# Modern Physics

A Collection of Notes and Problems

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## Chapter 1

## The Basics of Relativity

This chapter deals with unaccelerated motion, special relativity. General relativity will be revisited later.

## 1.1 Background

**Example 1.1.1.** Imagine a coordinate system S' fixed to a train moving with speed von a track while a second coordinate system S is fixed to the track. We assume that the track is at rest relative to the "ether". Suppose that at time t=0 lightning strikes at points x = -L and +L on the track. At this instant the train has its center, x' = 0, at the origin of the S-system, x=0. Then an observer on the ground at x = 0 will see the lightning flashes arrive from either side at a time t = L/c; that is they will arrive simultaneously. Will this be true for an observer stationed at the center of the train? If not, what is the time interval between the arrival of the flashes?

If the train was not moving, then, yes, the lightning would appear to have struck simultaneously. Since, the train is moving with speed v, lets say in the positive direction.

Then, the lightning at +L would have appeared to have happened before.

Going back to the question, the calculation for t = L/c comes from simply using velocity and distance. If we consider the lightning at -L the total distance it has to travel is L+vt. Where vt comes from the train moving away from -L. Since,  $\Delta x = \bar{v}t$ , we can express

$$L + vt = ct$$

solving for t

$$t = L/(c-v)$$

. We can similarly find the time for the right lightning. Since, the distance for the right one is L-vt

$$t=L/(c+v)$$

The time difference is then

$$\Delta t = L/(c-v) - L/(c+v)$$
$$= \frac{2L}{c(1-v^2/c^2)}$$

the assumption we made: and observer in a lation how far would they travel before they particular frame can measure the time that and event happens in his or her frame.

### 1.2 Einstein's Special Theory of Relativity

## Einstein's Postulates

- 1. The principal of relativity. The test of a physical law by any experiment carried out in a uniformly moving frame of reference does not depend of the speed of that frame relative to any other frame moving uniformly with respect to it.
- 2. The priciple of constancy. There exists a frame of reference S (call it the rest frame) with respect to which the speed of light is c. The speed is then also c in every other frame of reference moving uniformly with respect to S. The implies that the speed of light is independent of the motion of the source.

A length in its own rest frame is called the **proper length**. The period of a clock in frame in which it is resting is known as proper time.

Time Dilation

$$t = t' \frac{1}{\sqrt{1 - v^2/c^2}}$$

The purpose of this example is to consider with a speed of 0.99c. (a) Without time didecay? With time dilation?

1. 
$$x = vt = 0.99ct = 0.99 \times 3 \times 10^8 \times 2.2 \times 10^{-6} = 650m$$

2. using

$$t = t' \frac{1}{\sqrt{1 - v^2/c^2}}$$

we multiply  $650 \times 1/\sqrt{1 - .99^2} = 4620$ 

#### Transforma-Lorentz 1.3 tions

Lorentz transformations take the four coordinates (x, y, z, t) that describe an "event," something that occurs at a definite point in space and at a definite time.

The factor  $1/\sqrt{q-v^2/c^2}$  is used so often we will define

$$\gamma \equiv \frac{1}{\sqrt{1 - v^2/c^2}}$$

We can express the **spatial** Lorentz transformation as

$$x' = \gamma(x - vt)$$

The Lorentz transformation for **time** is

$$t' = \gamma \left[ t - \frac{v}{c^2} x \right]$$

Example 1.3.1. Consider a spaceship of proper length 100m that moves along the positive x-axis at 0.9c with respect to the **Example 1.2.1.** A beam of muons have a ground. If S is a coordinate frame fixed lifetime of  $2.2 \times 10^{-6}$ s are measured to move to the ground and S' is a coordinate frame

fixed to the ship, the origins are set so that at t = t' = 0 the front of the ship is at x = x' = 0. Where is the back of the ship at t = 0, according to an observer on the ground, and at t = 0 what time T' will a clock fixed to the back of the ship read, according to a ground-based observer? Do the problem (a) classically and (b) according to special relativity.

Classically, the answer is quite obvious. When the tip of the ship crosses x = 0 and time, t = 0 then the time at the back will also be T' = 0.

According to special relativity, these events do not happen at the same time. We can look at the distinct events that occur, and see we need to use both the time and spatial Lorentz transformation.

$$x' = \gamma(x - v(0)) = \gamma x$$
$$x = x'/\gamma$$

Now to use the time transformation

$$t' = \gamma \left[ 0 - \frac{v}{c^2} x \right] = \gamma \left[ 0 - \frac{v}{c^2} \frac{x'}{\gamma} \right]$$
$$t' = \frac{0.9}{c} x'$$
$$t' = \frac{0.9}{3 \times 10^8} 100$$
$$T' = 3 \times 10^{-7} s$$

# 1.4 Simultaneity and Relativity