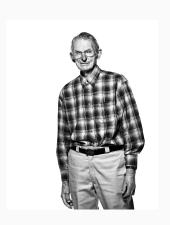
6 Algorithmic Journeys with Concepts

Taras Shevchenko

Rails Reactor / Giphy

The Software Industry is Not Industrialized

Software components (routines), to be widely applicable to different machines and users, should be available in families arranged according to precision, robustness, generality and time-space performance.



A Familiar Example. Douglas McIlroy about sin

Dimensions along which we wish to have variablity:

- 1. precision, for which perhaps ten different approximating functionsmight suffice
- 2. floating vs fixed computation
- 3. argument ranges $[0, \pi/2]$, [0, 2pi], also $[-\pi/2, pi/2]$, $[-\pi, \pi]$, [-big, +big]
- 4. robustness ranging from no argument validation through signaling of complete loss of significance, to signaling of specified range violations

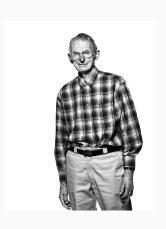
Douglas McIlroy

1. Choices

- 1.1 precision
- 1.2 robustness
- 1.3 generality
- 1.4 generality
- 1.5 algorithm
- 1.6 interfaces and error-handling

2. Application Areas

- 2.1 numerical approximation
- 2.2 1/0
- 2.3 2d and 3d geometry
- 2.4 text processing
- 2.5 storage management

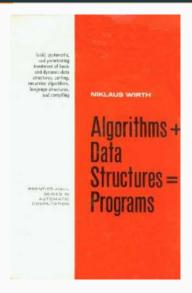


Donald Knuth

- 1. Fundamental Algorithms
- 2. Seminumerical Algorithms
- 3. Sorting and Searching
- 4. Combinatorial Algorithms
- 5. Syntactic Algorithms
- 6. The Theory of Context-free Languages
- 7. Compiler Techniques

