Chapter 5

Large and Fast: Exploiting Memory Hierarchy

Memory Technology

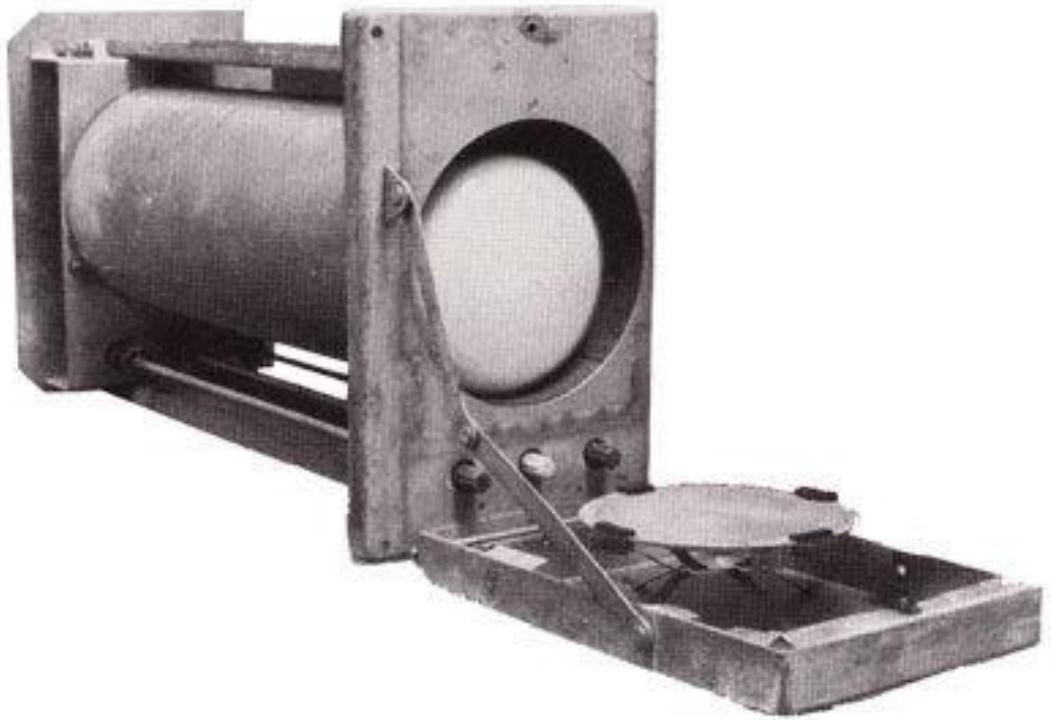
- Static RAM (SRAM)
  - 0.5ns – 2.5ns, $2000 – $5000 per GB
- Dynamic RAM (DRAM)
  - 50ns – 70ns, $20 – $75 per GB
- Magnetic disk
  - 5ms – 20ms, $0.20 – $2 per GB
- Ideal memory
  - Access time of SRAM
  - Capacity and cost/GB of disk

大約100倍時間

萬般不得已的事==>速度太慢

Memory Technology

- IBM 701 adopted 72 3-inch **Williams-Kilburn tubes** to realize 2048 36-bit words.



Principle of Locality

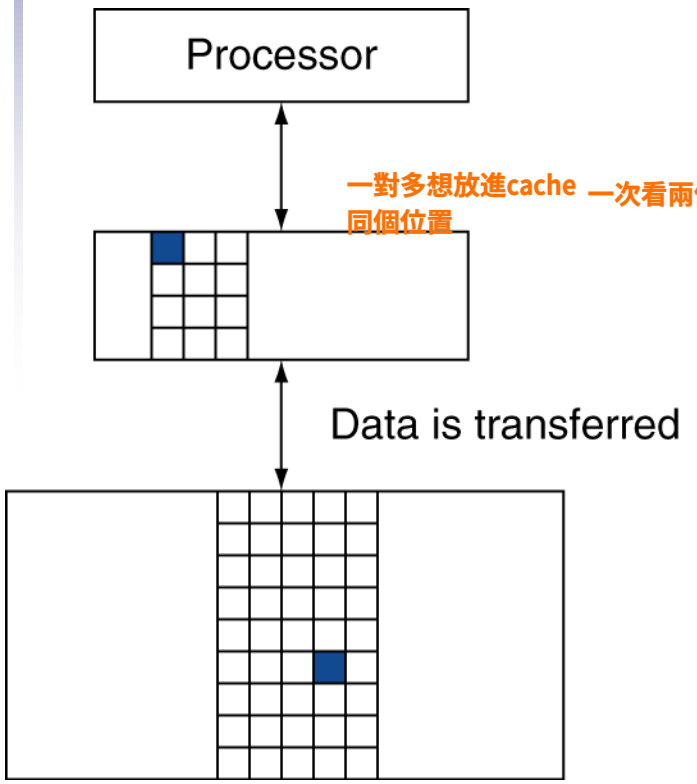
- Programs access a small proportion of their address space at any time
- Temporal locality
  - Items accessed recently are likely to be accessed again soon
  - e.g., instructions in a loop, induction variables
- Spatial locality
  - Items near those accessed recently are likely to be accessed soon
  - E.g., sequential instruction access, array data

Taking Advantage of Locality

- Memory hierarchy
- Store everything on disk
- Copy recently accessed (and nearby) items from disk to smaller DRAM memory
  - Main memory
- Copy more recently accessed (and nearby) items from DRAM to smaller SRAM memory
  - Cache memory attached to CPU

disk-->Dram-->cache

Memory Hierarchy Levels

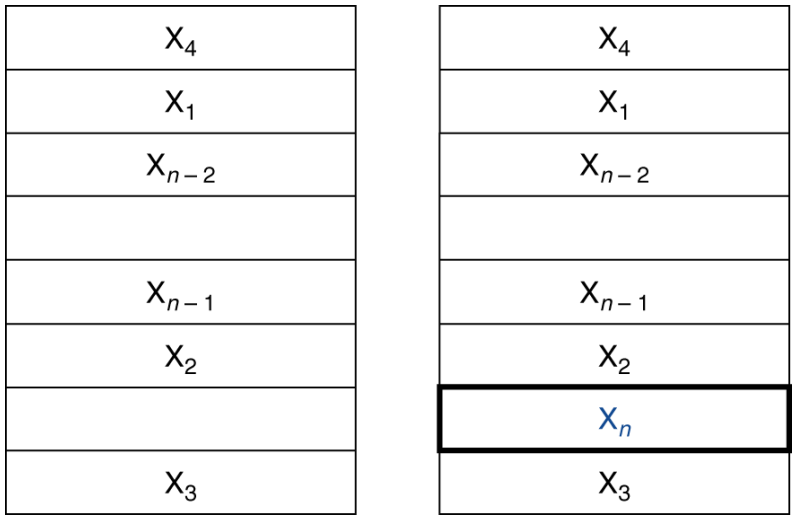


- Block (aka line): unit of copying
  - May be multiple words
- If accessed data is present in upper level
  - Hit: access satisfied by upper level
    - Hit ratio: hits/accesses
- If accessed data is absent
  - Miss: block copied from lower level
    - Time taken: miss penalty
    - Miss ratio: misses/accesses = 1 – hit ratio
  - Then accessed data supplied from upper level

發生在DRam

Cache Memory

- Cache memory
  - The level of the memory hierarchy closest to the CPU
- Given accesses X_1, …, X_{n-1}, X_n



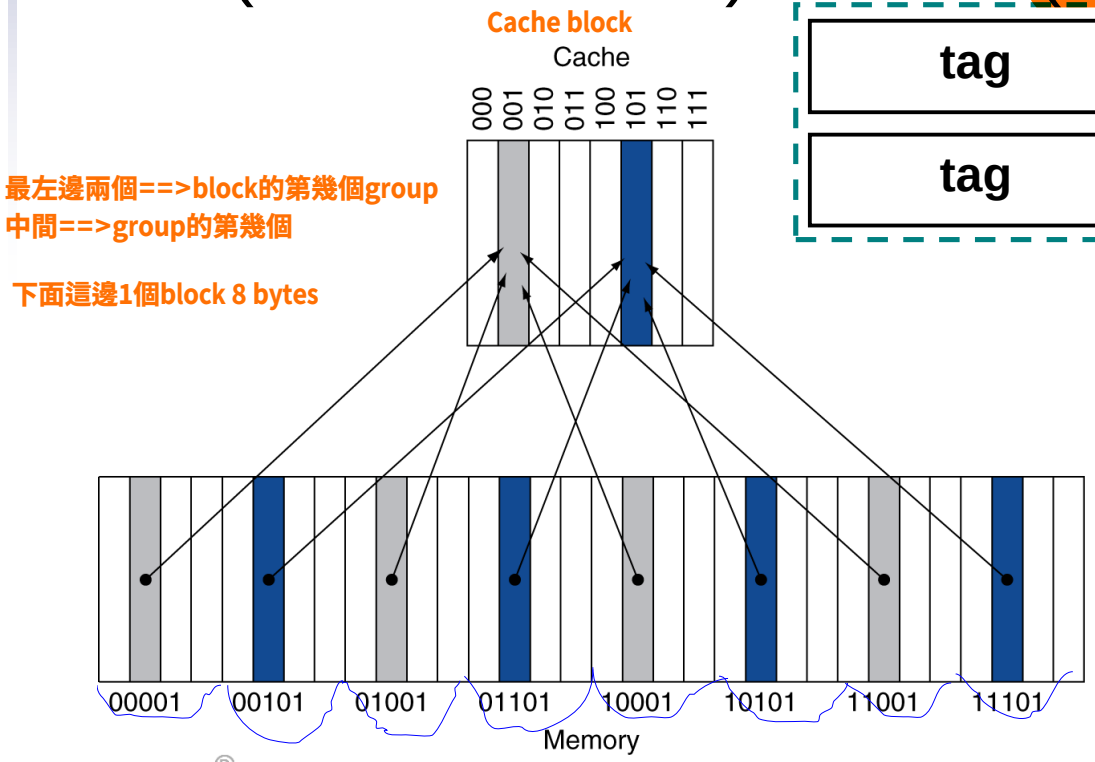
a. Before the reference to X_n b. After the reference to X_n

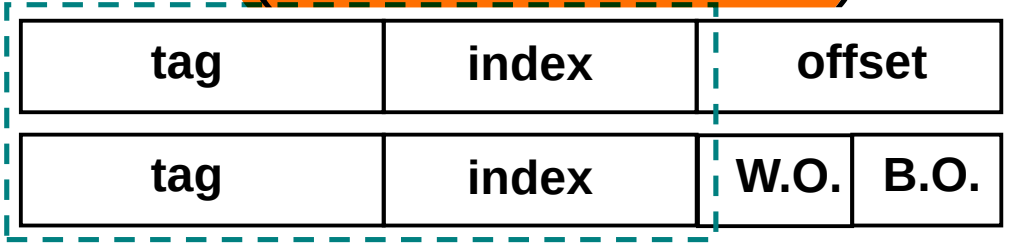
- How do we know if the data is present?
- Where do we look?

Direct Mapped Cache

- Location determined by address
- Direct mapped: only one choice
  - (Block address) modulo (#Blocks in cache)

00->01-->10-->11
word中第幾個byte





- #Blocks is a power of 2
- Use low-order address bits

Tags and Valid Bits

- How do we know which particular block is stored in a cache location?
  - Store block address as well as the data
  - Actually, only need the high-order bits
  - Called the tag
- What if there is no data in a location?
  - Valid bit: 1 = present, 0 = not present
  - Initially 0

Cache Example

- 8-blocks, 1 word/block, direct mapped
- Initial state

Index	V	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	N		
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
22	10 110	Miss	110

Index	V	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	**Y**	**10**	**Mem[10110]**
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
26	11 010	Miss	010

Index	V	Tag	Data
000	N		
001	N		
010	**Y**	**11**	**Mem[11010]**
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
22	10 110	Hit	110
26	11 010	Hit	010

Index	V	Tag	Data
000	N		
001	N		
010	Y	11	Mem[11010]
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
16	10 000	Miss	000
3	00 011	Miss	011
16	10 000	Hit	000

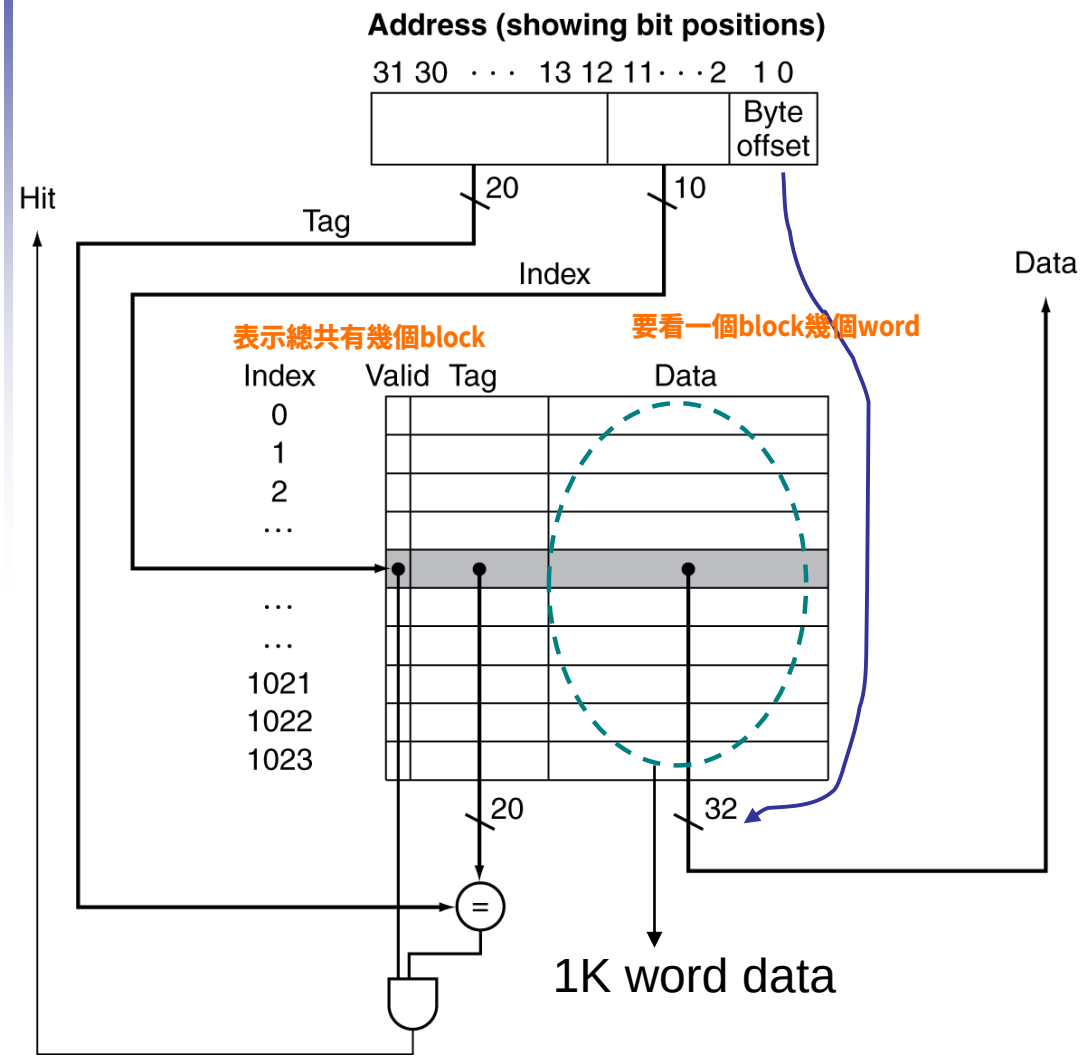
Index	V	Tag	Data
000	Y	10	Mem[10000]
001	N		
010	Y	11	Mem[11010]
011	Y	00	Mem[00011]
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
18	10 010	Miss	010

