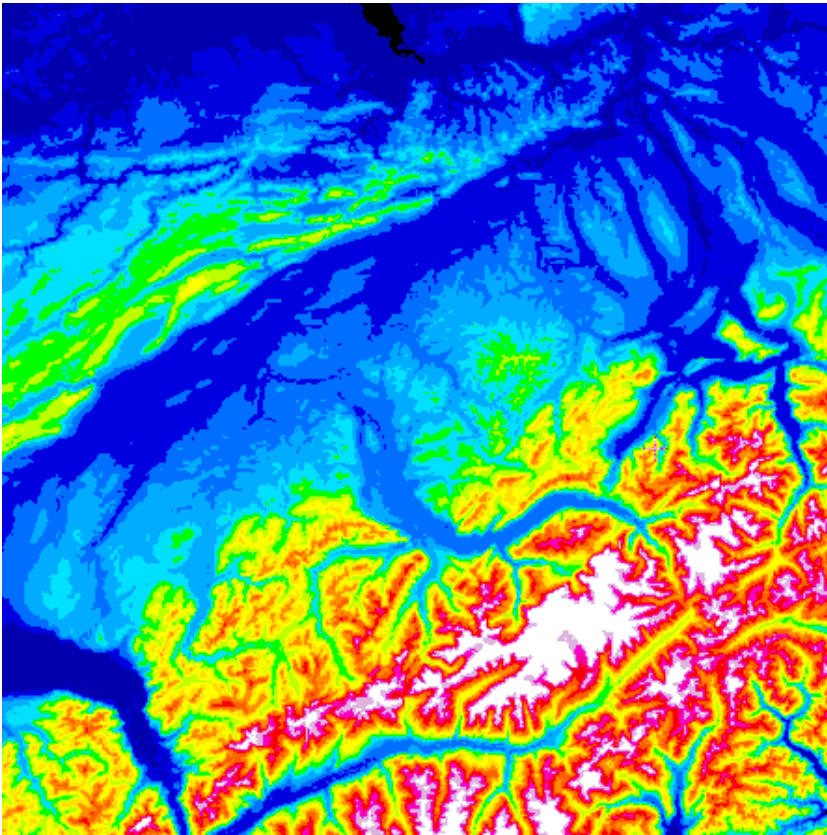
- The human eye can **distinct only 60 gray levels**.
- With **colors** we can visualize **more information**.
- Height map of Switzerland with **ImageJ Fire LUT**:





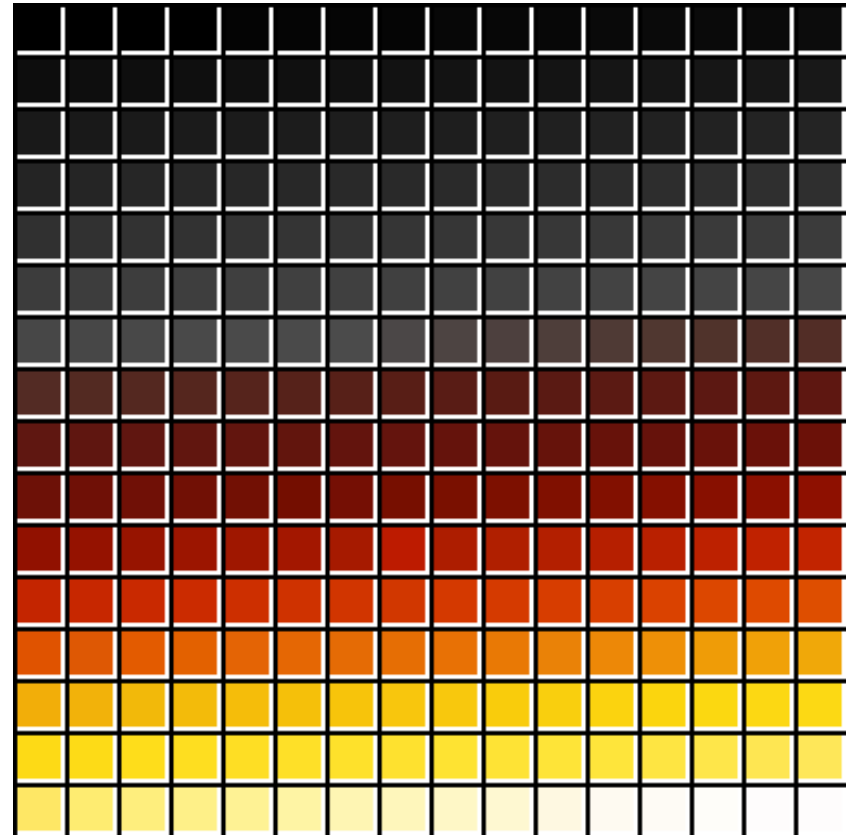
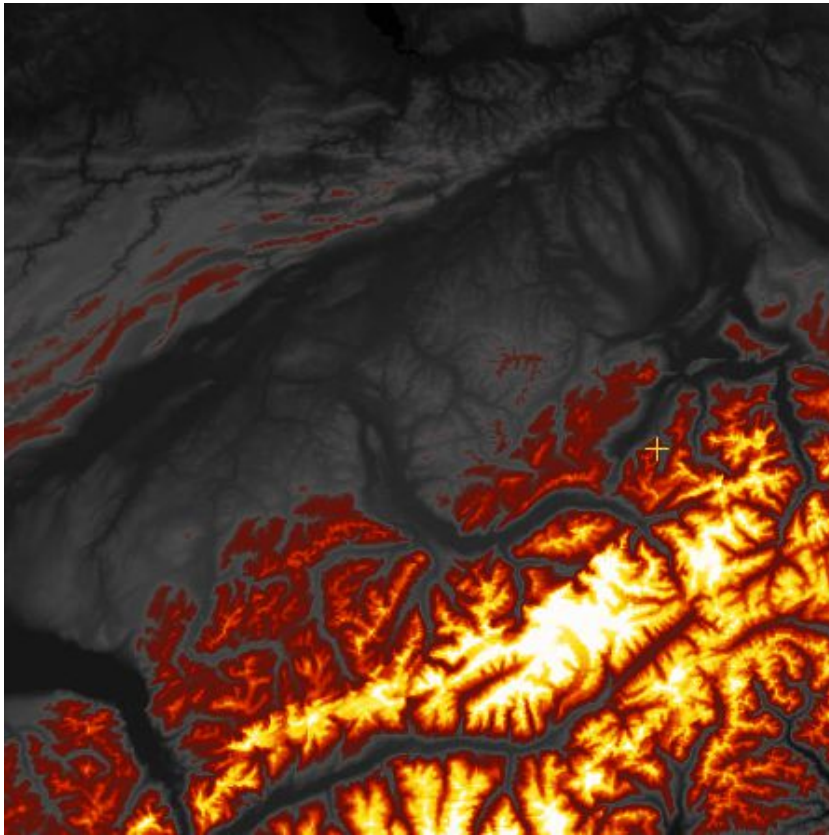
# Point Operation: Increase Contrast with Colors

- The human eye can **distinct only 60 gray levels**.
- With **color lookup tables** we can visualize **more information**.
- Height map of Switzerland with **ImageJ 16 Colors LUT**:



# Point Operation: Increase Contrast with Colors

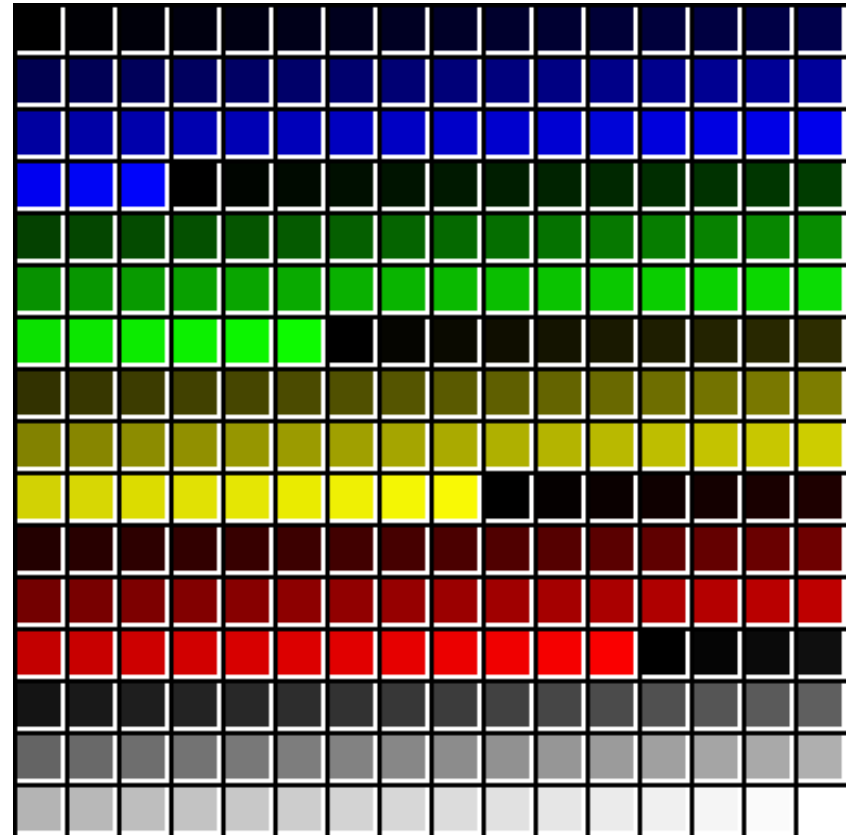
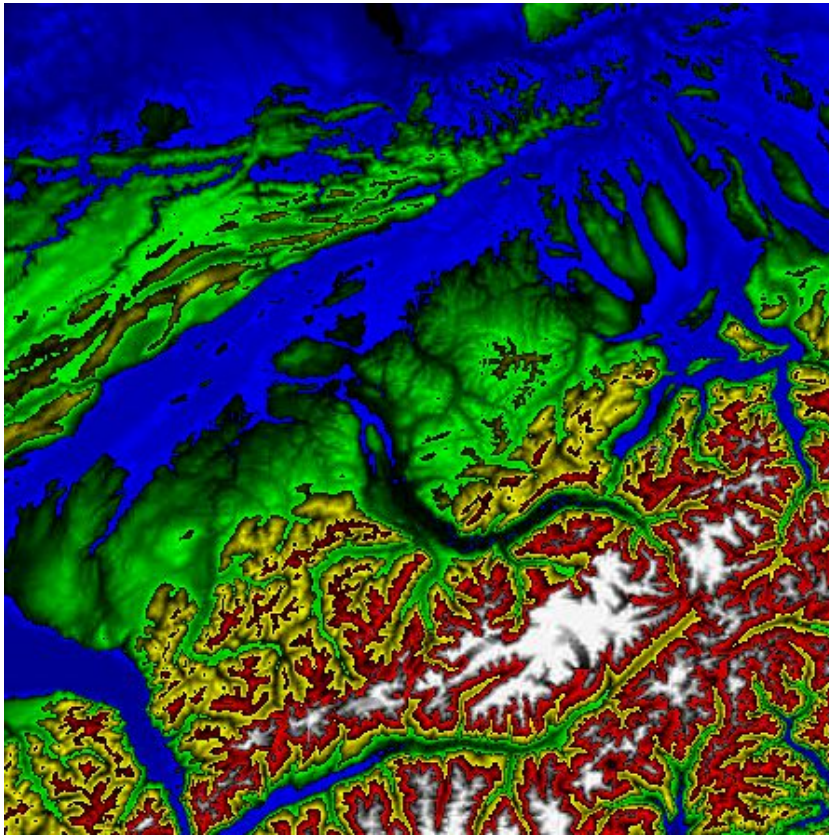
- The human eye can **distinct only 60 gray levels**.
- With **color lookup tables** we can visualize **more information**.
- Height map of Switzerland with **ImageJ Smart LUT**:





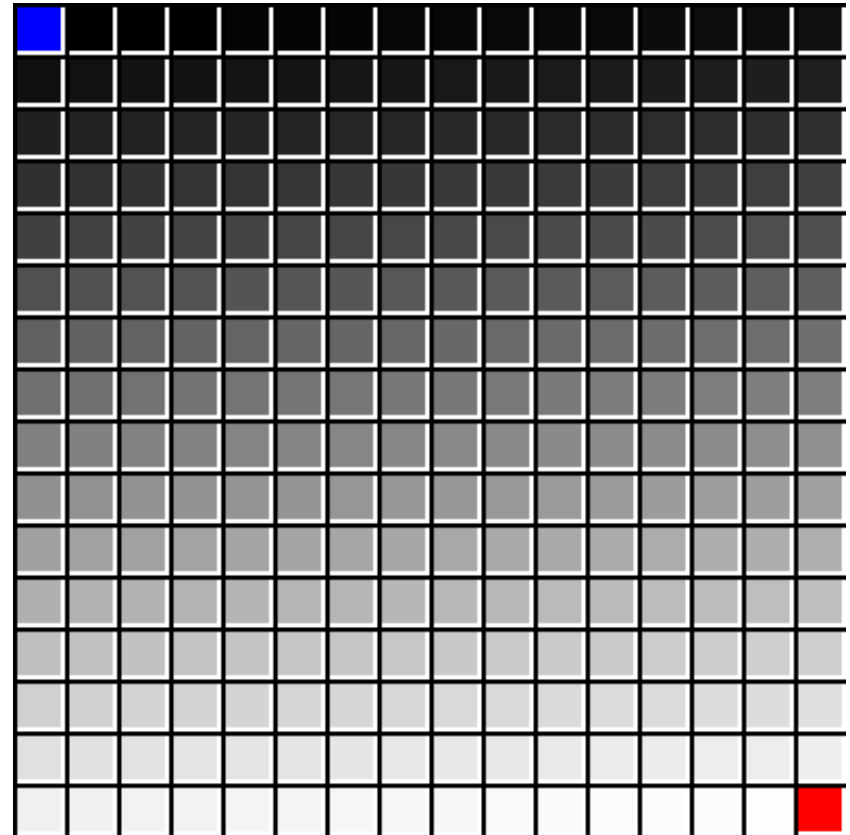
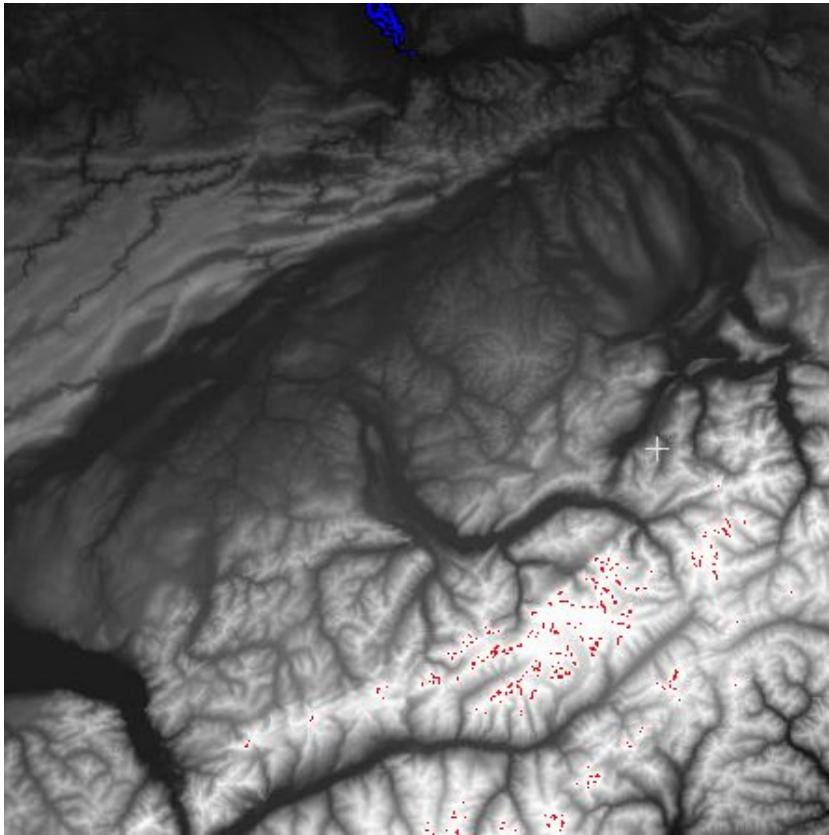
# Point Operation: Increase Contrast with Colors

- The human eye can **distinct only 60 gray levels**.
- With **color lookup tables** we can visualize **more information**.
- Height map of Switzerland with **ImageJ 5 Ramps LUT**:



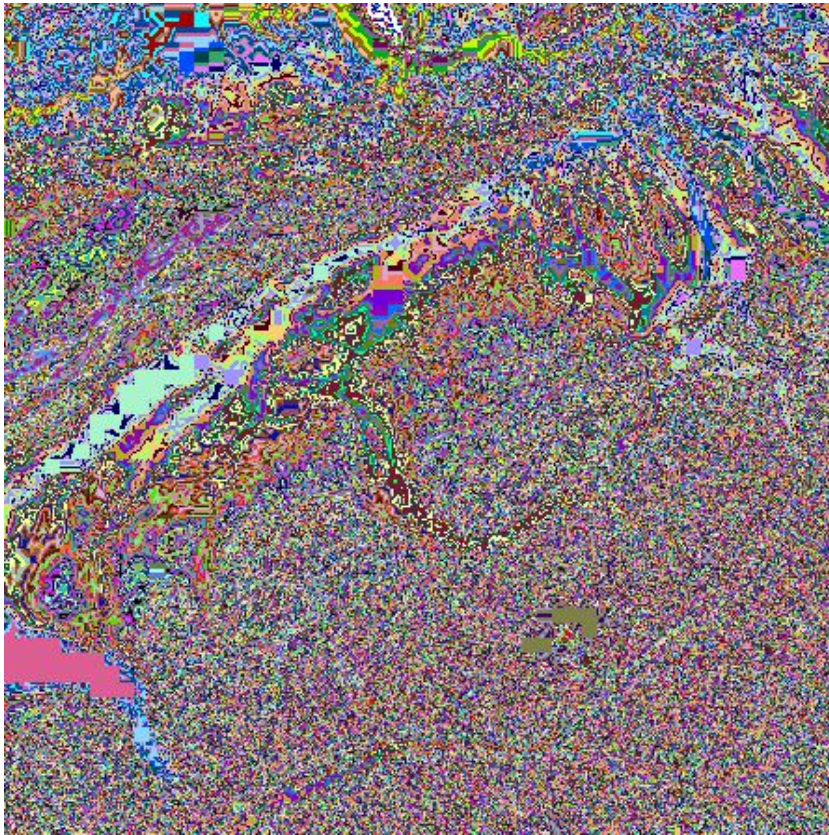
# Point Operation: Increase Contrast with Colors

- The human eye can **distinct only 60 gray levels**.
- With **color lookup tables** we can visualize **more information**.
- Height map of Switzerland with **ImageJ HiLo LUT**:



# Point Operation: Increase Contrast with Colors

- The human eye can **distinct only 60 gray levels**.
- With **color lookup tables** we can visualize **more information**.
- Height map of Switzerland with **ImageJ HiLo LUT**:



# Point Operation: Image Arithmetic

- With brightness & contrast correction we used arithmetics with constant  $c$  &  $b$ :

$$g_A(x, y) = c \cdot g_E(x, y) + b$$

- We can do also arithmetics with varying values of 2 images.
- With the constants  $k1$  and  $k2$  we take care to be within the range 0-255:

- Addition: 
$$g_A(x, y) = (g_{E1}(x, y) + g_{E2}(x, y)) \cdot k1 + k2$$

- Subtraction: 
$$g_A(x, y) = (g_{E1}(x, y) - g_{E2}(x, y)) \cdot k1 + k2$$

- Multiplication: 
$$g_A(x, y) = (g_{E1}(x, y) \cdot g_{E2}(x, y)) \cdot k1 + k2$$

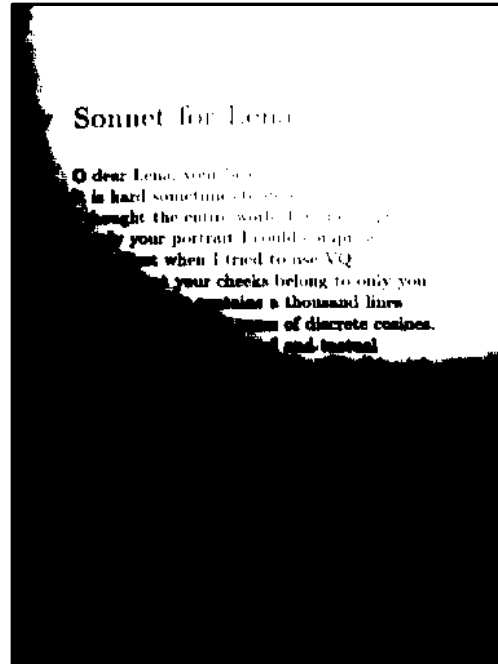
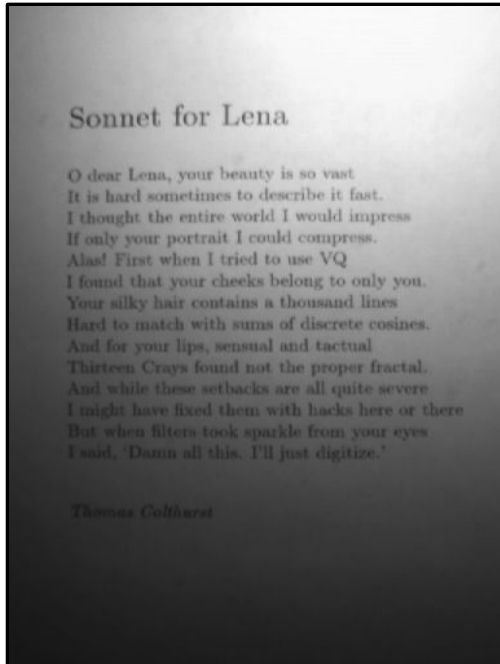
- Division: 
$$g_A(x, y) = (g_{E1}(x, y) / g_{E2}(x, y)) \cdot k1 + k2$$



