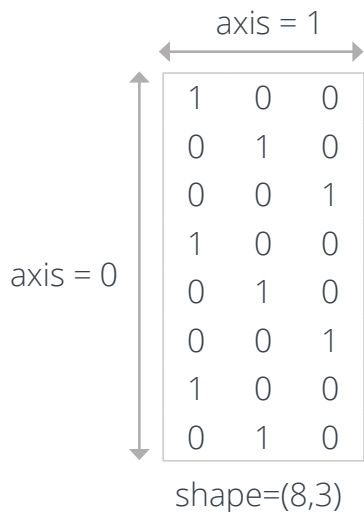


## TOOL

# NumPy Array Tip Sheet

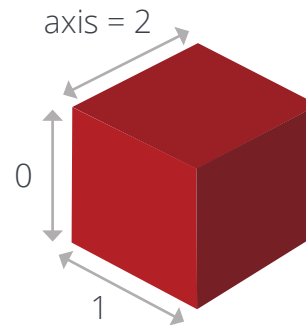
Arrays are the central data type introduced in the NumPy package. Technically, array objects are of type `numpy.ndarray`, which stands for “n-dimensional array.” Arrays are accessible by importing the NumPy module, although we will use the conventional shorthand here: `import numpy as np`. Arrays are similar in some respects to Python lists but are multidimensional, homogeneous in type, and support compact and efficient array-level manipulations. Documentation can be found online at [www.numpy.org/doc](http://www.numpy.org/doc).

## Anatomy of an array



The **axes** of an array describe the order of indexing into the array; e.g., `axis=0` refers to the first index coordinate, `axis=1` the second, etc.

The **shape** of an array is a tuple indicating the number of elements along each axis. An existing array `a` has an attribute `a.shape` which contains this tuple.



- All elements must be the same dtype (data type).
- The default dtype is float.
- Arrays constructed from a list of mixed dtype will be upcast to the “greatest” common type.



## Constructing arrays

- `np.array(alist)`: Construct an n-dimensional array from a Python list (all elements of list must be of same length).

```
a = np.array([[1,2,3],[4,5,6]])
b = np.array([i*i for i in range(100) if
i%2==1])                                # convert array back to Python list
c = b.tolist()
```

- `np.zeros(shape, dtype=float)`: Construct an n-dimensional array of the specified shape, filled with zeros of the specified dtype.

```
a = np.zeros(100)                        # a 100-element array of float zeros
b = np.zeros((2,8), int)                  # a 2x8 array of int zeros
c = np.zeros((N,M,L), bool)              # a NxMxL array of bool zeros
```

- `np.ones(shape, dtype=float)`: Construct an n-dimensional array of the specified shape, filled with ones of the specified dtype.

```
a = np.ones(10, int)                      # a 10-element array of int ones
b = np.pi * np.ones((5,5))              # a useful way to fill up an array with a specified value
```

- `np.transpose(a)`

```
b = np.transpose(a)                      # return new array with a's dimensions reversed
b = a.T                                  # equivalent to np.transpose(a)
```



- `np.arange` and `np.linspace`

```
a = np.arange(start, stop, increment)      # like Python range, but with (potentially) real-valued arrays
b = np.linspace(start, stop, num_elements)  # create array of equally spaced points based on
                                           # specified number of points
```

- Random array constructors in `np.random`

```
a = np.random.random((100,100))          # 100x100 array of floats uniform on [0.,1.)
b = np.random.randint(0,10, (100,))       # 100 random ints uniform on [0, 10); i.e., not
c = np.random.standard_normal((5,5,5))    # including the upper bound 10
                                           # zero-mean, unit-variance Gaussian random numbers in a
                                           # 5x5x5 array
```

## Indexing arrays

- Multidimensional indexing

```
elem = a[i,j,k]                          # extract element at position (i,j,k) in array
```

- “Negative” indexing (wrap around the end of the array)

```
last = a[-1]                             # the last element of the array (returns array if a.ndim
last_elem = a[-1,-1]                     > 1)
                                           # the lower-right element of an array (returns array if
                                           # a.ndim > 2)
```



