## Hands-on Exercise 4: Visual Analytics with R

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## **Learning Outcome**

In this hands-on exercise, you will gain hands-on experience on using:

- ggstatsplot to create visual graphics with rich statistical information,
- ggdist to visualise uncertainty on data, and
- ungeviz to build hypothetical outcome plots (HOPs).

## **Getting Started**

In this exercise, **infer**, **ggstatsplot** and **tidyverse** will be used.

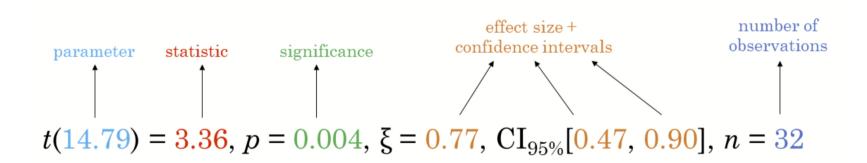
In this exercise, the Exam.csv data will be used.

```
exam <- read_csv("data/Exam_data.csv")
```



## Visual Statistical Analysis with ggstatsplot

- **ggstatsplot** is an extension of **ggplot2** package for creating graphics with details from statistical tests included in the information-rich plots themselves.
  - To provide alternative statistical inference methods by default.
  - To follow best practices for statistical reporting. For all statistical tests reported in the plots, the default template abides by the APA gold standard for statistical reporting.
     For example, here are results from a robust t-test:



#### One-sample test: gghistostats() method

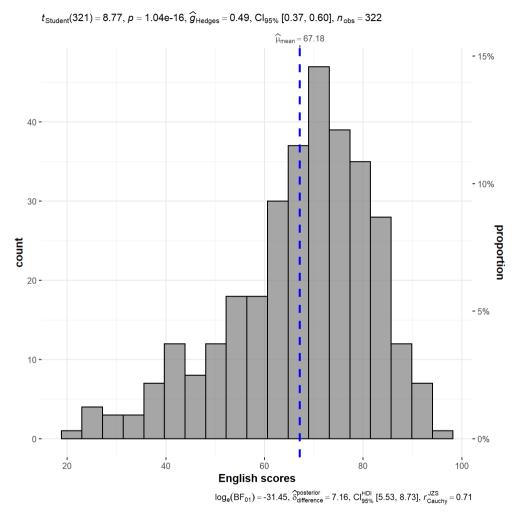
In the code chunk below, *gghistostats()* is used to to build an visual of one-sample test on English scores.

```
set.seed(1234)

gghistostats(
  data = exam,
  x = ENGLISH,
  type = "bayes",
  test.value = 60,
  xlab = "English scores"
)
```

#### Default information:

- statistical details
- Bayes Factor
- sample sizes
- distribution summary



#### **Unpacking the Bayes Factor**

- A Bayes factor is the ratio of the likelihood of one particular hypothesis to the likelihood of another. It can be interpreted as a measure of the strength of evidence in favor of one theory among two competing theories.
- That's because the Bayes factor gives us a way to evaluate the data in favor of a null hypothesis, and to use external information to do so. It tells us what the weight of the evidence is in favor of a given hypothesis.
- When we are comparing two hypotheses, H1 (the alternate hypothesis) and H0 (the null hypothesis), the Bayes Factor is often written as B10. It can be defined mathematically as

$$\frac{likelihood of data given H_1}{likelihood of data given H_0} = \frac{P(D|H_1)}{P(D|H_0)}$$

• The **Schwarz criterion** is one of the easiest ways to calculate rough approximation of the Bayes Factor.

#### How to interpret Bayes Factor

A **Bayes Factor** can be any positive number. One of the most common interpretations is this one—first proposed by Harold Jeffereys (1961) and slightly modified by Lee and Wagenmakers in 2013:

| IF B <sub>10</sub> IS | THEN YOU HAVE                         |
|-----------------------|---------------------------------------|
| > 100                 | Extreme evidence for H <sub>1</sub>   |
| 30 - 100              | Very strong evidence for ${\rm H}_1$  |
| 10 - 30               | Strong evidence for H <sub>1</sub>    |
| 3 – 10                | Moderate evidence for H <sub>1</sub>  |
| 1 - 3                 | Anecdotal evidence for H <sub>1</sub> |
| 1                     | No evidence                           |
| 1/3 - 1               | Anecdotal evidence for H <sub>1</sub> |
| 1/3 - 1/10            | Moderate evidence for $H_1$           |
| 1/10 - 1/30           | Strong evidence for H <sub>1</sub>    |
| 1/30 - 1/100          | Very strong evidence for ${\sf H}_1$  |
| < 1/100               | Extreme evidence for H <sub>1</sub>   |
|                       |                                       |

