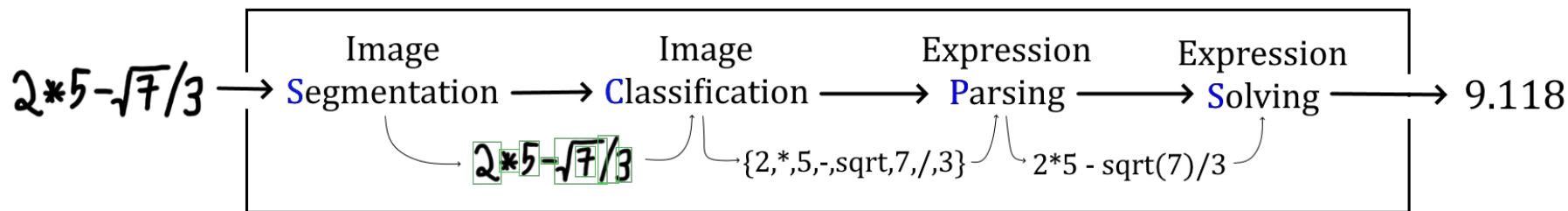


Automated Math Expression Solver



Relevant Topics:

- Image Processing
- Convolutional Neural Networks
- Data Augmentation

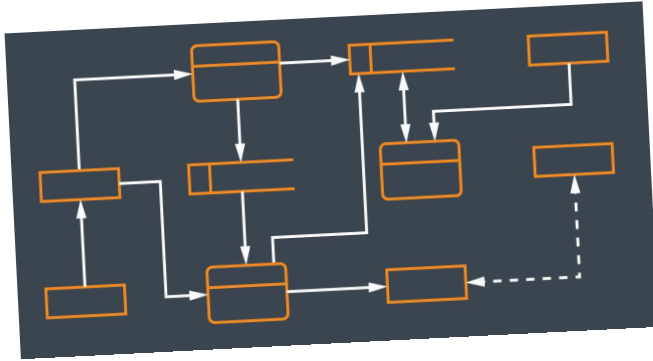
A (very) high-level overview



We built a **math expression solver**

$f(\text{handwritten expressions}) = ??? = \text{numerical output}$

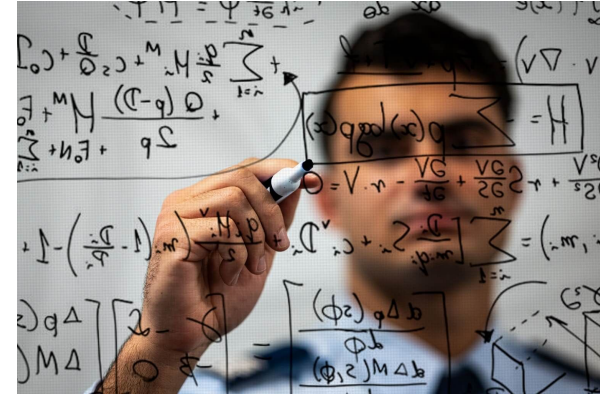
The Inspiration



We wanted an
end-to-end project,
a *full* product!



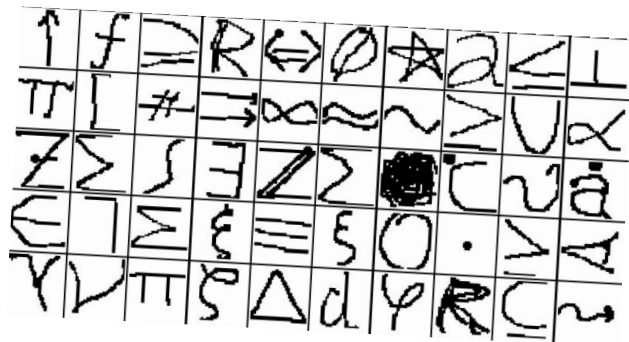
We thought images
were cool



Most of us are CS + **MATH** majors/minors!

