

Introduction to Computer Vision:

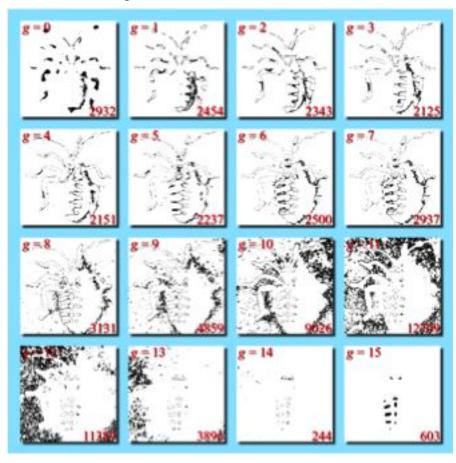
Image Statistics

Marcus Hudritsch (hsm4)

- Image Acquisition is a measuring process.
- It can be therefore **statistically analyzed**.
- ullet The most common statistic is the NO. of pixels (n_g) in each gray level:

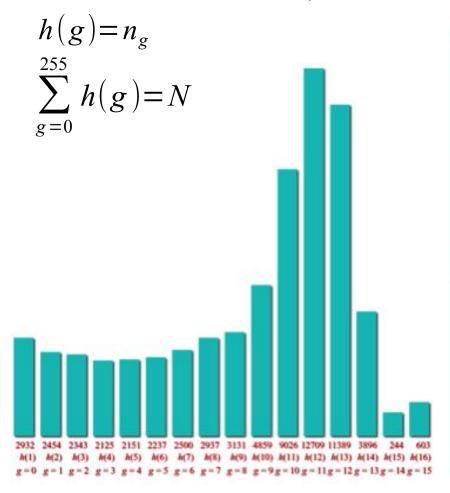
$$h(g)=n_g$$

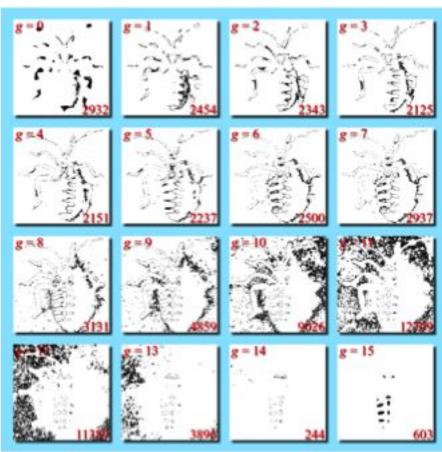




Images by R.A. Peters, Vanderbilt University

- The bar chart of 16 gray level count is called histogram.
- The sum of all levels is equal to the sum of all pixels:

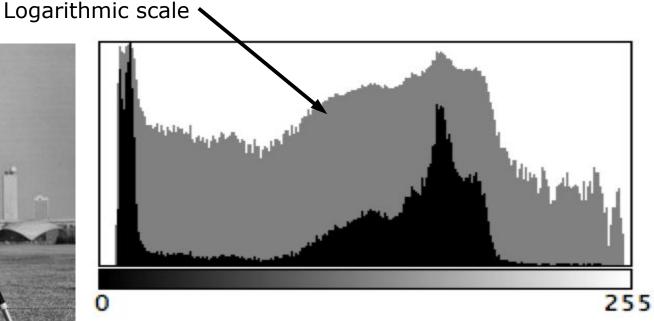




Images by R.A. Peters, Vanderbilt University

• The visualize small occurencies the histogram can be **lograrithmic scaled**:





Count: 65536 Min: 7

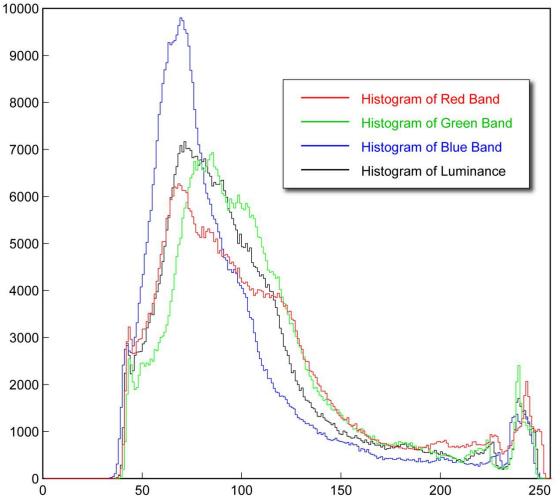
Mean: 118.724 Max: 253

StdDev: 62.342 Mode: 14 (1685)

