

HIGHER-ORDER FUNCTIONS AND RECURSION

COMPUTER SCIENCE MENTORS CS 61A

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1 Higher-Order Functions

1. What is the difference between lambda functions and def statements? What is one of the purposes of higher order functions?

2. Draw the environment diagram that results from running the code.

```
x = 20
def foo(y):
    x = 5
    def bar():
        return lambda y: x - y
    return bar
```

```
y = foo(7)
z = y()
print(z(2))
```

3. Draw the environment diagram that results from running the code.

```
apple = 4
def orange(apple):
    apple = 5
    def plum(x):
        return lambda plum: plum * 2
    return plum

orange(apple) ("hiii") (4)
```

4. Write a higher-order function that passes the following doctests.

[Challenge: Write the function body in one line.] - if you finish try doing this

```
def mystery(f, x):
    """
```

```
>>> from operator import add, mul
```

```
>>> a = mystery(add, 3)
```

```
>>> a(4) # add(3, 4)
```

```
7
```

```
>>> a(12)
```

```
15
```

```
>>> b = mystery(mul, 5)
```

```
>>> b(7) # mul(5, 7)
```

```
35
```

```
>>> b(1)
```

```
5
```

```
>>> c = mystery(lambda x, y: x * x + y, 4)
```

```
>>> c(5)
```

```
21
```

```
>>> c(7)
```

```
23
```

```
"""
```

```
def helper(y):
```

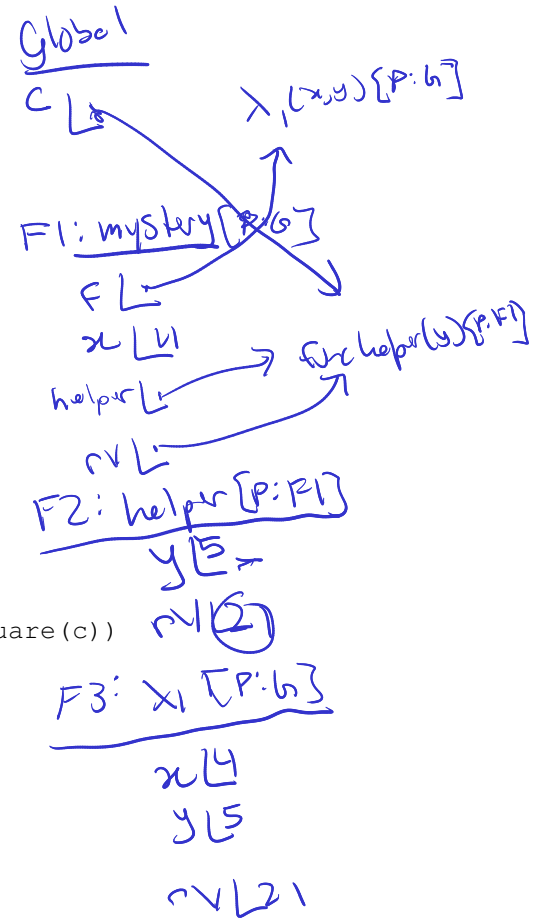
```
    return f(x, y)
```

```
    return helper
```

5. What would Python display?

```
>>> foo = mystery(lambda a, b: a(b), lambda c: 5 + square(c))
```

```
>>> foo(-2)
```



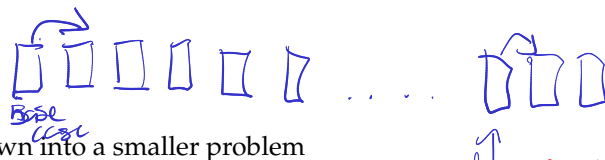
2 Recursion

Math 55/65/70

Introduction

Every Recursive function has three things.

1. One or more base cases
2. One or more ways to break the problem down into a smaller problem
 - E.g. Given a number as input, we need to break it down into a smaller number
3. Solve the smaller problem recursively; from that, form a solution to the original problem



$$\begin{cases} 0! = 1 \\ 1! = 1 \end{cases}$$

1. What is wrong with the following function? How can we fix it?

```
def factorial(n):
    return n * factorial(n)
    n-1
```

```
if n == 1:
    return n
else:
    return n * factorial(n-1)
```

2. Write a function `is_sorted` that takes in an integer `n` and returns true if the digits of that number are nondecreasing from right to left.

```
def is_sorted(n):
    """
    >>> is_sorted(2)
    True
    >>> is_sorted(2222)
    True
    >>> is_sorted(9876543210)
    True
    >>> is_sorted(9087654321)
    False
    """
```

Steps

↓ ask what the most trivial step is

What is the base case(s)?

What is my recursive call?

$$|n \% 10| \leftrightarrow |n // 10|$$

$$\uparrow \quad \uparrow$$

$$\text{len(str(n))} == 1 \checkmark$$

$$\begin{aligned} \text{right} &= n \% 10 \\ \text{rest} &= n // 10 \end{aligned}$$

$$\text{not}(\text{rest} \% 10 \geq \text{right})$$

```
if n < 10:
    return True
```

```
elif (rest \% 10) < right:
```

```
    return False
```

```
else:
```

```
    return is_sorted(rest)
```