The Dataset

32x32px image
369 symbols
150k samples



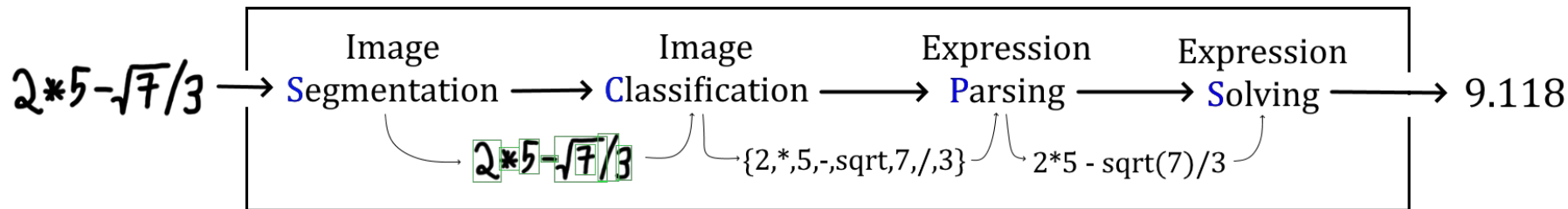
“[HASYv2](#)” → A Handwritten Symbol Database

- **Handwritten** Instances of symbols, numbers, letters.
- Labels = {"0", "A", "\sqrt", "\neq", "\inf", ...}

We want to use $\{0,1,2,3,4,5,6,7,8,9,*,/,+,-,(,),\sqrt\} \subset \text{HASYv2}$

- Goal: To simply perform arithmetic!

Ok, **how?**



1. Image Segmentation

- Perform image segmentation of input images into its individual components

2. Image Classification

- Classify the segments into what they actually are!

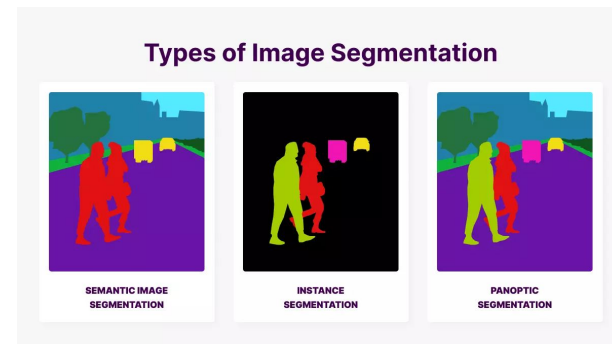
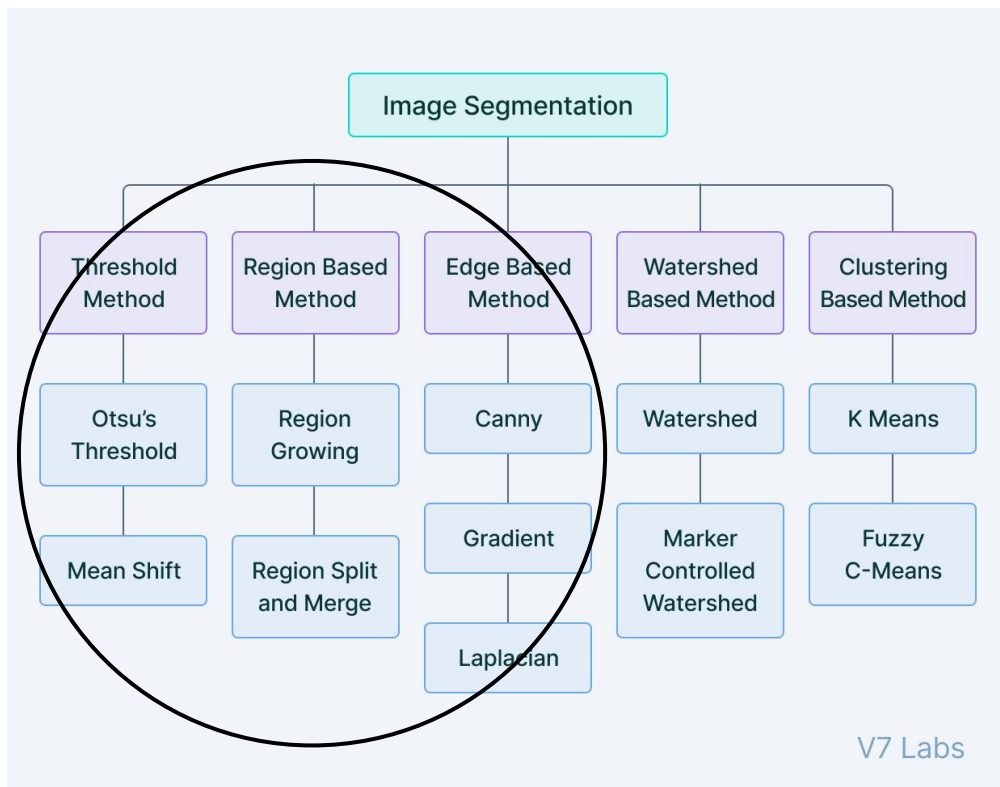
3. Expression Parsing

- Combine the segments, parse/handle them (dealing with roots, (), etc.)

