

**MACHINE** m12

**REFINES** m11

**SEES** c0

**VARIABLES**

CA  
PCA  
root  
OU  
RiO  
UH  
PRA  
EA  
ViO  
AiO  
UR  
PAA  
PVA  
CiO  
PCxA  
RV  
AV  
AA  
root1  
UH1  
OU1  
UR1  
RiO1  
EA1  
CA1  
PRA1  
PAA1  
PVA1  
PCA1  
PCxA1  
ViO1  
RV1  
AiO1  
AA1  
AV1  
CiO1  
Access\_Requested  
Request\_Treated  
time  
at  
PDA permission deadline assingment  
Discarded\_Request  
height  
PATH  
PDistA  
Final\_Decision  
Processing\_Time  
PAcA1

PAcA

## INVARIANTS

- inv3:  $height \in UNIT \rightarrow \mathbb{N}$
- inv4:  $\forall u. u \in \text{ran}(\text{root1}) \Rightarrow (\text{height}[\{u\}] \neq \emptyset \Rightarrow \text{height}(u) = 0)$
- inv5:  $\forall u, v. u \mapsto v \in UH1 \Rightarrow (\text{height}[\{u\}] \neq \emptyset \wedge \text{height}[\{v\}] \neq \emptyset \Rightarrow \text{height}(u) = \text{height}(v) + 1)$
- inv6:  $PATH \subseteq UNIT \times UNIT$
- inv7:  $PDistA \subseteq PERMISSION \times \mathbb{N}$
- inv8:  $Final\_Decision \in Access\_Requested \rightarrow 0 \dots 1$
- inv9:  $Processing\_Time \in Access\_Requested \rightarrow \mathbb{N}$
- inv10:  $PAcA1 \in PERMISSION \rightarrow CiO1$

## EVENTS

**Initialisation**  $\langle \text{extended} \rangle$

**begin**

- act1:  $CiO := \emptyset$
- act2:  $root := \in ORG \rightarrow UNIT$
- act3:  $OU := \in UNIT \rightarrow ORG$
- act4:  $AiO := \emptyset$
- act5:  $UH := \in UNIT \rightarrow UNIT$
- act6:  $ViO := \emptyset$
- act7:  $RiO := \emptyset$
- act9:  $PCA := \in PERMISSION \rightarrow COR$
- act10:  $PRA := \emptyset$
- act11:  $EA := \emptyset$
- act12:  $UR := \emptyset$
- act13:  $PAA := \emptyset$
- act14:  $PVA := \emptyset$
- act15:  $PCxA := \emptyset$
- act16:  $AV := \emptyset$
- act17:  $AA := \emptyset$
- act18:  $RV := \emptyset$
- act20:  $root1 := \emptyset$
- act21:  $OU1 := \in UNIT \rightarrow ORG$
- act22:  $UH1 := \emptyset$
- act23:  $CA := \emptyset$
- act24:  $UR1 := \emptyset$
- act25:  $RiO1 := \emptyset$
- act26:  $EA1 := \emptyset$
- act27:  $CA1 := \emptyset$
- act28:  $PRA1 := \emptyset$
- act29:  $PAA1 := \emptyset$
- act30:  $PVA1 := \emptyset$
- act31:  $PCA1 := \emptyset$
- act32:  $PCxA1 := \emptyset$
- act33:  $ViO1 := \emptyset$
- act34:  $RV1 := \emptyset$
- act35:  $AiO1 := \emptyset$
- act36:  $AV1 := \emptyset$
- act37:  $AA1 := \emptyset$
- act38:  $CiO1 := \emptyset$
- act39:  $Access\_Requested := \emptyset$
- act40:  $PDistA := \emptyset$
- act41:  $Request\_Treated := \emptyset$
- act42:  $PAcA := \emptyset$
- act43:  $time := 0$
- act44:  $at := \emptyset$
- act45:  $PDA := \emptyset$
- act46:  $Discarded\_Request := \emptyset$
- act50:  $height := \emptyset$