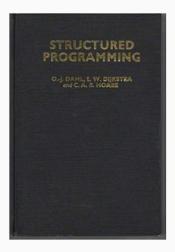


Niklaus Wirth





Edsger Wybe Dijkstra







John Backus

1977 ACM Turing Award Lecture

The 1977 ACM Turing Award was presented to John Backen at the ACM Annual Conference in Seatle, October 17. In intro-ducing the recipient, Jens E. Sammet, Chairman of the Awards petations cannot retrieval the same group congenio the first system to translate Fertines programs into machine diagongs. They employed novel optimizing techniques to generate fast machine-diagongs programs. Many other compilers for the lon-guage were developed, first on IBM machines, and later on vivu-Committee, made the fellowing comments and read a portion of the final citation. The full announcement is in the September 1977 issue of Communication, page 681. "Probably there is nother, page 681. gauge were cerestroped, from on 1850 macrones, and nater on versa-ally every make of computer. Fortran was adopted as a U.S. matiental standard in 1866. mational standard in 1966. During the Initer part of the 1990s, Bankus served on the international committees which developed Algail 38 and a latar version, Algail 60. The language Algail, and its derinative conglets, received broad acceptance in Europe as a mass for depicts, received broad acceptance on Europe as an assat for dealgorithms on which the programs are based agreement on which the programs are based. In 1999, Backes presented a paper at the UNESCO conference in Paris on the system and semantics of a proposed interceinion, are among the half dopen most important technical contributions to the computer field and both were made by John Backer (which in the Formus case also involved some culente in Faris on the systax and senantics of a proposed inter-national algorithmic language, In this poper, he was the first to employ a fermal suchaique for specifying the systax of popura-ning language. The formal notation became known in BNF— smading for "factus Normal Form," or "fluctus Nurs Form" in recomming the further contributions by Pour Nauer of Demmets. leagues). It is for these contributions that he is receiving this year's Turing award. The short form of his citation is for 'profound, influential, and lasting coercitations to the design of practical high-level programming systems, norably through his work on Fortrae, and for sentinal publication of formal procedures for the specifica-Thus, Ruckus has contributed strongly both to the pragmatic world of problem-solving on computers and to the theoretical tions of programming languages." The most significant part of the full citation is an follows: world existing at the interface between artificial languages and computational linguistics. Fortran remains one of the most ". . . Backes headed a small IBM group in New York City during the early 1950s. The earliest product of this group's widely used programming languages in the world. Almost all Can Programming Be Liberated from the von Neumann Style? A Functional Style and Its Algebra of Programs John Backus IBM Research Laboratory, San Jose Conventional programming languages are proving ever more enormous, but not stronger. Inherent defects at the most basic level cause them to be both fat and weak: their primitive word-at-a-time style of program ming inherited from their common ancestor—the von Neumann computer, their close coupling of semantics to state transitions, their division of programming into a world of expressions and a world of statements, their inability to effectively use powerful combining forms for building new programs from existing ones, and their lack of useful mathematical properties for reasoning about An alternative functional style of programming is Oriental permanion to make fair our in teaching or meants of all or part of this material is praised or individual reaches and to emprode handanic acting for the provided bar XVVV copyright nodes to give handanic acting for the provided bar XVVV copyright nodes to give handanic acting for the provided bar XVVV copyright nodes to large to the fact that representing previously not to the fact that the provided provided handanic fact that the provided provided provided bar and the fact that the Accession for Copyright Mechanics, it is netween regulate to gradies, table, other substantial account, or the earlier work requires specific provided in a fine expenditure of the provided or material proposition of the proposition of the provided or provided proposition of the provided or material account. founded on the use of combining forms for creating programs. Functional programs deal with structured data, are often nonrepetitive and nonrecursive, are hier archically constructed, do not name their arguments, and do not require the complex muchinery of procedure declarations to become generally applicable. Combining forms can use high level programs to build still higher level ones in a style not possible in conventional lan-Author's address: 91 Saint Germain Ave., San Francisco, CA D 1978 ACM 0001-0782/78/0800-0613 900 71 August 1978 Volume 21

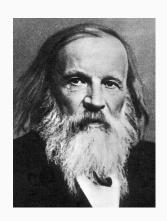
nutrations called Entres. This same group designed the first

Figure 2: We need a few functional forms

Dmitri Mendeleev



Figure 3: A Russian periodic table based on Dmitri Mendeleyev's original table of 1869.



Carl Linnaeus

Species Plantarum lists every species of plant known at the time, classified into genera. It is the first work to consistently apply binomial names and was the starting point for the naming of plants.



Euclid

- 1. Definitions
- 2. Postulates
- 3. Common notions



Common Notions

- 1. Things which are equal to the same thing are also equal to one other.
- 2. If equals be added to equals, the wholes are equal.
- 3. If equals be subructed from equals, the remainders are equal.
- 4. Things which coincide with one another are equal to one another.
- 5. The whole is greater than the part.

Basic idea

The essence of generic programming lies in the idea of concepts. A concept is a way of describing a family of related object types.

Natural	Mathematics	Programming	Programming
Science			Examples
genus	theory	concept	Integral, Character
species	model	type or class	uint8_t, char
individual	element	instance	01000001(65, 'A')

Definitions

- 1. Datum
- 2. Value
- 3. Value type
- 4. Object
- 5. Object type

Datum

Definition A datum is a sequence of bits.

Example 01000001 is an example of a datum.

Value

Definition

A value is a datum together with its interpretation.

Example

The datum 01000001 might have the interpretation of the integer 65, or the character "A".

Explanation

Every **value** must be associated with a **datum** in memory; there is no way to refer to disembodied **values** in modern programming languages.

Value type

Definition A **value type** is a set of values sharing a common interpretation.

Object

Definition

An **object** is a collection of bits in memory that contain a **value** of a given **value type**.

Explanation

An object is immutable if the value never changes, and mutable otherwise. An object is unrestricted if it can contain any value of its value type.

Object type

DefinitionAn **object type** is a uniform method of storing and retrieving **values** of a given **value type** from a particular **object** when given its address.

Journey

How algorithms were selected?