Index	V	Tag	Data
000	Y	10	Mem[10000]
001	N		
010	**Y**	**10** ← 11	**Mem[10010]**
011	Y	00	Mem[00011]
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Address Subdivision



- 32-bit byte address, a direct-mapped cache, cache size 2^n blocks, block data size 2^m words (2^{m+2} bytes)
  - Tag size: 32 – (n+m+2)
  - Total number of bits:

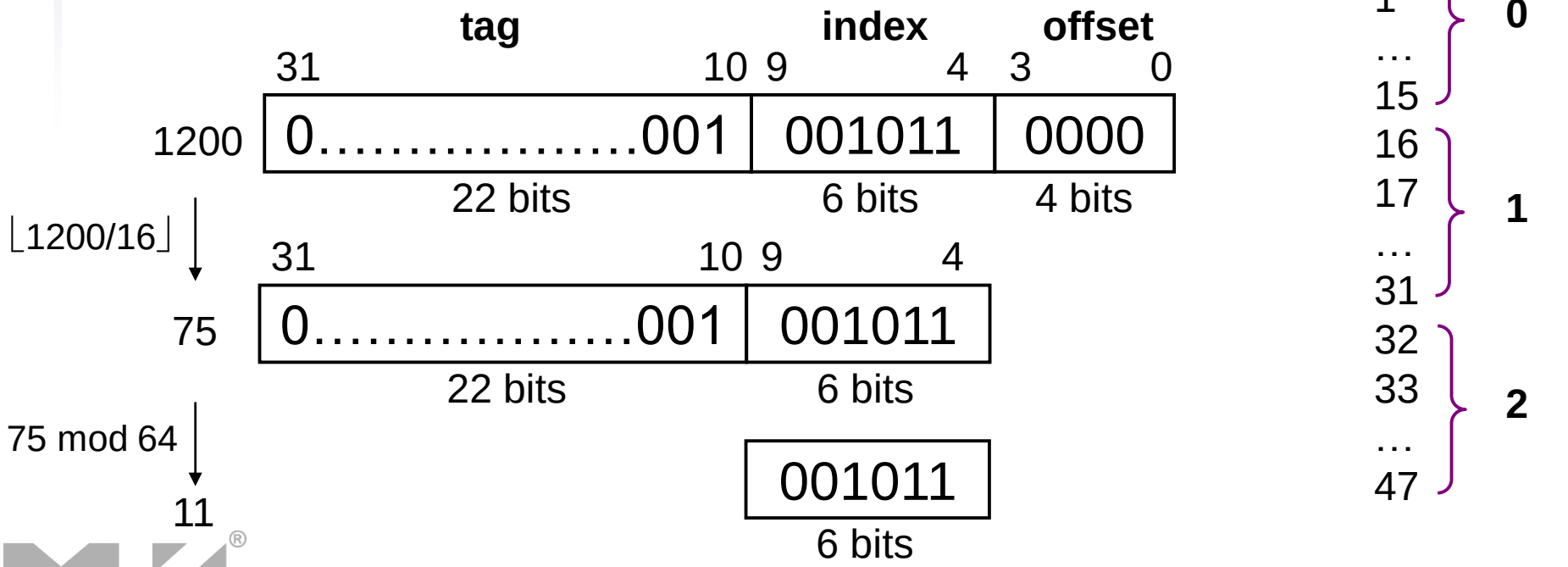
$$2^n \times (2^m \times 32 + (32 - n - m - 2) + 1) =$$
$$2^n \times (2^m \times 32 + 31 - n - m)$$

- 16KB data, 4-word blocks, assume a 32-bit address

$$2^{10} \times (4 \times 32 + (32 - 10 - 2 - 2) + 1) =$$
$$2^{10} \times 147 = 147 Kbits$$

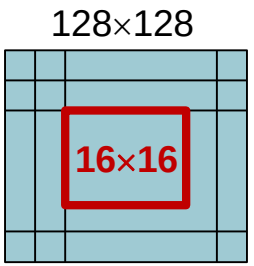
Example: Larger Block Size

- 64 blocks, 16 bytes/block
  - To what block number does address 1200 map?
- Block address = ⌊1200/16⌋ = 75
- Block number = 75 modulo 64 = 11



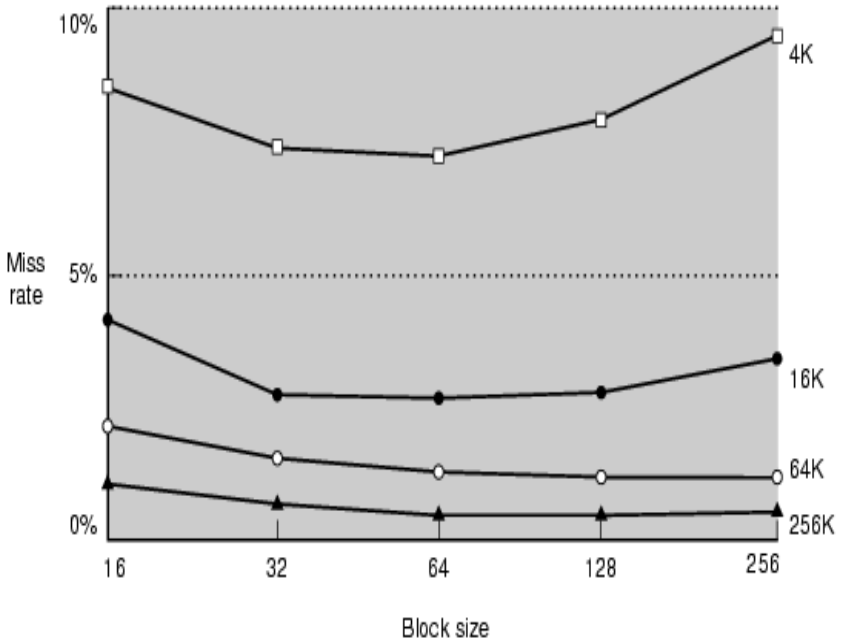
Block Size Considerations

- Larger blocks should reduce miss rate
  - Due to spatial locality
- But in a fixed-sized cache
  - Larger blocks ⇒ fewer of them
    - More competition ⇒ increased miss rate
    - e.g. 8 larger blocks vs. 16 smaller blocks
  - Larger blocks ⇒ pollution
- Larger miss penalty
  - Can override benefit of reduced miss rate
  - Early restart and critical-word-first can help



Cache Misses

- On cache hit, CPU proceeds normally
- On cache miss
  - Stall the CPU pipeline
  - Fetch block from next level of hierarchy
  - Instruction cache miss
    - Restart instruction fetch
  - Data cache miss
    - Complete data access



Write-Through

- On data-write hit, could just update the block in cache
  - But then cache and memory would be inconsistent
- Write through: also update memory
- But makes writes take longer
  - e.g., if base CPI = 1, 10% of instructions are stores, write to memory takes 100 cycles
    - Effective CPI = 1 + 0.1×100 = 11
- Solution: write buffer
  - Holds data waiting to be written to memory
  - CPU continues immediately
    - Only stalls on write if write buffer is already full

Write-Back

- Alternative: On data-write hit, just update the block in cache
  - Keep track of whether each block is dirty
- When a dirty block is replaced
  - Write it back to memory

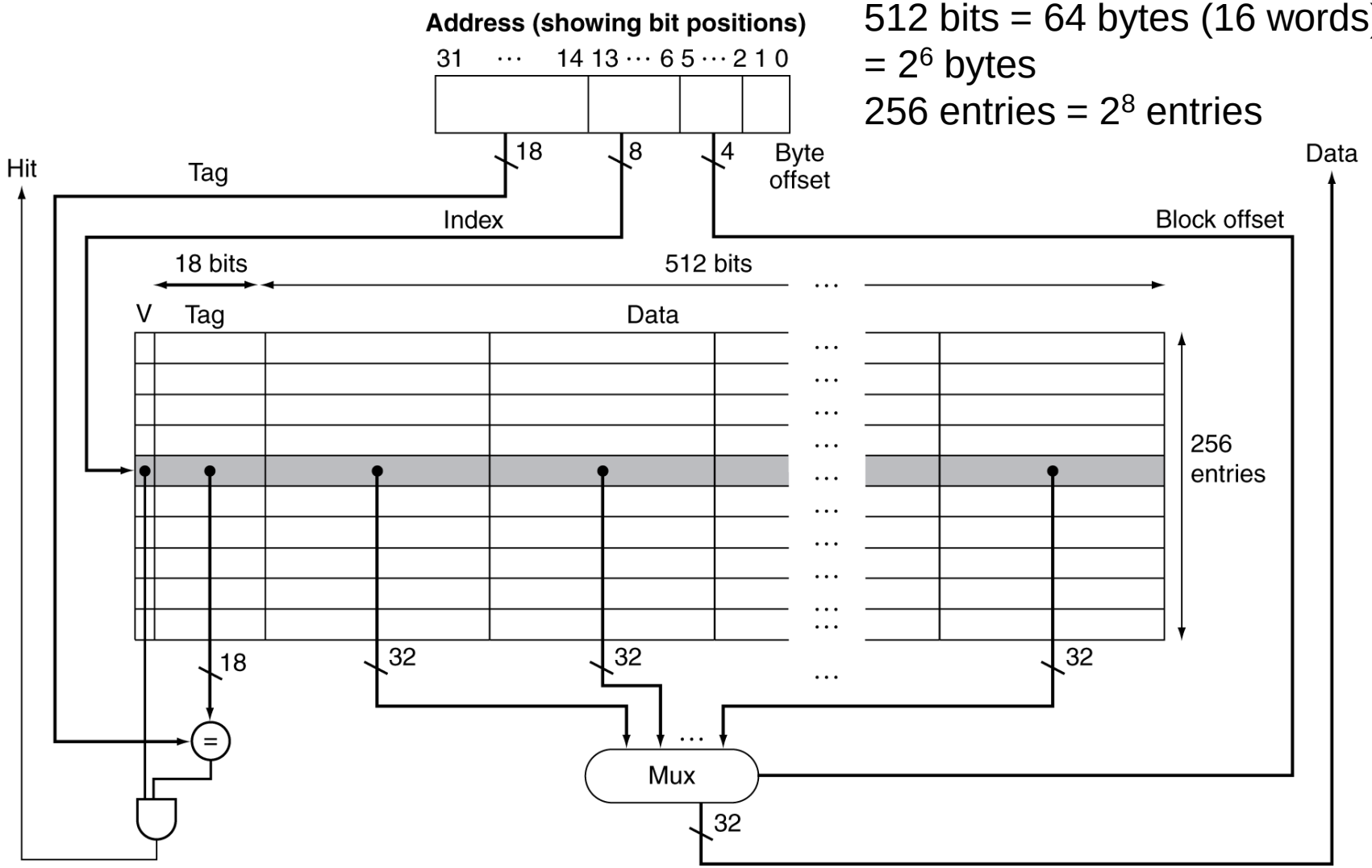
Write Allocation

- What should happen on a write miss?
- For write-through
  - Write around: don't fetch the block and write directly into memory (*write no-allocate*)
  - Allocate on miss: fetch the block into cache (*write allocate*)

Example: Intrinsity FastMATH

- Embedded MIPS processor
  - 12-stage pipeline
  - Instruction and data access on each cycle
- Split cache: separate I-cache and D-cache
  - Each 16KB: 256 blocks × 16 words/block
  - D-cache: write-through or write-back
- SPEC2000 miss rates
  - I-cache: 0.4%
  - D-cache: 11.4%
  - Weighted average: 3.2%

Example: Intrinsity FastMATH

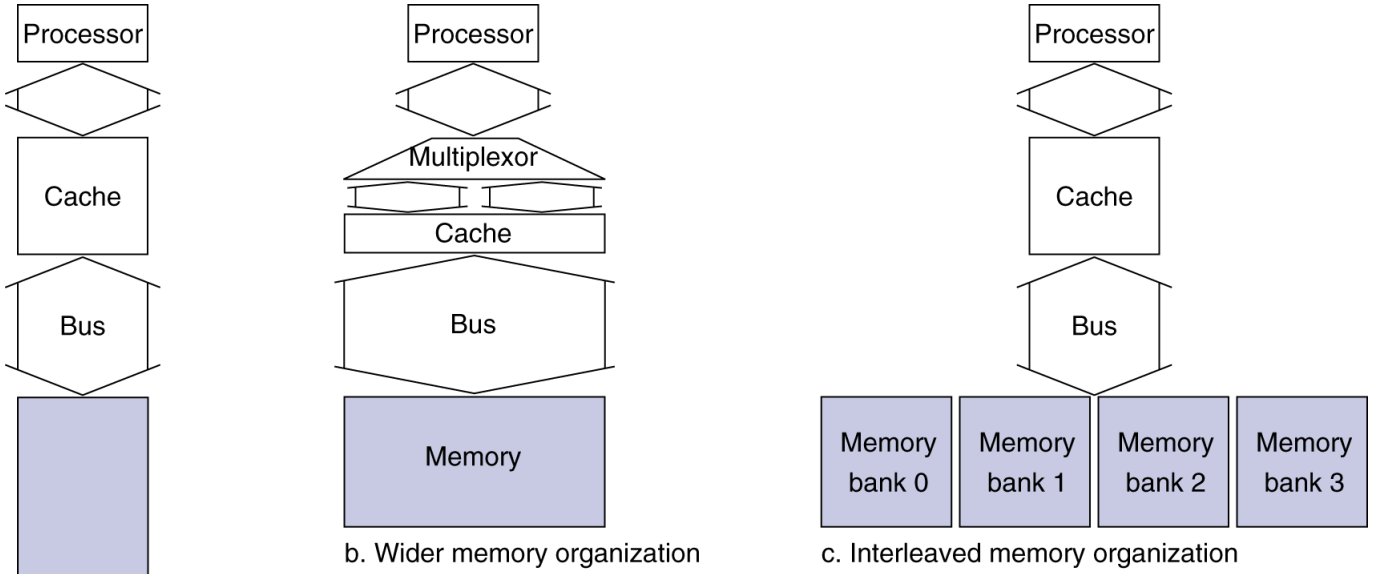


512 bits = 64 bytes (16 words)
= 2^6 bytes
256 entries = 2^8 entries

Main Memory Supporting Caches

- Use DRAMs for main memory
  - Fixed width (e.g., 1 word)
  - Connected by fixed-width clocked bus
    - Bus clock is typically slower than CPU clock
- Example cache block read
  - 1 bus cycle for address transfer
  - 15 bus cycles per DRAM access
  - 1 bus cycle per data transfer
- For 4-word block, 1-word-wide DRAM
  - Miss penalty = 1 + 4×15 + 4×1 = 65 bus cycles
  - Bandwidth = 16 bytes / 65 cycles = 0.25 B/cycle