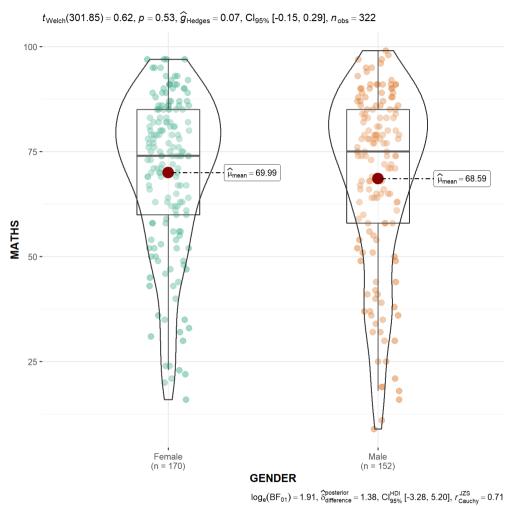
## Two-sample mean test: ggbetweenstats()

In the code chunk below, *ggbetweenstats()* is used to build a visual for two-sample mean test of Maths scores by gender.

```
ggbetweenstats(
  data = exam,
  x = GENDER,
  y = MATHS,
  type = "np",
  messages = FALSE
)
```

#### Default information:

- statistical details
- Bayes Factor
- sample sizes
- distribution summary

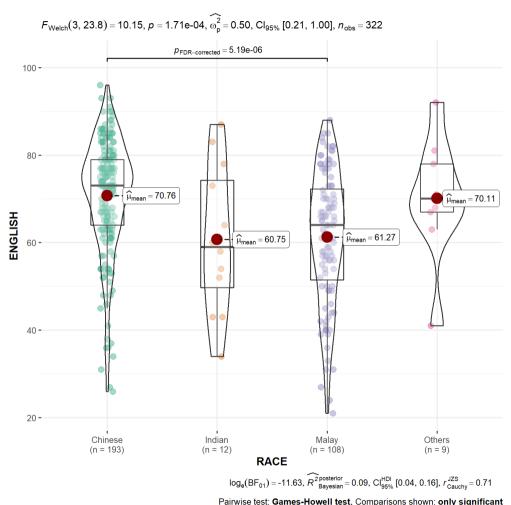


#### Oneway ANOVA Test: ggbetweenstats() method

In the code chunk below, *ggbetweenstats()* is used to build a visual for One-way ANOVA test on English score by race.

```
ggbetweenstats(
  data = exam,
  x = RACE,
  y = ENGLISH,
  type = "p",
  mean.ci = TRUE,
  pairwise.comparisons = TRUE,
  pairwise.display = "s",
  p.adjust.method = "fdr",
  messages = FALSE
)
```

- "ns" → only non-significant
- "s" → only significant
- "all" → everything



## ggbetweenstats - Summary of tests

Following (between-subjects) tests are carried out for each type of analyses-

| Туре           | No. of groups | Test  |
|----------------|---------------|---|
| Parametric     | > 2           | Fisher's or Welch's one-way ANOVA               |
| Non-parametric | > 2           | Kruskal-Wallis one-way ANOVA                    |
| Robust         | > 2           | Heteroscedastic one-way ANOVA for trimmed means |
| Bayes Factor   | > 2           | Fisher's ANOVA                                  |
| Parametric     | 2             | Student's or Welch's t-test                     |
| Non-parametric | 2             | Mann–Whitney <i>U</i> test                      |
| Robust         | 2             | Yuen's test for trimmed means                   |
| Bayes Factor   | 2             | Student's t-test                                |

