# Abstract Syntax Trees & Top-Down Parsing

### Review of Parsing

• Given a language L(G), a parser consumes a sequence of tokens s and produces a parse tree

### · Issues:

- How do we recognize that  $s \in L(G)$ ?
- A parse tree of s describes  $how s \in L(G)$
- Ambiguity: more than one parse tree (possible interpretation) for some string s
- Error: no parse tree for some string s
- How do we construct the parse tree?

### Abstract Syntax Trees

- So far, a parser traces the derivation of a sequence of tokens
- The rest of the compiler needs a structural representation of the program
- Abstract syntax trees
  - Like parse trees but ignore some details
  - Abbreviated as AST

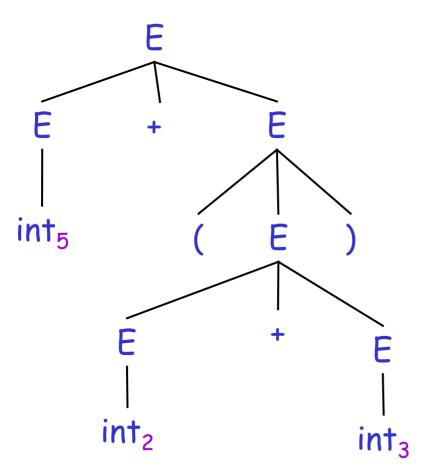
### Abstract Syntax Trees (Cont.)

Consider the grammar

$$E \rightarrow int | (E) | E + E$$

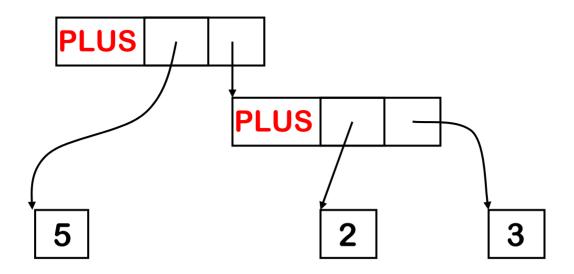
- And the string 5 + (2 + 3)
- After lexical analysis (a list of tokens)
   int<sub>5</sub> '+' '(' int<sub>2</sub> '+' int<sub>3</sub> ')'
- During parsing we build a parse tree ...

# Example of Parse Tree



- Traces the operation of the parser
- Captures the nesting structure
- But too much information
  - Parentheses
  - Single-successor nodes

### Example of Abstract Syntax Tree



- Also captures the nesting structure
- But <u>abstracts</u> from the concrete syntax  $\mapsto$  more compact and easier to use
- An important data structure in a compiler

### Semantic Actions

- This is what we will use to construct ASTs
- Each grammar symbol may have <u>attributes</u>
  - An attribute is a property of a programming language construct
  - For terminal symbols (lexical tokens) attributes can be calculated by the lexer
- Each production may have an <u>action</u>
  - Written as:  $X \rightarrow Y_1 \dots Y_n$  { action }
  - That can refer to or compute symbol attributes

### Semantic Actions: An Example

Consider the grammar

$$E \rightarrow int \mid E + E \mid (E)$$

- For each symbol X define an attribute X.val
  - For terminals, val is the associated lexeme
  - For non-terminals, val is the expression's value (which is computed from values of subexpressions)
- We annotate the grammar with actions:

```
E \rightarrow int { E.val = int.val }

\mid E_1 + E_2  { E.val = E_1.val + E_2.val }

\mid (E_1) { E.val = E_1.val }
```

### Semantic Actions: An Example (Cont.)

- String: 5 + (2 + 3)
- Tokens: int<sub>5</sub> '+' '(' int<sub>2</sub> '+' int<sub>3</sub> ')'

### Productions

$$E \rightarrow E_1 + E_2$$

$$E_1 \rightarrow int_5$$

$$E_2 \rightarrow (E_3)$$

$$E_3 \rightarrow E_4 + E_5$$

$$E_4 \rightarrow int_2$$

$$E_5 \rightarrow int_3$$

# Equations

E.val = 
$$E_1$$
.val +  $E_2$ .val  
 $E_1$ .val =  $int_5$ .val = 5  
 $E_2$ .val =  $E_3$ .val  
 $E_3$ .val =  $E_4$ .val +  $E_5$ .val  
 $E_4$ .val =  $int_2$ .val = 2  
 $E_5$ .val =  $int_3$ .val = 3

### Semantic Actions: Dependencies

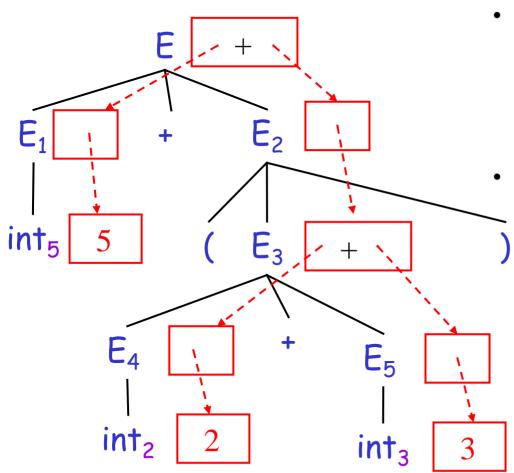
# Semantic actions specify a system of equations

- Order of executing the actions is not specified
- · Example:

```
E_3.val = E_4.val + E_5.val
```

- Must compute  $E_4$ .val and  $E_5$ .val before  $E_3$ .val
- We say that  $E_3$ .val depends on  $E_4$ .val and  $E_5$ .val
- The parser must find the order of evaluation

# Dependency Graph



- Each node labeled with a non-terminal E has one slot for its val attribute
  - Note the dependencies

# Evaluating Attributes

- An attribute must be computed after all its successors in the dependency graph have been computed
  - In the previous example attributes can be computed bottom-up
- · Such an order exists when there are no cycles
  - Cyclically defined attributes are not legal

### Semantic Actions: Notes (Cont.)

- Synthesized attributes
  - Calculated from attributes of descendents in the parse tree
  - E.val is a synthesized attribute
  - Can always be calculated in a bottom-up order
- Grammars with only synthesized attributes are called <u>S-attributed</u> grammars
  - Most frequent kinds of grammars

### Inherited Attributes

- Another kind of attributes
- Calculated from attributes of the parent node(s) and/or siblings in the parse tree
- · Example: a line calculator

### A Line Calculator

Each line contains an expression

$$E \rightarrow int \mid E + E$$

Each line is terminated with the = sign

$$L \rightarrow E = | + E =$$

- In the second form, the value of evaluation of the previous line is used as starting value
- A program is a sequence of lines

$$P \rightarrow \epsilon \mid P \perp$$

### Attributes for the Line Calculator

- Each E has a synthesized attribute val
  - Calculated as before
- Each L has a synthesized attribute val

```
L \rightarrow E = \{ L.val = E.val \}
 | + E = \{ L.val = E.val + L.prev \}
```

- We need the value of the previous line
- We use an inherited attribute L.prev

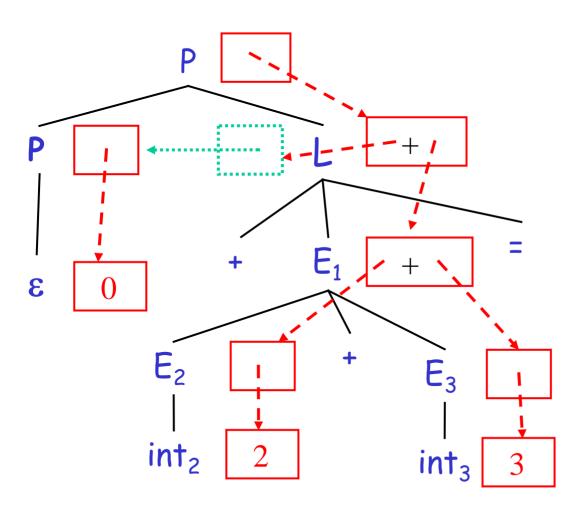
### Attributes for the Line Calculator (Cont.)

- Each P has a synthesized attribute val
  - The value of its last line

```
P \rightarrow \epsilon { P.val = 0 }
| P<sub>1</sub> L { P.val = L.val;
| L.prev = P<sub>1</sub>.val }
```

- · Each L has an inherited attribute prev
  - L.prev is inherited from sibling P<sub>1</sub>.val
- · Example ...

### Example of Inherited Attributes



val synthesized



prev inherited



 All can be computed in depth-first order

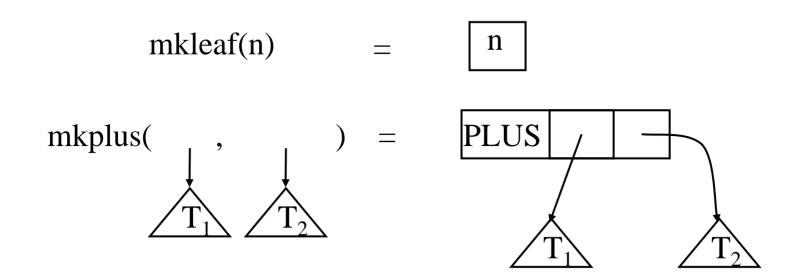
### Semantic Actions: Notes (Cont.)

Semantic actions can be used to build ASTs

- And many other things as well
  - Also used for type checking, code generation, ...
- · Process is called syntax-directed translation
  - Substantial generalization over CFGs

### Constructing an AST

- · We first define the AST data type
- Consider an abstract tree type with two constructors:



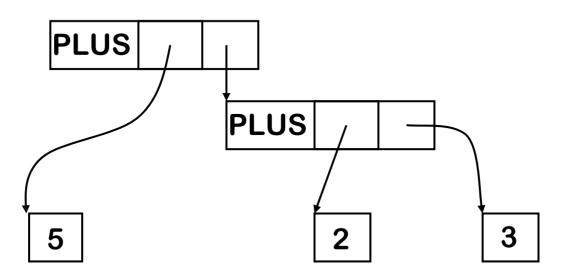
### Constructing a Parse Tree

- · We define a synthesized attribute ast
  - Values of ast values are ASTs
  - We assume that int.lexval is the value of the integer lexeme
  - Computed using semantic actions

### Parse Tree Example

- Consider the string int<sub>5</sub> '+' '(' int<sub>2</sub> '+' int<sub>3</sub> ')'
- A bottom-up evaluation of the ast attribute:

```
E.ast = mkplus(mkleaf(5),
mkplus(mkleaf(2), mkleaf(3))
```



### Review of Abstract Syntax Trees

- We can specify language syntax using CFG.
- The parser answers whether  $s \in L(G)$
- · ... and builds a parse tree
- · ... which it converts to an AST
- ... and passes on to the rest of the compiler.
- In the next "parsing" lectures:
  - How do we answer  $s \in L(G)$  and build a parse tree?
- After that: from AST to assembly language.

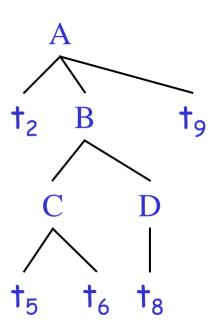
### Second-Half of Lecture: Outline

- Implementation of parsers
- Two approaches
  - Top-down
  - Bottom-up
- These slides: Top-Down
  - Easier to understand and program manually
- Next lectures: Bottom-Up
  - More powerful and used by most parser generators

# Introduction to Top-Down Parsing

 Terminals are seen in order of appearance in the token stream:

- The parse tree is constructed
  - From the top
  - From left to right



### Recursive Descent Parsing: Example

Consider the grammar

```
E \rightarrow T + E \mid T

T \rightarrow (E) \mid int \mid int * T
```

- Token stream is: int<sub>5</sub> \* int<sub>2</sub>
- Start with top-level non-terminal E
- Try the rules for E in order

### Recursive Descent Parsing: Example

• Try  $E_0 \rightarrow T_1 + E_2$ 

- Token stream: int5 \* int2
- Then try a rule for  $T_1 \rightarrow (E_3)$ 
  - But (does not match input token int<sub>5</sub>; we backtrack.
- Try  $T_1 \rightarrow int$ . Token matches.
  - But + after T<sub>1</sub> does not match input token \*
- Try  $T_1 \rightarrow int * T_2$ 
  - This will match and will consume the two tokens.
    - Try  $T_2 \rightarrow int$  (matches) but + after  $T_1$  will be unmatched.
    - Try  $T_2 \rightarrow int * T_3$  but \* does not match with end-of-input.
- We have exhausted all the choices for  $T_1$ 
  - Backtrack to choice for E<sub>0</sub>

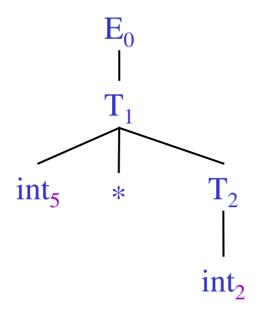
$$E \rightarrow T + E \mid T$$
  
 
$$T \rightarrow (E) \mid int \mid int * T$$

# Recursive Descent Parsing: Example

• Try  $E_0 \rightarrow T_1$ 

Token stream: ints \* int2

- Follow same steps as before for  $T_1$ 
  - And succeed with  $T_1 \rightarrow int_5 * T_2$  and  $T_2 \rightarrow int_2$
  - With the following parse tree



$$E \rightarrow T + E \mid T$$
  
 $T \rightarrow (E) \mid int \mid int * T$ 

### Recursive Descent Parsing: Notes

Easy to implement by hand

· Somewhat inefficient (due to backtracking)

But does not always work ...

### When Recursive Descent Does Not Work

• Consider a production  $5 \rightarrow 5$  a

```
bool S_1() { return S() && term(a); } bool S() { return S_1(); }
```

- 5() will get into an infinite loop
- We call a grammar <u>left-recursive</u> if it has a non-terminal S

```
5 \rightarrow^{+} 5\alpha for some \alpha
```

Recursive descent does not work in such cases
 it goes into an infinite loop.

### Elimination of Left Recursion

Consider the left-recursive grammar:

$$S \rightarrow S \alpha \mid \beta$$

- Generates all strings starting with a  $\beta$  and followed by any number of  $\alpha$ 's.
- The grammar can be rewritten using right recursion:

$$S \rightarrow \beta S'$$
  
 $S' \rightarrow \alpha S' \mid \epsilon$ 

### More Elimination of Left-Recursion

In general

$$S \rightarrow S \alpha_1 \mid ... \mid S \alpha_n \mid \beta_1 \mid ... \mid \beta_m$$

- All strings derived from 5 start with one of  $\beta_1, ..., \beta_m$  and continue with several instances of  $\alpha_1, ..., \alpha_n$
- Rewrite as

$$S \rightarrow \beta_1 S' \mid \dots \mid \beta_m S'$$
  
 $S' \rightarrow \alpha_1 S' \mid \dots \mid \alpha_n S' \mid \epsilon$ 

### General Left Recursion

The grammar

$$S \rightarrow A \alpha \mid \delta$$
 $A \rightarrow S \beta$ 

is also left-recursive because

$$S \rightarrow^+ S \beta \alpha$$

This left-recursion can also be eliminated

[See a Compilers book for a general algorithm]

### Summary of Recursive Descent

- Simple and general parsing strategy.
  - Left-recursion must be eliminated first
  - ... but that can be done automatically.
- Unpopular because of backtracking.
  - Thought to be too inefficient.
- In practice, backtracking is eliminated by restricting the grammar.

### **Predictive Parsers**

- Like recursive-descent but parser can "predict" which production to use
  - By looking at the next few tokens
  - No backtracking
- Predictive parsers accept LL(k) grammars
  - L means "left-to-right" scan of input
  - L means "leftmost derivation"
  - k means "predict based on k tokens of lookahead"
- In practice, LL(1) is used

# LL(1) Languages

- In recursive-descent, for each non-terminal and input token there may be a choice of productions
- LL(1) means that for each non-terminal and token there is only one production that could lead to success
- · Can be specified via 2D tables
  - One dimension for current non-terminal to expand
  - One dimension for next token
  - A table entry contains one production

# Predictive Parsing and Left Factoring

Recall the grammar for arithmetic expressions

$$E \rightarrow T + E \mid T$$
  
 $T \rightarrow (E) \mid int \mid int * T$ 

- Hard to predict because
  - For T two productions start with int
  - For E it is not clear how to predict
- A grammar must be <u>left-factored</u> before it is used for predictive parsing

# Left-Factoring Example

Recall the grammar

$$E \rightarrow T + E \mid T$$
  
 $T \rightarrow (E) \mid int \mid int * T$ 

Factor out common prefixes of productions:

$$E \rightarrow T X$$
  
 $X \rightarrow + E \mid \epsilon$   
 $T \rightarrow (E) \mid \text{int } Y$   
 $Y \rightarrow \epsilon \mid * T$ 

This grammar is equivalent to the original one.

# LL(1) Parsing Table Example

Left-factored grammar

$$E \rightarrow TX$$
  $X \rightarrow + E \mid \epsilon$   
 $T \rightarrow (E) \mid int Y$   $Y \rightarrow * T \mid \epsilon$ 

The LL(1) parsing table (\$ is the end marker)

	int	*	+	(	)	\$
E	ΤX			ΤX		
X			+ E		3	3
Т	int Y			(E)		
У		* T	3		3	3

# LL(1) Parsing Table Example (Cont.)

- · Consider the [E, int] entry
  - "When current non-terminal is E and next input is int, use production  $E \to T X$ "
  - This production can generate an int in the first place
- · Consider the [Y,+] entry
  - "When current non-terminal is Y and current token is +, get rid of Y"
  - Y can be followed by + only in a derivation in which  $Y \rightarrow \epsilon$

### LL(1) Parsing Tables: Errors

- Blank entries indicate error situations
  - Consider the [E,\*] entry
  - "There is no way to derive a string starting with \* from non-terminal E"

# Using Parsing Tables

- Method similar to recursive descent, except
  - For each non-terminal X
  - We look at the next token a
  - And choose the production shown at [X,a]
- We use a stack to keep track of pending nonterminals.
- · We reject when we encounter an error state.
- We accept when we encounter end-of-input.

# LL(1) Parsing Algorithm

# LL(1) Parsing Example

<u>Stack</u>	Input	Action
E\$	int * int \$	ΤX
TX\$	int * int \$	int Y
int Y X \$	int * int \$	terminal
Y X \$	* int \$	* T
* T X \$	* int \$	terminal
TX\$	int \$	int Y
int Y X \$	int \$	terminal
Y X \$	\$	3
X \$	\$	3
\$	\$	ACCEPT

	int	*	+	(	)	\$
Е	ΤX			ΤX		
X			+ E		3	3
Т	int Y			(E)		
У		* T	3		3	3