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    act51:  $PATH := \emptyset$ 
    act52:  $Final\_Decision := \emptyset$ 
    act53:  $Processing\_Time := \emptyset$ 
    act54:  $PAC1 := \emptyset$ 
end
Event Concrete_Model_Generation  $\langle \text{ordinary} \rangle \triangleq$ 
refines Concrete_Model_Generation
begin
    act1:  $CiO := CiO1$ 
    act4:  $AiO := AiO1$ 
    act6:  $ViO := ViO1$ 
    act16:  $AV := AV1$ 
    act17:  $AA := AA1$ 
    act18:  $RV := RV1$ 
    act2:  $root := root1$ 
    act5:  $UH := UH1$ 
    act3:  $OU := OU1$ 
    act7:  $RiO := RiO1$ 
    act12:  $UR := UR1$ 
    act11:  $EA := EA1$ 
    act9:  $PAC := PAC1$ 
    act10:  $PRA := PRA1$ 
    act13:  $PAA := PAA1$ 
    act14:  $PVA := PVA1$ 
    act15:  $PCxA := PCxA1$ 
    act19:  $CA := CA1$ 
    act20:  $PAC := PAC1$ 
end
Event Assign_Organization_Root  $\langle \text{ordinary} \rangle \triangleq$ 
refines Assign_Organization_Root
any
    u
    org
where
    grd1:  $org \in ORG \wedge u \in UNIT$ 
    grd2:  $org \notin dom(root1)$ 
    grd3:  $u \notin dom(UH1)$ 
    grd4:  $ran(root1 \cup \{org \mapsto u\}) \cap dom(UH1) = \emptyset$ 
    grd5:  $u \mapsto org \in OU1$ 
    grd6:  $u \notin ran(root1)$ 
    grd7:  $height[\{u\}] = \emptyset$ 
then
    act1:  $root1 := root1 \cup \{org \mapsto u\}$ 
    act2:  $height := height \triangleleft \{u \mapsto 0\}$ 
end
Event Add_Unit_Hierarchy  $\langle \text{ordinary} \rangle \triangleq$ 
refines Add_Unit_Hierarchy
any
    u1
    u2
where
    grd1:  $u1 \in UNIT \wedge u2 \in UNIT$ 
    grd3:  $u1 \notin dom(UH1)$ 
    grd7:  $u1 \mapsto u2 \notin UH1$ 
    grd4:  $u1 \neq u2$ 
    grd5:  $u2 \mapsto u1 \notin UH1$ 
    grd6:  $u1 \notin ran(root1)$ 
    grd8:  $OU1[\{u1\}] = OU1[\{u2\}]$ 

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    grd9:  $\forall e \cdot e \mapsto u1 \in EA1 \Rightarrow e \mapsto u2 \notin EA1$ 
    grd10:  $\forall e \cdot e \mapsto u2 \in EA1 \Rightarrow e \mapsto u1 \notin EA1$ 
    grd11:  $height[\{u2\}] \neq \emptyset$ 
  then
    act1:  $UH1 := UH1 \cup \{u1 \mapsto u2\}$ 
    act2:  $height := height \triangleleft \{u1 \mapsto (height(u2) + 1)\}$ 
    act3:  $PATH := PATH \cup \{u1 \mapsto u2\} \cup \{u3 \cdot u2 \mapsto u3 \in PATH | u1 \mapsto u3\}$ 
  end
Event Assign_Unit_to_Org <ordinary>  $\hat{=}$ 
extends Assign_Unit_to_Org
  any
    u
    org
  where
    grd1:  $u \mapsto org \notin OU1$ 
    grd2:  $u \notin dom(OU1)$ 
    grd3:  $\forall org1, role \cdot u \mapsto (role \mapsto org1) \in UR1 \Rightarrow org = org1$ 
  then
    act1:  $OU1 := OU1 \cup \{u \mapsto org\}$ 
  end
Event Assign_Role_to_Unit <ordinary>  $\hat{=}$ 
extends Assign_Role_to_Unit
  any
    r
    u
  where
    grd1:  $r \in RiO1 \wedge u \in UNIT \wedge (u \mapsto r) \notin UR1$ 
    grd2:  $\forall role, org \cdot r = role \mapsto org \Rightarrow (OU1[\{u\}] \neq \emptyset \Rightarrow OU1(u) = org)$ 
  then
    act1:  $UR1 := UR1 \cup \{(u \mapsto r)\}$ 
  end
Event Assign_Role_to_Organization <ordinary>  $\hat{=}$ 
extends Assign_Role_to_Organization
  any
    r
    org
  where
    grd1:  $r \in ROLE \wedge org \in ORG$ 
    grd2:  $r \mapsto org \notin RiO1$ 
  then
    act1:  $RiO1 := RiO1 \cup \{r \mapsto org\}$ 
  end
Event Assign_Employee_to_Unit <ordinary>  $\hat{=}$ 
extends Assign_Employee_to_Unit
  any
    e
    u
  where
    grd1:  $e \mapsto u \notin EA1$ 
    grd2:  $\forall u1 \cdot e \mapsto u1 \in EA1 \Rightarrow (u \mapsto u1 \notin UH1 \wedge u1 \mapsto u \notin UH1)$ 
  then
    act1:  $EA1 := EA1 \cup \{e \mapsto u\}$ 
  end
Event Assign_Approver <ordinary>  $\hat{=}$ 
refines Assign_Approver
  any
    p
    d