## ggbetweenstats - Summary of tests

Following effect sizes (and confidence intervals/CI) are available for each type of test-

| Туре           | No. of groups | Effect size  | CI? |
|----------------|---------------|--|-----|
| Parametric     | > 2           | $\eta_p^2$ , $\eta^2$ , $\omega_p^2$ , $\omega^2$                          | Yes |
| Non-parametric | > 2           | $\eta_H^2$ (H-statistic based eta-squared)                                 | Yes |
| Robust         | > 2           | $\xi$ (Explanatory measure of effect size)                                 | Yes |
| Bayes Factor   | > 2           | No   | No  |
| Parametric     | 2             | Cohen's $d$ , Hedge's $g$ (central-and noncentral- $t$ distribution based) | Yes |
| Non-parametric | 2             | $r$ (computed as $Z/\sqrt{N}$ )  | Yes |
| Robust         | 2             | $\xi$ (Explanatory measure of effect size)                                 | Yes |
| Bayes Factor   | 2             | No   | No  |

## ggbetweenstats - Summary of tests

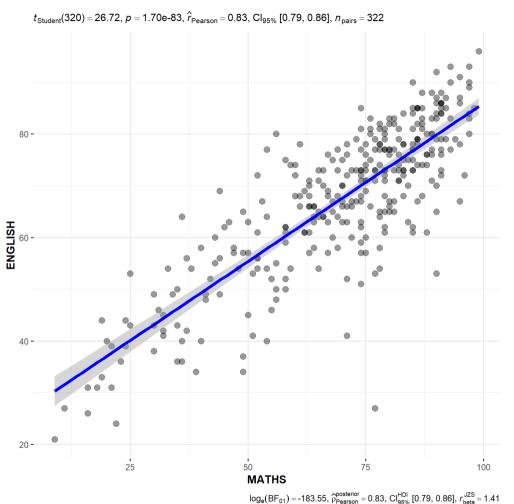
Here is a summary of multiple pairwise comparison tests supported in ggbetweenstats-

| Туре           | Equal variance? | Test                      | p-value adjustment? |
|----------------|-----------------|---------------------------|---------------------|
| Parametric     | No              | Games-Howell test         | Yes                 |
| Parametric     | Yes             | Student's t-test          | Yes                 |
| Non-parametric | No              | Dunn test                 | Yes                 |
| Robust         | No              | Yuen's trimmed means test | Yes                 |
| Bayes Factor   | NA              | Student's t-test          | NA                  |

#### Significant Test of Correlation: ggscatterstats()

In the code chunk below, *ggscatterstats()* is used to build a visual for Significant Test of Correlation between Maths scores and English scores.

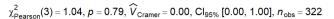
```
ggscatterstats(
  data = exam,
  x = MATHS,
  y = ENGLISH,
  marginal = FALSE,
)
```

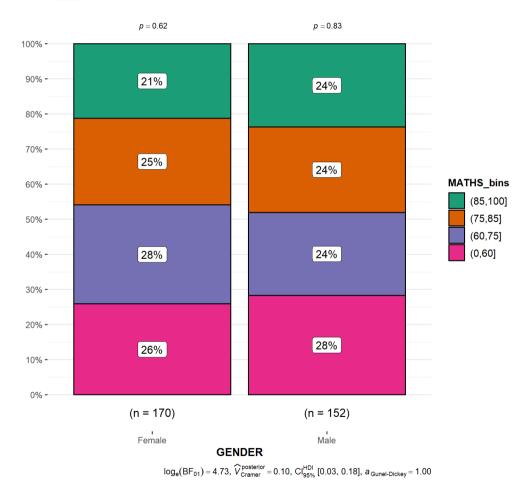


## Significant Test of Association (Depedence): ggbarstats() methods

In the code chunk below, the Maths scores is binned into a 4-class variable by using *cut()*.

In this code chunk below *ggbarstats()* is used to build a visual for Significant Test of Association





## Toyota Corolla case study

Build a model to discover factors
 affecting prices of used-cars by taking
 into consideration a set of explanatory
 variables.



## Installing and loading the required libraries

Type the code chunk below to install and launch the necessary R packages

# Importing Excel file: readxl methods

In the code chunk below, *read\_xls()* of **readxl** package is used to import the data worksheet of ToyotaCorolla.xls workbook into R.

Notice that the output object car\_resale is a tibble data frame.

## Multiple Regression Model using lm()

The code chunk below is used to calibrate a multiple linear regression model by using *lm()* of Base Stats of R.