- 1. useful
- 2. generic
- 3. fits into 1 slide

Semiregular

Operation

- 1. Copy construction
- 2. Assignment
- 3. Destruction

Semantic

$$\forall a \ \forall b \ \forall c : T \ a(b) \implies (b = c \implies a = c)$$
 $\forall a \ \forall b \ \forall c : a \leftarrow b \implies (b = c \implies a = c)$
 $\forall f \in Regular Function : a = b \implies f(a) = f(b)$

Semiregular

Regular type

Operation

- 1. Copy construction
- 2. Assignment
- 3. Equality
- 4. Destruction

Semantic

$$\forall a \ \forall b \ \forall c : T \ a(b) \implies (b = c \implies a = c)$$
 $\forall a \ \forall b \ \forall c : a \leftarrow b \implies (b = c \implies a = c)$
 $\forall f \in Regular Function : a = b \implies f(a) = f(b)$

Regular

```
template < typename T >
concept semiregular = semiregular < T > && is_equality_comparable < T > :: value;
```

Relation

FunctionalProcedure(F) \triangleq F is a regular procedure defined on regular types: replacing its inputs with equal objects results in equal output objects.

 $UnaryFunction(F) \triangleq FunctionalProcedure(F) \land Arity(F) = 1$ $\land Domain : UnaryFunction \rightarrow Regular$ $F \mapsto InputType(F, 0)$

HomogeneousFunction(F) \triangleq FunctionalProcedure(F) \land Arity(F) > 0 $\land (\forall i, j \in \mathbb{N})(i, j < Arity(F)) \Longrightarrow (InputType(F, i) = InputType(F, j))$ \land Domain : HomogeneousFunction \rightarrow Regular $F \Longrightarrow InputType(F, 0)$

Regular

 $Predicate(P) \triangleq FunctionalProcedure(F) \land Codomain(P) = bool$

 $HomogeneousPredicate(P) \triangleq Predicate(P) \land HomogeneousFunction(P)$

 $Relation(R) \triangleq HomogeneousPredicate(R) \land Arity(R) = 2$

Relation

Totally Ordered

```
property(R:Relation) transitive:R r\mapsto (\forall a,b,c\in Domain(R))(r(a,b)\land r(b,c)\implies r(a,c))
```

property(R : Relation)

total_ordering : R

 $r \mapsto transitive(r) \land (\forall a, b \in Domain(R))$ exactly one of following holds :

r(a, b), r(b, a), or a = b

 $TotallyOrdered(T) \triangleq Regular(T) \land <: T \times T \rightarrow bool \land total_ordering(<)$

Totally Ordered

```
template < typename T >
concept totally_ordered = regular < T > && is_less_than_comprable < T > :: value;
```

Journey 1

- 1. min
- 2. max

Journey #1

```
int min(int x, int y) {
    if (y < x) {
        return y;
    }
    return x;
}</pre>
```

```
int min(int x, int y) {
    if (y < x) {
        return y;
    }
    return x;
}

double min(double x, double y) {
    if (y < x) {
        return y;
    }
    return x;
}</pre>
```

Journey #1

```
template < typename T>
T min(T x, T y) {
    if (y < x) {
        return y;
    }
    return x;
}</pre>
```

Dealing with large objects

```
template < typename T>
const T& min(const T& x, const T& y) {
    if (y < x) {
        return y;
    }
    return x;
}</pre>
```

```
template < typename T, typename P>
const T& min(const T& x, const T& y, P pred) {
   if (pred(y, x)) {
      return y;
   }
   return x;
}
```

```
struct employee {
    std::string full_name;
    int64_t salary;
};

void usage() {
    employee e0{"Bjarne Stroustrup", 99999999!l};
    employee e1{"Alex Stepanov", 9999999!l};
    min(e0, e1, [](const auto& x, const auto& y) {
        return x.salary < y.salary;
    }).salary += 10000ll;
}</pre>
```

```
template < typename T, typename P>
T& min(T& x, T& y, P pred) {
    if (pred(y, x)) {
        return y;
    }
    return x;
}
```

```
template < totally_ordered T>
const T& min(const T& x, const T& y) {
    if (y < x) {
        return y;
    return x;
template < totally_ordered T>
T& min(T& x, T& y) {
    if (y < x) {
        return y;
    return x;
```

