

令  $V = \{U_0=0, U_1=0, U_2=0, U_3=1, U_4=1, U_5=1\}$

p.3. 计算 B 样条基函数

$$N_{0,0} = N_{1,0} = 0$$

$$N_{2,0} = \begin{cases} 1 & 0 \leq U < 1 \\ 0 & \text{otherwise} \end{cases}$$

$$N_{3,0} = N_{4,0} = 0$$

$$N_{0,1} = 0$$

$$\begin{aligned} N_{1,1} &= \frac{U_3 - U}{U_3 - U_2} \cdot N_{2,0} \\ &= \frac{1-U}{1} = \begin{cases} 1-U & 0 \leq U < 1 \\ 0 & \text{otherwise} \end{cases} \end{aligned}$$

$$\begin{aligned} N_{2,1} &= \frac{U - U_2}{U_3 - U_2} \cdot N_{2,0} \\ &= \begin{cases} U & 0 \leq U < 1 \\ 0 & \text{otherwise} \end{cases} \end{aligned}$$

$$N_{3,1} = 0$$

$$N_{0,2} = \frac{U - U_0}{U_2 - U_0} \cdot N_{2,1} + \frac{U_3 - U}{U_3 - U_1} \cdot N_{1,1} = \begin{cases} (1-U)^2 & 0 \leq U < 1 \\ 0 & \text{otherwise} \end{cases}$$

$$N_{1,2} = \frac{U - 0}{1 - 0} \cdot N_{1,1} + \frac{1-U}{1-0} \cdot N_{2,1} = \begin{cases} 2U(1-U) & 0 \leq U < 1 \\ 0 & \text{otherwise} \end{cases}$$

$$N_{2,2} = \frac{U - 0}{1 - 0} \cdot N_{2,1} + \frac{1-U}{1-1} \cdot N_{3,1} = \begin{cases} U^2 & 0 \leq U < 1 \\ 0 & \text{otherwise} \end{cases}$$

$$N_{0,3} = \frac{U - U_0}{U_3 - U_0} \cdot N_{0,2} + \frac{U_4 - U}{U_4 - U_1} \cdot N_{1,2}$$

$$= U \cdot N_{0,2} + (1-U) \cdot N_{1,2}$$

$$= \begin{cases} 3U(1-U)^2 & 0 \leq U < 1 \\ 0 & \text{otherwise} \end{cases}$$

$$N_{1,3} = \frac{U - U_1}{U_4 - U_1} \cdot N_{1,2} + \frac{U_5 - U}{U_5 - U_2} \cdot N_{2,2}$$

$$= U \cdot N_{1,2} + (1-U) \cdot N_{2,2}$$

$$= \begin{cases} 3U^2(1-U) & 0 \leq U < 1 \\ 0 & \text{otherwise} \end{cases}$$