Increasing Memory Bandwidth



a. One-word-wide memory organization

b. Wider memory organization

c. Interleaved memory organization

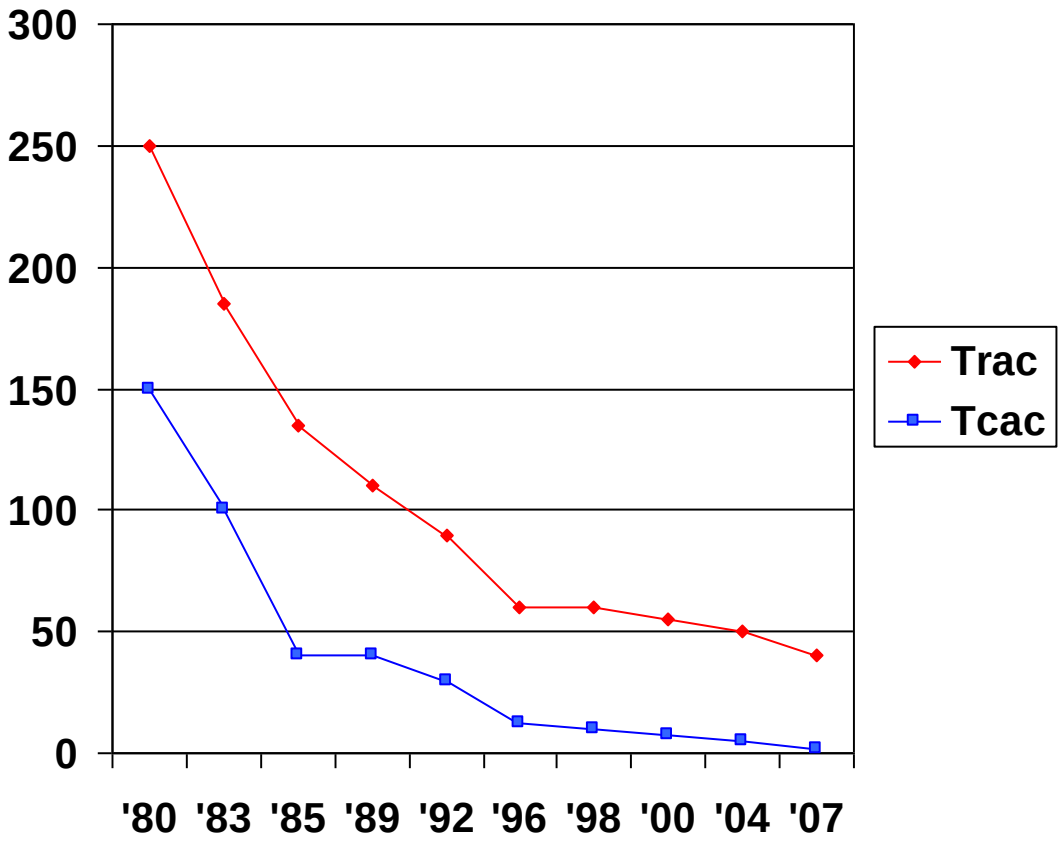
- 4-word wide memory
  - Miss penalty = 1 + 15 + 1 = 17 bus cycles
  - Bandwidth = 16 bytes / 17 cycles = 0.94 B/cycle
- 4-bank interleaved memory
  - Miss penalty = 1 + 15 + 4×1 = 20 bus cycles
  - Bandwidth = 16 bytes / 20 cycles = 0.8 B/cycle

Advanced DRAM Organization

- Bits in a DRAM are organized as a rectangular array
  - DRAM accesses an entire row
  - Burst mode: supply successive words from a row with reduced latency
- Double data rate (DDR) DRAM
  - Transfer on rising and falling clock edges
- Quad data rate (QDR) DRAM
  - Separate DDR inputs and outputs

DRAM Generations

Year	Capacity	$/GB
1980	64Kbit	$1500000
1983	256Kbit	$500000
1985	1Mbit	$200000
1989	4Mbit	$50000
1992	16Mbit	$15000
1996	64Mbit	$10000
1998	128Mbit	$4000
2000	256Mbit	$1000
2004	512Mbit	$250
2007	1Gbit	$50



Measuring Cache Performance

- Components of CPU time
  - Program execution cycles
    - Includes cache hit time
  - Memory stall cycles
    - Mainly from cache misses
- With simplifying assumptions:

$$\text{Memory stall cycles} = \frac{\text{Memory accesses}}{\text{Program}} \times \text{Miss rate} \times \text{Miss penalty}$$

$$= \frac{\text{Instructions}}{\text{Program}} \times \frac{\text{Misses}}{\text{Instruction}} \times \text{Miss penalty}$$

Cache Performance Example

- Given
  - I-cache miss rate = 2%
  - D-cache miss rate = 4%
  - Miss penalty = 100 cycles
  - Base CPI (ideal cache) = 2
  - Load & stores are 36% of instructions
- Miss cycles per instruction
  - I-cache: $0.02 \times 100 = 2$
  - D-cache: $0.36 \times 0.04 \times 100 = 1.44$
- Actual CPI = 2 + 2 + 1.44 = 5.44
  - Ideal CPU is 5.44/2 =2.72 times faster

Average Access Time

- Hit time is also important for performance
- Average memory access time (AMAT)
  - AMAT = Hit time + Miss rate $\times$ Miss penalty
- Example
  - CPU with 1ns clock, hit time = 1 cycle, miss penalty = 20 cycles, cache miss rate = 5%
  - AMAT = 1 + 0.05 $\times$ 20 = 2 *ns*
    - AMAT per instruction – 2 cycles

Performance Summary

- When CPU performance increased
  - Miss penalty becomes more significant
- Decreasing base CPI
  - Greater proportion of time spent on memory stalls
- Increasing clock rate
  - Memory stalls account for more CPU cycles
- Can’t neglect cache behavior when evaluating system performance

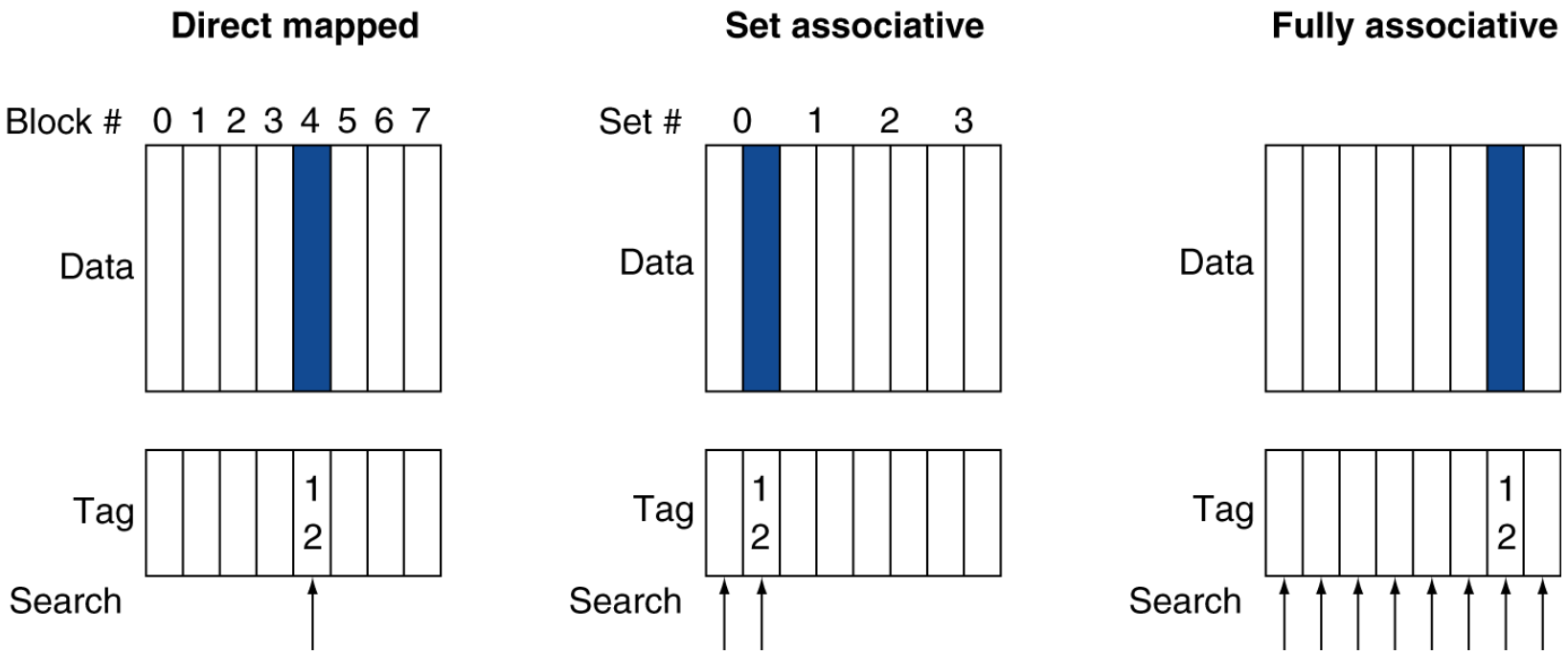
Associative Caches

- Fully associative
  - Allow a given block to go in any cache entry
  - Requires all entries to be searched at once
  - Comparator per entry (expensive)
- *n*-way set associative

同個set可以弄到滿==>降低取代率

  - Each set contains *n* entries
  - Block number determines which set
    - (Block number) modulo (#Sets in cache)
  - Search all entries in a given set at once
  - *n* comparators (less expensive)

Associative Cache Example



Spectrum of Associativity

- For a cache with 8 entries

One-way set associative (direct mapped)

Block	Tag	Data
0		
1		
2		
3		
4		
5		
6		
7		

Two-way set associative

Set	Tag	Data	Tag	Data
0				
1				
2				
3				

Four-way set associative

Set	Tag	Data	Tag	Data	Tag	Data	Tag	Data
0								
1								

Eight-way set associative (fully associative)

Tag	Data	Tag	Data	Tag	Data	Tag	Data	Tag	Data	Tag	Data	Tag	Data	Tag	Data

Associativity Example

- Compare 4-block caches
  - Direct mapped, 2-way set associative, fully associative
  - Block access sequence: 0, 8, 0, 6, 8
- Direct mapped

Block address	Cache index	Hit/miss	Cache content after access			
			0	1	2	3
0	0	miss	**Mem[0]**			
8	0	miss	**Mem[8]**			
0	0	miss	**Mem[0]**			
6	2	miss	Mem[0]		**Mem[6]**	
8	0	miss	**Mem[8]**		Mem[6]	

Associativity Example

- 2-way set associative

Block address	Cache index	Hit/miss	Cache content after access			
			Set 0		Set 1	
0	0	miss	**Mem[0]**			
8	0	miss	Mem[0]	**Mem[8]**		
0	0	hit	**Mem[0]**	Mem[8]		
6	0	miss	Mem[0]	**Mem[6]**		
8	0	miss	**Mem[8]**	Mem[6]		

0刚被access

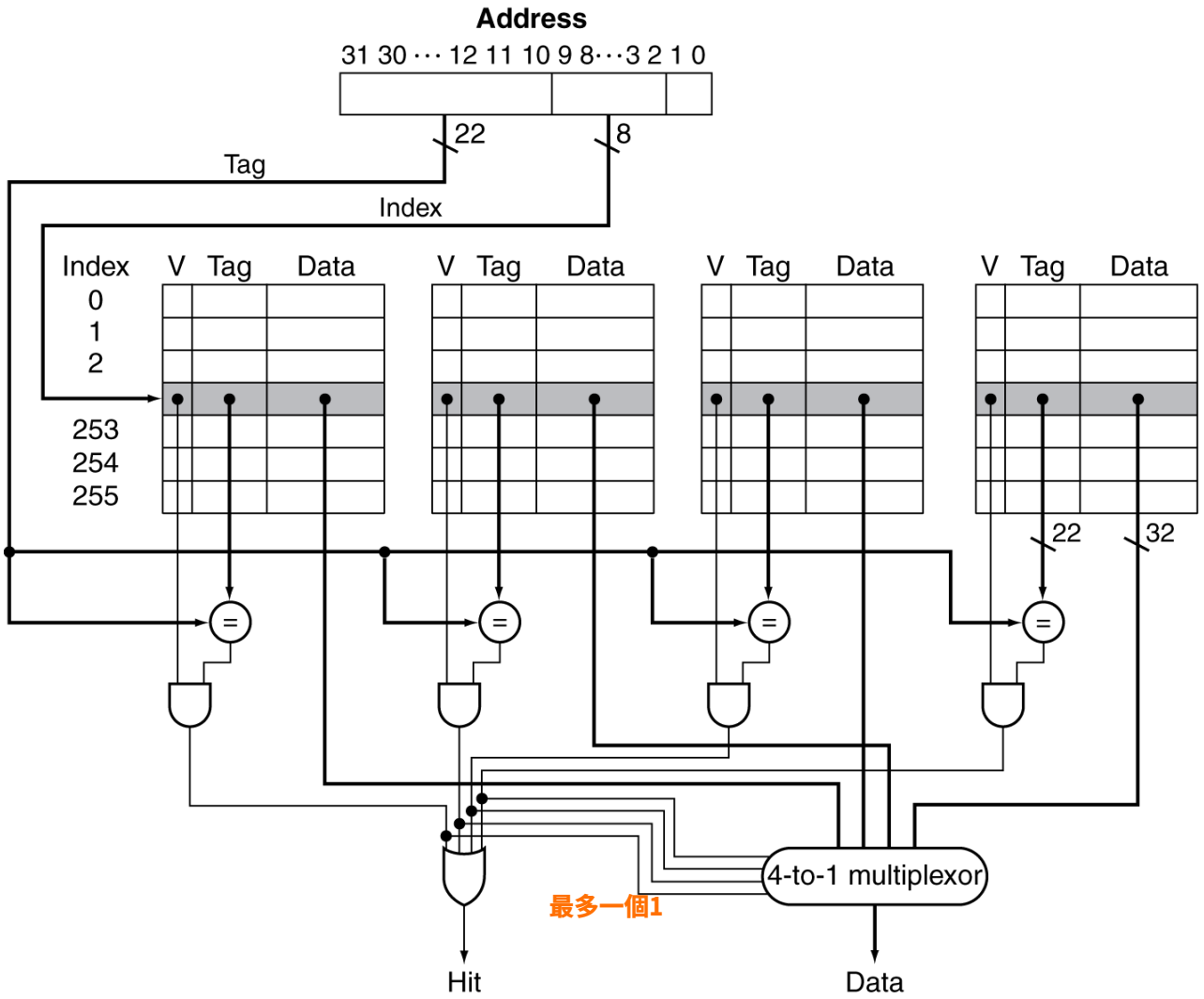
- Fully associative

Block address		Hit/miss	Cache content after access			
0		miss	**Mem[0]**			
8		miss	Mem[0]	**Mem[8]**		
0		hit	**Mem[0]**	Mem[8]		
6		miss	Mem[0]	Mem[8]	**Mem[6]**	
8		hit	Mem[0]	**Mem[8]**	Mem[6]	