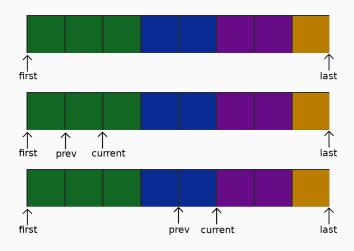
```
template < typename T, weak_strict_ordering < T > R >
const T& min(const T& x, const T& y, R r) {
    if (r(y, x)) {
        return y;
    return x;
template < typename T, weak_strict_ordering < T > R >
T\& min(T\& x, T\& y, R r) {
    if (r(y, x)) {
        return y;
    return x;
```

```
template < typename T, unary function < T > Projection >
requires totally_ordered < codomain_t < Projection , T >>
const T& min(const T& x, const T& y, Projection projection) {
    if (projection(v) < projection(x)) {</pre>
        return v:
    return x:
template < typename T, unary_function < T > Projection >
requires totally_ordered < codomain_t < Projection , T >>
T& min(T& x, T& y, Projection projection) {
    if (projection(y) < projection(x)) {</pre>
        return v:
    return x:
```

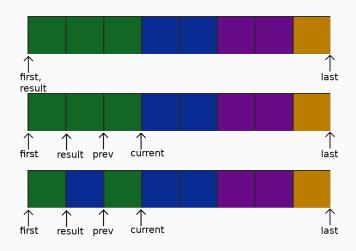
```
template < totally_ordered T>
const T& max(const T& x, const T& y) {
    if (y < x) {
        return x;
    return y;
template < totally_ordered T>
T\& max(T\& x, T\& y)  {
    if (y < x) {
        return x;
    return y;
```

- 1. unique_count
- 2. unique_copy
- 3. unique

Journey #2. Intuinition behind unique_count and unique_copy



Journey #2. Intuinition behind unique



Concepts

```
 \begin{split} \textit{Iterator}(\textit{T}) \; &\triangleq \; \textit{Regular}(\textit{T}) \; \land \\ & \quad \textit{DistanceType} : \textit{Iterator} \rightarrow \textit{Integer} \; \land \\ & \quad \textit{successor} : \textit{T} \rightarrow \textit{T} \; \land \\ & \quad \textit{successor} \; \textit{is not necessarily} - \textit{regular} \end{split}
```

 $ForwardIterator(T) \triangleq Iterator(T) \land regular_unary_function(successor)$

Concepts

```
template < typename | >
concept iterator = std::is same<std::forward iterator tag. typename std::
     iterator traits <1 >::iterator category >::value ||
                    std::is same<std::input iterator tag, typename std::
                         iterator traits < I > :: iterator category > :: value | |
                    std::is_same<std::output_iterator_tag, typename std::</pre>
                         iterator_traits <I >::iterator_category >::value ||
                    std::is same<std::bidirectional iterator tag. typename
                          std::iterator traits <1 >::iterator category >::
                         value II
                    std::is same<std::random access iterator tag. typename
                          std::iterator traits <1 >::iterator category >::
                         value:
template < typename | >
concept forward iterator = iterator <1 > && std::is base of <std::
     forward_iterator_tag, typename std::iterator_traits <I >::
     iterator category >:: value;
```

Concepts

```
BidirectionalIterator(T) \triangleq ForwardIterator(T) \land
                                 predecessor: T \rightarrow T \land
                                 predecessor takes constant type \wedge
                                 (\forall i \in T)successor(i)isdefined \Longrightarrow
                                     predecessor(successor(i)) is defined
                                     and equals to i \land
                                 (\forall i \in T) predecessor(i) is defined \implies
                                    successor(predecessor(i)) is defined
                                     and equals to i
```

Concepts. Bidirectioanal Iterator

```
template < typename | >
concept bidirectional_iterator = iterator < | > && std::is_base_of < std::
    bidirectional_iterator_tag , typename std::iterator_traits < | >::
    iterator_category >::value;
```

Concepts. Indexed Iterator.