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    u
    cor
  where
    grd5:  $\forall u1, p1, d1. cor \mapsto u1 \mapsto p1 \mapsto d1 \in CA1 \Rightarrow u1 \neq u \wedge (u1 \mapsto u \in UH1 \vee (\exists u2, p2, d2. cor \mapsto u2 \mapsto p2 \mapsto d2 \in CA1 \wedge u2 \mapsto u \in UH1))$ 
    grd1:  $\forall u2, p2, d2. cor \mapsto u2 \mapsto p2 \mapsto d2 \in CA1 \wedge u \neq u2 \Rightarrow (OU1[\{u\}] \neq \emptyset \wedge OU1[\{u2\}] \neq \emptyset \Rightarrow OU1(u) = OU1(u2))$ 
    grd2:  $cor \mapsto u \mapsto p \mapsto d \notin CA1$ 
    grd4:  $d \in \mathbb{N} \wedge p \in \mathbb{N}$ 
  then
    act1:  $CA1 := CA1 \cup \{cor \mapsto u \mapsto p \mapsto d\}$ 
  end
Event Define_Security_Rule  $\langle \text{ordinary} \rangle \triangleq$ 
extends Define_Security_Rule
  any
    rio
    aio
    vio
    cor
    cio
    perm
  where
    grd1:  $rio \in RiO1 \wedge aio \in AiO \wedge vio \in ViO \wedge cio \in CiO \wedge cor \in COR \wedge perm \in PERMISSION$ 
    grd2:  $\forall a, v, c, org1, org2, org3. aio = a \mapsto org1 \wedge vio = v \mapsto org2 \wedge cio = c \mapsto org3 \Rightarrow org1 = org2 \wedge org2 = org3$ 
    grd3:  $perm \notin dom(PRA1) \wedge perm \notin dom(PAA1) \wedge perm \notin dom(PVA1) \wedge perm \notin dom(PCA1) \wedge perm \notin dom(PCxA1)$ 
    grd4:  $\forall r, org. cio = r \mapsto org \Rightarrow (\forall u1, p1, d1, org1. cor \mapsto u1 \mapsto p1 \mapsto d1 \in CA1 \wedge OU1(u1) = org1 \Rightarrow org1 = org)$ 
  then
    act1:  $PRA1 := PRA1 \cup \{perm \mapsto rio\}$ 
    act2:  $PAA1 := PAA1 \cup \{perm \mapsto aio\}$ 
    act3:  $PVA1 := PVA1 \cup \{perm \mapsto vio\}$ 
    act4:  $PCA1 := PCA1 \cup \{perm \mapsto cor\}$ 
    act5:  $PCxA1 := PCxA1 \cup \{perm \mapsto cio\}$ 
    act6:  $PDA := PDA \cup \{perm \mapsto GLOBAL\_DEADLINE\}$ 
  end
Event Assign_Resource_to_View  $\langle \text{ordinary} \rangle \triangleq$ 
extends Assign_Resource_to_View
  any
    r
    vio
  where
    grd1:  $r \in RESOURCE \wedge vio \in ViO1$ 
    grd2:  $r \mapsto vio \notin RV1$ 
  then
    act1:  $RV1 := RV1 \cup \{r \mapsto vio\}$ 
  end
Event Assign_View_to_Organization  $\langle \text{ordinary} \rangle \triangleq$ 
extends Assign_View_to_Organization
  any
    v
    org
  where
    grd1:  $v \in VIEW \wedge org \in ORG$ 
    grd2:  $v \mapsto org \notin ViO1$ 
    grd3:  $v \mapsto org \notin ran(RV1)$ 
    grd4:  $v \mapsto org \notin ran(AV1)$ 