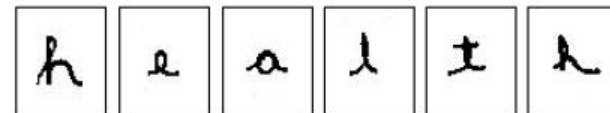
4. Expression Solving

- Solve it!

IMAGE SEGMENTATION



health health

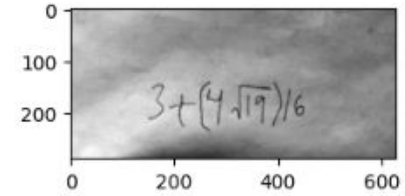


We use:

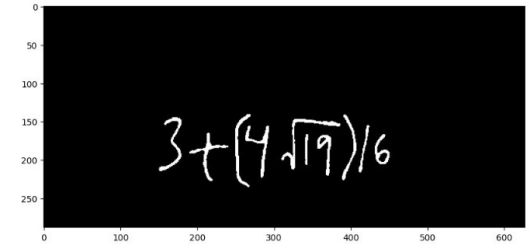
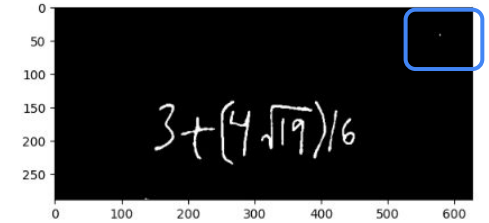
1. Basic image processing (blurring, B/W)
2. Thresholding (Otsu's Method)
3. Connected Components
4. **Contour** (borders) Detection



<matplotlib.image.AxesImage at 0x7f4ad1ea11b0>



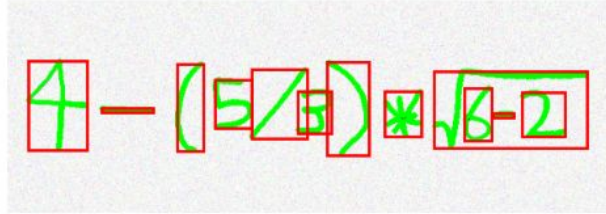
<matplotlib.image.AxesImage at 0x7f4ad1ad4d30>



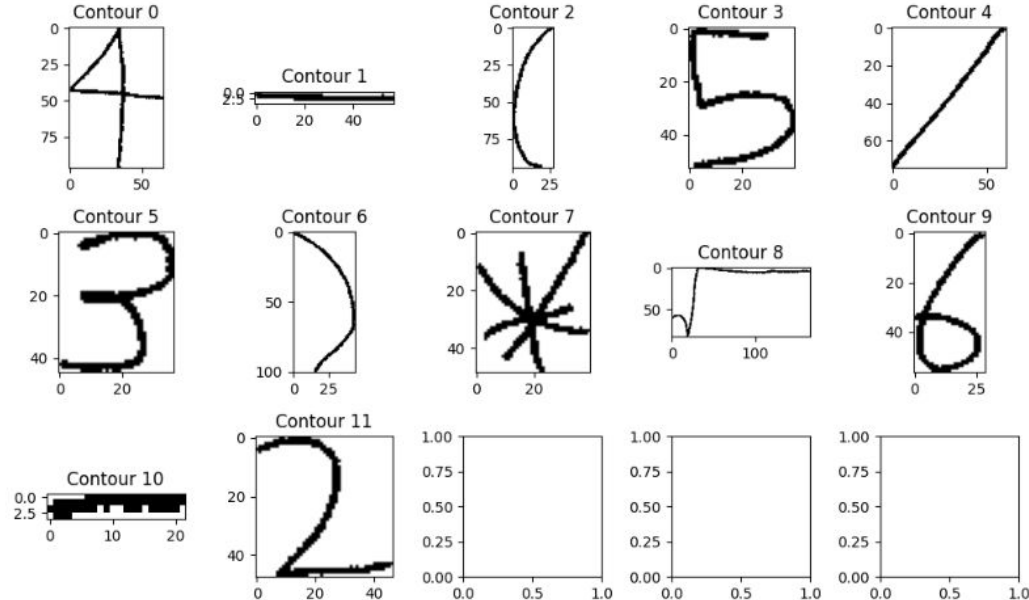
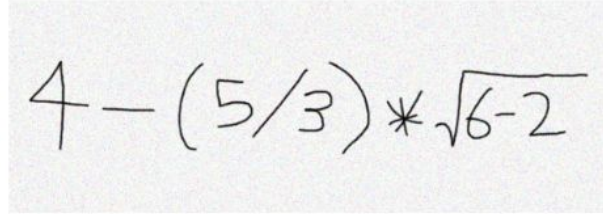
Contoured