Concepts. Random Access Iterator

```
IndexedIterator(T) \land
TotallyOrdered(T) \land
(\forall i, j \in T) \ i < j \iff i \prec j \land
DifferenceType:
   RandomAccessIterator \rightarrow Integer \land
+: T \times DifferenceType(T) \rightarrow T \wedge
-: T \times DifferenceType(T) \rightarrow T \wedge
-: T \times T \rightarrow DifferenceType(T) \wedge
< takes constant time \land

    between and iterator and an integer

   takes constant time
```

 $RandomAccessIterator(T) \triangleq BidirectionalIterator(T) \land$

Concepts. Random Access Iterator Iterator

```
template < typename | >
concept random_access_iterator = iterator < | > && std::is_base_of < std::
    random_access_iterator_tag, typename std::iterator_traits < | >::
    iterator_category >::value;
```

Concepts. Readable

```
\label{eq:Readable} \begin{aligned} \textit{Readable}(T) & \triangleq & \textit{Regular}(T) \land \\ & \textit{ValueType} : \textit{Readable} \rightarrow & \textit{Regular} \land \\ & \textit{source} : T \rightarrow \textit{ValueType}(T) \end{aligned}
```

Concepts. Readable

```
template < typename T > s
concept readable = std::is_same < decltype(*std::declval < T > ()),
      value_type_t < T > & >::value || std::is_same < decltype(*std::declval < T > ()
      ), const value_type_t < T > & >::value;
```

Concepts. Writable

```
\label{eq:writable} Writable(T) \triangleq ValueType : Writable \rightarrow Regular \land \\ (\forall x \in T)(\forall v \in ValueType(T)) \ sink(x) \leftarrow v \\ is \ a \ well - formed \ statement
```

Concept: writable

Concept: writable

```
N unique_count(It first, It last, N n, R r) {
   if (first == last) { return n; }
   // some algorithm
   return n;
}
```

```
N unique_count(It first, It last, N n, R r) {
   if (first == last) { return n; }
   It previous = first;
   ++first;
   // some algorithm
   return n;
}
```

```
template < forward_iterator It, additive_monoid N, relation < value_type_t < It
    >> R>
N unique_count(It first, It last, N n, R r) {
    if (first == last) { return n; }
    It previous = first;
    ++ first;
    while (first != last) {
        if (!r(*previous, *first)) {
            ++n:
       ++ previous:
       ++ first:
    ++n:
    return n:
```

unique_copy

```
template < forward_iterator It, output_iterator Out, relation < value_type_t <
     It >> R>
requires readable < It > && writable < Out, value_type_t < It >>
Out unique copy(It first, It last, Out out, R r) {
    if (first == last) { return out; }
    *out = *first:
    ++out:
    It previous = first; ++ first;
    while (first != last) {
        if (!r(*previous, *first)) {
          *out = *first;
          ++out:
        ++ first:
        ++ previous:
    return out:
```

unique_copy

unique

```
template < forward_iterator It , relation < value_type_t < It >> R>
requires readable < It > && writable < It >
It unique(It first, It last, R r) {
    if (first == last) { return last; }
    It result = first; ++ first;
    while (first != last) {
        if (r(*result, *first)) {
           ++ first;
        } else {
            ++result:
            *result = *first;
            ++first;
    ++result:
    return result;
```

Journey #2. unique

- 1. frequencies
- 2. transform_subgroups
- 3. squash_subgroups

Journey #3. frequencies

```
template < forward_iterator It, output_iterator Out>
requires readable < It > && writable < Out, std::pair < value_type_t < It >, size_t
     >>
Out frequencies(It f, It l, Out out) {
  typedef size_t N;
  while (f != l) {
   It it = f:
   N n = 1;
   ++f:
    auto r = find_not(f, l, *it, n);
    f = r.first;
    *out = { *it, r.second };
   ++out:
  return out;
```