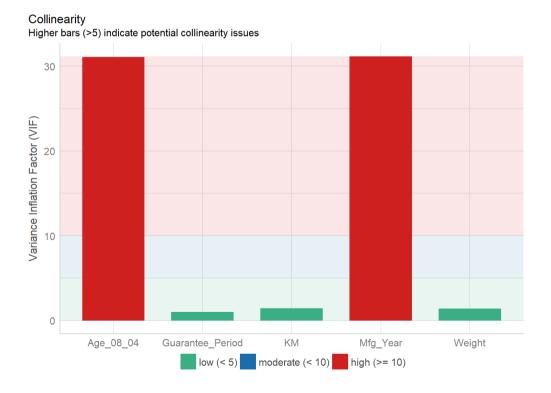
```
model <- lm(Price ~ Age_08_04 + Mfg_Year + KM +</pre>
               Weight + Guarantee Period, data = car resale)
model
##
## Call:
## lm(formula = Price ~ Age_08_04 + Mfg_Year + KM + Weight + Guarantee_Period,
       data = car resale)
##
##
## Coefficients:
        (Intercept)
                                               Mfg Year
##
                          Age 08 04
                                                                        \mathsf{KM}
                                               1.315e+03
##
         -2.637e+06
                           -1.409e+01
                                                                -2.323e-02
##
             Weight Guarantee Period
##
          1.903e+01
                            2.770e+01
```

## Model Diagnostic: checking for multicolinearity:

In the code chunk, *check\_collinearity()* of **performance** package.

```
check_collinearity(model)
    Check for Multicollinearity
##
   Low Correlation
##
##
                Term VIF Increased SE Tolerance
##
                  KM 1.46
                                   1.21
                                             0.68
              Weight 1.41
##
                                  1.19
                                             0.71
                                             0.97
##
    Guarantee Period 1.04
                                  1.02
##
  High Correlation
##
##
         Term
                VIF Increased SE Tolerance
##
    Age_08_04 31.07
                            5.57
                                       0.03
    Mfg_Year 31.16
##
                            5.58
                                       0.03
```

```
check_c <- check_collinearity(model)
plot(check_c)</pre>
```

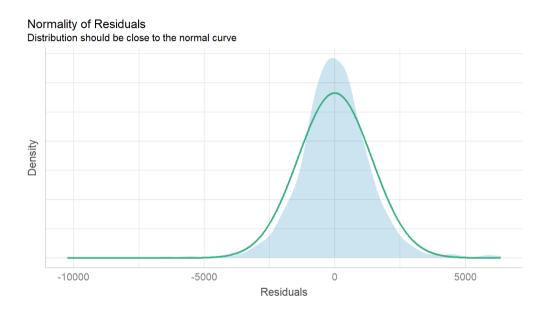


## Model Diagnostic: checking normality assumption

In the code chunk, *check\_normality()* of **performance** package.

```
check_n <- check_normality(model1)</pre>
```

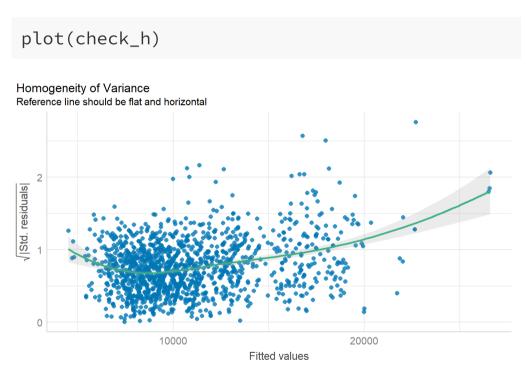
plot(check\_n)



# Model Diagnostic: Check model for homogeneity of variances

In the code chunk, *check\_heteroscedasticity()* of **performance** package.

check\_h <- check\_heteroscedasticity(model1)</pre>



## Model Diagnostic: Complete check

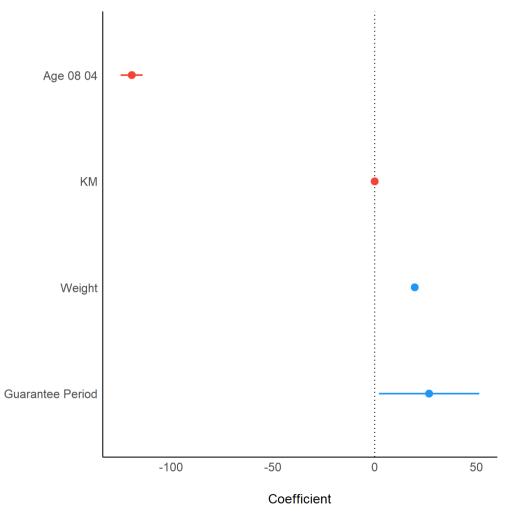
We can also perform the complete by using check\_model().