- Arrays as indices

```
i = np.array([0,1,2,1])
j = np.array([1,2,3,4])
a[i,j]
#
b = np.array([True, False, True, False])
a[b]
```

# array of indices for the first axis  
# array of indices for the second axis  
# return array([a[0,1], a[1,2], a[2,3], a[1,4]]) based on i and j above  
# return array([a[0], a[2]]) since only b[0] and b[2] are True

## Slicing arrays (extracting subsections)

- Slice a defined subblock

```
section = a[10:20, 30:40]
```

# 10x10 subblock starting at [10,30]

- Grab everything up to the beginning/end of the array

```
asection = a[10:, 30:]
bsection = b[:10, :30]
```

# missing stop index implies until end of array  
# missing start index implies until start of array

- Grab an entire column

```
x = a[:, 0]
y = a[:, 1]
```

# get everything in the 0th column (missing start and stop)  
# get everything in the 1st column

- Slice off the tail end of an array

```
tail = a[-10:]
slab = b[:, -10:]
interior = c[1:-1, 1:-1, 1:-1]
```

# grab the last 10 elements of the array  
# grab a slab of width 10 off the “side” of the array  
# slice out everything but the outer shell



## Element-wise functions on arrays

- Arithmetic operations

```
c = a + b
d = c + 2
h = e * f
g = -h
m = c ** 2
z = w > 0.0
logspace = 10**np.linspace(-6, -1, 50)
```

# add a and b element-wise (must be same shape)  
# add 2 to every element of c  
# multiply e and f element-wise (NOT matrix multiplication)  
# negate every element of h  
# compute the square of every element of c  
# return Boolean array indicating which elements are > 0.0  
# array of 50 equally spaced-in log points between 1.0e-06 and 1.0e-01

- Trigonometric operations

```
y = np.sin(x)
w = np.cos(2*np.pi*x)
```

# sin of every element of x  
# cos of 2\*pi\*x

## Summation of arrays

- Simple sums

```
s = np.sum(a)
s0 = np.sum(a, axis=0)
s1 = np.sum(a, axis=1)
```

# sum all elements in a, returning a scalar (single number)  
# sum elements along specified axis (=0), returning an array of remaining shape  
# sum elements along axis=1; i.e., over rows if a is 2-dimensional



- Averaging, etc.

```
m = np.mean(a, axis)
s = np.std(a, axis)
```

```
# compute mean along the specified axis (over entire
array if axis=None)
# compute standard deviation along the specified axis
(over entire array if axis=None)
```

- Cumulative sums

```
s0 = np.cumsum(a, axis=0)
s0 = np.cumsum(a)
```

```
# cumulatively sum over 0 axis, returning array with
same shape as a
# cumulatively sum over 0 axis, returning 1D array of
length shape[0]*shape[1]*...*shape[dim-1]
```



## Some other useful functions and methods

Many of these work both as separate functions (e.g., `np.sum(a)`) as well as array methods (e.g., `a.sum()`).

- `np.any(a)`: Return True if any element of a is True.
- `np.all(a)`: Return True if all elements of a are True.
- `np.concatenate((a1, a2, ...), axis)`: Concatenate tuple of arrays along specified axis.
- `np.min(a, axis=None)`, `np.max(a, axis=None)`: Get min/max values of a along specified axis (global min/max if axis=None).
- `np.argmin(a, axis=None)`, `np.argmax(a, axis=None)`: Get indices of min/max of a along specified axis (global min/max if axis=None).
- `np.reshape(a, newshape)`: Reshape a to new shape (must conserve total number of elements).
- `np.histogram`, `np.histogram2d`, `np.histogramdd`: 1-dimensional, 2-dimensional, and d-dimensional histograms, respectively.
- `np.round(a, decimals=0)`: Round elements of array a to specified number of decimals.
- `np.sign(a)`: Return array of same shape as a, with -1 where  $a < 0$ , 0 where  $a = 0$ , and +1 where  $a > 0$ .
- `np.abs(a)`: Return array of same shape as a, with the absolute value of each corresponding element.
- `np.unique(a)`: Return sorted unique elements of array a.
- `np.where(condition, x, y)`: Return array with same shape as condition, where values from x are inserted in positions where condition is True, and values from y where condition is False.