Journey #3. frequencies

```
template < forward_iterator It, output_iterator Out, relation < value_type_t <
     It >> R>
requires readable < It > && writable < Out, std::pair < value_type_t < It >, size_t
     >>
Out frequencies(It f, It l, Out out, R r) {
  tvpedef size t N:
  while (f != l) {
    It start = f;
    N n = 1;
    ++f:
    auto r = find_if_not(f, l, *start, r, n);
    f = r.first;
    *out = { *start, r.second };
    ++out:
  return out:
```

Journey #3. Frequencies

```
template < forward_iterator It, output_iterator Out0, output_iterator Out1>
requires readable < It > && writable < Out0, value_type_t < It >> && writable <
    Out1, size t>
std::pair<Out0, Out1> frequencies(It f, It l, Out0 out0, Out1 out1) {
  typedef size_t N;
  while (f != |) {
   It start = f;
   N n = 1;
    ++f:
    auto r = find not(f, l, *start, n):
    *out0 = *start;
    ++out0:
    *out1 = r.second;
    ++out1;
    f = r.first;
  return {out0, out1};
```

Journey # 3. Frequencies

```
template < forward_iterator It, output_iterator Out0, forward_iterator Out1
requires readable < It > && writable < Out0 > && writable < Out1 >
std::pair<Out0, Out1> frequencies(It f, It l, Out0 out0, Out1 out1) {
  typedef value_type_t < Out1 > N;
  while (f != |) {
   It it = f:
   N n = 1;
    ++f:
    It r = find_not(f, l, *it, n);
    *out0 = *it:
    ++out0:
    *out1 = r.second;
    ++out1;
    f = r.first;
  return {out0, out1};
```

Journey # 3. Transform subgroups

```
template < forward iterator It.
         output iterator Out,
         relation < value type t < It >> P.
         functional_procedure < It , It > F >
requires readable < It > && writable < Out, codomain_t < F, It, It >>
Out transform subgroups(It first, It last, Out out, P pred, F function) {
    if (first == last) { return out; }
    It previous = first:
    It fast = previous:
    ++fast:
    while (fast != last) {
        if (!pred(*previous, *fast)) {
            *out = function(first, fast);
            ++ out :
             first = fast;
        ++previous: ++fast:
    *out = function(first, fast);
    return ++ out;
```

Journey #3. Transform subgroups

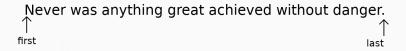
```
template < forward_iterator It,
         output_iterator Out,
          relation < value type t < It >> P.
         functional_procedure < It , distance_type_t < It >> F>
requires readable < It > && writable < Out, codomain_t < F, It, distance_type_t <
     It >> >
Out transform_subgroups(It first, It last, Out out, P pred, F function) {
    if (first == last) { return out; }
    It previous = first;
    It fast = previous:
    ++fast:
    distance type t < It > n = 0;
    while (fast != last) {
        if (!pred(*previous, *fast)) {
            *out = function(first, n);
            n = 0:
            ++out:
            first = fast;
        ++n:
        ++previous: ++fast:
    *out = function(first . n):
    return ++ out:
```

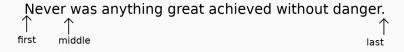
Journey # 3. Squash subgroups

Journey #4. split

- 1. split
- 2. transform_splits

Journey #4. Intuinition behind efficient split





Journey # 4. Split

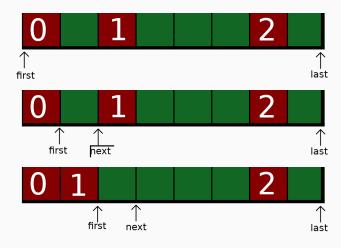
Journey # 4. Transform split

```
template < forward iterator ItO, output iterator Out, forward iterator It1,
      functional procedure < ItO . ItO > F>
requires readable < ItO > && readable < It1 > && writable < Out, codomain_t < F,
     ItO , ItO >>
Out transform split(ItO firstO, ItO lastO, Out out, It1 first1, It1 last1
    , F f) {
    auto step size = std::distance(first1. last1):
    while (first0 != last0) {
        ItO middle = std::search(first0, last0, first1, last1);
        *out = f(first0, middle);
        ++out:
        first0 = middle:
        if (first0 != last0) {
            std::advance(first0, step size);
    return out:
```