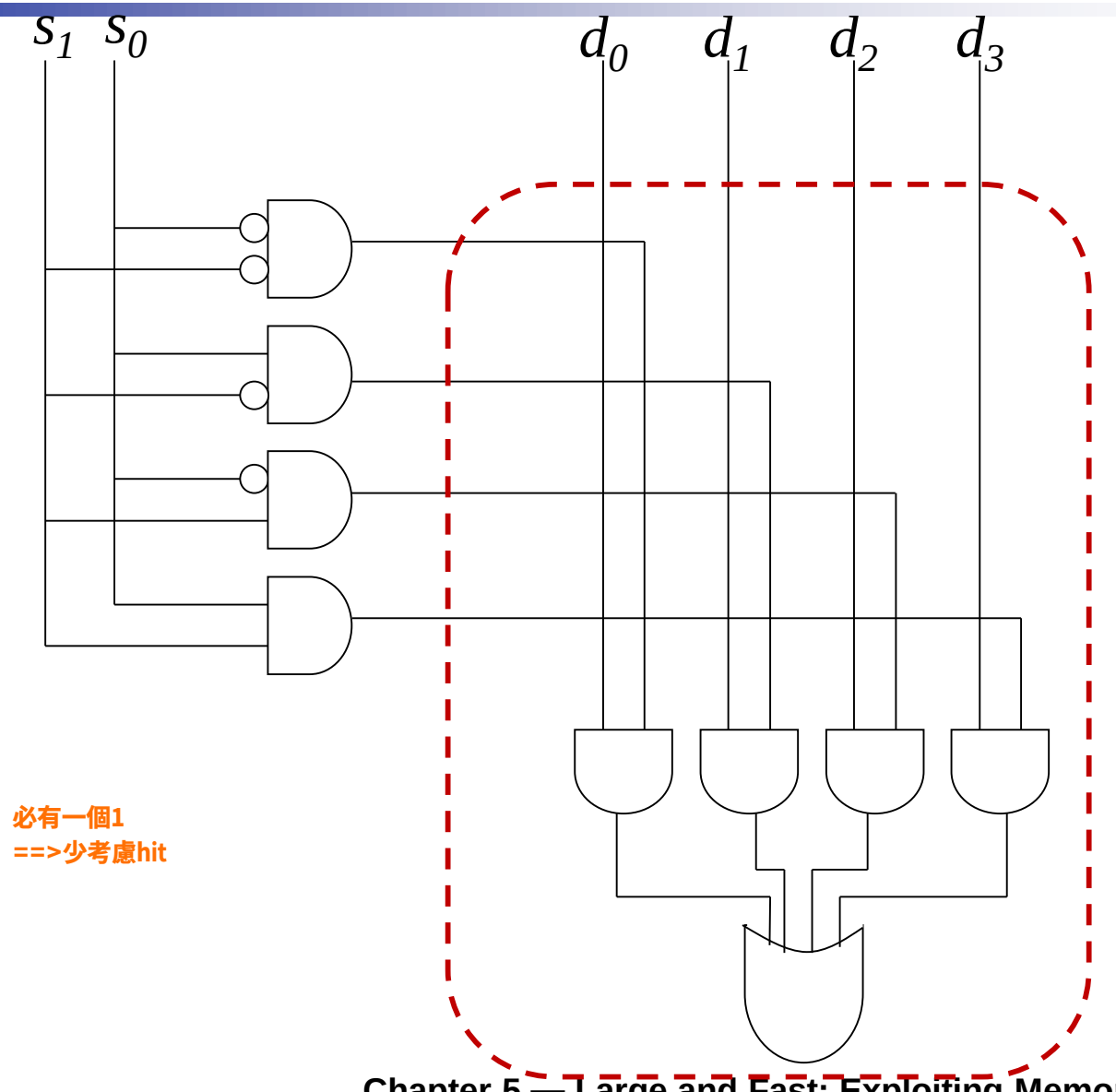
How Much Associativity

- Increased associativity decreases miss rate
  - But with diminishing returns
- Simulation of a system with 64KB D-cache, 16-word blocks, SPEC2000
  - 1-way: 10.3%
  - 2-way: 8.6%
  - 4-way: 8.3%
  - 8-way: 8.1%

Set Associative Cache Organization



4-1 Multiplexer



必有一個1
==>少考慮hit

Replacement Policy

- Direct mapped: no choice
- Set associative
  - Prefer non-valid entry, if there is one
  - Otherwise, choose among entries in the set
- Least-recently used (LRU)
  - Choose the one unused for the longest time
    - Simple for 2-way, manageable for 4-way, too hard beyond that
- Random
  - Gives approximately the same performance as LRU for high associativity

Multilevel Caches

- Primary cache attached to CPU
  - Small, but fast
- Level-2 cache services misses from primary cache
  - Larger, slower, but still faster than main memory
- Main memory services L-2 cache misses
- Some high-end systems include L-3 cache

Multilevel Cache Example

- Given
  - CPU base CPI = 1, clock rate = 4GHz
  - Miss rate/instruction = 2%
  - Main memory access time = 100ns
- With just primary cache
  - Miss penalty = 100ns/0.25ns = 400 cycles
  - Effective CPI = 1 + 0.02 × 400 = 9

Example (cont.)

- Now add L-2 cache
  - Access time = 5ns
  - Global miss rate to main memory = 0.5%
- Primary miss with L-2 hit
  - Penalty = 5ns/0.25ns = 20 cycles
- Primary miss with L-2 miss
  - Extra penalty = 400 cycles
- CPI = 1 + 0.02 × 20 + 0.005 × 400 = 3.4
- Performance ratio = 9/3.4 = 2.6

Multilevel Cache Considerations

- Primary cache
  - Focus on minimal hit time
- L-2 cache
  - Focus on low miss rate to avoid main memory access
  - Hit time has less overall impact
- Results

Hit time要小

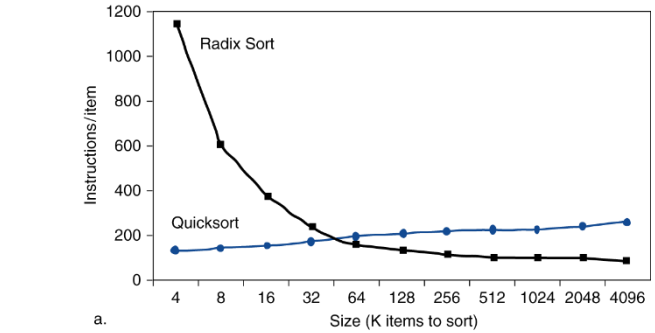
  - L-1 cache usually smaller than a single cache
  - L-1 block size smaller than L-2 block size

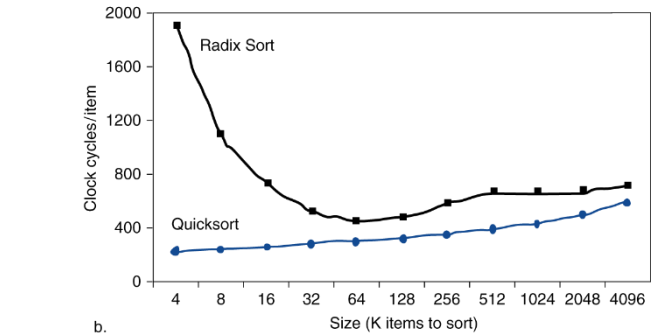
Interactions with Advanced CPUs

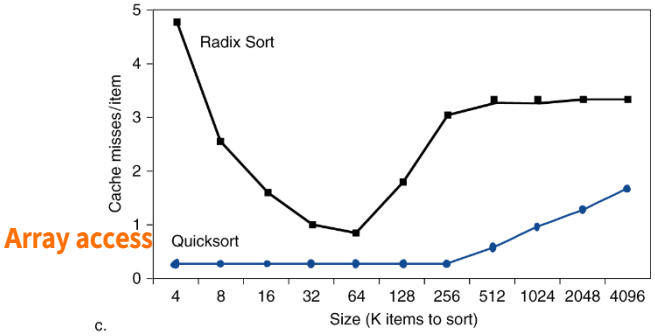
- Out-of-order CPUs can execute instructions during cache miss
  - Pending store stays in load/store unit
  - Dependent instructions wait in reservation stations
    - Independent instructions continue
- Effect of miss depends on program data flow
  - Much harder to analyze
  - Use system simulation

Interactions with Software

- Misses depend on memory access patterns
  - Algorithm behavior
  - Compiler optimization for memory access







Software Optimization via Blocking

- Goal: maximize accesses to data before it is replaced
- Consider inner loops of DGEMM (Double-Precision General Matrix Multiply):

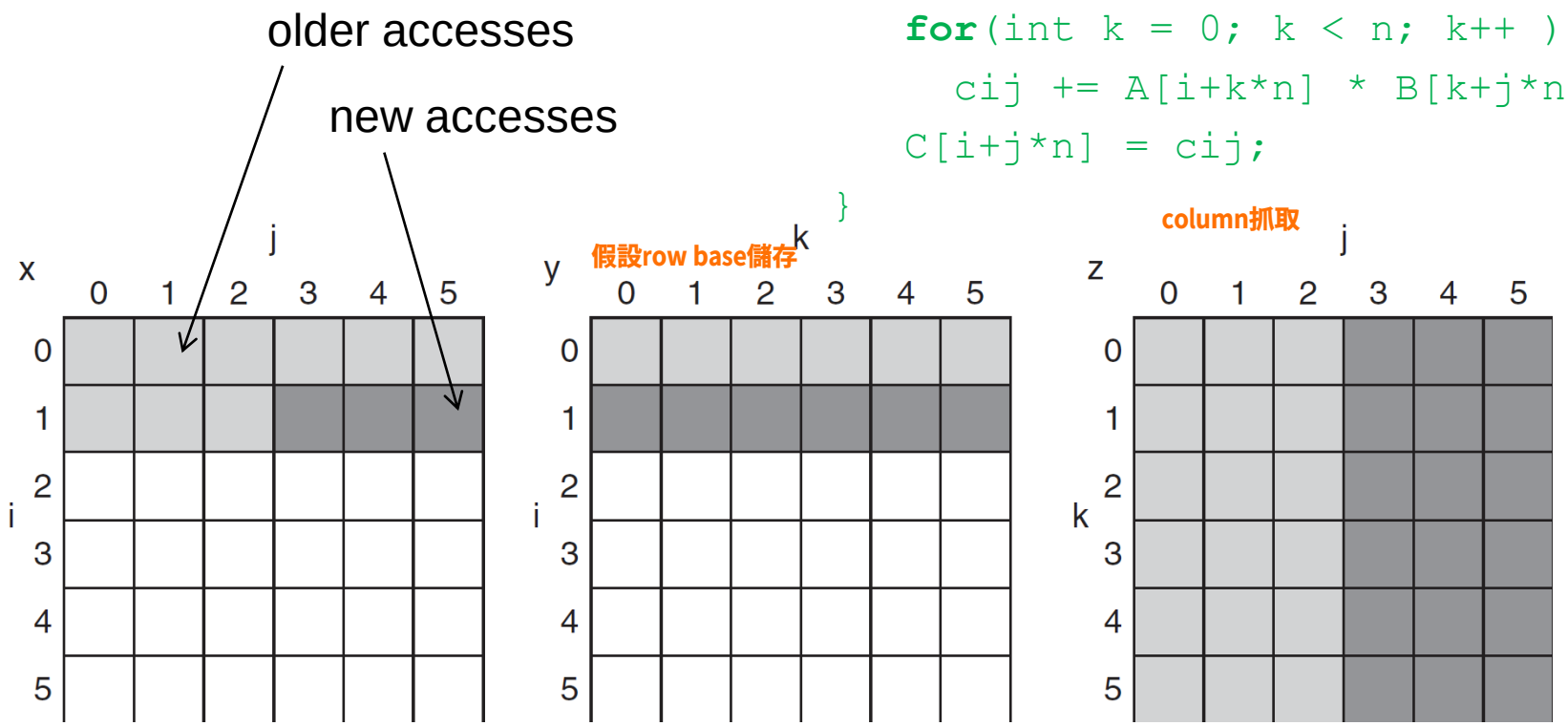
```
1. void dgemm (int n, double* A, double* B, double* C)
2. {
3.  for (int i = 0; i < n; ++i)
4.    for (int j = 0; j < n; ++j)
5.    {
6.     double cij = C[i+j*n]; /* cij = C[i][j] */
7.     for(int k = 0; k < n; k++ )
8.      cij += A[i+k*n] * B[k+j*n]; /* cij += A[i][k]*B[k][j] */
9.     C[i+j*n] = cij; /* C[i][j] = cij */
10.   }
11. }
```