# Point Operation: Image Arithmetic

## Example: Separate text from background:

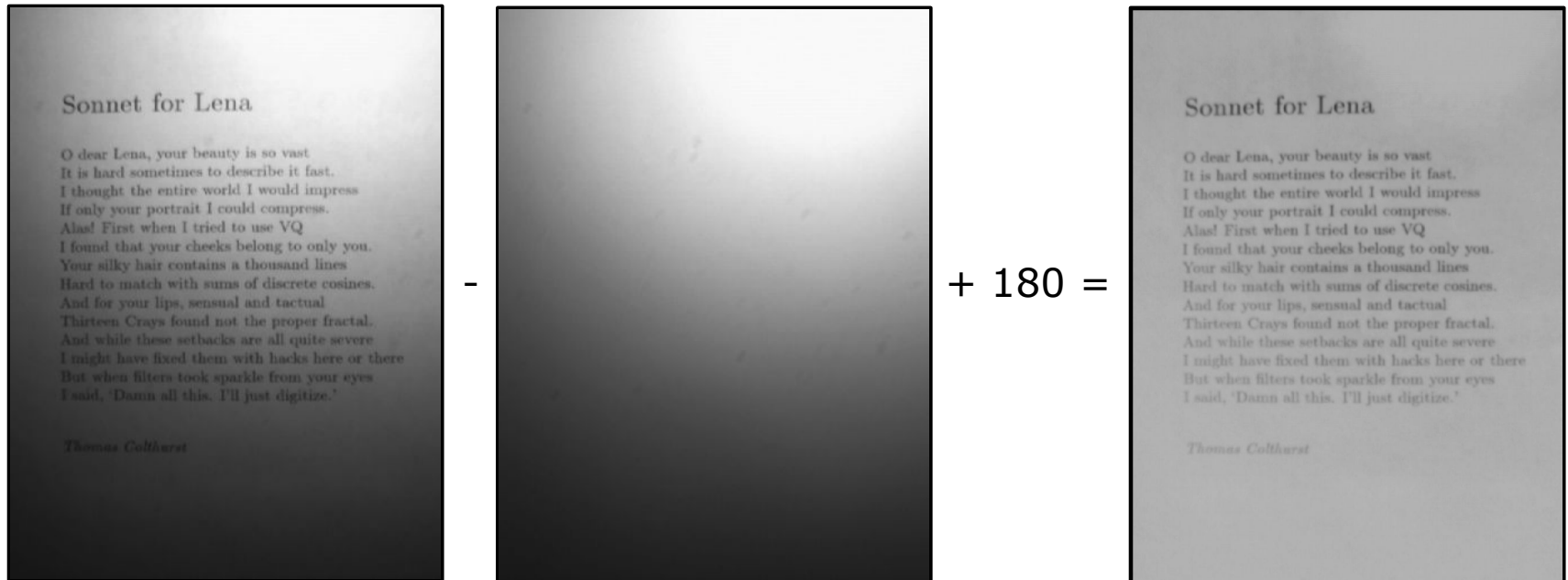
- Not possible with one distinct threshold:



# Point Operation: Image Arithmetic

## Example: Separate text from background:

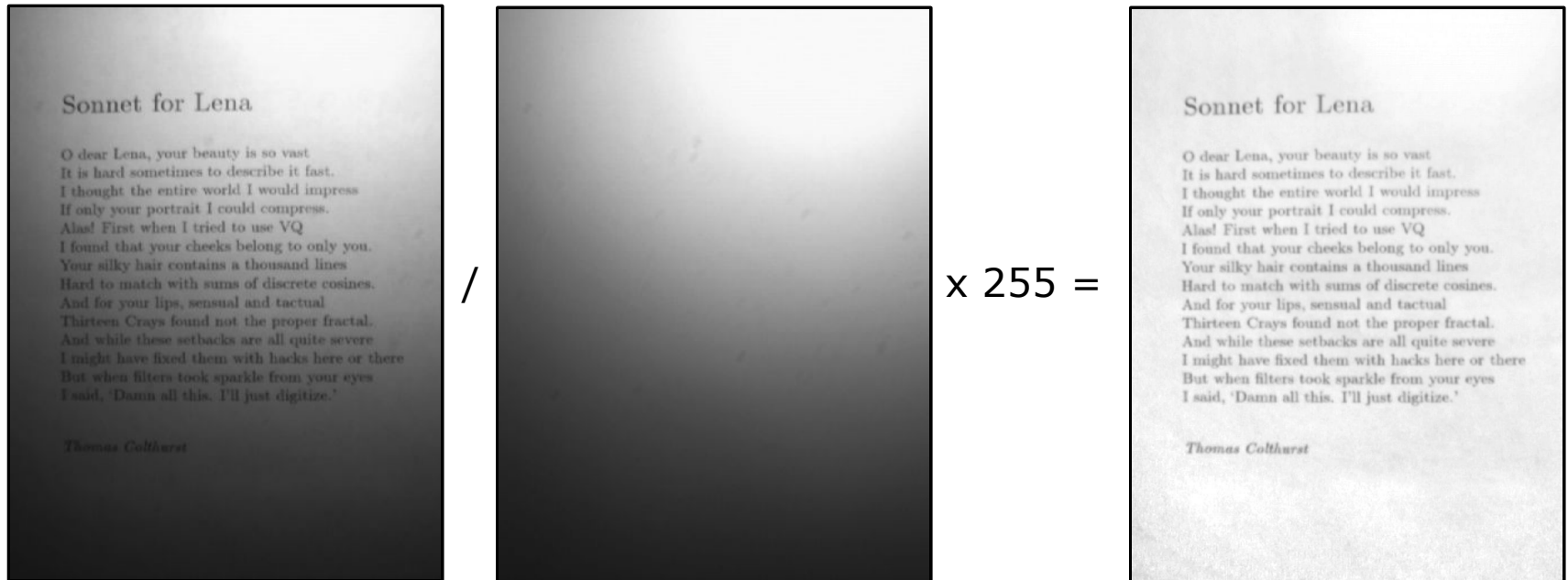
- We can subtract the background:



# Point Operation: Image Arithmetic

## Example: Separate text from background:

- We can divide by the background:



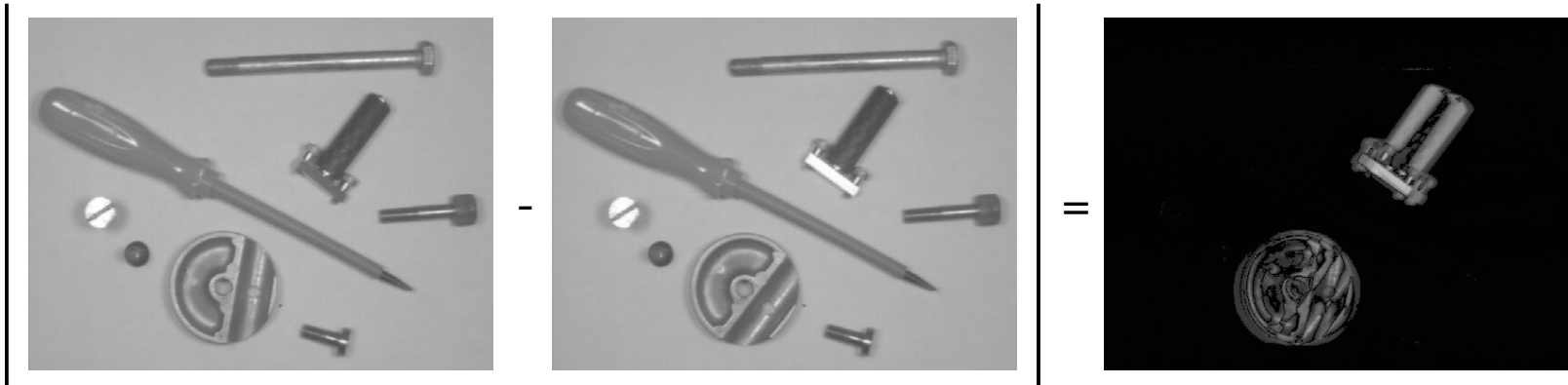
Remains the question how to get the background?