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    then
      act1:  $ViO1 := ViO1 \cup \{v \mapsto org\}$ 
    end
  Event Assign_activity_to_Organization  $\langle ordinary \rangle \hat{=}$ 
  extends Assign_activity_to_Organization
  any
    a
    org
  where
    grd1:  $a \in ACTIVITY \wedge org \in ORG$ 
    grd2:  $a \mapsto org \notin AiO1$ 
    grd3:  $a \mapsto org \notin ran(AA1)$ 
  then
    act1:  $AiO1 := AiO1 \cup \{a \mapsto org\}$ 
  end
  Event Assign_Action_to_Activity  $\langle ordinary \rangle \hat{=}$ 
  extends Assign_Action_to_Activity
  any
    a
    aio
    vio
  where
    grd1:  $a \in ACTION \wedge aio \in AiO1 \wedge vio \in ViO1$ 
    grd2:  $a \mapsto aio \notin AA1 \wedge a \mapsto vio \notin AV1$ 
  then
    act1:  $AA1 := AA1 \cup \{a \mapsto aio\}$ 
    act2:  $AV1 := AV1 \cup \{a \mapsto vio\}$ 
  end
  Event Assign_Context_to_Organization  $\langle ordinary \rangle \hat{=}$ 
  extends Assign_Context_to_Organization
  any
    org
    c
  where
    grd1:  $org \in ORG \wedge c \in CONTEXT$ 
    grd2:  $c \mapsto org \notin CiO1$ 
  then
    act1:  $CiO1 := CiO1 \cup \{c \mapsto org\}$ 
  end
  Event Request_Access  $\langle ordinary \rangle \hat{=}$ 
  refines Request_Access
  any
    e
    a
    o
    t
    dist
    ac
    d
  where
    grd1:  $e \in EMPLOYEE \wedge a \in ACTION \wedge o \in RESOURCE \wedge t \in \mathbb{N}_1$ 
    grd3:  $dist \in ran(PDistA)$ 
    grd8:  $ac \in CONTEXT$ 
    grd6:  $d \in \mathbb{N}$ 
    grd4:  $\forall e1, a1, o1, t1, dl, d1, ctx. t1 \mapsto e1 \mapsto a1 \mapsto o1 \mapsto dl \mapsto d1 \mapsto ctx \in Access\_Requested \Rightarrow t > t1$ 
    grd2:  $\exists u, r, v, p, org, act, c, rio, aio, vio, cio, acio. e \mapsto u \in EA \wedge u \mapsto org \in OU \wedge rio = (r \mapsto org) \wedge rio \in RiO \wedge u \mapsto rio \in UR \wedge p \mapsto rio \in PRA \wedge vio = (v \mapsto org) \wedge vio \in ViO \wedge o \mapsto vio \in RV \wedge (p \mapsto vio) \in PVA \wedge aio = (act \mapsto org) \wedge (p \mapsto aio) \in PAA \wedge a \mapsto vio \in AV \wedge (a \mapsto aio) \in AA \wedge cio = (c \mapsto org) \wedge (p \mapsto cio) \in PCxA \wedge (p \mapsto dist) \in PDistA \wedge acio = (ac \mapsto org) \wedge (p \mapsto acio) \in PAcA \wedge (p \mapsto d) \in PDA$ 