DGEMM Access Pattern

- C, A, and B arrays

==>不理想
Array有可能大小超過cache

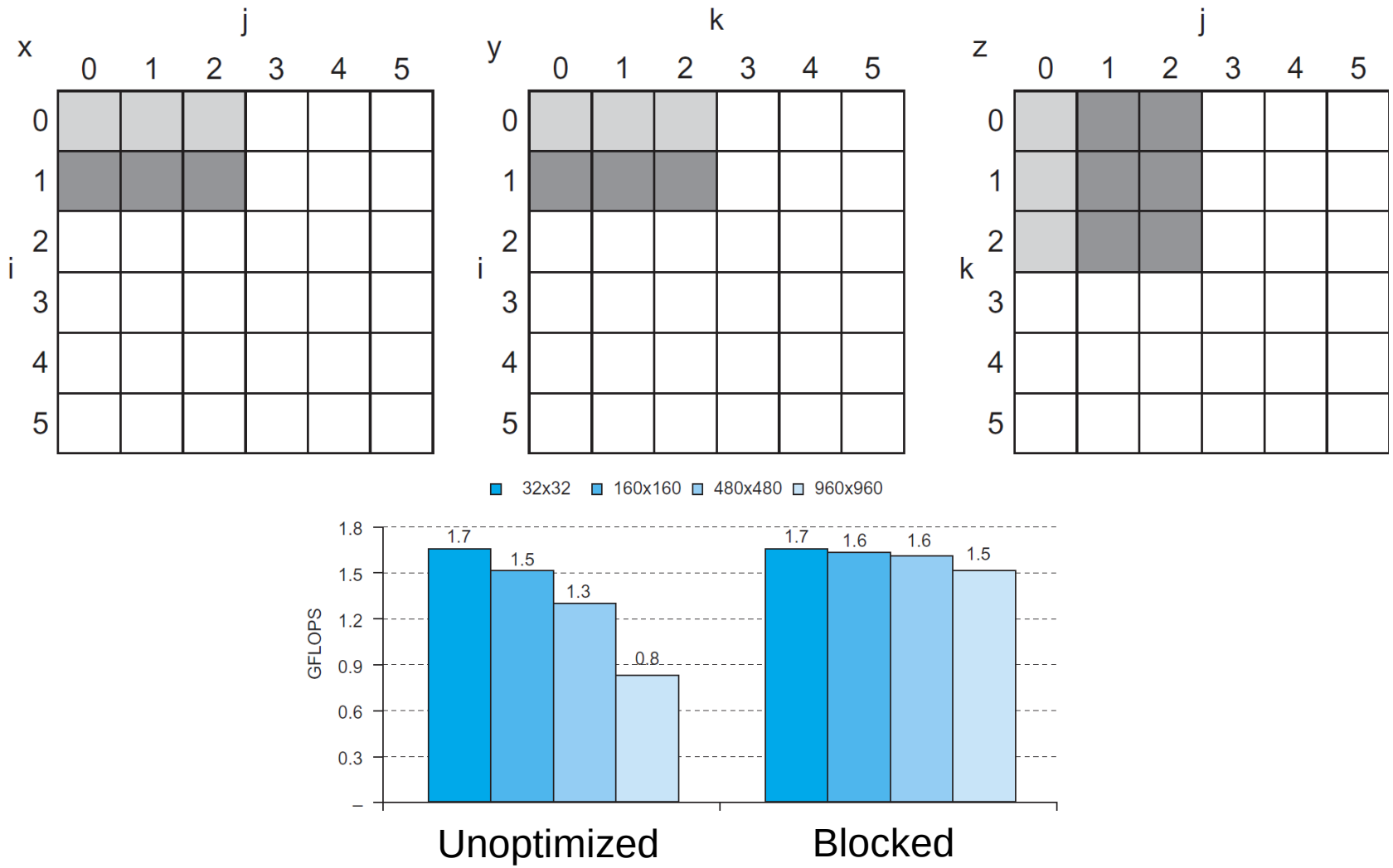
```
for (int i = 0; i < n; ++i)
  for (int j = 0; j < n; ++j)
  {
    double cij = C[i+j*n];
    for(int k = 0; k < n; k++ )
      cij += A[i+k*n] * B[k+j*n];
    C[i+j*n] = cij;
  }
```



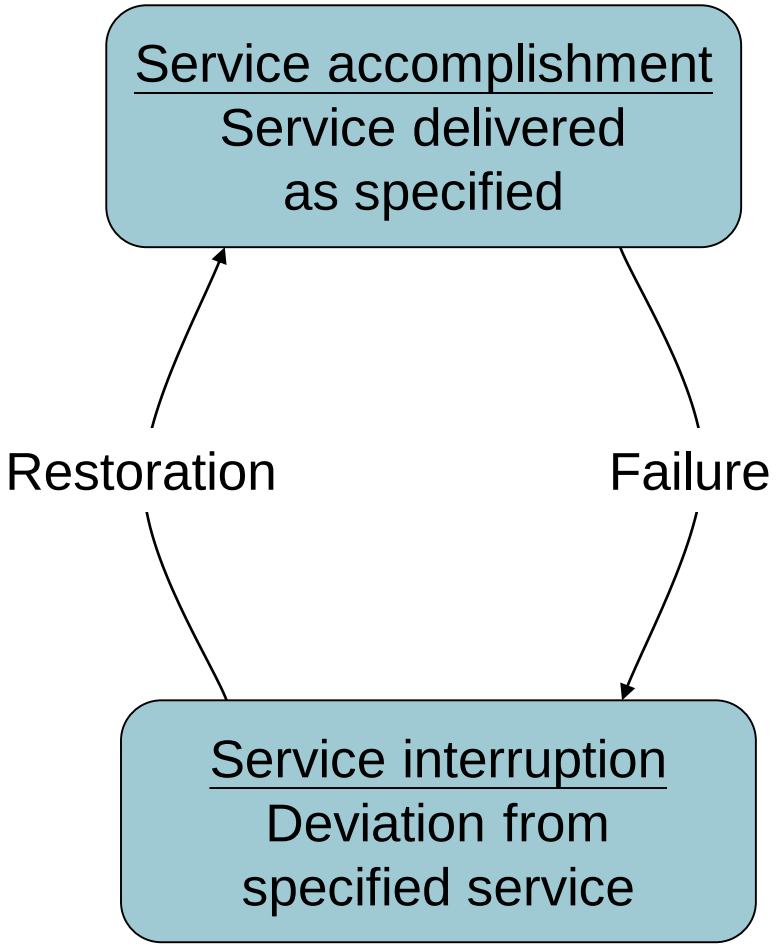
Cache Blocked DGEMM

```
1 #define BLOCKSIZE 32
2 void do_block (int n, int si, int sj, int sk, double *A, double
3 *B, double *C)
4 {
5  for (int i = si; i < si+BLOCKSIZE; ++i)
6   for (int j = sj; j < sj+BLOCKSIZE; ++j)
7   {
8    double cij = C[i+j*n];/* cij = C[i][j] */
9    for( int k = sk; k < sk+BLOCKSIZE; k++ )
10    cij += A[i+k*n] * B[k+j*n];/* cij+=A[i][k]*B[k][j] */
11   C[i+j*n] = cij;/* C[i][j] = cij */
12  }
13 }
14 void dgemm (int n, double* A, double* B, double* C)
15 {
16  for ( int sj = 0; sj < n; sj += BLOCKSIZE )
17   for ( int si = 0; si < n; si += BLOCKSIZE )
18    for ( int sk = 0; sk < n; sk += BLOCKSIZE )
19     do_block(n, si, sj, sk, A, B, C);
20 }
```

Blocked DGEMM Access Pattern



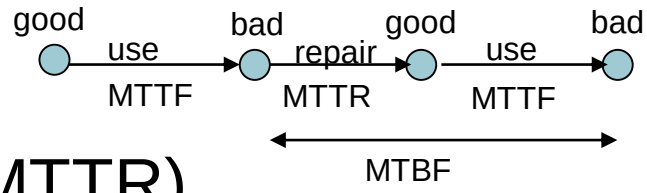
Dependability



- Fault: failure of a component
  - May or may not lead to system failure

Dependability Measures

- Reliability: mean time to failure (MTTF)
- Service interruption: mean time to repair (MTTR)
- Mean time between failures
  - MTBF = MTTF + MTTR
- Availability = MTTF / (MTTF + MTTR)
- Improving Availability
  - Increase MTTF: fault avoidance, fault tolerance, fault forecasting
  - Reduce MTTR: improved tools and processes for diagnosis and repair
- “nines of availability” per year
  - One nine: 90% → 36.5 days of repair/year
  - Two nines: 99% → 3.65 days of repair/year
  - Thee nines: 99.9% → 526 minutes of repair/year



The Hamming SEC Code

- Hamming distance
  - Number of bits that are different between two bit patterns
- Minimum distance = 2 provides single bit error detection
  - E.g. parity code
- Minimum distance = 3 provides single error correction

The Hamming SEC Code

- (7,4) Hamming code – 16 7-bit codewords, SEC (distance of 3)

$$c_1 \oplus c_3 \oplus c_5 \oplus c_7 = 0$$
$$c_2 \oplus c_3 \oplus c_6 \oplus c_7 = 0$$
$$c_4 \oplus c_5 \oplus c_6 \oplus c_7 = 0$$

根據3 5 7 的binary bits
決定要是C1C2C3的哪個==>C1C2C3
相當於是bit123有沒有用

With parity-check matrix *H*

$$\mathbf{c}H^T = [\, c_1\ c_2\ c_3\ c_4\ c_5\ c_6\ c_7 \,] \begin{bmatrix} 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 \end{bmatrix}^T = 0$$

$$\begin{aligned} c_1 &= c_3 \oplus c_5 \oplus c_7 \\ c_2 &= c_3 \oplus c_6 \oplus c_7 \\ c_4 &= c_5 \oplus c_6 \oplus c_7 \end{aligned} \iff [\, c_1\ c_2\ c_4 \,] = [\, c_3\ c_5\ c_6\ c_7 \,] \begin{bmatrix} 1 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}.$$

c_1	c_2	c_3	c_4	c_5	c_6	c_7
C1	C2	D1	C3	D2	D3	D4
0	0	0	0	0	0	0
1	1	0	1	0	0	1
0	1	0	1	0	1	0
1	0	0	0	0	1	1
1	0	0	1	1	0	0
0	1	0	0	1	0	1
1	1	0	0	1	1	0
0	0	0	1	1	1	1
1	1	1	0	0	0	0
0	0	1	1	0	0	1
1	0	1	1	0	1	0
0	1	1	0	0	1	1
0	1	1	1	1	0	0
1	0	1	0	1	0	1
0	0	1	0	1	1	0
1	1	1	1	1	1	1

Encoding SEC

- To calculate Hamming code:
  - Number bits from 1 on the left
  - All bit positions that are a power 2 are parity bits
  - Each parity bit checks certain data bits:

Bit position		1	2	3	4	5	6	7	8	9	10	11	12
Encoded date bits		p1	p2	d1	p4	d2	d3	d4	p8	d5	d6	d7	d8
Parity bit coverate	p1	X		X		X		X		X		X	
	p2		X	X			X	X			X	X	
	p4				X	X	X	X					X
	p8								X	X	X	X	X

Decoding SEC

- Value of parity bits indicates which bits are in error
  - Use numbering from encoding procedure
  - E.g.
    - Parity bits = 000 ($P_3P_2P_1$) indicates no error
    - Parity bits = 110 indicates bit 6 was flipped

	1	2	3	4	5	6	7
	P_1	P_2	d_1	P_3	d_2	d_3	d_4
raw	0	1	0	1	0	1	0
read	0	1	0	1	0	0	0
computed	0	0	0	0	0	0	0
	0	1		1	→	3	==>6

$P_1 = d_1\,(3) \oplus d_2\,(5) \oplus d_4\,(7)$

$P_2 = d_1\,(3) \oplus d_3\,(6) \oplus d_4\,(7)$

$P_3 = d_2\,(5) \oplus d_3\,(6) \oplus d_4\,(7)$

SEC/DED Code

- Add an additional parity bit for the whole word (p_n)
  - $p_1+p_2+d_1+p_3+d_2+d_3+d_4+p_4 = 0$;
- Make Hamming distance = 4
- Decoding:
  - Let H = SEC parity bits
    - H even, p_n even, no error
    - H odd, p_n odd, correctable single bit error
    - H even, p_n odd, error in p_n bit
    - H odd, p_n even, double error occurred
- Note: ECC DRAM uses SEC/DED with 8 bits protecting each 64 bits

SEC/DED Code

A. H even, p_n even, no error
B. H odd, p_n odd, correctable single bit error
C. H even, p_n odd, error in p_n bit
D. H odd, p_n even, double error occurred

	1	2	3	4	5	6	7	8
	P_1	P_2	d_1	P_3	d_2	d_3	d_4	P_4
	1	1	0	0	1	1	0	0
B	1	1	1	0	1	1	0	0
	0	0	1	0	1	1	0	1
C	1	1	0	0	1	1	0	1
	1	1	0	0	1	1	0	0
D	1	1	1	0	0	1	0	0
	1	0	1	1	0	1	0	0

$P_1 = d_1\,(3) \oplus d_2\,(5) \oplus d_4\,(7)$

$P_2 = d_1\,(3) \oplus d_3\,(6) \oplus d_4\,(7)$

$P_3 = d_2\,(5) \oplus d_3\,(6) \oplus d_4\,(7)$

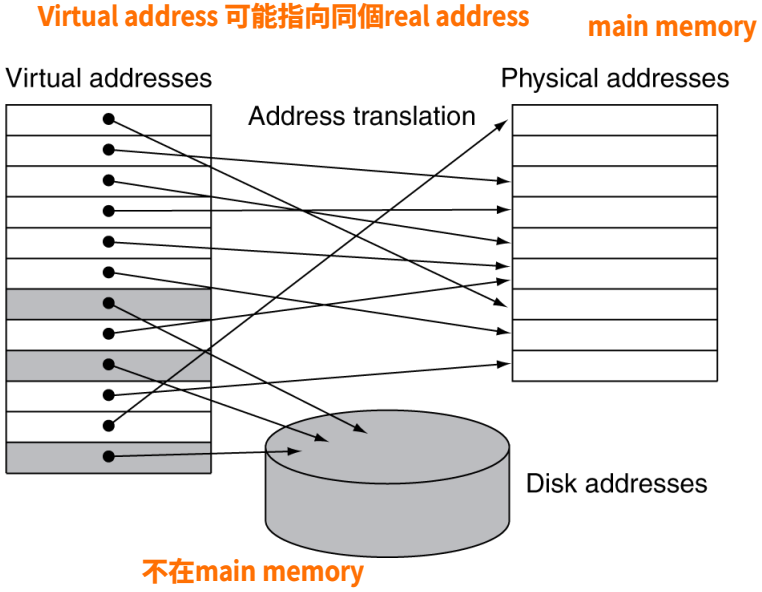
Virtual Memory

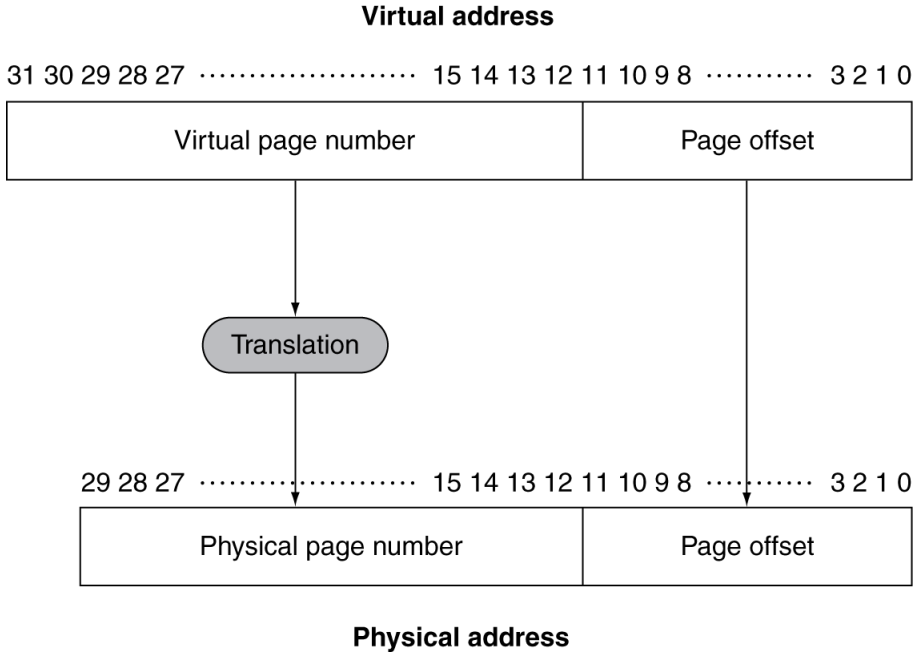
- Use main memory as a “cache” for secondary (disk) storage
  - Managed jointly by CPU hardware and the operating system (OS)
- Programs share main memory
  - Each gets a private virtual address space holding its frequently used code and data
  - Protected from other programs
- CPU and OS translate virtual addresses to physical addresses
  - VM “block” is called a page
  - VM translation “miss” is called a page fault

Address Translation

- Fixed-size pages (e.g., 4K)

很多不同process,user因此
Virtual address 可能指向同個real address





Page Fault Penalty

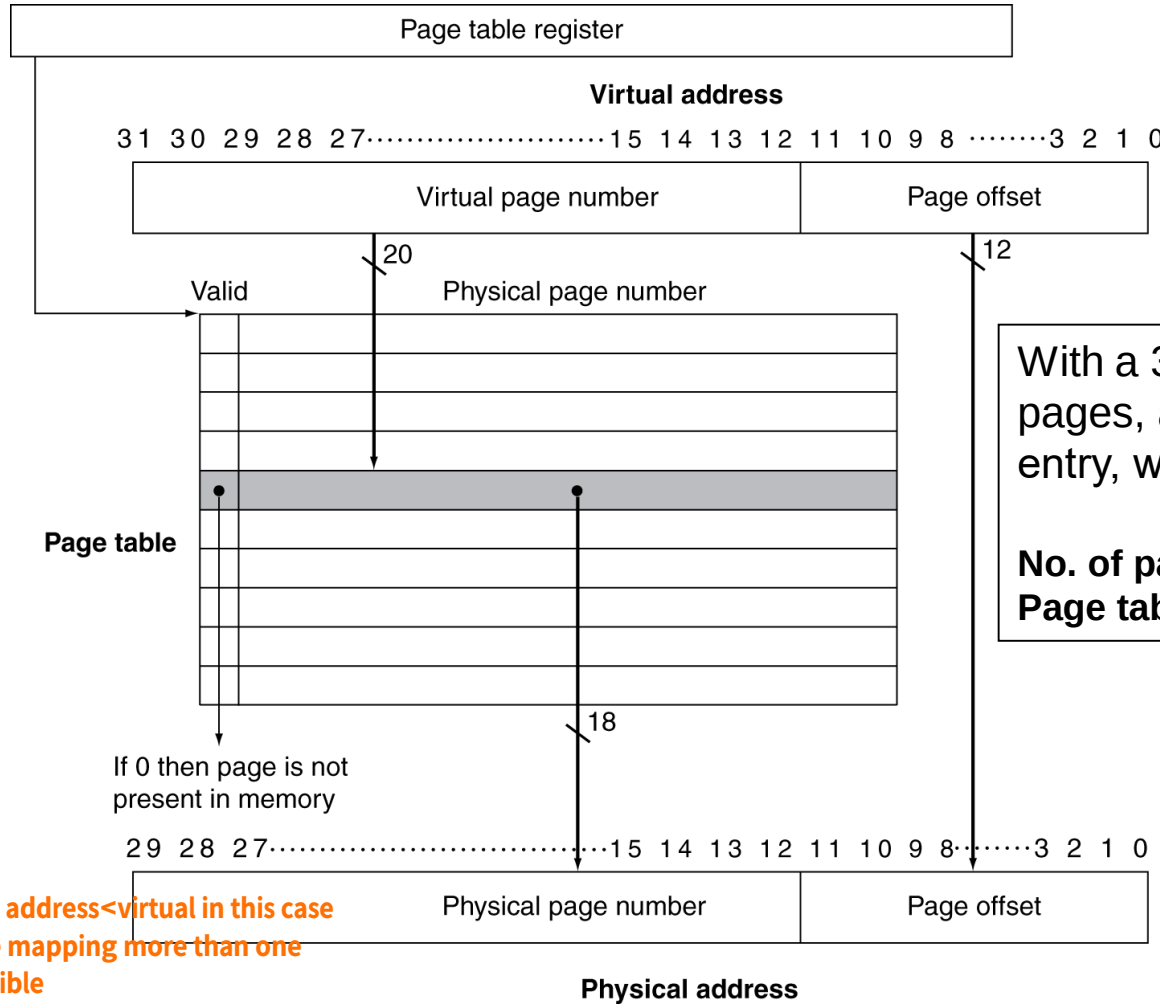
- On page fault, the page must be fetched from disk
  - Takes millions of clock cycles
  - Handled by OS code
- Try to minimize page fault rate
  - Fully associative placement
  - Smart replacement algorithms

Page Tables

- Stores placement information
  - Array of page table entries, indexed by virtual page number
  - Page table register in CPU points to page table in physical memory
- If page is present in memory
  - PTE stores the physical page number
  - Plus other status bits (referenced, dirty, …)
- If page is not present
  - PTE can refer to location in swap space on disk

page table entry

Translation Using a Page Table

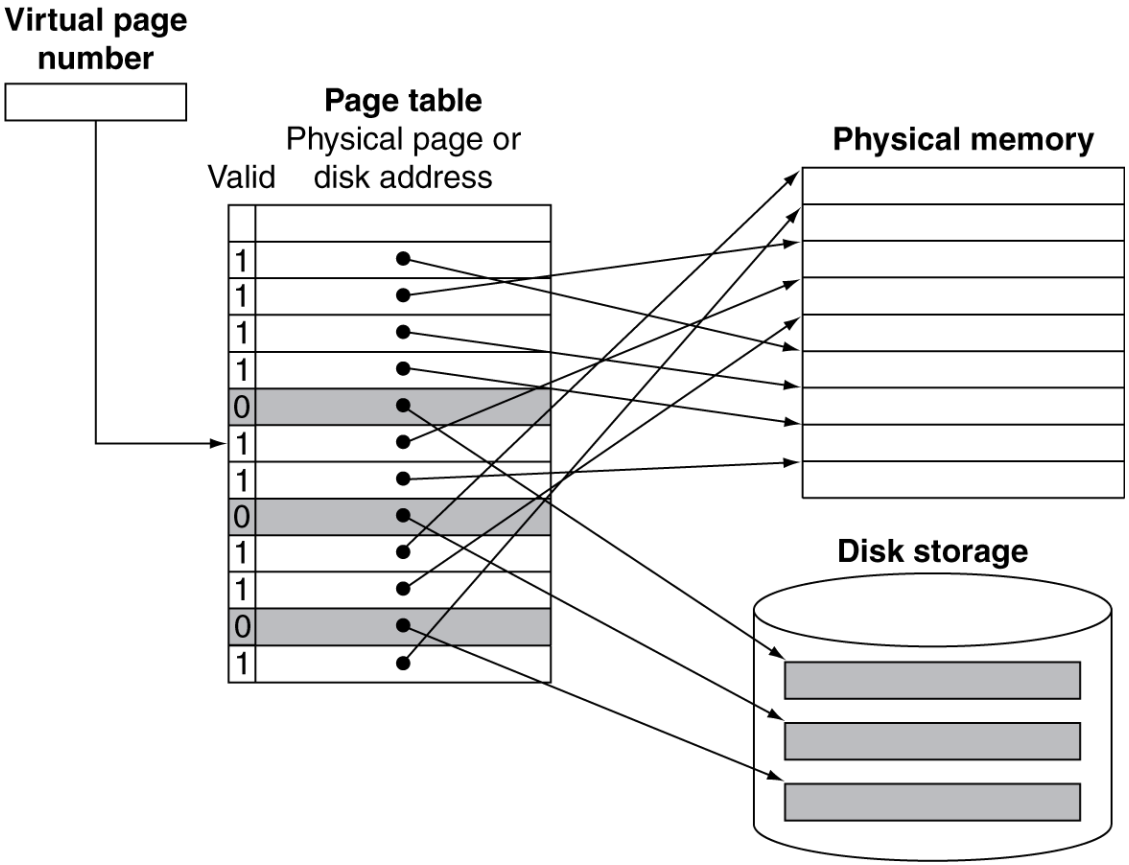


With a 32-bit virtual address, 4 KB pages, and 4 bytes per page table entry, what's the page table size?

No. of page table entries= $2^{32}/2^{12} = 2^{20}$
Page table size = $2^{20} \times 4 = 4$MB

physical address<virtual in this case
==>one mapping more than one
==>flexible

Mapping Pages to Storage



Replacement and Writes

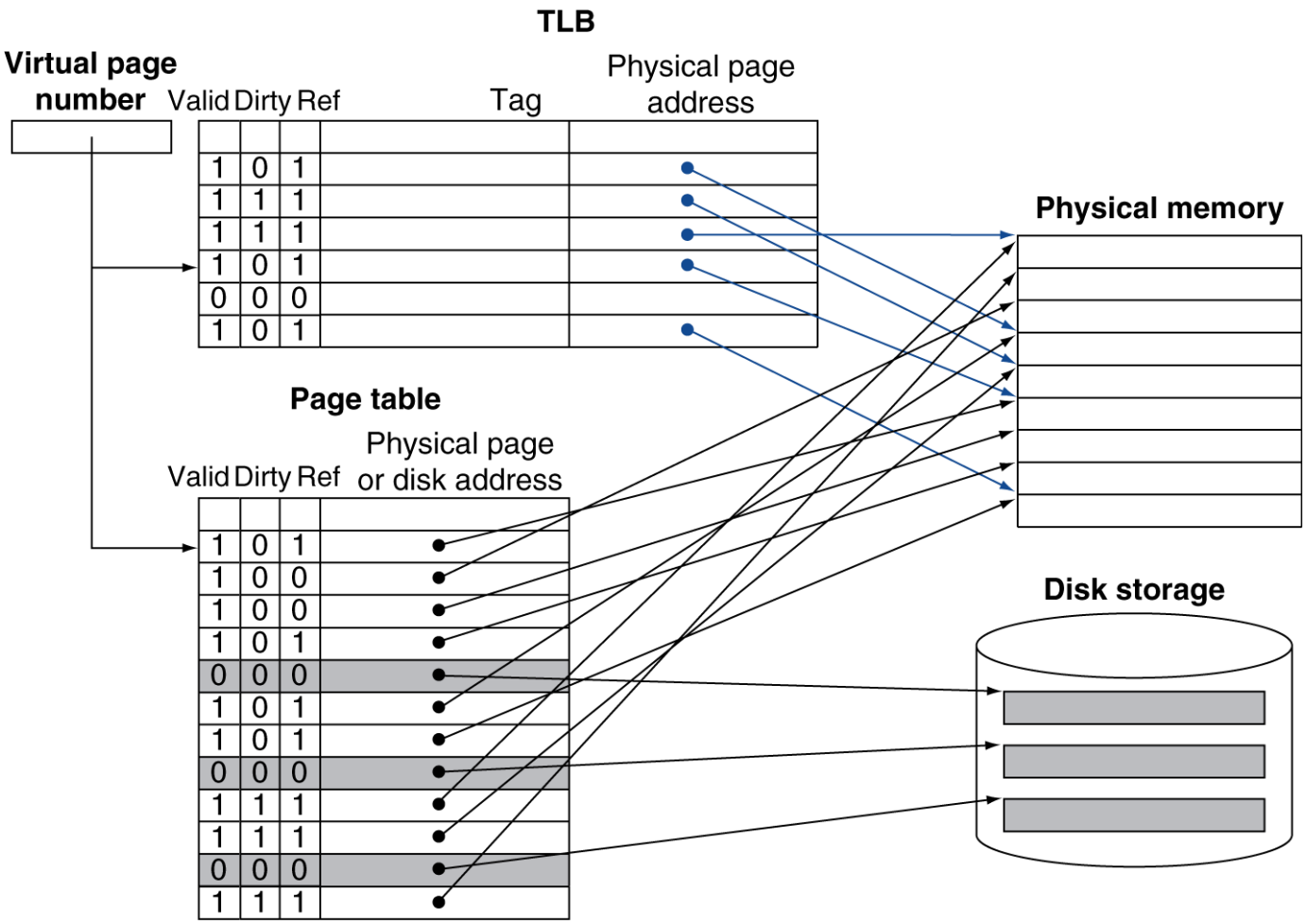
- To reduce page fault rate, prefer least-recently used (LRU) replacement
  - Reference bit (aka use bit) in PTE set to 1 on access to page 可以算被access的次數
  - Periodically cleared to 0 by OS
  - A page with reference bit = 0 has not been used recently
- Disk writes take millions of cycles
  - Block at once, not individual locations
  - Write through is impractical
  - Use write-back
  - Dirty bit in PTE set when page is written

Fast Translation Using a TLB

可以看成一種cache

- Address translation would appear to require extra memory references
  - One to access the PTE
  - Then the actual memory access
- But access to page tables has good locality
  - So use a fast cache of PTEs within the CPU
  - Called a Translation Look-aside Buffer (TLB)
  - Typical: 16–512 PTEs, 0.5–1 cycle for hit, 10–100 cycles for miss, 0.01%–1% miss rate
  - Misses could be handled by hardware or software

Fast Translation Using a TLB



TLB Misses

- If page is in memory
  - Load the PTE from memory and retry
  - Could be handled in hardware
    - Can get complex for more complicated page table structures
  - Or in software
    - Raise a special exception, with optimized handler
- If page is not in memory (page fault)
  - OS handles fetching the page and updating the page table
  - Then restart the faulting instruction