Journey #5

- 1. remove
- 2. remove_if
- 3. partition_semistable

Journey #5. Intuinition behind the scene



Journey # 5. Remove

```
template < forward_iterator It >
requires readable < It > && writable < It >
It remove(It first, It last, const value_type_t<It>& value) {
    first = std::find(first, last, value);
    if (first == last) { return last; }
    It fast = first; ++fast;
    while (fast != last) {
        if (*fast == value) {
            ++fast:
        } else {
            *first = std::move(*fast):
            ++ first: ++ fast:
    return first:
```

Journey # 5. Remove if

```
template < forward_iterator It , unary_predicate < value_type_t < It >> P>
requires readable < It > && writable < It >
It remove_if(It first, It last, P pred) {
    first = std::find if(first, last, pred);
    if (first == last) { return last; }
    It fast = first; ++fast;
    while (fast != last) {
        if (pred(*fast)) {
            ++fast:
        } else {
            *first = std::move(*fast):
            ++ first: ++ fast:
    return first:
```

Journey # 5. Semistable Partition

```
template < forward_iterator It , unary_predicate < value_type_t < It >> P>
requires readable < It > && writable < It >
It semistable_partition(It first, It last, P pred) {
    first = std::find_if(first, last, pred);
    if (first == last) { return last; }
    It fast = first; ++fast;
    while (fast != last) {
        if (pred(*fast)) {
            ++fast:
        } else {
             std::swap(*first, *fast);
            ++ first: ++ fast:
    return first:
```

Journey # 5. Semistable Partition

```
template < forward_iterator ItO, forward_iterator It1, binary_predicate <
    value type t<It0 >. value type t<It1 >> P>
requires (readable < ItO > && writable < ItO >) && (readable < It1 > && writable <
    |t1>
std::pair<It0, It1 > semistable partition(It0 first0, It0 last0, It1
    first1, P pred) {
    std::pair<It0, It1> r = find_if(first0, last0, first1, pred);
    first0 = r.first; first1 = r.second;
    if (first0 == last0) { return {first0, first1}; }
    ItO fast0 = first0; ++fast0;
    It1 fast1 = first1: ++fast1:
    while (fast0 != last0) {
        if (pred(*fast0, *fast1)) {
            ++fast0: ++fast1:
        } else {
            std::swap(*first0. *fast0):
            ++first0: ++fast0:
            std::swap(*first1, *fast1);
            ++ first1: ++ fast1:
    return {first0 , first1 };
```

Demo

Conclusion

Conclusion

- 1. Concepts are mathematical. They are not specific to C++.
- 2. Know as many algorithms as you can.
- 3. Algorithms come in groups.
- 4. Transform complicated loops into well-defined algorithms.
- 5. Use mathematics for everything you do.
- 6. Don't obey mathematical conventions in programming.
- 7. Prefer fast concrete algorithms to more general where concreteness gives you better performance.
- 8. Have a little Euclid, Knuth, Dijkstra in your mind and let them argue.
- 9. It is good to organise your code.

Questions?

```
while (first != last) {
   // write good code
}
```

Sources and Related Materials

- 1. The Thirteen Books of the Elements, Vol. 1: Books 1-2 2nd ed. Edition by Thomas L. Heath (Author), Euclid (Author).
- 2. From Mathematics to Generic Programming 1st Edition by Alexander A. Stepanov (Author), Daniel E. Rose (Author).
- 3. Elements of Programming 1st Edition by Alexander A. Stepanov (Author), Paul McJones (Author).
- 4. Species Plantarum by Carolus Linnaeus.
- 5. EOP concepts.
- 6. Source code for the lecture.
- 7. The latest version of this presentation.