Contoured



Old



Bounding boxes
Segment 1: (22, 66, 65, 97)

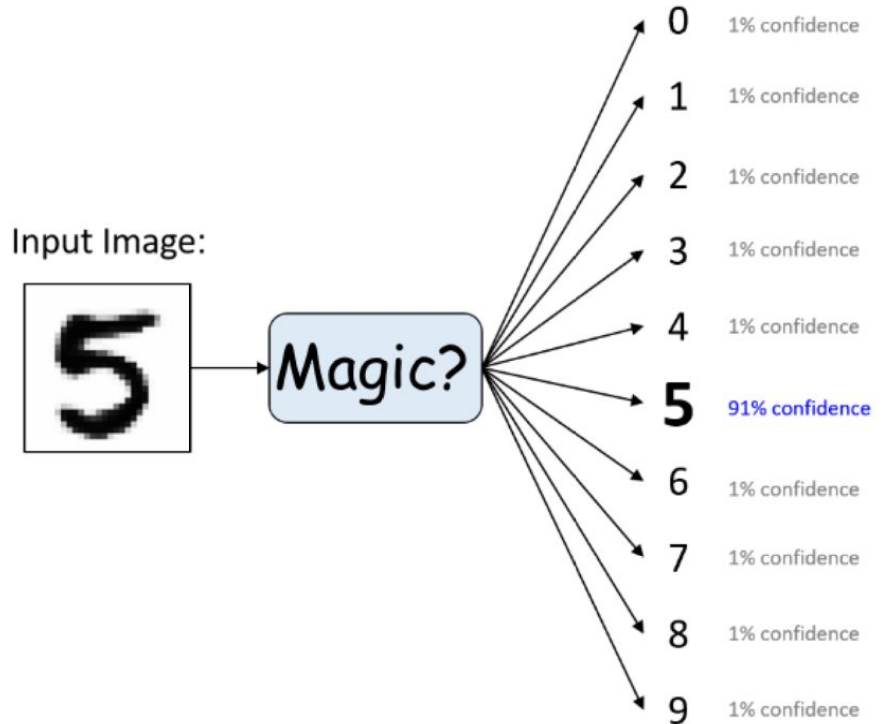
Thresholding is very important to get rid of noise!

IMAGE CLASSIFICATION

We now want to *classify* each segment of the expression

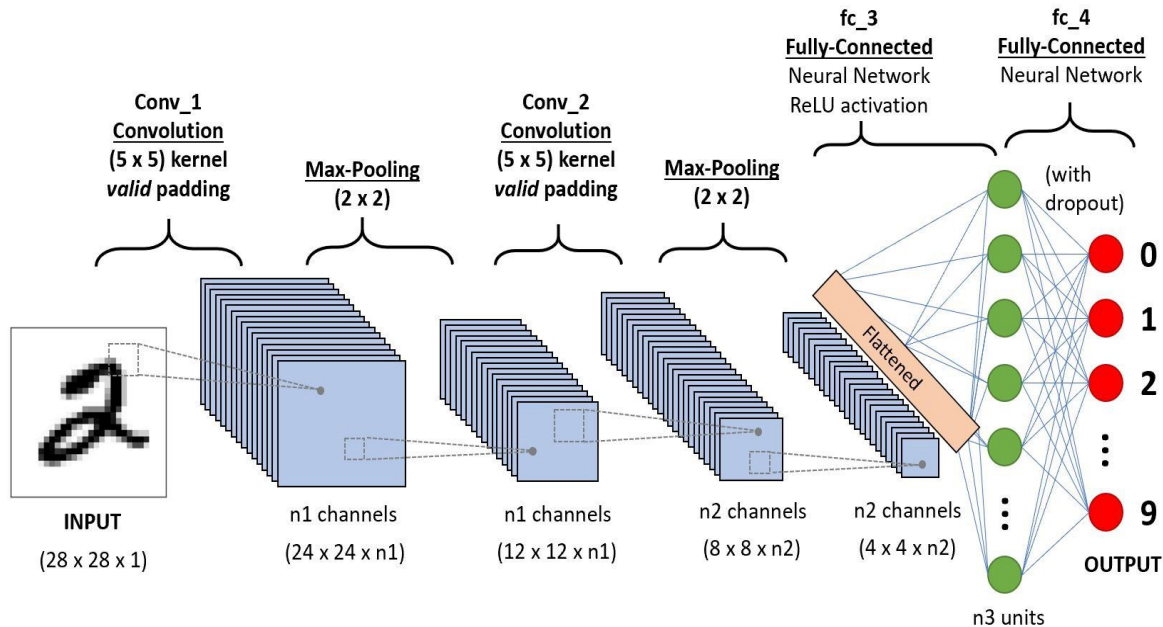
Numerous different methods. But most popular:

Convolutional Neural Networks
(Yann LeCun et al, 1998)



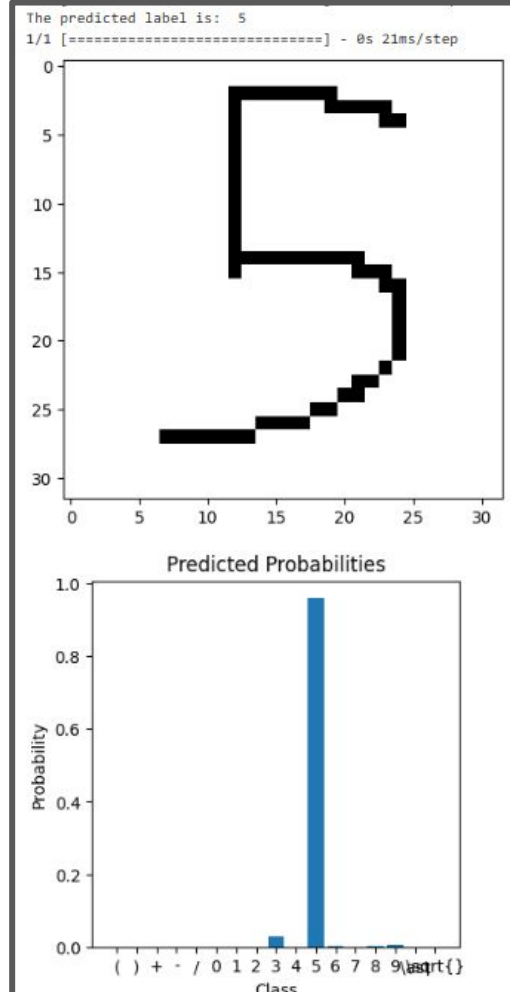
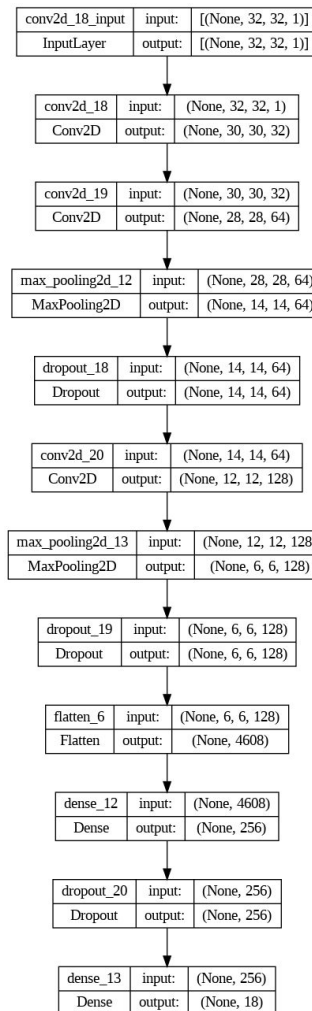
An overview of CNNs

- Input layer
- **Convolutional Layers**
 - Where the core learning happens. Key structures of the images are learned (edges, botches, eventually learning entire shapes)
- **Max Pooling**
 - Reduces dimensions but retains most important information
- **Fully connected layers**
 - Back to neural network, classification occurs