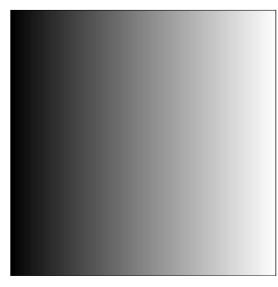
Image Statistics: Color Histogram

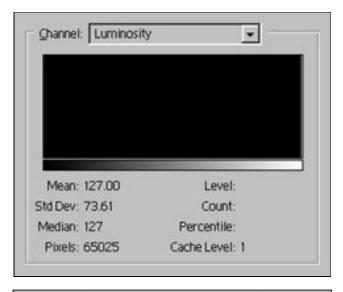


Images by R.A. Peters, Vanderbilt University



How does the histogram look like from the followin images:





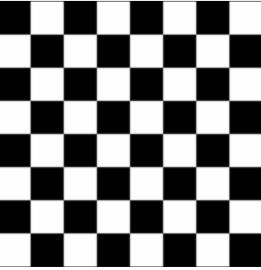




Image Statistics: Probability Density Function

- If the histogram is normalized we get the **Probability Density Function (PDF)**.
- To normalize it we divide all frequencies h(g) by the sum of all pixels.
- p(g) sais how probable a pixel has a gray value = g.
- The sum of all probabilities is 1 (100%).

$$p(g) = \frac{n_g}{N}$$

$$\sum_{g=0}^{255} p(g) = 1$$

Image Statistics: Cumulative Histogram

- The **cumulative histogram** sums up all level frequencies.
- It is used in algorithms like the histogram equalization.

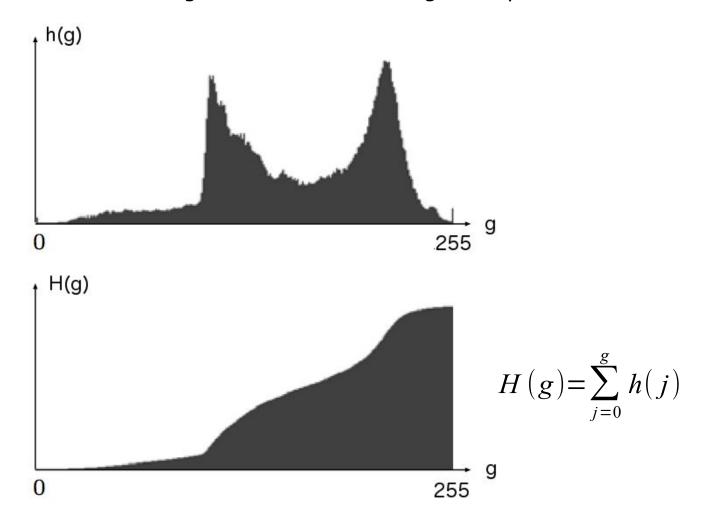
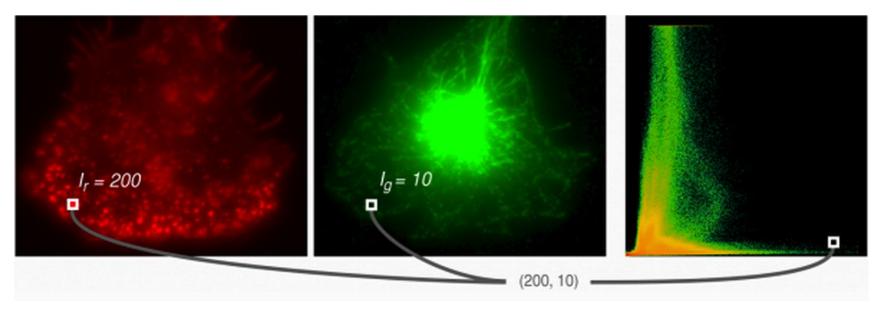


Image Statistics: Cumulative Density Function

- If the cumulative histogram is normalized we get the **Cumulative Probability Density Function (cdf)**.
- To normalize it we divide all cumulative sums H(G) by the sum of all pixels.
- P(g) sais how probable a pixel has a gray value <= g.

$$P(g) = \frac{H(g)}{N}$$

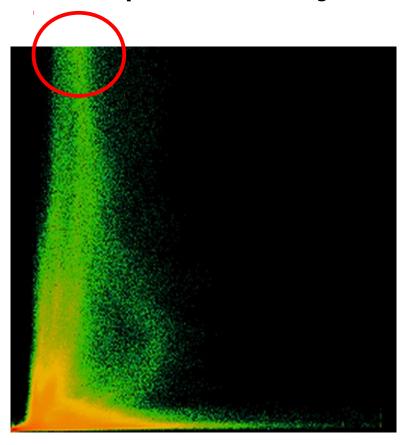
- A histogram can be built from multiple images.
- E.g. from 2 color channels of the same image:
- The gray value in each pixel is used as the coordiante of the counter in 256 x 256 histogram image:



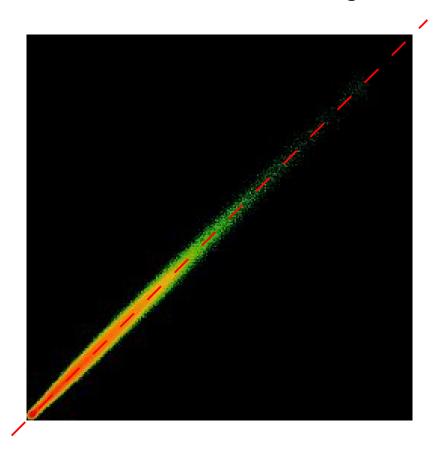
The frequencies of occurence are scaled and displayed with color palettes:

$$h(g_0, h_1, ...h_{N-1}) = \frac{a_{g_0g_1...g_{N-1}}}{N}$$
 $s(x, y) = s(g_0, g_1) = C \cdot h(g_0, h_1)$

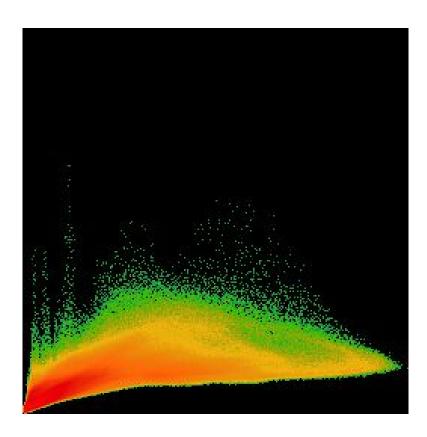
- A **2D-Histogram** can show:
 - Over-exposure of an image:



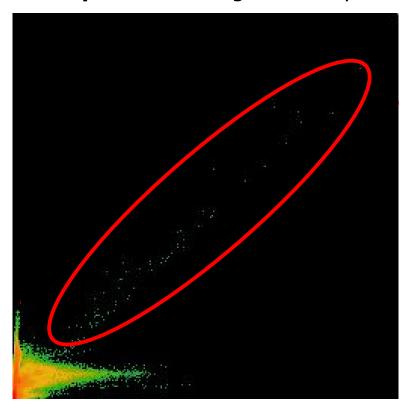
- A **2D-Histogram** can show:
 - Over-exposure of an image
 - Correlation between 2 images show in concentration along the diagonal:



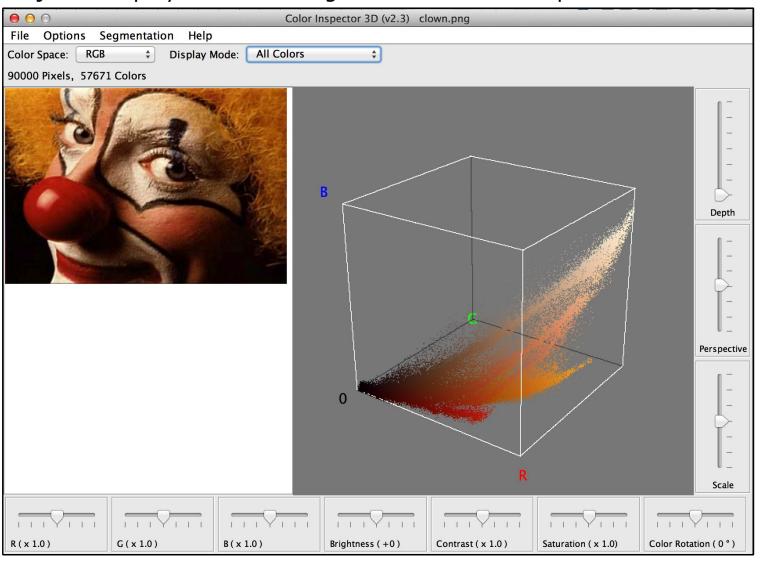
- A **2D-Histogram** can show:
 - Over-exposure of an image
 - Correlation between 2 images
 - Distribution of Dynamic in one color channel:



- A **2D-Histogram** can show:
 - Over-exposure of an image
 - Correlation between 2 images
 - Distribution of Dynamic
 - Hot pixels are single defect pixels that saturate without light:



• Fiji can display also 3D histograms in the color inspector:



Min. & max.:

$$D = g_{max} - g_{min}$$

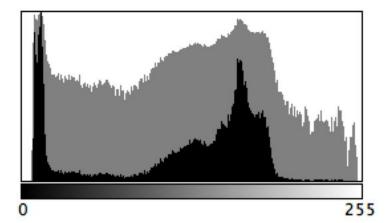
Contrast:

$$C = \frac{g_{max} - g_{min}}{g_{max} + g_{min}}$$

Mean (Mittelwert):

$$\bar{g} = \frac{1}{N} \sum_{x=0}^{m-1} \sum_{y=0}^{n-1} g(x, y)$$

• Mode (Modalwert): $\mathring{g} = max(h(g))$



Count: 65536 Mean: 118.724

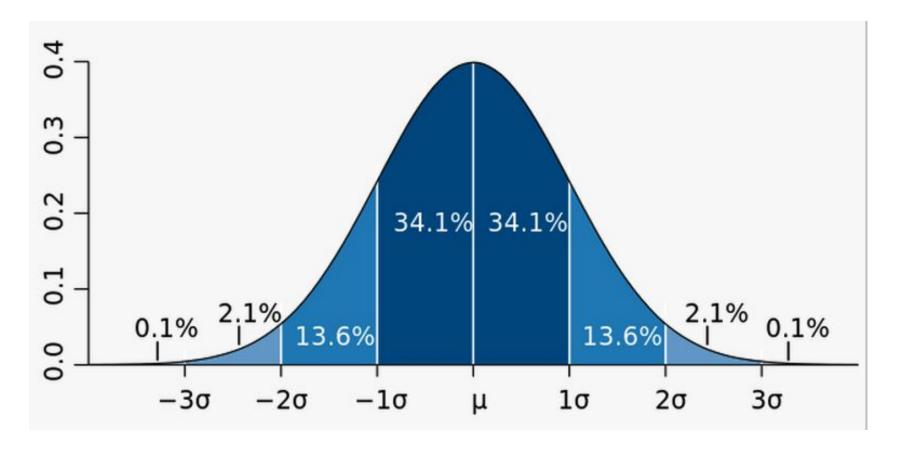
: 118.724 Max: 253

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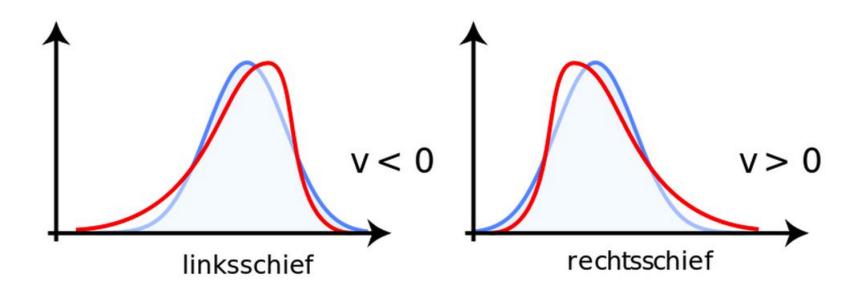
Min: 7

• Variance (Varianz):
$$var = \frac{1}{N} \sum_{x=0}^{m-1} \sum_{y=0}^{n-1} (g(x, y) - \overline{g})^2$$

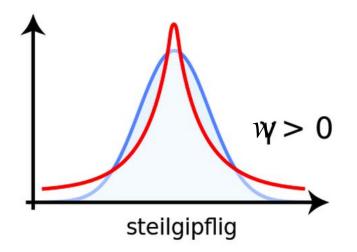
• Stadard Deviation: $s = \sigma = \sqrt{var}$

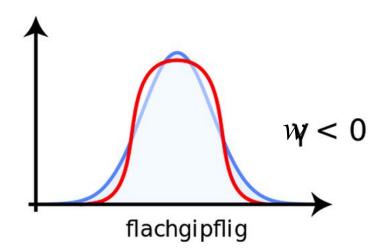


• Skewness (Schiefe):
$$v = \frac{1}{N} \sum_{x=0}^{m-1} \sum_{y=0}^{n-1} \left(\frac{g(x, y) - \overline{g}}{s} \right)^3$$



• Kurtosis (Wölbung):
$$w = \frac{1}{N} \sum_{x=0}^{m-1} \sum_{y=0}^{n-1} \left(\frac{g(x, y) - \overline{g}}{s} \right)^4$$





• Entropy (Entropie):
$$H = -\sum_{0}^{255} h(g) \log_2(h(g))$$

Informationsgehalt eines Zeichens mit Auftrittswahrscheinlichkeit p

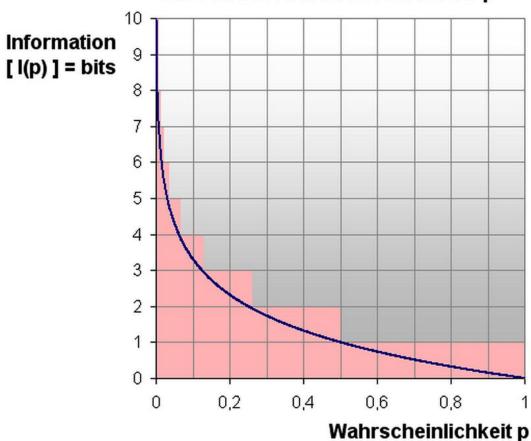


Image Statistics Examples:

