

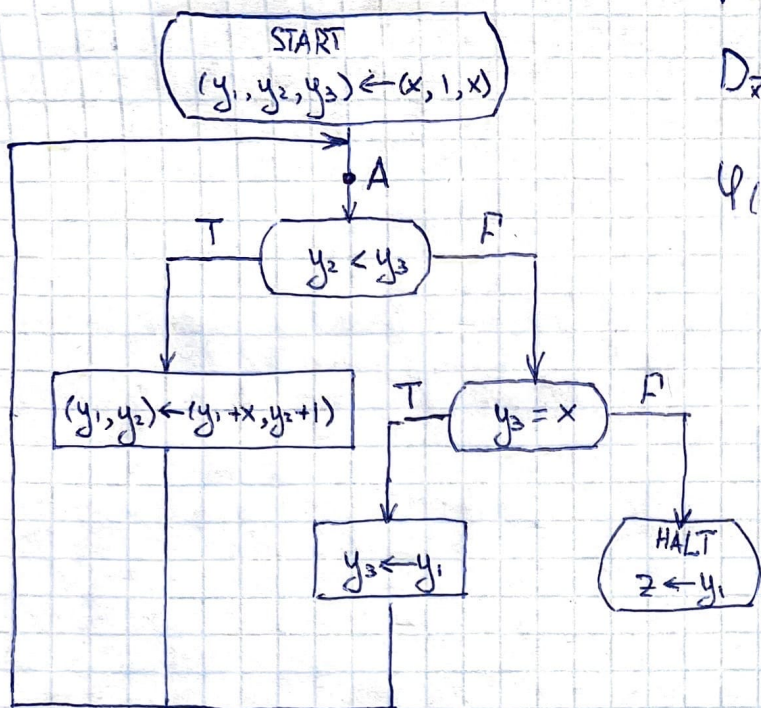
Задание 1.3

$$V = \{x, y_1, y_2, y_3, z\}$$

$$D_{\bar{x}} = D_{\bar{y}} = D_{\bar{z}} = \mathbb{Z}$$

$$\varphi(x) \equiv x > 1$$

$$W = \{N \cup \{0\}, >\}$$



$$S-A: x > 1 \Rightarrow q(x, x, 1, x)$$

$$A-T-A: x > 1 \wedge q(x, y_1, y_2, y_3) \Rightarrow U(x, y_1, y_2, y_3) \in W$$

$$A-T-A: x > 1 \wedge q(x, y_1, y_2, y_3) \wedge y_2 < y_3 \Rightarrow q(x, y_1 + x, y_2 + 1, y_3)$$

$$A-T-A: x > 1 \wedge q(x, y_1, y_2, y_3) \wedge y_2 < y_3 \Rightarrow U(x, y_1 + x, y_2 + 1, y_3) < U(x, y_1, y_2, y_3)$$

$$A-F-T-A: x > 1 \wedge q(x, y_1, y_2, y_3) \wedge y_2 \geq y_3 \wedge y_3 = x \Rightarrow q(x, y_1, y_2, y_1)$$

$$A-F-T-A: x > 1 \wedge q(x, y_1, y_2, y_3) \Rightarrow U(x, y_1, y_2, y_3) \in W$$

$$A-F-T-A: x > 1 \wedge q(x, y_1, y_2, y_3) \wedge y_2 \geq y_3 \wedge y_3 = x \Rightarrow U(x, y_1, y_2, y_1) < U(x, y_1, y_2, y_3)$$

$$q(x, y_1, y_2, y_3) \equiv y_1 = y_2 \cdot x \wedge ((y_3 = x \wedge y_2 \leq x) \vee (y_3 = x^2 \wedge y_2 \leq x^2))$$

$$S-A: x > 1 \Rightarrow x = 1 \cdot x \wedge ((x = x \wedge 1 \leq x) \vee (x = x^2 \wedge 1 \leq x^2))$$

$$A-T-A: x > 1 \wedge y_1 = y_2 \cdot x \wedge ((y_3 = x \wedge y_2 \leq x) \vee (y_3 = x^2 \wedge y_2 \leq x^2)) \wedge y_2 < y_3 \Rightarrow y_1 + x = (y_2 + 1) \cdot x \wedge ((y_3 = x \wedge y_2 + 1 \leq x) \vee (y_3 = x^2 \wedge y_2 + 1 \leq x^2)) \wedge y_2 + 1 < y_3$$

$$A-F-T-A: x > 1 \wedge y_1 = y_2 \cdot x \wedge ((y_3 = x \wedge y_2 \leq x) \vee (y_3 = x^2 \wedge y_2 \leq x^2)) \wedge y_2 \geq y_3 \wedge y_3 = x \Rightarrow y_1 = y_2 \cdot x \wedge ((y_1 = x \wedge y_2 \leq x) \vee (y_1 = x^2 \wedge y_2 \leq x^2))$$

$$U(x, y_1, y_2, y_3) = x^3 - y_2 - y_3$$

$$A: x > 1 \wedge q(x, y_1, y_2, y_3) \Rightarrow U(x, y_1, y_2, y_3) \in W$$

$$x > 1 \wedge y_1 = y_2 \cdot x \wedge ((y_3 = x \wedge y_2 \leq x) \vee (y_3 = x^2 \wedge y_2 \leq x^2)) \Rightarrow x^3 - y_2 - y_3 \geq 0$$

$$x > 1 \wedge y_1 = y_2 \cdot x \wedge ((y_3 = x \wedge y_2 \leq x) \vee (y_3 = x^2 \wedge y_2 \leq x^2)) \Rightarrow x^3 \geq y_2 + y_3$$