Layer (type)	Output Shape	Param #
=====		
conv2d_18 (Conv2D)	(None, 30, 30, 32)	320
conv2d_19 (Conv2D)	(None, 28, 28, 64)	18496
max_pooling2d_12 (MaxPooling2D)	(None, 14, 14, 64)	0
dropout_18 (Dropout)	(None, 14, 14, 64)	0
conv2d_20 (Conv2D)	(None, 12, 12, 128)	73856
max_pooling2d_13 (MaxPooling2D)	(None, 6, 6, 128)	0
dropout_19 (Dropout)	(None, 6, 6, 128)	0
flatten_6 (Flatten)	(None, 4608)	0
dense_12 (Dense)	(None, 256)	1179904
dropout_20 (Dropout)	(None, 256)	0
dense_13 (Dense)	(None, 18)	4626
=====		
Total params: 1,277,202		
Trainable params: 1,277,202		
Non-trainable params: 0		

Around 98% accuracy

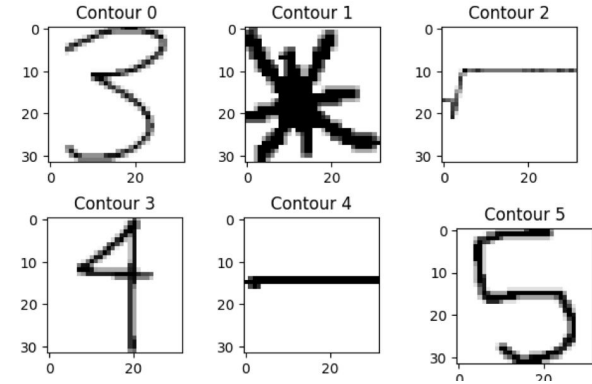


EXPRESSION PARSING AND SOLVING

$$3 * \sqrt{4-5}$$

After classifying: Parse it

- Finding square root with bounding boxes
- Handling parentheses
- Converting “\ast” into “*”



```
array(['3', '\\ast', '\\sqrt{', '1', '-', '5'], dtype='<U7')
```

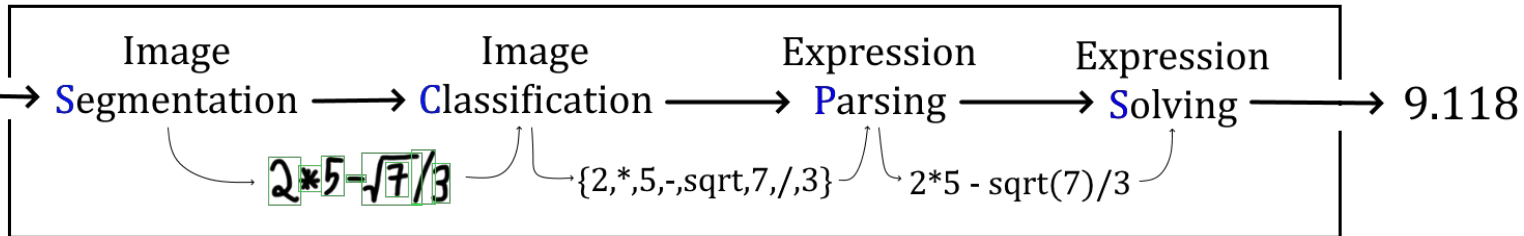
```
A square root found at index 2 has bounds: (151 331)
Added current bound of (192 223)
Added current bound of (234 259)
Added current bound of (271 304)
```

After parsing: **solve** it!

- SymPy
 - Symbolic computation library
- We use SymPy library to solve and evaluate the expression