TLB Miss Handler

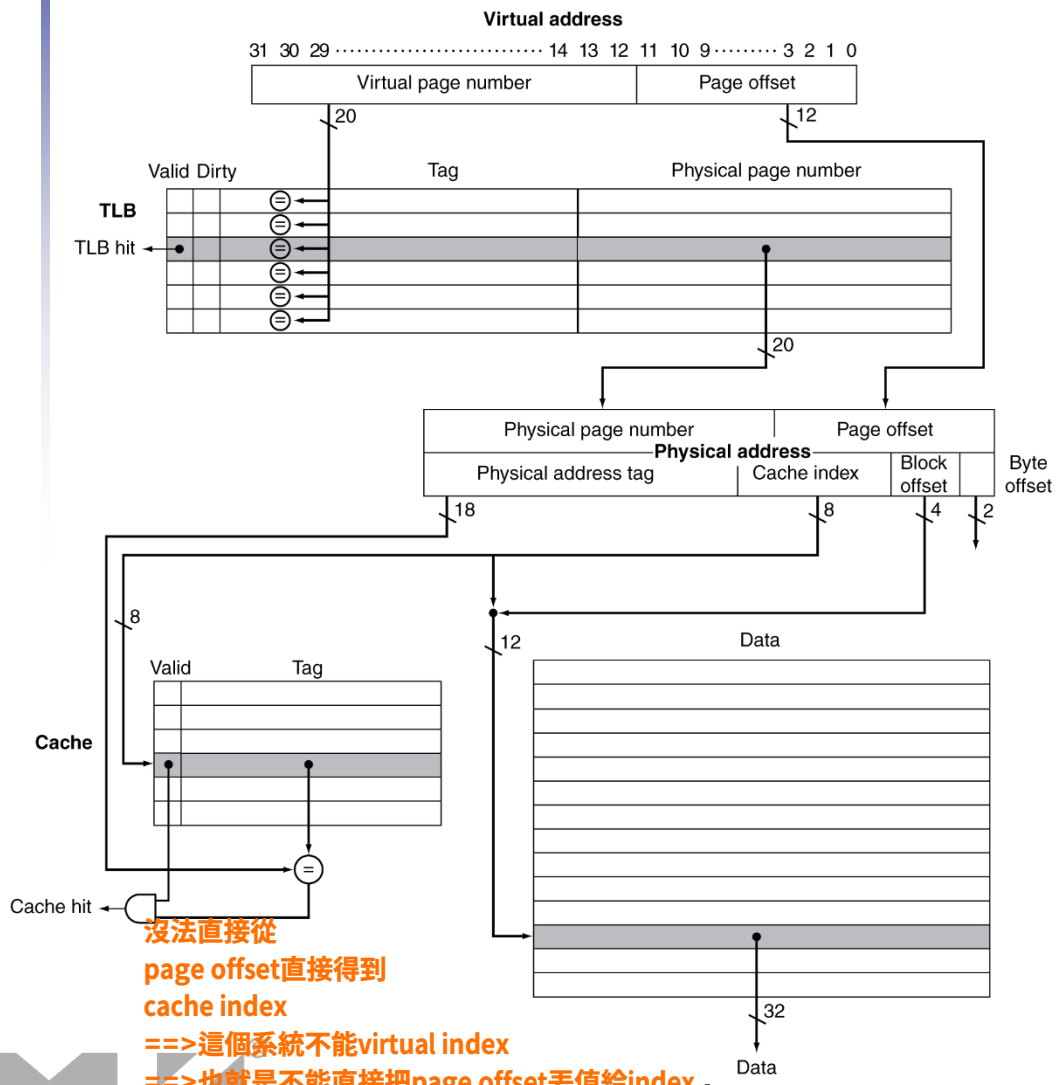
- TLB miss indicates
  - Page present, but PTE not in TLB
  - Page not present
- Must recognize TLB miss before destination register overwritten
  - Raise exception
- Handler copies PTE from memory to TLB
  - Then restarts instruction
  - If page not present, page fault will occur

Page Fault Handler

- Use faulting virtual address to find PTE
- Locate page on disk
- Choose page to replace if there is no free memory page
  - If dirty, write to disk first
- Read page into memory and update page table
- Make process runnable again
  - Restart from faulting instruction

TLB and Cache Interaction

Physically/virtually addressed cache



沒法直接從
page offset直接得到
cache index
==>這個系統不能virtual index
==>也就是不能直接把page offset丟值給index
==>增加需要更多等待時間的可能

- If cache tag uses physical address
  - Need to translate before cache lookup
  - Cache hit requires a TLB access and a cache access.
- Virtually addressed cache
  - remove TLB access
  - Complications due to aliasing
    - Different virtual addresses for shared physical address

Memory Protection

- Different tasks can share parts of their virtual address spaces
  - But need to protect against errant access
  - Requires OS assistance
- Hardware support for OS protection
  - Privileged supervisor mode (aka kernel mode)
  - Privileged instructions
  - Page tables and other state information only accessible in supervisor mode
  - System call exception (e.g., syscall in MIPS)

The Memory Hierarchy

The BIG Picture

- Common principles apply at all levels of the memory hierarchy
  - Based on notions of caching
- At each level in the hierarchy
  - Block placement
  - Finding a block
  - Replacement on a miss
  - Write policy

Block Placement

- Determined by associativity
  - Direct mapped (1-way associative)
    - One choice for placement
  - n-way set associative
    - n choices within a set
  - Fully associative
    - Any location
- Higher associativity reduces miss rate
  - Increases complexity, cost, and access time

Finding a Block

Associativity	Location method	Tag comparisons
Direct mapped	Index	1
n-way set associative	Set index, then search entries within the set	n
Fully associative	Search all entries	#entries
	Full lookup table	0

- Hardware caches
  - Reduce comparisons to reduce cost
- Virtual memory
  - Full table lookup makes full associativity feasible
  - Benefit in reduced miss rate

Replacement

- Choice of entry to replace on a miss
  - Least recently used (LRU)
    - Complex and costly hardware for high associativity
  - Random
    - Close to LRU, easier to implement
- Virtual memory
  - LRU approximation with hardware support

Write Policy

- Write-through
  - Update both upper and lower levels
  - Simplifies replacement, but may require write buffer
- Write-back
  - Update upper level only
  - Update lower level when block is replaced
  - Need to keep more state
- Virtual memory
  - Only write-back is feasible, given disk write latency

Sources of Misses

- Compulsory misses (aka cold start misses)
  - First access to a block
- Capacity misses 塞滿的miss
  - Due to finite cache size
  - A replaced block is later accessed again
- Conflict misses (aka collision misses)
  - In a non-fully associative cache
  - Due to competition for entries in a set
  - Would not occur in a fully associative cache of the same total size

Cache Design Trade-offs

Design change	Effect on miss rate	Negative performance effect
Increase cache size	Decrease capacity misses	May increase access time
Increase associativity	Decrease conflict misses	May increase access time
Increase block size	Decrease compulsory misses	Increases miss penalty. For very large block size, may increase miss rate due to pollution.

TLB, Page Table and Cache

- The possible combinations of events in the TLB, virtual memory system, and physically indexed (tagged) cache.

如果在TLB就一定在page table(不是指兩個都讀)

physical address 不一定保證在cache，但保證在main memory

TLB	Page table	Cache	Possible ? If so, under what circumstance ?
Hit	Hit	Miss	**Possible**
Miss	Hit	Hit	**Possible**
Miss	Hit	Miss	**Possible**
Miss	Miss	Miss	**Possible**
Hit	Miss	Miss	Impossible
Hit	Miss	Hit	Impossible
Miss	Miss	Hit	Impossible

cache hit==>Page table hit

Virtual Machines

- Host computer emulates guest operating system and machine resources
  - Improved isolation of multiple guests
  - Avoids security and reliability problems
  - Aids sharing of resources
- Virtualization has some performance impact
  - Feasible with modern high-performance computers
- Examples
  - IBM VM/370 (1970s technology!)
  - VMWare
  - Microsoft Virtual PC

Virtual Machine Monitor

- Maps virtual resources to physical resources
  - Memory, I/O devices, CPUs
- Guest code runs on native machine in user mode
  - Traps to VMM on privileged instructions and access to protected resources
- Guest OS may be different from host OS
- VMM handles real I/O devices
  - Emulates generic virtual I/O devices for guest

Example: Timer Virtualization

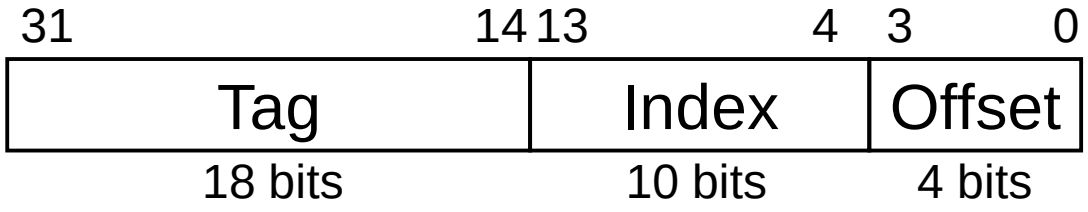
- In native machine, on timer interrupt
  - OS suspends current process, handles interrupt, selects and resumes next process
- With Virtual Machine Monitor
  - VMM suspends current VM, handles interrupt, selects and resumes next VM
- If a VM requires timer interrupts
  - VMM emulates a virtual timer
  - Emulates interrupt for VM when physical timer interrupt occurs

Instruction Set Support

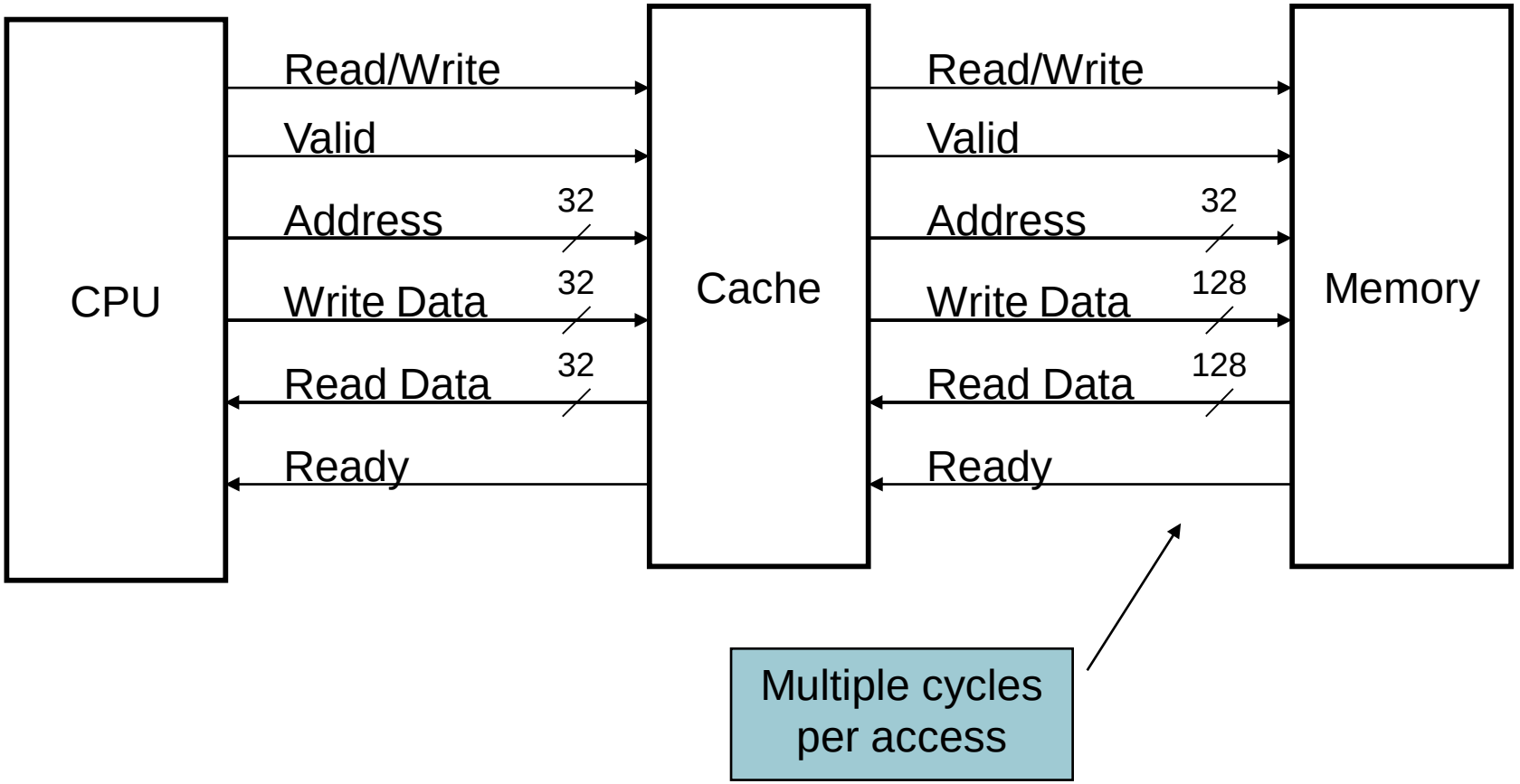
- User and System modes
- Privileged instructions only available in system mode
  - Trap to system if executed in user mode
- All physical resources only accessible using privileged instructions
  - Including page tables, interrupt controls, I/O registers
- Renaissance of virtualization support
  - Current ISAs (e.g., x86) adapting

Cache Control

- Example cache characteristics
  - Direct-mapped, write-back, write allocate
  - Block size: 4 words (16 bytes)
  - Cache size: 16 KB (1024 blocks)
  - 32-bit byte addresses
  - Valid bit and dirty bit per block
  - Blocking cache
    - CPU waits until access is complete

