

Homework for Week 3  
(Due Date: Check eCampus)

1. A computer system has a 36-bit virtual address space with a page size of 8K, and 4 bytes per page table entry.
  - (a) How many pages are in the virtual address space?
  - (b) What is the maximum size of addressable physical memory in this system?
  - (c) If the average process size is 8GB, would you use a one-level, two-level, or three-level page table? Why?
  - (d) Compute the average size of a page table in question 3 above.
2. In a 32-bit machine we subdivide the virtual address into 4 segments as follows:

10-bit	8-bit	6-bit	8-bit
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We use a 3-level page table, such that the first 10-bit are for the first level and so on.

- (a) What is the page size in such a system?
  - (b) What is the size of a page table for a process that has 256K of memory starting at address 0?
  - (c) What is the size of a page table for a process that has a code segment of 48K starting at address 0x1000000, a data segment of 600K starting at address 0x80000000 and a stack segment of 64K starting at address 0xf0000000 and growing upward (like in the PA-RISC of HP)?
3. In a 32-bit machine we subdivide the virtual address into 4 pieces as follows:

8-bit	4-bit	8-bit	12-bit
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We use a 3-level page table, such that the first 8 bits are for the first level and so on. Physical addresses are 44 bits and there are 4 protection bits per page. Answer the following questions, showing all the steps you take to reach the answer. A simple number will not receive any credit.

- (a) What is the page size in such a system? Explain your answer (a number without justification will not get any credit).
  - (b) How much memory is consumed by the page table and wasted by internal fragmentation for a process that has 64K of memory starting at address 0?
  - (c) How much memory is consumed by the page table and wasted by internal fragmentation for a process that has a code segment of 48K starting at address 0x1000000, a data segment of 600K starting at address 0x80000000 and a stack segment of 64K starting at address 0xf0000000 and growing upward (towards higher addresses)?

4. A computer system has a page size of 1,024 bytes and maintains the page table for each process in main memory. The overhead required for doing a lookup in the page table is 500 ns. To reduce this overhead, the computer has a TLB that caches 32 virtual pages to physical frame mappings. A TLB lookup requires 100ns. What TLB hit-rate is required to ensure an average virtual address translation time of 200ns?

## References

- [1] A. Silberschatz, P. Galvin, and G. Gagne, *Applied Operating Systems Concepts*, John Wiley & Sons, Inc., New York, NY, 2000.
- [2] Deitel, Deitel, and Choffnes, *Operating Systems*, Pearson / Prentice Hall, 2004.
- [3] A. S. Tanenbaum, *Modern Operating Systems*, Pearson / Prentice Hall, 2008.
- [4] L. F. Bic, A. C. Shaw, *Operating Systems Principles*, Prentice Hall 2003.
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- [6] M. Herlihy, N. Shavit, *The Art of Multiprocessor Programming*, Elsevier, 2008