$$2*5-\sqrt{7}/3$$



THE DEMO

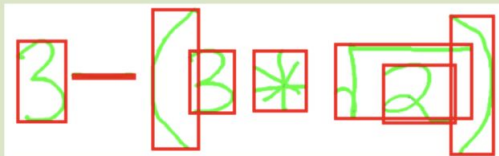
Please look at laptop #3

Group 18 - Expression Solver

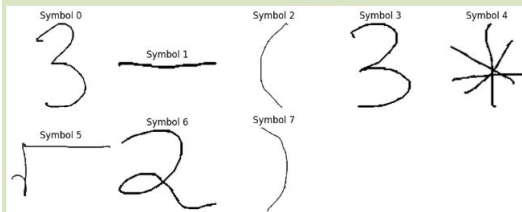
Original



Contours

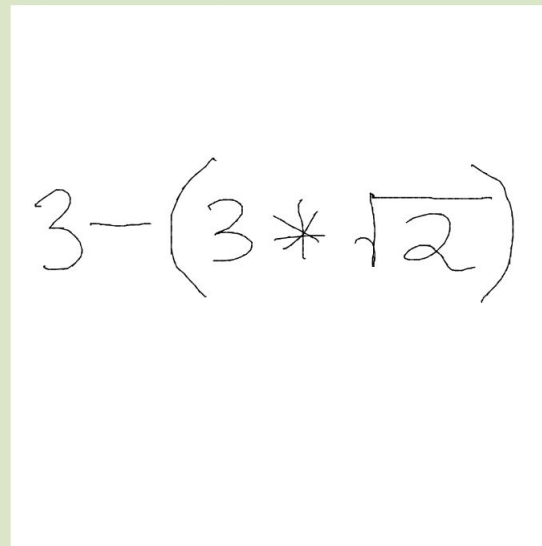


Terms



Expression

$$3 - (3 * \text{sqrt}(2))$$



Upload

Browse... equation3.jpg

Result

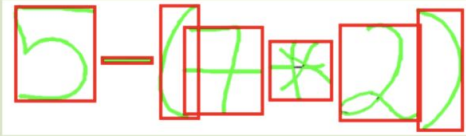
$$-1.243$$

Group 18 - Expression Solver

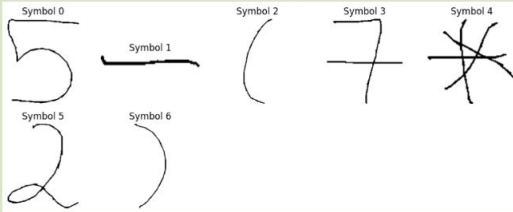
Original

A handwritten mathematical expression $5 - (7 * 2)$ in black ink on a white background.

Contours



Terms

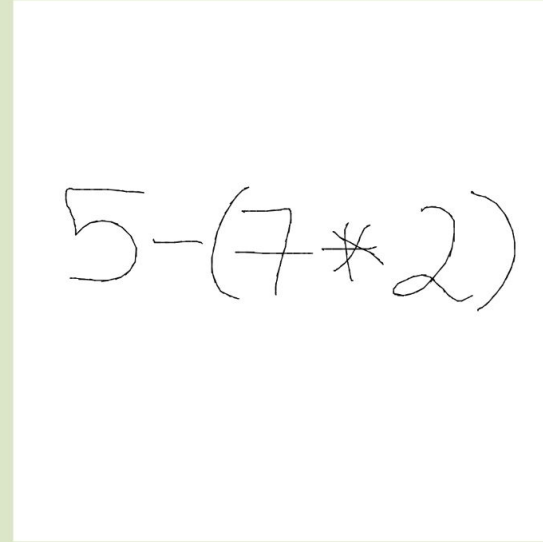


Expression

$$5 - (7 * 2)$$

Result

-9



Upload

Browse... equation2.jpg

Group 18 - Expression Solver

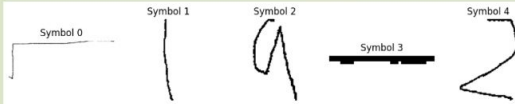
Original

A handwritten mathematical expression $\sqrt{19-2}$ on a white background.

Contours

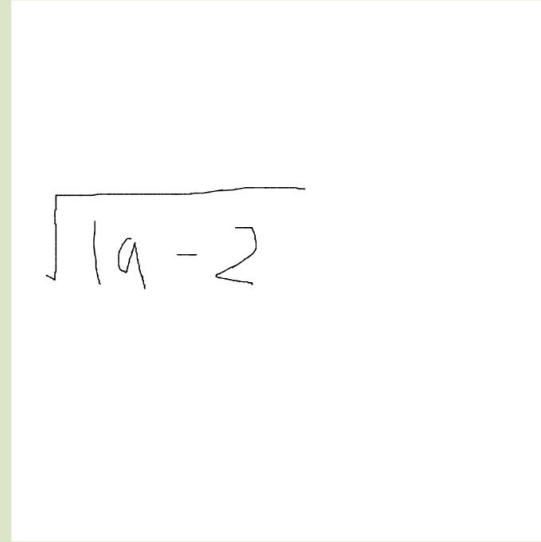


Terms



Expression

sqrt(1 9 - 2)



Upload

Browse... equation6.jpg

Result

4.123