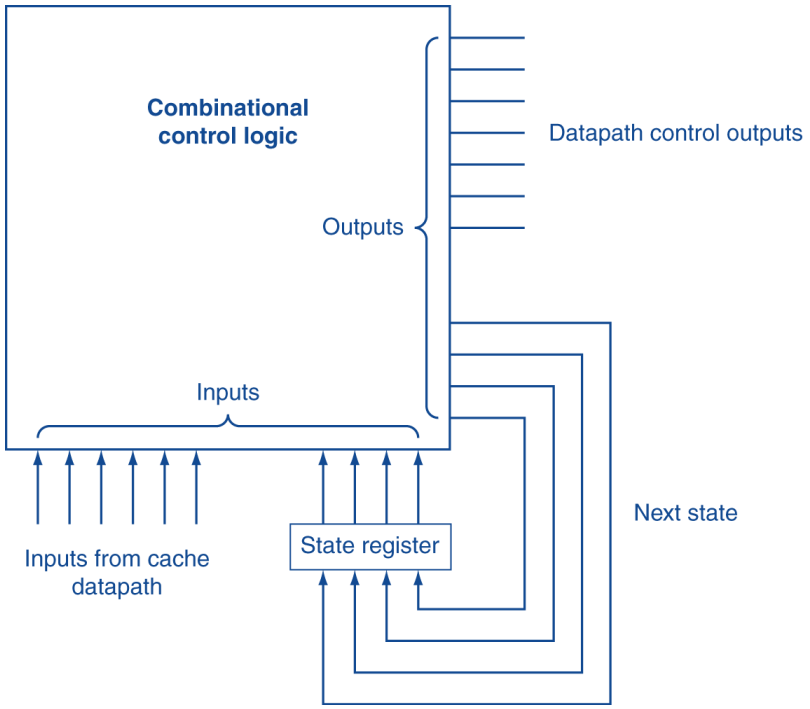


Interface Signals

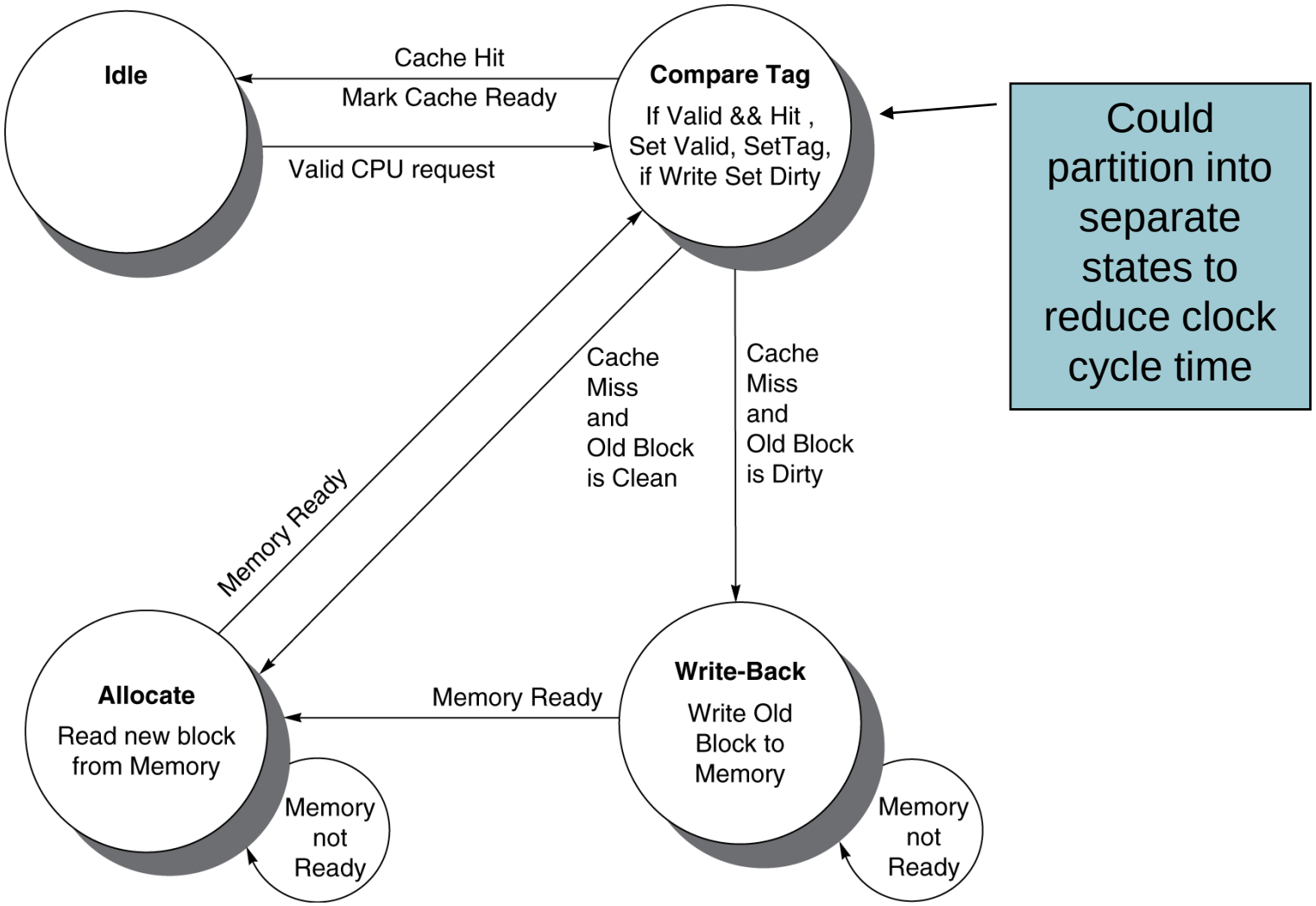


Finite State Machines

- Use an FSM to sequence control steps
- Set of states, transition on each clock edge
  - State values are binary encoded
  - Current state stored in a register
  - Next state = f_n (current state, current inputs)
- Control output signals = f_o (current state)



Cache Controller FSM



Cache Coherence Problem

- Suppose two CPU cores share a physical address space
  - Write-through caches

Time step	Event	CPU A's cache	CPU B's cache	Memory
0				0
1	CPU A reads X	0		0
2	CPU B reads X	0	0	0
3	CPU A writes 1 to X	1	0	1

Coherence Defined

- Informally: Reads return most recently written value
- Formally:
  - P writes X; P reads X (no intervening writes)
    ⇒ read returns written value (program order)
  - P_1 writes X; P_2 reads X (sufficiently later)
    ⇒ read returns written value (coherence)
    - c.f. CPU B reading X after step 3 in example
  - P_1 writes X, P_2 writes X
    ⇒ all processors see writes in the same order
    - End up with the same final value for X

Cache Coherence Protocols

- Operations performed by caches in multiprocessors to ensure coherence
  - Migration of data to local caches
    - Reduces bandwidth for shared memory
  - Replication of read-shared data
    - Reduces contention for access
- Snooping protocols
  - Each cache monitors bus reads/writes
- Directory-based protocols
  - Caches and memory record sharing status of blocks in a directory

Invalidating Snooping Protocols

- Cache gets exclusive access to a block when it is to be written
  - Broadcasts an invalidate message on the bus
  - Subsequent read in another cache misses
    - Owning cache supplies updated value

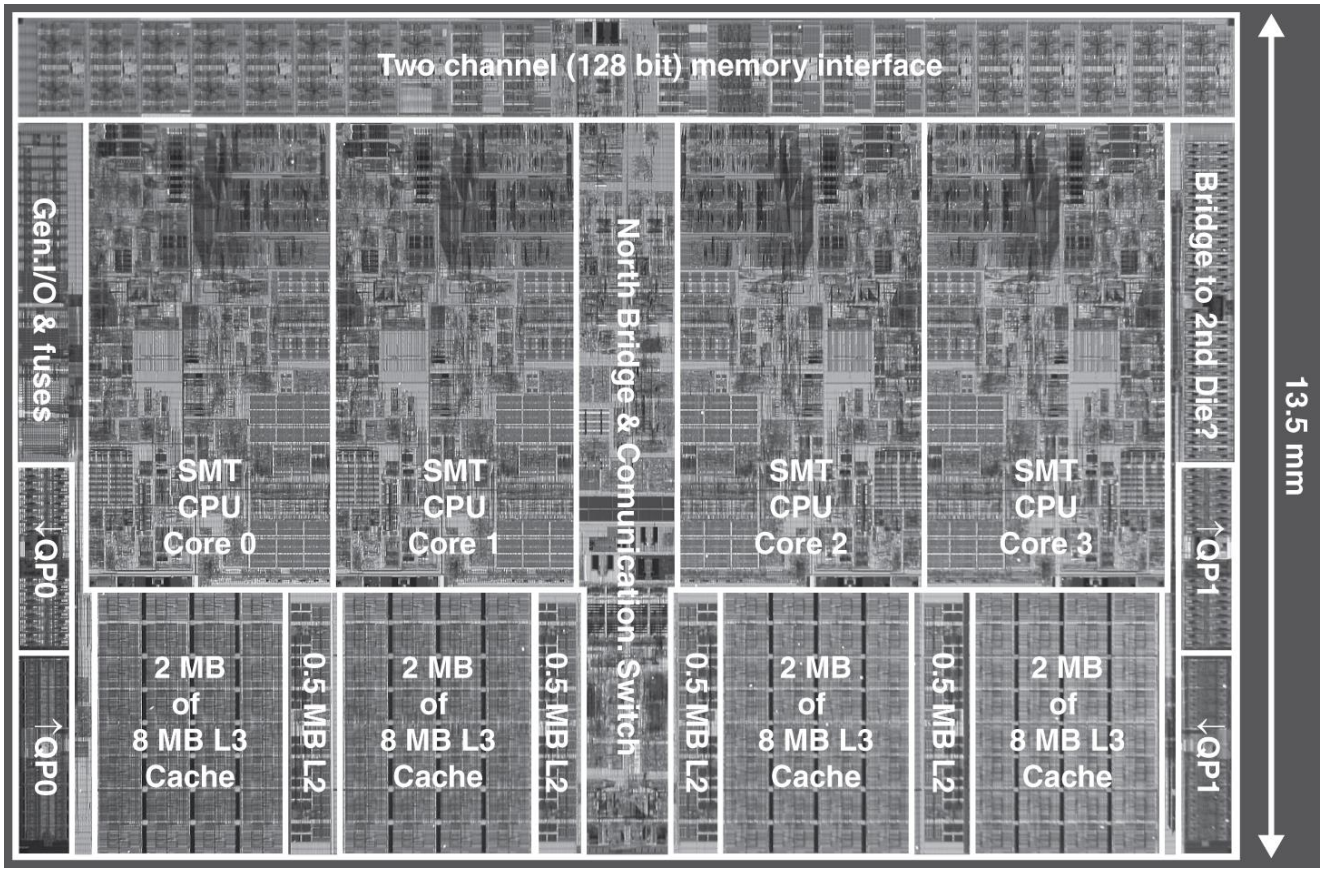
CPU activity	Bus activity	CPU A's cache	CPU B's cache	Memory
				0
CPU A reads X	Cache miss for X	0		0
CPU B reads X	Cache miss for X	0	0	0
CPU A writes 1 to X	Invalidate for X	1		0
CPU B read X	Cache miss for X	1	1	1

Memory Consistency

- When are writes seen by other processors
  - “Seen” means a read returns the written value
  - Can’t be instantaneously
- Assumptions
  - A write completes only when all processors have seen it
  - A processor does not reorder writes with other accesses
- Consequence
  - P writes location X then writes location Y
    $\Rightarrow$ all processors that see new Y also see new X
  - Processors can reorder reads, but not writes

Multilevel On-Chip Caches

Intel Nehalem 4-core processor



Per core: 32KB L1 I-cache, 32KB L1 D-cache, 512KB L2 cache

2-Level TLB Organization

	Intel Nehalem	AMD Opteron X4
Virtual addr	48 bits	48 bits
Physical addr	44 bits	48 bits
Page size	4KB, 2/4MB	4KB, 2/4MB
L1 TLB (per core)	L1 I-TLB: 128 entries for small pages, 7 per thread (2×) for large pages L1 D-TLB: 64 entries for small pages, 32 for large pages Both 4-way, LRU replacement	L1 I-TLB: 48 entries L1 D-TLB: 48 entries Both fully associative, LRU replacement
L2 TLB (per core)	Single L2 TLB: 512 entries 4-way, LRU replacement	L2 I-TLB: 512 entries L2 D-TLB: 512 entries Both 4-way, round-robin LRU
TLB misses	Handled in hardware	Handled in hardware

3-Level Cache Organization

	Intel Nehalem	AMD Opteron X4
L1 caches (per core)	L1 I-cache: 32KB, 64-byte blocks, 4-way, approx LRU replacement, hit time n/a L1 D-cache: 32KB, 64-byte blocks, 8-way, approx LRU replacement, write-back/allocate, hit time n/a	L1 I-cache: 32KB, 64-byte blocks, 2-way, LRU replacement, hit time 3 cycles L1 D-cache: 32KB, 64-byte blocks, 2-way, LRU replacement, write-back/allocate, hit time 9 cycles
L2 unified cache (per core)	256KB, 64-byte blocks, 8-way, approx LRU replacement, write-back/allocate, hit time n/a	512KB, 64-byte blocks, 16-way, approx LRU replacement, write-back/allocate, hit time n/a
L3 unified cache (shared)	8MB, 64-byte blocks, 16-way, replacement n/a, write-back/allocate, hit time n/a	2MB, 64-byte blocks, 32-way, replace block shared by fewest cores, write-back/allocate, hit time 32 cycles

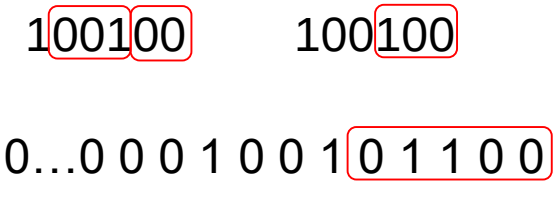
n/a: data not available

Miss Penalty Reduction

- Return requested word first
  - Then back-fill rest of block
- Non-blocking miss processing
  - Hit under miss: allow hits to proceed
  - Mis under miss: allow multiple outstanding misses
- Hardware prefetch: instructions and data
- Opteron X4: bank interleaved L1 D-cache
  - Two concurrent accesses per cycle

Pitfalls

- Byte vs. word addressing
  - Example: 32-byte direct-mapped cache, 4-byte blocks
    - Byte 36 maps to block 1
    - Word 36 maps to block 4



  - Example: 256-byte cache and 32 bytes per block
    - Byte address 300 maps to block number 1
- Ignoring memory system effects when writing or generating code
  - Example: iterating over rows vs. columns of arrays
  - Large strides result in poor locality

```
for (i = 0; …)
   for (j = 0; …)
        x[i][j] = x[i][j]+y[i][j]
```

Pitfalls

- In multiprocessor with shared L2 or L3 cache
  - Less associativity than cores results in conflict misses
  - More cores $\Rightarrow$ need to increase associativity
- Using AMAT to evaluate performance of out-of-order processors
  - Ignores effect of non-blocked accesses
  - Instead, evaluate performance by simulation

Fallacy: Disk Dependability

- If a disk manufacturer quotes MTTF as 1,200,000hr (140yr)
  - A disk will work that long
- Wrong: this is the mean time to failure
  - What is the distribution of failures?
  - What if you have 1000 disks
    - How many will fail per year?

$$\text{Annual Failure Rate (AFR)} = \frac{1000 \text{ disks} \times 8760 \text{ hrs/disk}}{1200000 \text{ hrs/failure}} / 1000 = 0.73\%$$

Fallacies

- Disk failure rates are as specified
  - Studies of failure rates in the field
    - Schroeder and Gibson: 2% to 4% vs. 0.6% to 0.8%
    - Pinheiro, *et al.*: 1.7% (first year) to 8.6% (third year) vs. 1.5%
  - Why?
- Extending address range using segments
  - E.g., Intel 80286
  - But a segment is not always big enough
  - Makes address arithmetic complicated

Pitfalls

- Implementing a VMM on an ISA not designed for virtualization
  - E.g., non-privileged instructions accessing hardware resources
  - Either extend ISA, or require guest OS not to use problematic instructions

Concluding Remarks

- Fast memories are small, large memories are slow
  - We really want fast, large memories ☹
  - Caching gives this illusion ☺
- Principle of locality
  - Programs use a small part of their memory space frequently
- Memory hierarchy
  - L1 cache ↔ L2 cache ↔ … ↔ DRAM memory ↔ disk
- Memory system design is critical for multiprocessors