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    grd7:  $dist \in \text{ran}(P\text{Dist}A)$ 
    grd5:  $t > \text{time}$ 
  then
    act1:  $\text{Access\_Requested} := \text{Access\_Requested} \cup \{t \mapsto e \mapsto a \mapsto o \mapsto d \mapsto dist \mapsto ac\}$ 
    act2:  $at := at \cup \{t\}$ 
  end
Event Treat_Request  $\langle \text{ordinary} \rangle \hat{=}$ 
refines Treat_Request
any
  r
  s
  t
  dec
where
  grd1:  $r \in \text{Access\_Requested} \wedge t \in \mathbb{N}_1$ 
  grd8:  $dec \in 0 \dots 1$ 
  grd3:  $\forall t1, s1, dec1. t1 \mapsto r \mapsto s1 \mapsto dec1 \in \text{Request\_Treated} \Rightarrow t > t1 \wedge s1 \neq s$ 
    approve once per approver
  grd4:  $\forall u, u1, t1, s1, dec1. s \mapsto u \in EA \wedge s1 \mapsto u1 \in EA \wedge t1 < t \wedge t1 \mapsto r \mapsto s1 \mapsto dec1 \in$ 
    Request_Treated  $\Rightarrow u \neq u1$ 
    approve once per unit
  grd5:  $\forall e, a, o, t0, dist, d, ac. r = t0 \mapsto e \mapsto a \mapsto o \mapsto d \mapsto dist \mapsto ac \Rightarrow EA(s) \in \text{PATH}[\{EA(e)\}]$ 
  grd6:  $\forall e, a, o, t0, dist, d, ac. r = t0 \mapsto e \mapsto a \mapsto o \mapsto d \mapsto dist \mapsto ac \Rightarrow \text{height}(EA(e)) -$ 
    height( $EA(s)$ )  $\leq dist$ 
  grd7:  $\forall e, a, o, t0, dist, d, ac, current. r = t0 \mapsto e \mapsto a \mapsto o \mapsto d \mapsto dist \mapsto ac \wedge current =$ 
    card( $\{tr, t1, s1, dec1. tr = t1 \mapsto r \mapsto s1 \mapsto dec1 \wedge tr \in \text{Request\_Treated} | tr\}$ )  $\Rightarrow t \leq \max(\{t0\} \cup$ 
     $\{t1, s1, dec1. t1 \mapsto r \mapsto s1 \mapsto dec1 \in \text{Request\_Treated} | t1\}) + (\text{height}(EA(e)) - \text{height}(EA(s)) -$ 
    current)  $* d$ 
  grd9:  $\forall e, a, o, t0, dist, d, ac. r = t0 \mapsto e \mapsto a \mapsto o \mapsto d \mapsto dist \mapsto ac \Rightarrow \text{isTrue}(ac) = \text{TRUE}$ 
  then
    act1:  $\text{Request\_Treated} := \text{Request\_Treated} \cup \{t \mapsto r \mapsto s \mapsto dec\}$ 
    act2:  $at := at \setminus \{time\}$ 
  end
Event Execute_Request  $\langle \text{ordinary} \rangle \hat{=}$ 
any
  r
  t
where
  grd1:  $r \in \text{Access\_Requested}$ 
  grd2:  $r \notin \text{dom}(\text{Final\_Decision})$ 
  grd4:  $t \in \mathbb{N}$ 
  grd3:  $\forall e, a, o, t0, dist, d, total, last, ac. r = t0 \mapsto e \mapsto a \mapsto o \mapsto d \mapsto dist \mapsto ac \wedge total =$ 
    card( $\{tr, t1, s1, dec. tr = t1 \mapsto r \mapsto s1 \mapsto dec \wedge tr \in \text{Request\_Treated} | tr\}$ )  $\wedge last = \max(\{t0\} \cup$ 
     $\{t1, s1, dec. t1 \mapsto r \mapsto s1 \mapsto dec \in \text{Request\_Treated} | t1\}) \Rightarrow (dist = total \wedge t = last) \vee (t =$ 
    last + (dist - total)  $* d \wedge time \geq t)$ 
  then
    act1:  $\text{Final\_Decision}(r) := \max(\{0\} \cup \{last, s, dec. last = \max(\{t1, s1, dec1. t1 \mapsto r \mapsto s1 \mapsto dec1 \in$ 
    Request_Treated  $| t1\}) \wedge last \mapsto r \mapsto s \mapsto dec \in \text{Request\_Treated} | dec\})$ 
    act2:  $\text{Processing\_Time}(r) := t$ 
  end
Event tick_tock  $\langle \text{ordinary} \rangle \hat{=}$ 
extends tick_tock
any
  tm
where
  grd1:  $tm \in \mathbb{N} \wedge tm > \text{time} \wedge (at \neq \emptyset \Rightarrow tm \leq \min(at))$ 
  then
    act1:  $\text{time} := tm$ 
  end
end

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Event Assign_Approval_Deadline  $\langle \text{ordinary} \rangle \hat{=}$ 
refines Assign_Approval_Deadline
  any
    p
    d
  where
    grd1:  $p \in \text{PERMISSION} \wedge d \in \mathbb{N}$ 
    grd2:  $p \mapsto d \notin PDA$ 
  then
    act1:  $PDA := PDA \Leftarrow \{p \mapsto d\}$ 
  end
Event Assign_approval_perimeter  $\langle \text{ordinary} \rangle \hat{=}$ 
  any
    dist
    perm
  where
    grd1:  $perm \mapsto dist \notin PDistA$ 
  then
    act1:  $PDistA := PDistA \cup \{perm \mapsto dist\}$ 
  end
Event Assign_Approval_Context  $\langle \text{ordinary} \rangle \hat{=}$ 
  any
    c
    p
  where
    grd1:  $p \mapsto c \notin PAcA1$ 
    grd2:  $c \in CiO1$ 
  then
    act1:  $PAcA1 := PAcA1 \cup \{p \mapsto c\}$ 
  end
END

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