check\_model(model1) Posterior Predictive Check Linearity Model-predicted lines should resemble observed data line Reference line should be flat and horizontal Residuals 0.00010 -5000 0.00005 -10000 0.00000 10000 10000 20000 30000 20000 Price Fitted values — Model-predicted data — Observed data Homogeneity of Variance Influential Observations Reference line should be flat and horizontal Points should be inside the contour lines residual 40 V|Std. Std. -80 10000 20000 0.000 0.025 0.050 0.075 0.100 Leverage (h<sub>ii</sub>) Fitted values ©llinearity Normality of Residuals Higher bars (>5) indicate potential collinearity issues Oots should fall along the line Variance Inflation Fac Quantile 10.0 7.5 5.0 Sample 2.5 0.0 Guarantee Period KM Weight -2 0 Age 08 04 Standard Normal Distribution Quantiles low (< 5) moderate (< 10) high (>= 10)

#### Visualising Regression Parameters: see methods

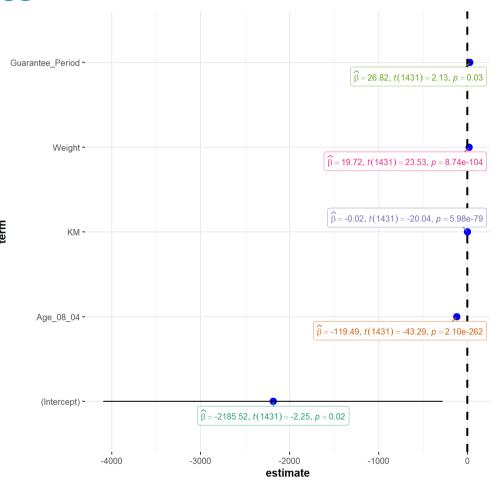
In the code below, plot() of see package and parameters() of parameters package is used to visualise the parameters of a regression model.

plot(parameters(model1))



## Visualising Regression Parameters: ggcoefstats() methods

In the code below, *ggcoefstats()* of ggstatsplot package to visualise the parameters of a regression model.



AIC = 24915, BIC = 24946

## Visualizing the uncertainty of point estimates

- A point estimate is a single number, such as a mean.
- Uncertainty is expressed as standard error, confidence interval, or credible interval
- Important:
  - Don't confuse the uncertainty of a point estimate with the variation in the sample

## Visualizing the uncertainty of point estimates: ggplot2 methods

The code chunk below performs the followings:

- group the observation by RACE,
- computes the count of observations, mean, standard deviation and standard error of Maths by RACE, and
- save the output as a tibble data table called my\_sum.

```
my_sum <- exam %>%
  group_by(RACE) %>%
  summarise(
    n=n(),
    mean=mean(MATHS),
    sd=sd(MATHS)
    ) %>%
  mutate(se=sd/sqrt(n-1))
```

Note: For the mathematical explanation, please refer to Slide 20 of Lesson 4.

Next, the code chunk below will

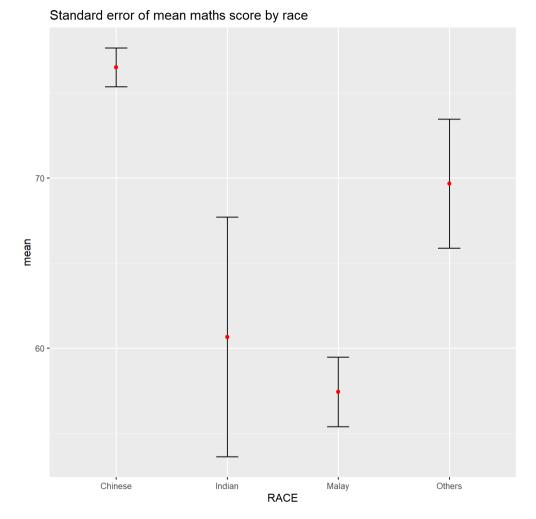
```
knitr::kable(head(my_sum), format = 'html')
```

| RACE    | n   | mean     | sd       | se       |
|---------|-----|----------|----------|----------|
| Chinese | 193 | 76.50777 | 15.69040 | 1.132357 |
| Indian  | 12  | 60.66667 | 23.35237 | 7.041005 |
| Malay   | 108 | 57.44444 | 21.13478 | 2.043177 |
| Others  | 9   | 69.66667 | 10.72381 | 3.791438 |

## Visualizing the uncertainty of point estimates: ggplot2 methods

The code chunk below is used to reveal the standard error of mean maths score by race .

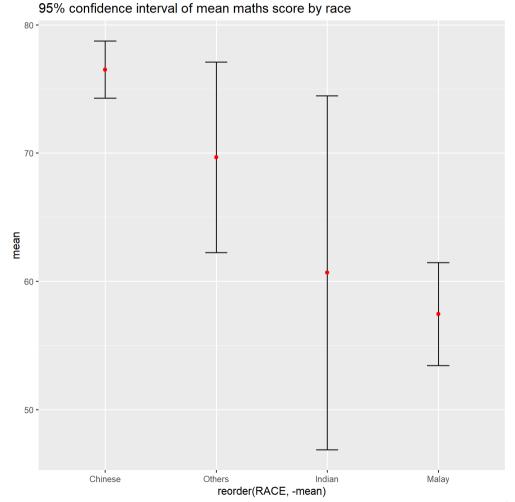
```
ggplot(my_sum) +
  geom_errorbar(
    aes(x=RACE,
        ymin=mean-se,
        ymax=mean+se),
   width=0.2,
    colour="black",
    alpha=0.9,
    size=0.5) +
  geom_point(aes
           (x=RACE,
            y=mean),
           stat="identity",
           color="red",
           size = 1.5,
           alpha=1) +
  ggtitle("Standard error of mean
          maths score by rac")
```



## Visualizing the uncertainty of point estimates: ggplot2 methods

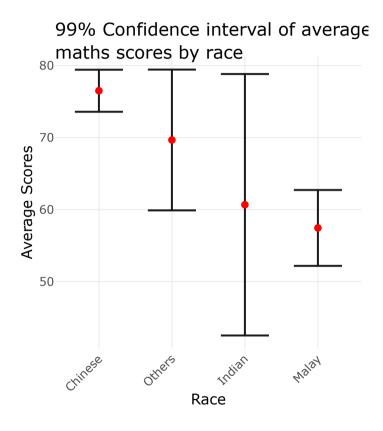
**Exercise:** Plot the 95% confidence interval of mean maths score by race. The error bars should be sorted by the average maths scores.

#### The solution:



#### Visualizing the uncertainty of point estimates with interactive error bars

Exercise: Plot interactive error bars for the 99% confidence interval of mean maths score by race.



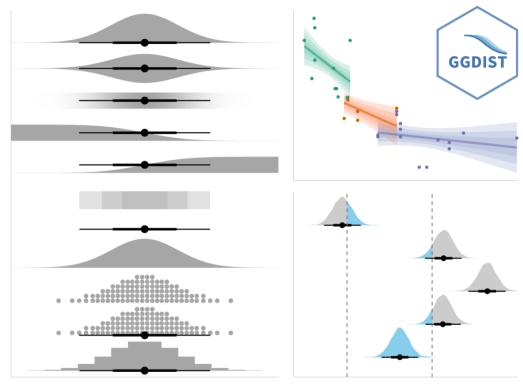
| Show 10                     | entries         | Search:    |          |           |  |
|-----------------------------|-----------------|------------|----------|-----------|--|
|                             | No. of pupils * | Avg Scores | Std Dev* | Std Error |  |
| Chinese                     | 193             | 76.51      | 15.69    | 1.13      |  |
| Indian                      | 12              | 60.67      | 23.35    | 7.04      |  |
| Malay                       | 108             | 57.44      | 21.13    | 2.04      |  |
| Others                      | 9               | 69.67      | 10.72    | 3.79      |  |
| Showing 1 to 4 of 4 entries |                 |            | Previous | 1 Next    |  |

### Visualizing the uncertainty of point estimates with interactive error bars

The code chunk:

## Visualising Uncertainty: ggdist package

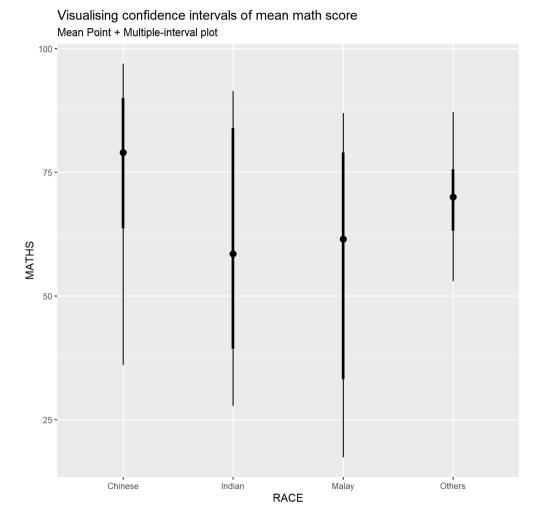
- **ggdist** is an R package that provides a flexible set of ggplot2 geoms and stats designed especially for visualising distributions and uncertainty.
- It is designed for both frequentist and Bayesian uncertainty visualization, taking the view that uncertainty visualization can be unified through the perspective of distribution visualization:
  - for frequentist models, one visualises confidence distributions or bootstrap distributions (see vignette("freq-uncertaintyvis"));
  - for Bayesian models, one visualises probability distributions (see the tidybayes package, which builds on top of ggdist).



## Visualizing the uncertainty of point estimates: ggdist methods

In the code chunk below, stat\_pointinterval() of **ggdist** is used to build a visual for displaying distribution of maths scores by race.

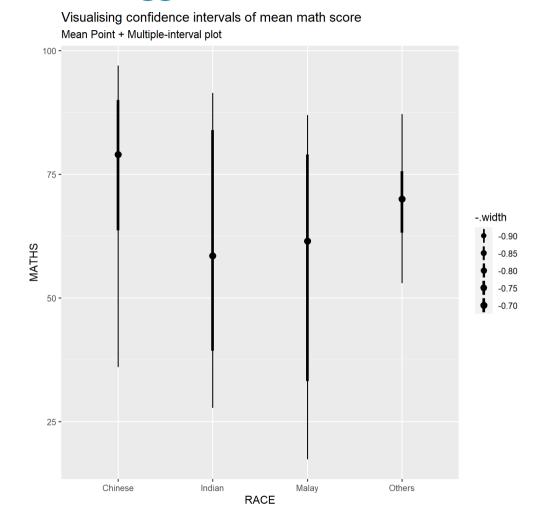
Gentle advice: This function comes with many arguments, students are advised to read the syntax reference for more detail.



## Visualizing the uncertainty of point estimates: ggdist methods

**Exercise:** Makeover the plot on previous slide by showing 95% and 99% confidence intervals.

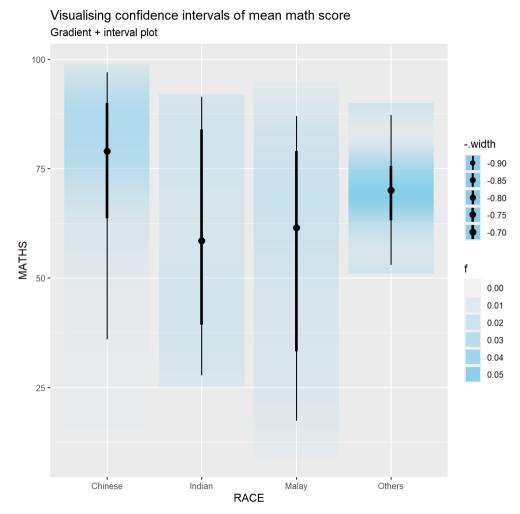
Gentle advice: This function comes with many arguments, students are advised to read the syntax reference for more detail.



## Visualizing the uncertainty of point estimates: ggdist methods

In the code chunk below, stat\_gradientinterval() of **ggdist** is used to build a visual for displaying distribution of maths scores by race.

Gentle advice: This function comes with many arguments, students are advised to read the syntax reference for more detail.



# Visualising Uncertainty with Hypothetical Outcome Plots (HOPs)

Step 1: Installing ungeviz package

```
devtools::install_github("wilkelab/ungeviz")
```

Note: You only need to perform this step once.

Step 2: Launch the application in R

library(ungeviz)