

## Answers to problems set 1.1: P12-15(12, 28, 36)

Please look up questions from the textbook.

**12.**

- a.  $p \rightarrow q$  : If you have the flu, then you miss the final examination.
- b.  $\neg q \leftrightarrow r$  : You don't miss the final examination if and only if you pass the course.
- c.  $q \rightarrow \neg r$  : If you miss the final examination, then you do not pass the course.
- d.  $p \vee q \vee r$  : You have the flu or you miss the final examination or you pass the course.
- e.  $(p \rightarrow \neg r) \vee (q \rightarrow \neg r)$  : If you have the flu, then you do not pass the course or if you miss the final examination, then you do not pass the course.
- f.  $(p \wedge q) \vee (\neg q \wedge r)$  : You have the flu and you miss the final examination or you don't miss the final examination and you pass the course.

**28.**

A) Proposition: **If it snows tonight, then I will stay at home**

**converse**: If I stay at home then it snows tonight

**inverse**: If it doesn't snow tonight then I will not stay at home

**contrapositive**: If I will not stay at home, then it doesn't snow tonight

B) Proposition: **I go to the beach whenever it is sunny summer day**

**converse**: If it sunny summer day, then I go to the beach

**inverse**: If I do not go the beach, then it is not sunny summer day

**contrapositive**: If it is not sunny summer day, then I do not go to the beach

C) Proposition: **When I stay up late, it is necessary that I sleep until noon**

**converse**: If I sleep until noon, then I stay up late

**inverse**: If I do not stay up late, then it is not necessary that I sleep until noon

**contrapositive**: If it is not necessary that I sleep until noon, then I do not stay up late

**36.**

A)  $(p \vee q) \vee r$

$p$	$q$	$r$	$p \vee q$	$(p \vee q) \vee r$
T	T	T	T	T
T	T	F	T	T
T	F	T	T	T
T	F	F	T	T

<b>F</b>	<b>T</b>	<b>T</b>	<b>T</b>	<b>T</b>
<b>F</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>T</b>
<b>F</b>	<b>F</b>	<b>T</b>	<b>F</b>	<b>T</b>
<b>F</b>	<b>F</b>	<b>F</b>	<b>F</b>	<b>F</b>

B)  $(p \vee q) \wedge r$

$p$	$q$	$r$	$p \vee q$	$(p \vee q) \wedge r$
<b>T</b>	<b>T</b>	<b>T</b>	<b>T</b>	<b>T</b>
<b>T</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>F</b>
<b>T</b>	<b>F</b>	<b>T</b>	<b>T</b>	<b>T</b>
<b>T</b>	<b>F</b>	<b>F</b>	<b>T</b>	<b>F</b>
<b>F</b>	<b>T</b>	<b>T</b>	<b>T</b>	<b>T</b>
<b>F</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>F</b>
<b>F</b>	<b>F</b>	<b>T</b>	<b>F</b>	<b>F</b>
<b>F</b>	<b>F</b>	<b>F</b>	<b>F</b>	<b>F</b>

C)  $(p \wedge q) \vee r$

$p$	$q$	$r$	$p \wedge q$	$(p \wedge q) \vee r$
<b>T</b>	<b>T</b>	<b>T</b>	<b>T</b>	<b>T</b>
<b>T</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>T</b>
<b>T</b>	<b>F</b>	<b>T</b>	<b>F</b>	<b>T</b>
<b>T</b>	<b>F</b>	<b>F</b>	<b>F</b>	<b>F</b>
<b>F</b>	<b>T</b>	<b>T</b>	<b>F</b>	<b>T</b>
<b>F</b>	<b>T</b>	<b>F</b>	<b>F</b>	<b>F</b>

<b>F</b>	<b>F</b>	<b>T</b>	<b>F</b>	<b>T</b>
<b>F</b>	<b>F</b>	<b>F</b>	<b>F</b>	<b>F</b>

D)  $(p \wedge q) \wedge r$

$p$	$q$	$r$	$p \wedge q$	$(p \wedge q) \wedge r$
<b>T</b>	<b>T</b>	<b>T</b>	<b>T</b>	<b>T</b>
<b>T</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>F</b>
<b>T</b>	<b>F</b>	<b>T</b>	<b>F</b>	<b>F</b>
<b>T</b>	<b>F</b>	<b>F</b>	<b>F</b>	<b>F</b>
<b>F</b>	<b>T</b>	<b>T</b>	<b>F</b>	<b>F</b>
<b>F</b>	<b>T</b>	<b>F</b>	<b>F</b>	<b>F</b>
<b>F</b>	<b>F</b>	<b>T</b>	<b>F</b>	<b>F</b>
<b>F</b>	<b>F</b>	<b>F</b>	<b>F</b>	<b>F</b>

E)  $(p \vee q) \wedge \neg r$

$p$	$q$	$r$	$\neg r$	$p \vee q$	$(p \vee q) \wedge \neg r$
<b>T</b>	<b>T</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>F</b>
<b>T</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>T</b>	<b>T</b>
<b>T</b>	<b>F</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>F</b>
<b>T</b>	<b>F</b>	<b>F</b>	<b>T</b>	<b>T</b>	<b>T</b>
<b>F</b>	<b>T</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>F</b>
<b>F</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>T</b>	<b>T</b>
<b>F</b>	<b>F</b>	<b>T</b>	<b>F</b>	<b>F</b>	<b>F</b>
<b>F</b>	<b>F</b>	<b>F</b>	<b>T</b>	<b>F</b>	<b>F</b>

F)  $(p \wedge q) \vee \neg r$

$p$	$q$	$r$	$\neg r$	$p \wedge q$	$(p \wedge q) \vee \neg r$
T	T	T	F	T	T
T	T	F	T	T	T
T	F	T	F	F	F
T	F	F	T	F	T
F	T	T	F	F	F
F	T	F	T	F	T
F	F	T	F	F	F
F	F	F	T	F	T