- With a median filter (denoising filter, chapter 6)
- and/or with a gaussian (averaging filter, chapter 6)

# Point Operation: Image Arithmetic

**Example: Detecting shifted object with absolute difference:**

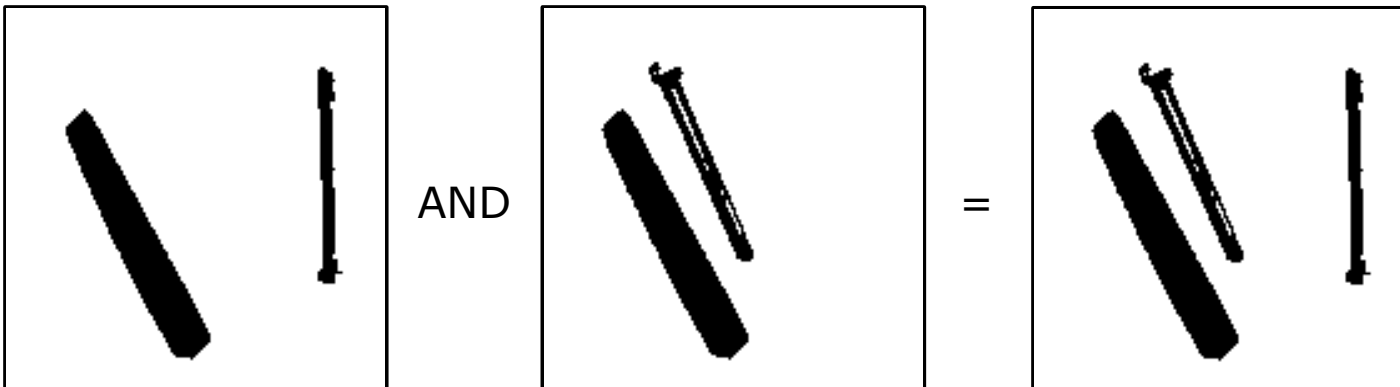
$$g_A(x, y) = |g_{E1}(x, y) - g_{E2}(x, y)|$$





# Point Operation: Logic Operations

- Boolean operations like AND, OR and XOR can be used to combine image:



# Point Operation: Logic Operations

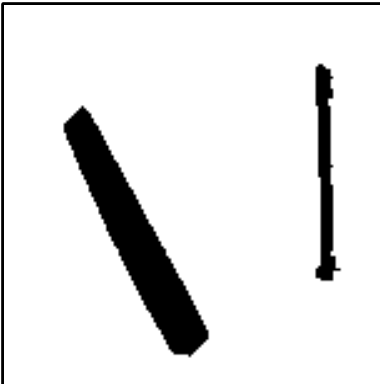
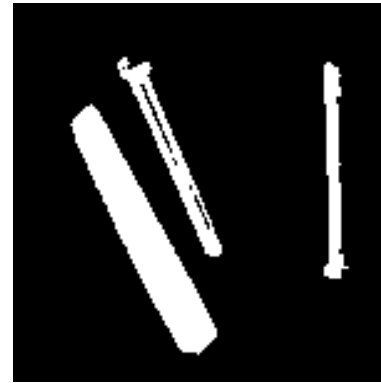
- Boolean operations like AND, OR and XOR can be used to combine image:



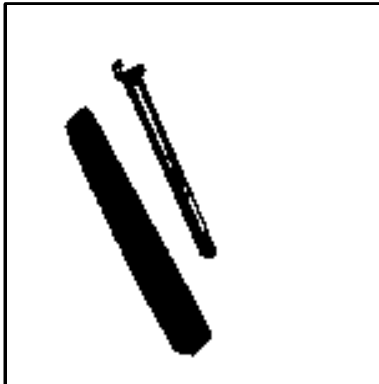
OR



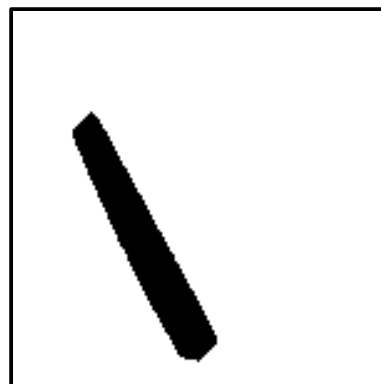
=



OR



=



# Point Operation: Logic Operations

- Boolean operations like AND, OR and XOR can be used to combine image:

