# Rationalizing the Payday Loan Puzzle: A Credit Scoring Explanation\*

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#### **Abstract**

Many credit cardholders in the U.S. turn to expensive payday loans, even though they have not yet exhausted their credit lines. This results in significant monetary losses and has been coined the "Payday Loan Puzzle". One proposed but not yet examined explanation is that households use payday loans to protect their credit scores since payday lenders do not report to credit bureaus. To verify this hypothesis, we build a two-asset Huggett-type model with two default options as well as both hidden information and actions. Our calibrated model is the first able to endogenously generate the puzzle. In particular, we can quantitatively account for 40% of the puzzle occurrence and match the magnitude of monetary losses due to this seeming pecuniary mistake. To inform the policy debate over payday lending, we assess the welfare implications of several policy counterfactuals such as banning payday loans or increasing the default costs. The welfare conclusion hinges upon the trade-off between pooling due to unobservable payday loan usage and insurance through payday loans.

**Keywords**: Consumer Credit, Bankruptcy, Default, Payday Loan, Financial Regulation, Type Score, Asymmetric Information, Hidden Action, Cross-Subsidization

**JEL Classifications**: D82, E21, E49, G18, G51, K35

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# 1 Introduction

Why do households take out expensive payday loans while they have far cheaper credit options (e.g., on their credit cards) available? It has been documented that many credit card holders turn to payday loans, even though they have not yet exhausted their card limits. For example, Agarwal, Skiba, and Tobacman (2009) observe that two-thirds of individuals, who use both credit cards and payday loans, have significant liquidity left on their cards. The authors calculate that this "seeming pecuniary mistake" is very costly: these people could have saved on average \$200 by borrowing up to their credit card limits first. In a similar vein, Carter, Skiba, and Tobacman (2011) find monetary losses of a comparable magnitude for individuals using payday loans when cheaper alternatives are available. This phenomenon has been termed the "Payday Loan Puzzle" and a variety of irrational explanations have been put forward, such as self control and financial illiteracy.

The objective of this project is to examine to what extent this at-first-glance puzzling behavior can be explained by the optimal decision of rational and well-informed agents. In particular, the following "reputation protection" mechanism has been proposed:<sup>4</sup>

"Why are people taking out [payday] loans instead of using their cards?" Ranney told me, "This guy was implying that these people weren't smart enough to make the 'right' decision. I laughed in his face. 'They're protecting the card!' I told him. [...]" Whereas failure to repay a payday loan won't affect a consumer's credit score, failure to repay a credit card will.

— Lisa Servon (2017): The Unbanking of America

That is, people do not exhaust their credit card limits because they want to protect their credit score, since payday lenders in the U.S. in general do not report to the credit bureaus

<sup>&</sup>lt;sup>1</sup> A payday loan is an unsecured short-term loan (usually with a duration of a few weeks) for a typically small amount of around \$300. Crucially, it is usually charged with very high interests corresponding to a annualized percentage rate up to several hundred percent.

<sup>&</sup>lt;sup>2</sup> In data, it's not uncommon that payday loan borrowers possess or use credit cards at the same time. For example, Elliehausen and Lawrence (2001) conducted a nationwide survey of a representative sample of 1,000 payday loan users in the U.S. and found that 56.5% of participants having credit cards. Io Data Corporation (2002) found 55% with a survey of 2,600 payday loan borrowers across six states in the U.S. In an online survey by Understanding America Study (UAS) from April 2015 to March 2018, there are 56% of payday loan users using credit cards.

<sup>&</sup>lt;sup>3</sup> In particular, the unused liquidity is more than three times the amount of a typical payday loan \$300 left in available credit lines on their credit cards on the day taking up the first payday loan.

<sup>&</sup>lt;sup>4</sup> Servon was interviewing Tim Ranney, a payday lender, and Ranny was sharing a conversation he had with a risk manager at one of the largest credit card issuers in the U.S.

whereas borrowing or defaulting on credit cards will appear on credit history.<sup>5</sup> People do care about their credit score as it influences credit access, credit cost, mortgage terms, and even job application prospects.

To better understand the reasons behind the occurrence of the payday loan puzzle and to formalize/examine the above hypothesis, we build on the type scoring framework by Chatterjee, Corbae, Dempsey, and Ríos-Rull (2020) which is a Huggett-type model with consumer default and asymmetric information. In their setup, households are subject to idiosyncratic income shocks and can save or borrow bank loans to smooth consumption. They could default on their loans as an additional insurance mechanism. In addition, households differ in their discount factors (called their "types") which influence their default behavior and thus their riskiness as a borrower. Banks provide a borrowing price schedule to each borrower characterized by her credit riskiness. However, banks are unable to directly observe household types. As a result, banks resort to using "type scores" to infer the probability of each individual being the good type based on observable information and update the scores each period via Bayes' rule. A type score thus represents an individual's reputation in the credit markets as credit scores do in practice.

We extend their framework by adding a second asset (payday loans) and a second default option on payday loans exclusively. Thus, in addition to bank loans, households in our model can now also borrow using payday loans which are offered by a second type of financial intermediaries called payday lenders. Now, there are two default choices available: (1) "formal default" where households default on both bank and payday loans; 10 (2) "payday default" where households default on their payday loans only. Payday loans are significantly more expensive than bank loans but, crucially, banks cannot observe the payday loan choices and holdings of households. Payday loans thus introduce hidden actions into the price setting and type score updating problem of banks.

<sup>&</sup>lt;sup>5</sup> A credit score is a statistic that tells lenders how likely a person is to pay back her debts. The most well-known credit score in the U.S. is the FICO score, 35% of which is determined by the payment history and 30% by the debt burden.

<sup>&</sup>lt;sup>6</sup> The workhorse consumer default frameworks were developed by Chatterjee, Corbae, Nakajima, and Ríos-Rull (2007) and Livshits, MacGee, and Tertilt (2007). See also Section 2 for related literature.

<sup>&</sup>lt;sup>7</sup> Note that households themselves can observe their own types.

<sup>&</sup>lt;sup>8</sup> Chatterjee et al. (2020) show that there exists a mapping from type scoring economy to credit scoring economy under some sufficient conditions.

<sup>&</sup>lt;sup>9</sup> Saving using payday loans is not possible. Moreover, we rule out the possibility that households can borrow payday loans while saving at banks. If allowed, households would borrow payday loans to solely protect the access to bank asset markets.

<sup>&</sup>lt;sup>10</sup>This is modeled after Chapter 7 bankruptcy in the U.S.

Essentially, this introduces a trade-off for households between the marginal benefit of maintaining type scores (reputation in the credit markets) versus the marginal cost of borrowing on payday loans instead of cheaper bank loans. The economic intuition behind the type score protection using payday loans is straightforward. Banks cannot observe both households' types and payday loan usage (including payday loan holdings and choices as well as defaulting on payday loans). Hence, households are observationally equivalent to banks along these two dimensions. If a household is hit by a bad income shock and borrows on bank loans to smooth consumption, banks regard this as being solely indicative of impatience, thereby downgrading her type score. On the contrary, taking up payday loans can not only help avoid being misclassified in the current period, but also minimize the chance of lowering her type score if she will default on bank loans in the next period due to another unfortunate financial event.

To quantify the payday loan puzzle documented in Agarwal et al. (2009), we calibrate our model to the whole U.S. population in 2004.<sup>11</sup> Most parameters are exogenously determined by direct emperical evidence or estimates from literature. We internally calibrated the stigma costs for defaults to match the formal and payday default rates. Our calibrated model can account for various untargeted moments. For instance, the salient gap in the average interest rates between bank and payday loans observed in the data.

Our calibrated model can endogenously gives rise to a reputation protection channel: households are willing to incur extra monetary costs by paying higher interest costs in order to maintain their type scores. We can quantitatively account for 40% of the puzzle occurrence identified in the data as well as match the magnitude of the monetary costs, both of which were not targeted in the calibration. In particular, the model's prediction for the average annual monetary costs, \$230, is aligned with the empirical statistic, \$200, calculated by Agarwal et al. (2009).

Since payday loans have been a popular target of legislation in the U.S. in the recent years, it is of great importance to gain a better understanding of how and why households use payday loans as well as in what ways the proposed regulations affect payday loan

<sup>&</sup>lt;sup>11</sup>We choose 2004 as the baseline year for two reasons. First, Agarwal et al. (2009) use the payday loan dataset collected around 2004. The other reason is to avoid the effects of the 2005 bankruptcy reform, which significantly increases the attorney fees for bankruptcy filing.

<sup>&</sup>lt;sup>12</sup>As mentioned, the unaccounted 60% of the puzzle occurrence could be potentially explained by other irrational explanations.

<sup>&</sup>lt;sup>13</sup>Note that these monetary costs refer to the amounts that these puzzling payday loan users could have saved if they firstly max out the cheaper credits on their cards before turning to payday loans over a year.

users and potentially others. Without a thorough understanding, legislation designed to protect households can easily end up harming them. However, the current literature does not offer much guidance for policy makers.<sup>14</sup>

We contribute to this policy debate by using our framework as a laboratory to conduct a series of counterfactual policy experiments. First, we investigate the effects of limiting the maximum payday loan size (a quantity cap) and even outright banning payday loans, respectively. 15 In the former case, we find that this policy change is overall welfare decreasing. However, there is heterogeneity across households: impatient households lose while patient ones gain. The first reason is that in our economy impatient households are more likely to borrow larger payday loans and are thus more affected directly by the quantity cap. In addition, the quantity cap also reduces the amount of information asymmetry in the bank market. 16 This reduces the amount of pooling and in turn leads to a decline in cross-subsidization of impatient by patient households. In contrast to the quantity cap, the policy implementing a full ban on payday loans is in fact welfare decreasing for both types of households. The reason for the welfare loss of patient households is the reduction in available risk-sharing/insurance. <sup>17</sup> In the full ban counterfactual, this loss outweighs the gain for patient households from the reduction in cross-subsidization. These results imply that current regulatory efforts in certain U.S. states to ban payday loans may be misguided in the sense that they end up hurting all households.

Second, we examine the implications of increasing either the formal or payday default cost. The increase in default costs is calibrated to reflect the increase in Chapter 7 filing costs after the 2005 Bankruptcy Abuse Prevention and Consumer Protection Act (BAPCPA) in the U.S.<sup>18</sup> We find that increasing formal default costs leads to a welfare gain whereas increasing payday default costs leads to a welfare loss for households. Theoretically, higher default costs make it harder to *smooth consumption across states* by defaulting but easier to *smooth consumption over time* by borrowing through lower default premia

<sup>&</sup>lt;sup>14</sup>The empirical papers studying the effects of payday loans on consumers are largely divided between finding positive and negative effects. See Section 2 for a more detailed discussion.

<sup>&</sup>lt;sup>15</sup>For the experiment of quantity caps, we restrict the payday loan size by \$300, which denotes the average payday loan size in practice.

<sup>&</sup>lt;sup>16</sup>Recall that banks cannot observe payday loan choices of households.

<sup>&</sup>lt;sup>17</sup>Payday loans are used by both impatient and patient households to smooth idiosyncratic shocks without harming their type scores. See Section 7.1 for a more detailed explanation.

<sup>&</sup>lt;sup>18</sup>Chapter 7 is one of the bankruptcy alternatives available to households in the U.S. It entails the liquidation of non-exempt assets in return for debt dischargement. The 2005 BAPCPA was the most significant reform of bankruptcy law in recent years. Among other changes, it significantly increased the total out-of-pocket filing costs for households. See also Albanesi and Nosal (2020).

(Zame, 1993). In the equilibrium, households prefer smoothing across states by defaulting on payday loans while smoothing over time by borrowing bank loans for three reasons: (1) defaulting on payday loans does not directly affect a household's type score whereas formally defaulting on a bank loan does; (2) interest rates for bank loans are much lower than payday loans; and (3) payday default costs are lower than formal default costs. Higher formal (payday) default cost exactly help (hamper) households in achieving smoothing over time (across states).

The contributions of our paper are fourfold. To our knowledge, we are the first to explicitly model payday loans using a two-asset structure and study its interaction with bank loans and strategic defaulting behavior with two default options.<sup>19</sup> Second, our calibrated model is the first that can generate and quantitatively match the empirically identified payday loan puzzle. Third, we are the first to examine the reputation protection explanation for the payday loan puzzle rigorously in a model. Fourth, we are the first to inform the payday loan policy debate under a full-fledged structural framework where there are hidden information and actions as well as substitution between bank and payday loans.

The rest of the paper is organized as follows. Section 2 gives an overview of the related literature. Section 3 details the model framework. Section 4 presents the calibration of the model. Section 5 illustrates the fundamental mechanism of pooling and cross-subsidization in our framework. In Section 6, we discuss in detail the payday loan puzzle and the reputation protection channel in our model. Section 7 presents the policy experiments and Section 8 concludes with some potential extensions.

## 2 Related Literature

In this section we discuss the literature related to our paper. The consumer finance literature (both empirical and theoretical) is extensive, thus we will only focus here on the papers most directly related to our own. We start with the papers that we build on in terms of methodology and then give a brief summary of the literature on payday loans.

Our theoretical framework is based on the type scoring framework developed by Chat-

<sup>&</sup>lt;sup>19</sup>Until now, there are very few theoretical studies on payday loans (or in general unsecured, small-amount, and expensive loans). See Section 2 for an overview of related papers.

terjee et al. (2020). In their paper, they build on the consumer default workhorse models developed by Chatterjee et al. (2007) and Livshits et al. (2007) in which households save and borrow to achieve consumption smoothing over time. In addition, households are allowed to default on their loans as insurance against idiosyncratic risk. Crucially, both Chatterjee et al. (2007) and Livshits et al. (2007) assume that lenders are fully informed about all household's characteristics that affect repayment in the next period. Chatterjee et al. (2020) depart from this assumption and introduce heterogeneity across households in the form of different discount factors, which is not observable by the banks. As the patience of households affects their loan repayment probability, banks try to infer households' types by computing an individual-specific type score. This score denotes the assessment of individual type by banks based on observable household behavior à la Bayesian updating. Our paper extends their model by introducing a second asset and an additional default option.

Our paper is also closely related to the literature on the seeming pecuniary mistakes in using payday loans. Using matched credit card and payday loan data, Agarwal et al. (2009) document that many borrowers use payday loans when they still have sufficient credit left on their credit cards, even though payday loans carry much higher interest rates. They compute that this behavior is very costly and leads to monetary losses of several hundred US dollar over one year and they coin this finding the "Payday Loan Puzzle". Furthermore, Carter et al. (2011) look at a dataset of credit union members and their payday loan borrowing behavior. They find a pecuniary loss due to usage of payday loans instead of cheaper alternatives similar to the previous paper. We contribute to this literature by generating the payday loan puzzle in a theoretical model for the first time and by offering a rational explanation behind its occurrence.

Payday loans and their effects on consumers are also a hotly debated regulatory topic in the United States. The literature on the effects of payday loans on consumers is in disagreement about its sign. On the one hand, using household panel survey data Zinman (2010) finds that restricting access to payday loans leads consumers to shift to bank overdrafts and late payments. The result is a decline in the financial health of affected households and an overall harmful effect of restricting payday loans. Morse (2011) uses natural disasters to estimate that access to payday lenders leads to welfare increases. Morgan, Strain, and Seblani (2012) find that the banning of payday lending leads to an increase in bounced checks and overdraft fees. These papers stress that payday loans are instru-

mental for households to mitigate the negative effects of transitory income or expenditure shocks, especially when access to the mainstream financial system is impaired. On the other hand, many papers point out that employing such high-cost alternatives can potentially even further worsen the financial situation of these households afterwards. Skiba and Tobacman (2019) estimate that using payday loans significantly increases bankruptcy rates by depressing the cash flow of households. Melzer (2011) finds that access to payday loans worsens the ability of households to pay mortgage, rent and utility bills. Carrell and Zinman (2014) use exogenous variation in payday loan access for military personnel to estimate that usage of payday loans decreases job performance, retention and readiness. Campbell, Martínez-Jerez, and Tufano (2012) find that access to payday lending increases rates of involuntary bank account closures. Our paper contributes to this literature by offering a theoretic framework which jointly models mainstream financial and payday loans as well as their interaction with credit scores. We then use our framework to conduct counterfactual policy exercises, such as banning payday loans, and to investigate the resulting welfare implications for households.

Our paper is also related to Exler (2020). He examines the welfare impact of different alternatives to regulate small dollar loans, such as payday loans, by building and calibrating a quantitative model of unsecured lending where individuals can declare bankruptcy or become delinquent. His findings suggest the scope for possible welfare improving regulation compared to current proposed legislation by the Consumer Financial Protection Bureau (CFPB). In contrast to our approach, he considers only one asset and does not model credit scores. Saldain (2021) considers a model of only payday loans with irrational households and studies the policy regulations on payday lending.

## 3 The Model

Time is discrete and infinite.<sup>20</sup> There is a continuum of measure one rational households populating the economy. Every period, households can survive at rate  $\rho$  and receive persistent earnings e following a stationary finite state Markov process  $Q^e(e'|e)$  and transitory earnings z determined by an i.i.d. process  $Q^z(z)$ . All income realizations are independent across individuals. There is no aggregate uncertainty. There exist two financial intermedi-

<sup>&</sup>lt;sup>20</sup>We follow the convention of dynamic programming that the time subscript is removed and the next-period variable is expressed with prime '.

aries, banks and payday lenders, both of which operate in perfectly competitive markets.

There are two types of households: impatient households with a lower discount factor  $\beta_L$  and patient households with a higher discount factor  $\beta_H$ . A household's discount factor follows a stationary two-state Markov process  $Q^{\beta}(\beta'|\beta)$  and evolves independently across individuals. We call an individual's discount factor her type. Since an individual's type is unobservable to all intermediaries, they would like to infer it using type score s, which denotes the probability of being patient.<sup>21</sup>

At the beginning of each period, if a household has any kind of debt, i.e., either bank debt b < 0 or payday debt p < 0, she can choose to repay both (d = R) or not. There are two default options available: formal default (d = FD) and payday default (d = PD). She can consider formal default to discharge all debts (including potential payday loans). In this case, she is excluded by both lenders in the current period b' = p' = 0 and subject to the out-of-pocket bankruptcy costs  $\kappa_{FD}$  (e.g., attorney fees) and stigma (utility) costs  $\xi_{FD}$ . Alternatively, she may choose payday default (d = PD) to get rid of her payday loan only. In this case, she has to pay the bounced check fees  $\kappa_{PD}$  and endure utility loss  $\xi_{PD}$ . Compare to formal default, she is now excluded from only the payday lending market and potential bank loans b < 0 still need to be repaid but she can retain the access to the bank asset market.

Conditional on whether to repay and to default with which option, households can either borrow or save b' at the discount price  $q_b$  with banking institutions. Furthermore, there exists a second type of financial sector, payday lenders, from which she may also borrow payday loans p' at the discount price  $q_p$ .<sup>23</sup> An individual's consumption c is thus pinned down by her actions (d, b', p'), income (z, e), previous asset/debt holdings (b, p), prices  $(q_b, q_p)$ , type  $\beta$ , and type score s.

Bank intermediaries can observe individuals' persistent earnings e, bank loan holdings and choices (b,b'), and type scores s. We denote (e,b,s) as the bank-observable state  $\omega_b$ . On the contrary, banks cannot observe individuals' transitory earnings z, payday loan positions or choices (p,p'), payday default (d=PD), and discount factors  $\beta$ . As these

<sup>&</sup>lt;sup>21</sup>More on the type score in Section 3.3.1.

<sup>&</sup>lt;sup>22</sup>Formal default is thus modeled as Chapter 7 bankruptcy in the U.S.

<sup>&</sup>lt;sup>23</sup>Borrowing payday loans is allowed only if not saving at banks.

<sup>&</sup>lt;sup>24</sup>Since banks only observe bank loan but not payday loan choices, we assume that they can observe only if formal default d = FD has occurred (i.e., bank loans are not repaid), but that they cannot distinguish between full repayment d = R or payday default d = PD (i.e., whether or not payday loans are repaid).

unobservable variables are relevant for the repayment probability of loans in the next period, banks would like to infer them. While transitory earnings z cannot be inferred by banks as they are i.i.d. across time and households, p, p', d = PD, and  $\beta$  can be inferred.

In terms of bank inference regarding a household's payday loan assets p, we assume that banks are not able to track payday loan holdings at an individual level but know the aggregate distribution of payday loans in the population (rational expectations). As a result, banks exploit the cross-sectional distribution to form their expectation about a household's payday loan assets.<sup>25</sup> As for payday loan and default choices (p', d = PD), they can be filtered out with choice probabilities to obtain the bank-observable choices  $(\tilde{d}, b')$ .<sup>26</sup>

Past actions of a household are informative for inferring its discount factor  $\beta$  since it follows a persistent process. Banks use type scores for this inference. The banks' prior assessment of an individual i's type being patient at the beginning of a given period before any actions is denoted as  $s \equiv \mathbb{P}(\beta_i = \beta_H)$ . Given the bank-observable states  $\omega_b$  and choices  $(\tilde{d},b')$ , banks will update the individual's type score s using Bayes' rule. The posterior type score is denoted as  $s' = \psi_{\beta'_H}^{(\tilde{d},b')}(\omega_b)$  and is transformed to  $Q^s(s'|\psi)$  on the score grid. Thus, the bank loan pricing function  $q_b^{(NFD,b')}(\omega_b)$  will be affected by an individual's choices and observable characteristics, including type scores. <sup>29</sup>

Payday lenders are modeled as more informed than banks—in addition to what banks can observe, payday lenders can of course tell payday loan decisions. The payday loan pricing function  $q_p^{(R,b',p')}(\omega_b)$  thus depends additionally on payday loan choices. For simplicity, we assume payday lenders use the the same type scores as banks to infer households' discount factors.<sup>30</sup> The layout of the economy and the information structure of both lenders are summarized in Figure 1.

<sup>&</sup>lt;sup>25</sup>See Section 3.3.1 for the mathematical details. In principle it is also possible to assume that banks form a joint score over type and payday loan choices  $s(\beta, p)$  for each household.

<sup>&</sup>lt;sup>26</sup>Since banks cannot observe d = PD, they can differentiate only formal default  $\tilde{d} = FD$  from non-formal default  $\tilde{d} = NFD$  consisting of R and PD.

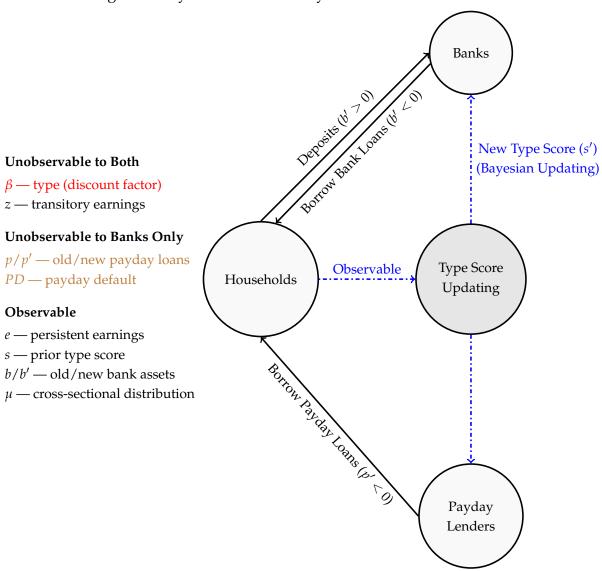
<sup>&</sup>lt;sup>27</sup>As s' may not lie on the score grid, it will be randomly assigned to one of the two nearest points with probabilities proportional to the relative distances of s' from the two adjacent grid points. This assignment is captured by the function  $Q^s(s'|\psi)$ .

<sup>&</sup>lt;sup>28</sup>To be clear, we follow the convention of using the superscript to denote actions and using the collection in parentheses to denote state variables.

<sup>&</sup>lt;sup>29</sup>Note that, compared to most papers in the consumer finance literature, there is no long-term exogenous exclusion imposed in our model.

<sup>&</sup>lt;sup>30</sup>In principle, payday lenders are able to form another type score using their richer information set compared to banks. In reality, they exists another subprime credit score widely used in payday lending industry, called Teletrack. This simplifying assumption is meant to keep computation numerically tractable.

Figure 1: Layout of the Economy and Information Structure



The rest of the section is structured as follows. Section 3.1 summarizes the timing in each period. Section 3.2 details the household's maximization problem. Section 3.3 presents the problems of both financial intermediaries. In particular, type score updating is discussed in Section 3.3.1. Section 3.4 shows the evolution of the cross-sectional distribution of households. In Section 3.5, we close the section by defining the equilibrium.

# 3.1 Timing

The timing in every period is summarized as follows:

- 1. Individuals begin each period with state  $(\beta, z, \omega_b, p)$ .
- 2. Given bank prices  $q_b^{(NFD,b')}(\omega_b)$  and payday prices  $q_p^{(R,b',p')}(\omega_b)$ , individuals choose

to either repay all debts d = R, default on payday loans only d = PD, or formally default on both loans d = FD.

- If d = R, they also choose b' and p' and consume  $c^{(R,b',p')}$ .
- If d = PD, they also choose b' and p' = 0 and consume  $c^{(PD,b',0)}$ .
- If d = FD, they consume the leftover earnings  $c^{(FD,0,0)}$ .
- 3. Based on individual bank-observable choices  $(\tilde{d}, b')$  and states  $\omega_b$ , banks update their type scores from prior s to posterior  $\psi_{\beta'_H}^{(\tilde{d},b')}(\omega_b)$ .
- 4.  $\beta'$ , z', e', and s' are drawn from  $Q^{\beta}(\beta'|\beta)$ ,  $Q^{z}(z')$ ,  $Q^{e}(e'|e)$ , and  $Q^{s}(s'|\psi)$ . Newborn households begin with discount factor  $\beta'$  drawn from the initial distribution  $G_{\beta}$ , transitory earnings z' from  $G_{z}$ , persistent earnings e' from  $G_{e}$ , no bank or payday loan assets (b', p') = (0, 0), and a type score s' consistent with  $G_{\beta}$ .

## 3.2 Households

Individuals take as given the bank and payday loan pricing functions  $q_b^{(NFD,b')}(\omega_b)$  and  $q_p^{(R,b',p')}(\omega_b)$  as well as the type scoring function  $\psi_{\beta_H'}^{(\tilde{d},b')}(\omega_b)$ . Recall that the bank-observable state  $\omega_b \equiv (e,b,s)$  includes persistent earnings e, bank assets b, and prior type score s. Households can choose between repayment (d=R), defaulting on payday loans only (d=PD), or formally defaulting on both bank and payday loans (d=FD).

The value function is thus given by:

$$V(\epsilon, \beta, z, \omega_b, p) = \max_{(d, b', p')} v^{(d, b', p')}(\beta, z, \omega_b, p) + \epsilon^{(d, b', p')}, \tag{1}$$

where  $e^{(d,b',p')}$  denotes the action-specific preference shocks which follow an extreme value distribution with the following cumulative distribution function:

$$EV(\epsilon) = \exp\left\{-\exp\left(-\frac{\epsilon - \mu_{\epsilon}}{\alpha}\right)\right\},\tag{2}$$

where  $\alpha > 0$  determines the variance of the shocks and  $\mu_{\epsilon} = -\alpha \gamma_{E}$  makes the shocks mean zero and  $\gamma_{E}$  is the Euler's constant. Following the discrete choice literature, for each action (d,b',p') and individual, an unobervable additive utilitarian shock  $\epsilon^{(d,b',p')}$  is drawn from a extreme value distribution  $EV(\epsilon)$  with scale parameter  $\alpha$ . These shocks are i.i.d

across both time and individuals. More importantly, they can capture other unobservable heterogeneity that are not explicitly modeled in a reduced but tractable way. With these shocks, policy functions become probabilistic.<sup>31</sup>

The conditional value function is given by:

$$v^{(d,b',p')}(\beta,z,\omega_{b},p) = u\left(c^{(d,b',p')}(z,\omega_{b},p)\right) - \xi_{PD} \cdot \mathbb{I}_{[d=PD]} - \xi_{FD} \cdot \mathbb{I}_{[d=FD]} + \beta \rho \cdot \sum_{(\beta',z',e',s')} Q^{\beta}(\beta'|\beta) \cdot Q^{z}(z') \cdot Q^{e}(e'|e) \cdot Q^{s}(s'|\psi) \cdot W(\beta',z',\omega'_{b},p'),$$
(3)

where utility function defined on consumption u(c) is additively separable over time, continuous, increasing, and concave;  $\xi_{PD}$  and  $\xi_{FD}$  represents the sitigma costs for payday and formal defaults;  $\mathbb{I}$  denotes the indicator function equal to one if the condition in the squared parentheses is true; W is the unconditional value function which will be shortly defined below; and consumption  $c^{(d,b',p')}(z,\omega_b,p)$  is defined as:

$$\begin{cases} e \cdot z + b + p - q_b^{(NFD,b')}(\omega_b) \cdot b' - q_p^{(R,b',p')}(\omega_b) \cdot p', & \text{if } (d,b',p') = (R,b',p') \\ e \cdot z - \kappa_{PD} + b - q_b^{(NFD,b')}(\omega_b) \cdot b', & \text{if } (d,b',p') = (PD,b',0), \\ e \cdot z - \kappa_{FD}, & \text{if } (d,b',p') = (FD,0,0) \end{cases}$$

$$(4)$$

where  $\kappa_{PD}$  and  $\kappa_{FD}$  denotes the out-of-pocket bankruptcy costs for payday and formal defaults, respectively.<sup>32</sup>

Let the set of feasible actions (i.e., positive consumption) be denoted as:

$$\mathcal{F}(z,\omega_{b},p) = \left\{ (d,b',p') | c^{(d,b',p')}(z,\omega_{b},p) > 0 \right\}.$$
 (5)

Note that the noise of extreme value shocks is not the reason why our model is able to generate the payday loan puzzle. In fact, we control for it while identifying the puzzle. Refer to Section 6.1 for details.

<sup>&</sup>lt;sup>32</sup>There are two technical notions worth being mentioned here. First, to avoid the situation where households might hold bank assets while borrowing payday loans for the insurance purpose (i.e., (d = R, b' > 0, p' < 0)), we assume that households can only take up payday loans if they do not save at the banking sector. Second, we assume households do not make any pecuniary mistakes in defaulting. In other words, defaulting is restricted to those who have debts larger than the respective monetary bankruptcy costs. For example, formal default FD is feasible only if  $b + p < -\kappa_{FD}$ .

The standard Logit assumption implies the following choice probabilities:<sup>33</sup>

$$\sigma^{(d,b',p')}(\beta,z,\omega_{b},p) = \begin{cases} \frac{\exp\left\{v^{(d,b',p')}(\beta,z,\omega_{b},p)/\alpha\right\}}{\sum_{(\hat{d},\hat{b}',\hat{p}')\in\mathcal{F}} \exp\left\{v^{(\hat{d},\hat{b}',\hat{p}')}(\beta,z,\omega_{b},p)/\alpha\right\}} & \text{if } (d,b',p') \in \mathcal{F}(z,\omega_{b},p) \\ 0 & \text{otherwise} \end{cases}; \quad (6)$$

and the following unconditional value function:

$$W(\beta, z, \omega_b, p) = \mathbb{E}_{\epsilon} V(\epsilon, \beta, z, \omega_b, p)$$

$$= \alpha \cdot \ln \left( \sum_{(d, b', p') \in \mathcal{F}(\beta, z, \omega_b, p)} \exp \left\{ \frac{v^{(d, b', p')}(\beta, z, \omega_b, p)}{\alpha} \right\} \right). \tag{7}$$

## 3.3 Financial Intermediaries

There are two types of financial intermediaries, banks and payday lenders. Both operate in perfectly competitive markets. They differ in their information set and operating costs. In particular, banks cannot observe payday-related variables whereas payday lenders can.

#### 3.3.1 Banks

Banks have deep pockets so can borrow from the international credit market at risk-free interest rate  $r_f$ . Due to perfect competitiveness, every bank takes pricing schedule  $q_b^{(NFD,b')}(\omega_b)$  and type score updating function  $\psi_{\beta_H'}^{(\tilde{d},b')}(\omega_b)$  as given. The bank's profit  $\pi_b^{(NFD,b')}(\omega_b)$  for a contract (NFD,b') is then given by:

$$\pi_b^{(NFD,b')}(\omega_b) = \begin{cases} \rho \cdot \frac{\mathbb{P}_b^{(NFD,b')}(\omega_b) \cdot (-b')}{1 + r_f} - q_b^{(NFD,b')}(\omega_b) \cdot (-b') & \text{if } b' < 0\\ q_b^{(NFD,b')}(\omega_b) \cdot b' - \rho \cdot \frac{b'}{1 + r_f} & \text{if } b' \ge 0 \end{cases}$$
(8)

where  $\rho$  is the survival probability and  $\mathbb{P}_b^{(NFD,b')}(\omega_b)$  denotes the probability of repayment of a contract (NFD,b') for an individual with bank-observable state  $\omega_b$ . Given perfect competition and constant returns to scale in lending, optimization by banks implies for

<sup>&</sup>lt;sup>33</sup>See, for example, Rust (1987).

each contract that:

$$q_b^{(NFD,b')}(\omega_b) = \begin{cases} \rho \cdot \frac{\mathbb{P}_b^{(NFD,b')}(\omega_b)}{1+r_f} & \text{if } b' < 0\\ \frac{\rho}{1+r_f} & \text{if } b' \ge 0 \end{cases}$$
(9)

In order to determine the probability of repayment tomorrow  $\mathbb{P}_b^{(NFD,b')}(\omega_b)$ , the banking intermediary solves an inference problem since type  $\beta$ , transitory earnings z, utility shock  $\epsilon$ , payday loan holdings and choices (p,p'), as well as the exact choice of repayment or payday default  $(d=PD\vee R)$  are unobserved by the bank. Banks' tasks can be summarized into three steps.

- 1. Filter out a number of unobservable states and actions  $(\epsilon, p, p', R, PD)$  to obtain the bank-observable choice probabilities  $\tilde{\sigma}_b^{(\tilde{d},b')}(\beta, z, \omega_b)$ .
- 2. Assess the probability that an individual is of type  $\beta'$  tomorrow given observable state  $\omega_b$  and choices  $(\tilde{d}, b')$ , i.e.,  $\psi_{\beta'_H}^{\tilde{d}, b'}(\omega_b)$ . Then, assign resulting posterior to type score grid using  $Q^s(s'|\psi)$ .
- 3. Compute for each possible  $\beta'$  the individual's repayment probability given transition over  $\omega_b$  and then use the weighted sum over  $\beta'$  to compute  $\mathbb{P}_b^{(NFD,b')}(\omega_b)$ .

First of all, banks use the standard Logit formula to filter out utility shock  $\epsilon$  and obtain the general choice probabilities  $\sigma^{(d,b',p')}(\beta,z,\omega_b,p)$  in Equation (6). Then, payday loan holdings p can be weighted with the cross-sectional distribution  $\mu$  and sum out payday loan choices p' as follows.

$$\sigma_b^{(d,b')}(\beta, z, \omega_b) = \sum_{p'} \underbrace{\sum_{p} \sigma^{(d,b',p')}(\beta, z, \omega_b, p) \cdot \frac{\mu(\beta, z, \omega_b, p)}{\sum_{\hat{p}} \mu(\beta, z, \omega_b, \hat{p})}}_{=\hat{\sigma}_b^{(d,b',p')}(\beta, z, \omega_b)}$$
(10)

where the last fraction denotes the marginal distribution of p conditional on  $(\beta, z, \omega_b)$ . Finally, form the probability of formal default  $\tilde{d} = FD$  versus non-formal default  $\tilde{d} = NFD$  to obtain the bank-observable choice probabilities.

$$\tilde{\sigma}_b^{(\tilde{d},b')}(\beta,z,\omega_b) = \begin{cases} \sigma_b^{(d,b')}(\beta,z,\omega_b) & \text{if } \tilde{d} = FD\\ \sum_{d \in \{R,PD\}} \sigma_b^{(d,b')}(\beta,z,\omega_b) & \text{if } \tilde{d} = NFD \end{cases}$$
 (11)

Accordingly, the feasible set from the bank's perspective can be defined as:

$$\tilde{\mathcal{F}}_b(\beta, z, \omega_b) = \left\{ (\tilde{d}, b') \middle| \tilde{\sigma}_b^{(\tilde{d}, b')}(\beta, z, \omega_b) > 0 \right\}. \tag{12}$$

The intuition behind the different  $\sigma$  variables is as follows: since banks are not able to observe a household's payday loan holdings p and they have rational expectations, they impute the distribution of unobservables conditional on the observables, namely, using the marginal distribution of p conditional on  $(\beta, z, \omega_b)$  to compute the weighted choice probabilities. This yields  $\hat{\sigma}_b$  in Equation (10) based on the objective choice probabilities  $\sigma$  in Equation (6). Furthermore, the payday loan choices p' are also unobservable by the banks. As  $\sigma$  denotes probabilities, banks can simply compute  $\sigma_b$  as in equation (10) to eliminate p'. Finally, banks can not distinguish between payday default (d = PD) and full repayment (d = R). In order to form an expectation of this unobservable choice as  $\tilde{d} = NFD$ , banks compute  $\tilde{\sigma}_b$  in Equation (11).

Second, an individual's type probability distribution in the next period is computed using Bayes rule and transitory earnings z is weighted with its i.i.d. distribution  $Q^z(z)$ . The type scoring function  $\psi_{\beta_H'}^{(\tilde{d},b')}(\omega_b)$  is computed as:<sup>34</sup>

$$\psi_{\beta'_{H}}^{(\tilde{d},b')}(\omega_{b}) = \begin{cases} \sum_{z} Q^{z}(z) \cdot \sum_{\beta} Q^{\beta}(\beta'|\beta) \cdot \frac{\tilde{\sigma}_{b}^{(\tilde{d},b')}(\beta,z,\omega_{b}) \cdot s(\beta)}{\sum_{\hat{\beta}} \tilde{\sigma}_{b}^{(\tilde{d},b')}(\hat{\beta},z,\omega_{b}) \cdot s(\hat{\beta})} & \text{for } (\tilde{d},b') \in \tilde{\mathcal{F}}_{b} \\ \sum_{\beta} Q^{\beta}(\beta'|\beta) \cdot s(\beta) & \text{for } (\tilde{d},b') \notin \tilde{\mathcal{F}}_{b} \end{cases}$$

$$(13)$$

where  $s(\beta_L)=1-s$  and an infeasible action is updated with prior and exogenous type transition in an uninformative way. Hence,  $\psi_{\beta_H'}^{(\tilde{a},b')}(\omega_b)$  denotes the posterior type score s'. As it may not lie on the score grid in computation, we randomly assigned it to one of the two nearest points with probabilities proportional inversely to the relative distances from the two adjacent grid points. This assignment is characterized by the function  $Q^s(s'|\psi)$ . Refer to Appendix A.1 for details.

In the final step, the probability of the next period's repayment of a contract (NFD, b')

<sup>34</sup> Note that  $\psi_{\beta_H'}^{(\tilde{d},b')}(\omega_b) < 1$  and its value is bounded by the transition probability of turning to patience for all  $\omega_b$  and  $(\tilde{d},b')$ .

for the bank is computed as:

$$\mathbb{P}_{b}^{(NFD,b')}(\omega_{b}) = \sum_{(\beta',z',e',s')} s'(\beta') \cdot Q^{z}(z') \cdot Q^{e}(e'|e) \cdot Q^{s} \left(s'(\beta') \middle| \psi_{\beta'}^{(NFD,b')}(\omega_{b}) \right) \\
\left[ \mathcal{W}_{PD}^{b'}(\omega_{b}) \cdot \left(1 - \sigma^{(FD,0,0)}(\beta',z',\omega_{b}',p'=0)\right) + \left(1 - \mathcal{W}_{PD}^{b'}(\omega_{b})\right) \cdot \sum_{p'} \mathcal{W}_{p'}^{(R,b')}(\omega_{b}) \cdot \left(1 - \sigma^{(FD,0,0)}(\beta',z',\omega_{b}',p')\right) \right], \quad (14)$$

where the weighting factor  $W_{PD}^{b'}(\omega_b)$  denotes the probability that a household in a bank-observable state  $\omega_b$  and bank loan choice b' chooses to partially default d = PD in the current period. It is given by:

$$\mathcal{W}_{PD}^{b'}(\omega_b) = \sum_{z} Q^z(z) \cdot \frac{\sum_{\beta} s(\beta) \cdot \sigma_b^{(PD,b')}(\beta, z, \omega_b)}{\sum_{\hat{d} \in \{PD,R\}} \sum_{\beta} s(\beta) \cdot \sigma_b^{(\hat{d},b')}(\beta, z, \omega_b)}.$$
 (15)

In this case, provided that an individual has chosen to default on his payday loans in the current period, the bank realizes the only possible payday loan choice in the next period is zero p' = 0.

Analogously,  $1 - W_{PD}^{b'}(\omega_b)$  gives the probability of choosing full repayment d = R in the current period. As banks do not observe p', they must additionally form an expectation over the individual's payday loan choice. Conditional on full repayment,  $W_{p'}^{(R,b')}(\omega_b)$  denotes the probability of a household choosing a certain payday loan p' and is given by:

$$\mathcal{W}_{p'}^{(R,b')}(\omega_b) = \sum_{z} Q^z(z) \cdot \frac{\sum_{\beta} s(\beta) \cdot \hat{\sigma}_b^{(R,b',p')}(\beta, z, \omega_b)}{\sum_{\hat{p}'} \sum_{\beta} s(\beta) \cdot \hat{\sigma}_b^{(R,b',\hat{p}')}(\beta, z, \omega_b)}.$$
 (16)

#### 3.3.2 Payday Lenders

The payday loan pricing schedule is also endogenously determined by the zero-profit condition due to the assumption of perfect competition.<sup>35</sup> We assume that the payday lending sector cannot observe type  $\beta$  and transitory earnings z but all the others. For simplicity, we assume payday lenders use the same type score as banks to infer individual's hidden

<sup>&</sup>lt;sup>35</sup>This assumption can be justified by: (1) the number of payday loan storefronts are more than the number of McDonald's and Starbucks combined in the U.S (Karger, 2005); (2) Flannery and Samolyk (2005) find that the annual interest rates of payday loans can be accounted by significant fixed operating costs and higher default premia.

type. The repayment probability for a contract (R, b', p') for an bank-observable state  $\omega_b$  is thus given by:<sup>36</sup>

$$\mathbb{P}_{p}^{(R,b',p')}(\omega_{b}) = \sum_{(\beta',z',e',s')} s(\beta') \cdot Q^{z}(z') \cdot Q^{e}(e'|e) \cdot Q^{s}\left(s'(\beta')|\psi_{\beta'}^{(NFD,b')}(\omega_{b})\right) \\
\left(1 - \sum_{d' \in \{FD,PD\}} \sum_{b'' < 0} \sigma^{(d',b'',0)}(\beta',z',\omega_{b}',p')\right), \tag{17}$$

where note that payday lenders have to take into account both formal default FD and payday default PD because payday loans can be discharged in both cases. Moreover, a payday loan can be taken only if she does not save at banks b'' < 0. The payday loan pricing function is thus given by:

$$q_p^{(R,b',p')}(\omega_b) = \rho \cdot \frac{\mathbb{P}_p^{(R,b',p')}(\omega_b)}{1 + r_b},\tag{18}$$

where  $r_b$  denotes the operating costs in the payday lending industry.

## 3.4 Evolution of Distribution

The probability for an individual to move from state  $(\beta, z, \omega_b, p)$  to  $(\beta', z', \omega_b', p')$  is governed by the following mapping:

$$T^{*}(\beta', z', \omega_{b}', p'|\beta, z, \omega_{b}, p)$$

$$= \rho \cdot Q^{\beta}(\beta'|\beta) \cdot Q^{z}(z') \cdot Q^{e}(e'|e) \cdot \sigma^{(d,b',p')}(\beta, z, \omega_{b}, p) \cdot Q^{s}\left(s'(\beta')|\psi_{\beta'_{H}}^{(\tilde{d},b')}(\omega_{b})\right)$$

$$+ (1 - \rho) \cdot G_{\beta}(\beta') \cdot G_{z}(z') \cdot G_{e}(e') \cdot \mathbb{1}_{b'=0} \cdot \mathbb{1}_{s'=G_{\beta}} \cdot \mathbb{1}_{p'=0}.$$

$$(19)$$

The second line describes the transition of surviving households while the third line describes the birth of newborn households. Therefore, the cross-sectional distribution  $\mu$  evolves according to:

$$\mu'(\beta', z', \omega_b', p') = \sum_{(\beta, z, \omega_b, p)} T^*(\beta', z', \omega_b', p' | \beta, z, \omega_b, p) \cdot \mu(\beta, z, \omega_b, p). \tag{20}$$

<sup>&</sup>lt;sup>36</sup>Note that the current payday loan holdings are not predictive of payday default in the next period.

# 3.5 Equilibrium

A stationary Recursive Competitive Equilibrium (RCE) is a set of (un)conditional value functions  $v^*$  and  $W^*$ , bank loan pricing functions  $q_b^*$  and repayment probability  $\mathbb{P}_p^*$ , payday loan pricing functions  $q_p^*$  and repayment probability  $\mathbb{P}_p^*$ , a type scoring function  $\psi^*$ , choice probability functions  $\sigma^*$  and  $\tilde{\sigma}_b^*$ , and a distribution  $\overline{\mu}^*$  such that:

- 1. Optimality:  $v^{*(d,b',p')}(\beta,z,\omega_b,p)$ ,  $W^*(\beta,z,\omega_b,p)$ , and  $\sigma^{*(d,b',p')}(\beta,z,\omega_b,p)$  satisfy Equation (3), (7), and (6) for all  $(\beta,z,\omega_b,p)$ , respectively.
- 2. Type Score Updating:  $\psi_{\beta'_H}^{*(\tilde{d},b')}(\omega_b)$  and  $\tilde{\sigma}_b^{*(\tilde{d},b')}(\beta,z,\omega_b)$  satisfy (13) and (11) for all  $(\beta,z,\omega_b)$ , respectively.
- 3. Zero Profits for Bank Lenders:  $q_b^{*(NFD,b')}(\omega_b)$  and  $\mathbb{P}_b^{*(NFD,b')}(\omega_b)$  satisfy Equation (9) and (14) for all  $\omega_b$ , respectively.
- 4. Zero Profits for Payday Lenders:  $q_p^{*(R,b',p')}(\omega_b)$  and  $\mathbb{P}_p^{*(R,b',p')}(\omega_b)$  satisfy Equation (18) and (17) for all  $\omega_b$ , respectively.
- 5. Stationary Distribution:  $\overline{\mu}^*(\beta, z, \omega_b, p)$  solves (20).

Note that the banking problem requires the knowledge of the cross-sectional distribution of households  $\mu$ . As a result, all equilibrium objects depend on the distribution and solving the model computationally becomes a daunting task. To accelerate the computation, we implement the one-loop algorithm where value functions, type score function, pricing schedules, and the distribution are updated simultaneously in each iteration until convergence. Refer to Appendix B for computational details.

# 4 Calibration

The goal of the paper is to rationalize the payday loan puzzle documented in Agarwal et al. (2009). Given they used a payday loan dataset collected from 2000 to 2004 and to circumvent the effects of the 2005 BAPCPA reform, we set the baseline calibration year to 2004. The model period is one year. We calibrate the model to the whole U.S. population and the median earnings is thus set to \$33,176 in 2004 from the Current Population Survey (CPS).<sup>37</sup> Our strategy for the parameterization is threefold: Standard parameters are

 $<sup>^{37}</sup>$ In particular, \$638 per week × 52 weeks = \$33,176.

Parameter		Value	Target / Source
		0.0127	TI 1 (0004)
Persistence of persistent earnings	$\rho_e$	0.9136	Floden and Lindé (2001)
S.D. to persistent earnings	$\sigma_e^2$	0.0426	Floden and Lindé (2001)
S.D. to transitory earnings	$egin{array}{l}  ho_e \ \sigma_e^2 \ \sigma_z^2 \ G_e \end{array}$	0.0421	Floden and Lindé (2001)
Persistent earnings at birth	$G_e$	(1,0,0)	Upward earnings profile
Transitory Earnings at birth	$G_z$	(1/3,1/3,1/3)	Upward earnings profile
Low discount factor	$eta_L$	0.886	Chatterjee et al. (2020)
High discount factor	$eta_H$	0.915	Chatterjee et al. (2020)
Transition from low to high	$Q^{\beta}(\beta_L \beta_H)$	0.013	Chatterjee et al. (2020)
Transition from high to low	$Q^{\beta}(\beta_H \beta_L)$	0.011	Chatterjee et al. (2020)
Discount factor at birth	$G_{\beta}$	(0.72,0.28)	Chatterjee et al. (2020)
CRRA	$\gamma$	2	Standard
Survival probability	$\stackrel{\cdot}{ ho}$	0.975	40 years
Risk-free rate	$r_f$	0.014	Effective interest rate = 4%
Formal default cost	$\kappa_{FD}$	0.02	Albanesi and Nosal (2020)
Payday default cost	$\kappa_{PD}$	0.002	Montezemolo and Wolff (2015)
Operating cost for payday lenders	$r_p$	1.925	Flannery and Samolyk (2005)
S.D. of extreme value shocks	α	0.005	

Table 1: Exogenously Chosen Parameters

taken from the literature, parameters with a direct empirical counterpart are exogenously calibrated, and the rest are internally calibrated to match targeted data moments.

The persistent and transitory earnings processes e and z are taken from Floden and Lindé (2001) because they estimated the processes using wage earnings in the U.S. of the same frequency, within the same periods considered in our paper, and without life-cycle components. We assume the newborn is endowed with the lowest persistent earnings  $G_e$  while with the transitory earnings subject randomly to the estimated process  $G_z$ . These assumptions are meant to capture the fact of low earnings at the early life cycle. Following Chatterjee et al. (2020),<sup>38</sup> we set discount factors to 0.886 and 0.915, respectively. The turn-over rates are  $Q^{\beta}(\beta_L|\beta_H) = 0.013$  and  $Q^{\beta}(\beta_H|\beta_L) = 0.011$ , implying households are more likely to become patient by 20%. The share of newborn's types  $G_{\beta}$  is set to 72% of impatient households. This is consistent with the fact that households are more impatient at the early stage of their life cycle.<sup>39</sup> All are summarized in Table 1.

<sup>&</sup>lt;sup>38</sup>To determine discount factors, Chatterjee et al. (2020) use an affine approximation using the model-generated data to match the means and standard deviations of credit rankings across ages. Our calibrated model can match these moments fairly well.

<sup>&</sup>lt;sup>39</sup>It implies there are 41% of patient and 59% of impatient households in the equilibrium.

Parameter		Value	Target	Data	Model
Formal stigma cost	$\xi_{FD}$	0.02235	Formal default rate	0.99%	0.99%
Payday stigma cost	$\xi_{PD}$	0.00702	Payday default rate (cond.)	29.7%	29.7%

Table 2: Internally Calibrated Parameters

We choose the CRRA parameter to be 2, the standard value in the macro literature. The working life span of people is targeted at 40 years, implying the survival probability of 0.975. The risk-free rate  $r_f$  is 1.4% and implies the effective interest rate of 4% consistent with the commonly used value in the literature. Albanesi and Nosal (2020) estimated the out-of-pocket filing costs for Chapter 7 before the 2005 bankruptcy reform is approximately \$697, implying  $\kappa_{FD}=0.02$ . As Montezemolo and Wolff (2015) pointed out payday defaults in practice involves two bounced checked fees (one by banks and the other by payday lenders, \$35 each), we set the out-of-pocket filing costs for payday defaults  $\kappa_{PD}$  to 0.002. According to Flannery and Samolyk (2005), the average operating costs (without default losses) per two-week payday loan of size \$230 is around \$19, thus implying the annualized operating cost for payday lenders  $r_p$  is 1.925. The dispersion parameter of the extreme value distribution is set to 0.005.<sup>40</sup> Table 1 provides a summary.

We internally calibrate the stigma costs for formal default  $\kappa_{FD}$  and for payday default  $\kappa_{PD}$  jointly in order to match formal default rate and conditional payday default rate. Results are summarized in Table 2. The formal default rate in the data is computed with the total number of non-business Chapter 7 filings from American Bankruptcy Institute (ABI) normalized by the total number of U.S. households in 2004. The conditional payday default rate is taken from Skiba and Tobacman (2018) where the same payday loan data is used. The formal and payday stigma costs are accordingly set to 0.02235 and 0.00702, respectively.

We also evaluate our model fit on a set of untargeted moments standard in the consumer finance literature. The data and model moments are summarized in Table 3.<sup>42</sup> For the fraction of bank loan users in the data, we use the 2004 Survey of Consumer Finances

<sup>&</sup>lt;sup>40</sup>In order to rule out the contribution of extreme value shocks to the payday loan puzzle, we check whether households are making such a seemingly pecuniary mistake with higher values. See Section 6.1. In addition, our value is comparable the those used in Chatterjee et al. (2020).

<sup>&</sup>lt;sup>41</sup>To be specific, the conditional payday default rate refers to the write-off default rate among the bi-weekly payday loan borrowers over a year since they took the first payday loan.

<sup>&</sup>lt;sup>42</sup>Note that for all SCF related data moments, we restrict the sample to households with household heads aged between 20 and 60. We do this since our model does not account for retirement or childhood.

Moment (in %)	Data	Model
W 111 1 D 1		
Households in Debt		
Fraction of bank loan users	20.9	24.26
Fraction of payday loan users	5.61	9.46
Bank debt-to-earnings (cond. on borr.)	11.75	6.48
Interest Rate		
Ave. interest rate for bank loans	9.26	8.56
Ave. interest rate for payday loans	447.88	410.85

Table 3: Untargeted Moments: Data v.s. Model

(SCF) and construct a measure of liquid net worth.<sup>43</sup> We then compute the fraction of households with negative net worth. The fraction of payday loan users is computed with the 2010 SCF since information on payday loans was firstly collected in the 2010 wave. We also compute the bank debt-to-earnings ratio using the 2004 SCF.<sup>44</sup> Bank debt is measured using the same liquid net worth definition as above. Income is computed as wage income as measured in the SCF.

The average interest rate for bank loans is computed as the average credit card interest rate in the 2004 SCF (among those having a positive credit card balance, net of the one-year ahead CPI inflation). We use the payday loan statistics reported in Skiba and Tobacman (2018) to calculate the average interest rate for payday loans, deflated with the one-year ahead CPI inflation. See Appendix C and D for details.

# 5 Pooling and Cross-Subsidization

In our economy, there is hidden information (about a household's type) in addition to hidden actions (a household's payday loan choice is unobservable to banks). Because banks cannot observe households' types and payday loan choices, they cannot design

<sup>&</sup>lt;sup>43</sup>We follow Herkenhoff (2019) in constructing this measure of liquid net worth. It is calculated as the difference between a household's liquid assets, such as checking and savings accounts, and credit card debt. We prefer this measure of net worth as we do not explicitly model illiquid assets such as housing in our framework.

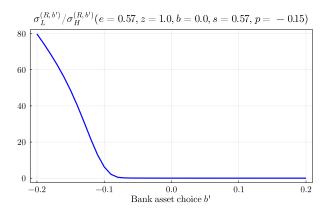
<sup>&</sup>lt;sup>44</sup>More specifically, we compute the ratio of average debt relative to average earnings conditional on having debt.

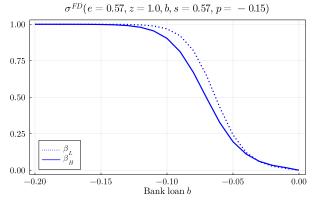
 $<sup>^{45}</sup>$  In particular, the average bi-weekly payday loan size is \$317.55 with average interest payment of \$56.4. It follows that  $\frac{56.4}{317.55} \times \frac{365}{14} \times \frac{1}{1.03388} \times 100 = 447.88\%$ .

Figure 2: Borrowing and Defaulting Behavior Across Types

#### (a) Choice Likelihood Ratio

### (b) Formal Default Probability





contracts that condition on these variables directly.<sup>46</sup> This then leads to two dimensional pooling across household types and payday loans when banks price their loans.<sup>47</sup>

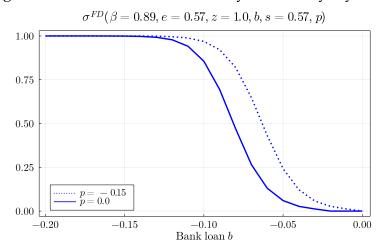
Because our model generates significant heterogeneity in behavior across types and payday loan users, this pooling will in turn lead to cross-subsidization of bank loans between these groups. Figure 2 illustrates these differences in borrowing and defaulting behavior compared across impatient and patient households. In Figure 2a, we can see how impatient households are much more likely to borrow and to borrow more relative to patient households. This is intuitive as households with a lower discount factor value consumption today more and will therefore tend to borrow more. Figure 2b illustrates how the formal default probability varies across levels of debt and household types. It can be seen that the impatient is more likely to formally default than the patient. Consequently, conditional on the same state (and in particular, the same bank loan size), impatient households are riskier borrowers for banks.

Moreover, there are also differences in defaulting behavior across payday loan users. In Figure 3 we can see that, conditional on the same bank loan size, households indebted with extra payday loans are more likely to formally default on both loans. This is straightforward as those with extra payday loans, condition on the same bank loam, have higher total debt burden and thus are more likely to default. Thus, bank loan users who borrow extra payday loans are riskier for banks.

<sup>&</sup>lt;sup>46</sup>As we discussed in Section 3.3.1, banks will instead use type scores and the conditional distribution of payday loans given observed variables.

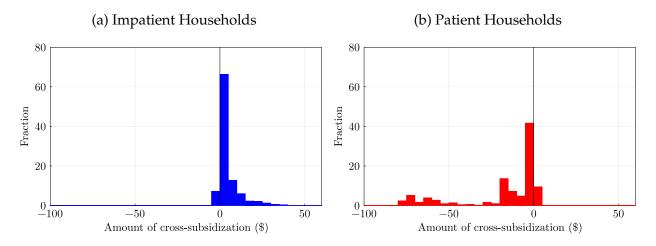
<sup>&</sup>lt;sup>47</sup>For payday lenders, there is only pooling across types since they can of course observe a household's payday loan choice and holding. In this section, we will focus on pooling and cross-subsidization in the bank lending market.

Figure 3: Formal Default Probability Across Payday Loans



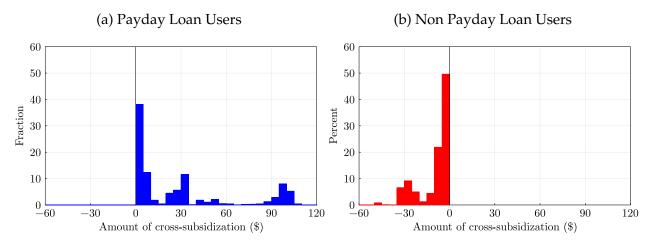
Putting the pooling across types and payday loan users together with differences in default and borrowing behavior between these groups leads to cross-subsidization in the bank loan market. Conditional on the level of bank borrowing, impatient households face lower bank loan rates than actuarially fair rates (i.e. the rates borrowers would face if banks were able to observe households' types). This is shown in Figure 4, where we plot the distribution of cross-subsidization amounts in U.S. dollars across types and one can see that it is mostly impatient households who are cross-subsidized by patient households. This is due to the fact that the impatient tend to be riskier borrowers as they are more likely to default.

Figure 4: Cross-Subsidization of Bank Loans across Types



In addition, there also exists cross-subsidization of bank loans between borrowers who use payday loans and those who do not. Because banks cannot observe payday loan usage by households, borrowers who use payday loans face the same bank loan pricing schedule as borrowers who do not use payday loans. Conditional on the same level of

Figure 5: Cross-Subsidization of Bank Loans across (Non-)Payday Loan Users



bank loan, payday loan users tend to have a higher default probability as they have more total debt. As a result, payday (non-payday) loan users pay rates on bank loans that are lower (higher) than actuarially fair rates (i.e. the rates borrowers would face if banks were able to observe payday loan usage). This is illustrated in Figure 5 where distribution of the difference between the actual and actuarially fair interest rates across payday loan and non-payday loan users is plotted.

Table 4 summarizes the main equilibrium outcomes across types. Compared to patient households, impatient households are more likely to default and borrow, and hold larger debts for both bank and payday loans. This leads to overall higher borrowing costs for the impatient even though they are partially cross-subsidized by patient households as seen above.

Moment (in %)	Aggregate	Impatient	Patient
Default			
Formal default rate	0.99	1.27	0.57
Payday default rate (cond.)	29.7	30.6	27.9
Households in debt			
Fraction of bank loan users	24.26	27.5	19.55
Fraction of payday loan users	9.46	10.7	7.65
Bank debt-to-earnings (cond.)	6.48	6.54	6.36
Payday debt-to-earnings (cond.)	1.91	2.00	1.73
Interest rate			
Ave. interest rate for bank loans	8.56	8.79	8.06
Ave. interest rate for payday loans	410.85	433.89	362.74

Table 4: Equilibrium Across Types

# 6 The Payday Loan Puzzle

The central result of our paper is that our model can offer a rational explanation for the payday loan puzzle observed in the data. In this section, we first illustrate how we identify the payday loan puzzle in our model. Then, we show that our model can account for around 40% of the fraction of puzzle households observed in the data as well as match the magnitude of monetary losses caused by this behavior. In addition, we quantify the type score gains and interest costs from using payday loans and investigate under what circumstances households engage in this kind of puzzle behavior in our model.

## 6.1 Identification of Payday Loan Puzzle

Our calibrated model can generate the payday loan puzzle found in the empirical literature. In the model, we identify the households who make this seeming pecuniary mistakes that are consistent with the payday loan puzzle in the following way: for each possible state  $(\beta, z, \omega_b, p)$ , we identify those feasible borrowing choices with repayment  $(R, b' < 0, p' < 0) \in \mathcal{F}(z, \omega_b, p)$  that involve a payday loan where the same total amount of borrowing  $\hat{b}' = b' + p'$  could have been achieved at lower borrowing costs using bank loans only. That is:

$$\left| q_b^{(NFD,b')}(\omega_b) \cdot b' + q_p^{(R,b',p')}(\omega_b) \cdot p' \right| < \left| q_b^{(NFD,\hat{b}')}(\omega_b) \cdot \hat{b}' \right|. \tag{21}$$

The borrowing choices that fulfil the above condition are choices that we classify as the payday loan puzzle. Let the set of these choices be called  $\mathcal{P}(\beta, z, \omega_b, p)$ .<sup>48</sup>

To illustrate where the region with payday loan puzzle can happen, Condition (21) is visualized in Figure 6, where red line denotes the term on the left-hand side for a given payday loan size p' and blue line represents the term on the right-hand side in Condition

$$v^{(R,b',p')}(\beta,z,\omega_b,p) > v^{(R,\hat{b}',p=0)}(\beta,z,\omega_b,p).$$
 (22)

Hence, there exists the general dependency of  $\mathcal{P}(\cdot)$  on  $\beta$ .

<sup>&</sup>lt;sup>48</sup>Recall that, in a model with taste shocks, any feasible action will be chosen with positive probability (not just the choice with the highest value). As a result, households might take up payday loans because mainly of such shocks. To control for this nuisance, we additionally check whether households are conscious of making this decision with higher values. Specifically, for each state  $(\beta, z, \omega_b, p)$ , the feasible borrowing choices with repayment  $(R, b' < 0, p' < 0) \in \mathcal{F}(z, \omega_b, p)$  where the value of borrowing a certain amount is higher when using payday loans compared to only using bank loans. That is:

Figure 6: Identification of Payday Loan Puzzle

(21). The region of choices satisfying the condition is marked by asterisks and labeled as "Potential Puzzle Area". 49

The central result of the model is the average rate of puzzle occurrence which is computed as the fraction of households that make a choice that would be classified as the payday loan puzzle relative to all households that borrow using both bank and payday loans. More specifically, this rate  $\mathcal{R}$  is calculated as follows in the model:

$$\mathcal{R} \equiv \frac{\sum_{\beta,z,\omega_b,p} \mu(\beta,z,\omega_b,p) \cdot \sum_{(d,b',p') \in \mathcal{P}(\beta,z,\omega_b,p)} \sigma^{(d,b',p')}(\beta,z,\omega_b,p)}{\sum_{\beta,z,\omega_b,p} \mu(\beta,z,\omega_b,p) \cdot \sum_{(d,b',p') \in \mathcal{F}_{both}(z,\omega_b,p)} \sigma^{(d,b',p')}(\beta,z,\omega_b,p)},$$
(23)

where the numerator represents the unconditional fraction of households making the puzzle behavior, called the average likelihood of puzzle occurrence; the feasible set of borrowings choices using both loans  $\mathcal{F}_{both}(z, \omega_b, p)$  is defined as:

$$\mathcal{F}_{both}(z,\omega_b,p) \equiv \{(d,b',p') | (d=R,b'<0,p'<0) \in \mathcal{F}(z,\omega_b,p) \}.$$
 (24)

Table 5 shows the average likelihood and rate of puzzle occurrence across types. Our model can account for a significant fraction of puzzle households identified in the data. In the model, the average rate of puzzle occurrence is around 26.44%. Using a matched credit card and payday loan dataset, Agarwal et al. (2009) have found that the corresponding moment amounts to around two-thirds. That is, our model can account for about 40% of the payday loan puzzle found in the data.

<sup>&</sup>lt;sup>49</sup>In fact, Condition (22) is pretty weak as almost all borrowing choices using both loans are fulfilled. Please refer to Figure in Appendix.

Moment	Aggregate	Impatient	Patient
Average likelihood of puzzle occurrence	2.28	1.50	0.78
Average rate of puzzle occurrence	26.44	25.55	28.31

Table 5: Payday Loan Puzzle Across Types

Our model can also match the magnitude of monetary losses from the payday loan puzzle (the price of type score/reputation protection). Figure 7 shows the distribution of the corresponding monetary losses in both data and our model. We can see that the magnitude of the losses amount to a level very similar to the one observed in the data. In the subsequent discussions, we label households choosing puzzle actions as "puzzle users". We use "non-puzzle users" to instead denote the both loan users who do not make the seeming pecuniary mistakes.

40
30
10
0
1-50
51-100
100-150
151-200
201-300
300-500
500+
Losses (\$)

Figure 7: Histogram of Monetary Costs of Payday Loan Puzzle

Data source: Agarwal et al. (2009).

# **6.2** The Reputation Protection Channel

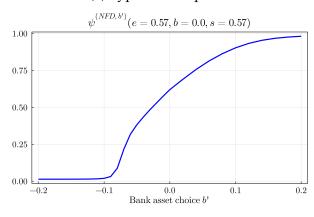
Does the proposed reputation protection hypothesis work theoretically in our model? Yes, because: (1) borrowing more bank loans leads to a lower type score; (2) households with lower type scores face lower discounted bank loan prices. Hence, households have an incentive to borrow using payday loans instead of bank loans in order to avoid a negative impact on their type scores, thus giving them access to cheaper bank credit in the future.

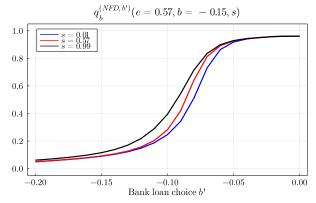
Figure 2 and 8 illustrate how this mechanism works. Figure 2a and 8a explains the first point. In Figure 2a, we could see how impatient households are more likely to borrow and

Figure 8: Reputation Protection Incentive

#### (a) Type Score Update

#### (b) Bank Loan Discounted Price Schedule





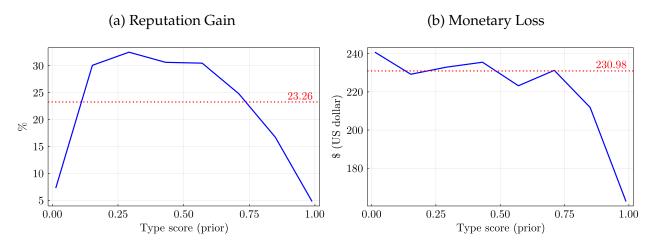
to borrow more relative to patient households. Figure 8a illustrates how this difference in borrowing behavior translates into different type scores. As banks realize that the impatient is more likely to borrow, they will also assign a lower type score to households who borrow more bank loans (ceteris paribus). The second point is shown in Figure 2b and 8b. Figure 2b illustrated how low types are more likely to formally default across different levels of debt. This in turn leads to heterogeneity in bank loan discounted price schedules across types as shown in Figure 8b. Banks will charge households of lower type scores, who are more likely to be of low type, with lower discounted prices (higher interest rates) in order to be compensated for the additional default risk.

Figure 9 looks at the trade-off between type score protection and monetary costs (extra interest payments) for puzzle users. First of all, Figure 9a illustrates the reputation gain of puzzle users compared to the counterfactual where they were to use only bank loans conditional on prior type scores. There exists significant heterogeneity dependent on priors. Particularly, the gain is even over 30% for those who have lower medium type scores. On the other hand, Figure 9b calculates the interest losses relative to the case if they were to firstly borrow using bank loans in U.S. dollars. Such pecuniary losses are significant. Those with lowest type scores are willing to pay extra \$240 for achieving higher posterior type scores than the ones if there were to be fully indebted in bank loans. On average, puzzle users are willing to pay extra \$230 interest payments in exchange for a increase in

<sup>&</sup>lt;sup>50</sup>The hump shape results from the fact that prior dominates in the type score updating at both ends (i.e., when banks believe a households to be a certain type).

<sup>&</sup>lt;sup>51</sup>If we express these monetary losses in percentage points (relative to the counterfactual), it also exhibits hump-shaped.

Figure 9: Cost-Benefit Analysis among Puzzle Users



type scores by 23%. This is aligned with the average magnitude of the monetary losses reported in Agarwal et al. (2009) where the average losses are around \$200.

#### 6.3 Profile of Puzzle Users

In the previous subsection, we illustrated how using payday instead of bank loans can lead to significant type score (i.e., reputation in the credit markets) gains at the cost of substantially increased interest costs. In this subsection, we further investigate when households engage in this puzzle behavior (i.e., puzzle users).

The first result is that households engage in puzzle behavior when they have medium to high persistent earnings but low transitory earnings in our model. This is illustrated in Figure 10, where Figure 10a depicts the distribution of persistent earnings conditional on puzzle versus non-puzzle users (the same for transitory earnings in Figure 10b). Compared to non-puzzle users, who possess both relatively low persistent and transitory earnings, puzzle users have higher persistent but lower transitory earnings.

These results indicate that puzzle users borrow using payday loans to smooth out the shortfall in transitory earnings without damaging theirs type scores too much (such a trade-off has been explained in Figure 9). Recall that persistent earnings are observable to banks, whereas transitory earnings are not. Hence, borrowing using bank loans to smooth out a negative transitory earnings shocks while having high persistent earnings will lead to a downgraded type score more severely. This is illustrated in Figure 11 which shows the type score updating for different bank asset choices across persistent earnings (similar to

Figure 10: Earnings Distribution among Puzzle Users

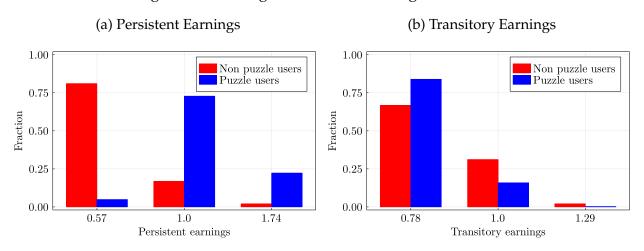
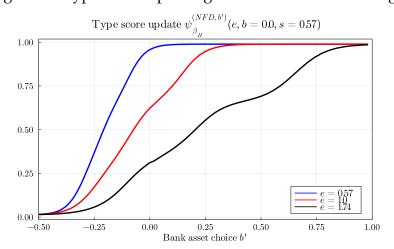


Figure 2b). The intuition is simple: borrowing a lot is more indicative of impatience (low discount factor) when having high compared to low persistent earnings because banks think those with higher persistent earnings are not supposed to borrow that much. Instead, by complementing bank loans with payday loans, which are unobservable to banks, households can reduce the negative impact on their type scores while still being able to smooth out the transitory earnings shocks.

Figure 11: Type Score Updating Across Persistent Earnings



# 7 Policy Experiments

Our rich framework allows us to simulate policy counterfactuals and investigate the (potentially heterogeneous) welfare implications. In this section, we consider two different policy experiments that are highly relevant in the consumer credit market: policies cur-

Variables (in %)	Benchmark	Quantity Cap	Full Ban
Formal Default Rate	0.99	0.96	0.89
Payday Default Rate	2.81	2.19	_
Eff. Cond. Payday Default Rate	34.68	31.24	_
Fraction of Bank Loan Users	24.26	24.06	23.15
Fraction of Payday loan Users	9.46	8.22	_
Bank Debt-to-Earnings	6.48	6.61	6.84
Ave. Bank Interest Rate	8.56	8.53	8.46
Ave. Payday Interest Rate	410.85	341.88	_
Welfare (CEV)	_	-0.0012	-0.0291
Welfare (CEV) – Impatient Households	_	-0.0029	-0.0331
Welfare (CEV) – Patient Households	_	0.0013	-0.0233

Table 6: Policy Counterfactual: Restricting Payday Loan Size

tailing (or outright banning) payday loans and bankruptcy law regulation.

## 7.1 Payday Loan Regulation

Payday loans have been a subject of intensive public debate. Opponents of payday loans have long argued that payday lenders prey on poor households and should be banned. Advocates emphasized the role of payday loans in smoothing consumption and claimed that regulating payday loans would lead the needy to alternatives carrying even higher interest rates.

We contribute to this debate by investigating the welfare implications of limiting access to payday loans through quantity caps or an outright ban on payday loans in our model. Table 6 summarizes the key results of these policy counterfactuals where we report the key moments and welfare outcomes measured by the consumption equivalent variation (CEV) relative to the benchmark in percentage points. The column "Quantity Cap" denotes the counterfactual where the possible payday loan choices are limited to the smallest possible payday loan of size \$300 in the benchmark economy. The column "Full Ban" describes the counterfactual where payday loans become unavailable in the economy.

Compared to the benchmark, a quantity cap leads to a lower fraction of payday loan users as there are less payday loan choices available. It also leads to a decrease in the

 $<sup>^{52}\$300</sup>$  is also the average payday loan size in practice.

(unconditional) payday default rate to 2.2% since it becomes less advantageous to default on smaller payday loans.<sup>53</sup> The unconditional payday default rate also drops mechanically as there are less payday loan borrowers. In addition, it can be easily seen that the conditional effective default rate on payday loans also decreases from around 34.68% in the benchmark to 31.24%. Accordingly, the average payday interest rate decreases. The formal default also decreases slightly and as such there is no substitution from payday default to formal default as a consequence of the payday loan cap. This in turn gives rise to a mild decrease in average bank interest rate. Surprisingly, the *extensive margin* of bank loan borrowing also decreases: the fraction of bank loan users drops slightly. The lack of an increase in the extensive margin of bank loan users is explained by the fact that most payday loan users were already borrowing bank loans in the benchmark economy.<sup>54</sup> Instead, limiting the size of payday loans leads to an increase in the *intensive margin* of bank loan usage: conditional on borrowing, bank debt-to-earnings rises. This is because borrowers now partially substitute bank loans for payday loans. In the full ban counterfactual, all of these changes are magnified.

The overall welfare effects of both policy counterfactuals are negative. More interestingly, the welfare implications of experiments are heterogenous across household types. Impatient households lose in terms of welfare whenever the payday loan market becomes more constrained. In contrast, patient households have higher welfare in the quantity cap counterfactual but lower welfare in the full ban counterfactual compared to the benchmark economy. The reasons for the declines in welfare for impatient households are intuitive. Firstly, they are more likely to borrow larger payday loans in the benchmark economy and are thus more affected by the quantity cap/ban, as shown in Figure 12 of the distribution of payday loan size conditional payday loan users across types in the benchmark. In addition, imposing a payday loan quantity cap (or banning them) also reduces the informational asymmetry in the bank market and thus reduces pooling. As we could see in Figure 4, this pooling led to cross-subsidization of impatient households by patient ones in the benchmark economy.<sup>55</sup> The end result is that constraining the payday loan market leads to less subsidization of impatient households by patient households. In turn, this explains the increase in welfare for patient households but the decrease in

<sup>&</sup>lt;sup>53</sup>The monetary filing cost stays the same as in the benchmark economy.

<sup>&</sup>lt;sup>54</sup>There are around 1% of the total population borrowing only payday loans in the benchmark.

<sup>&</sup>lt;sup>55</sup>The average amount of cross-subsidization of impatient households in the bank loan market across three scenarios are: \$4.57 (Benchmark), \$4.09 (Quantity Cap), and \$3.88 (Full Ban). We can clearly see that to the larger extent payday loans are restricted by size the less pooling of bank loans across types there exits.

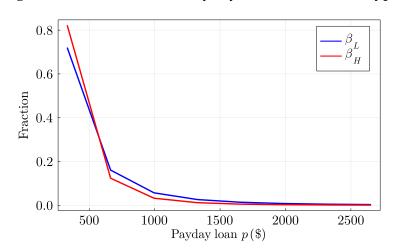


Figure 12: Distribution of Payday Loan Size Across Types

welfare for impatient households in the quantity cap counterfactual.

So what explains the decrease in welfare for patient households when payday loans are fully banned? The answer is that there is a second factor at play apart from cross-subsidization: risk-sharing/insurance. Constraining payday loan choices makes it harder for everyone in the economy, including patient households, to insure against idiosyncratic shocks. When payday loans are quantity capped but still available in the economy, the reduction in cross-subsidization outweighs this loss in insurance for patient households. But patient households do depend on payday loans to smooth shocks, for example in order to reduce the negative effect on type scores of a transitory earnings shock as discussed in Section 6. In the full ban economy, this loss of insurance outweighs the gain from reduced cross-subsidization for patient households. This result implies that in our model fully banning payday loans makes *everyone* worse off.

# 7.2 Bankruptcy Regulation

Another approach to regulation in the consumer finance market taken by policy makers is through bankruptcy laws. The most notable overhaul of bankruptcy regulation in recent years is the Bankruptcy Abuse Prevention and Consumer Protection Act (BAPCPA) in 2005. Among other changes, this legislation increased the total out-of-pocket filing cost for Chapter 7 filings by around 35% (Albanesi and Nosal, 2020). To examine the effect of such an increase in monetary filing cost in our model, we simulate a counterfactual where the formal default cost is increased by 35% (1.35 ×  $\kappa_{FD}$ ). Additionally, we also consider the policy counterfactual where the payday default cost rises by the same magnitude (1.35 ×

Variables (in %)	Benchmark	$1.35 \times \kappa_{FD}$	$1.35 \times \kappa_{PD}$
Formal Default Rate	0.99	0.84	0.99
Payday Default Rate	2.81	3.03	2.60
Eff. Cond. Payday Default Rate	34.68	33.59	33.78
Fraction of Bank Loan Users	24.26	26.25	24.21
	24.26	26.35	
Fraction of Payday loan Users	9.46	10.11	9.07
Bank Debt-to-Earnings	6.48	7.56	6.48
Ave. Bank Interest Rate	8.56	7.51	8.56
Ave. Payday Interest Rate	410.85	395.01	398.23
Welfare (CEV)		0.1236	-0.0032
,	_		
Welfare (CEV) – Impatient Households	_	0.1404	-0.0036
Welfare (CEV) – Patient Households	_	0.0991	-0.0026

Table 7: Policy Counterfactual: Higher Default Costs

 $\kappa_{PD}$ ) to assess the implication of a stricter regulation on payday lending. This allows to fairly compare the roles of bank and payday loans in terms of the efficiency-insurance trade-off. The essential results of these policy counterfactuals are summarized in Table 7.

Focusing first on the increased formal default cost, we can observe that this change leads to a significant decrease in the formal default rate. This is caused by a substitution from formal default to payday default as the payday default rate rises. The drop in the formal default rate leads to a decrease in the average bank interest rate as banks require a lower default premium on their loans. This in turns makes borrowing using bank loans cheaper and increases bank loan borrowing both in terms of the extensive and intensive margins. Interestingly, the increase in bank loan borrowing is not accompanied by a decrease in payday loan borrowing. Rather payday loan usage also increases leading to an overall higher level of debt in the economy. This is because the conditional effective default rate on payday loans actually drops from 34.68% in the benchmark to 33.59%, thus implying cheaper borrowing costs for payday loans.

The explanation for the heterogeneous welfare implications of the two policy experiments is somewhat subtle. In consumer finance models, the key insurance-efficiency trade-off between different bankruptcy regimes/strictness is between *smoothing over time* and *smoothing across states* (Zame, 1993). Smoothing over time means households borrow to achieve consumption smoothing intertemporally while smoothing across states means households could file for bankruptcy to discharge debt burdens under worse earnings re-

alization ex-post. Apparently, more lenient regime makes smoothing across states easier while smoothing over time more costly as higher default premia result in higher borrowing costs.

In the benchmark economy, we can observe that it is much cheaper to achieve smoothing over time using bank loans rather payday loans since the average borrowing costs for bank interest rates are around 50 times cheaper than payday loans. In contrast, it is less costly in terms of type score (reputation) and filing costs to smooth across states using payday loans rather bank loans since payday default is not perfectly captured in type score updating and the fixed filing cost for payday default is ten times less than the one for formal default in the absolute sense. As a result, households tend to borrow bank loans for smoothing over time and payday loans for smoothing across states.

A higher formal filing cost regulates the financial market toward the direction that all would prefer. Essentially, higher  $\kappa_{FD}$  not only renders a stricter regime on bank loans—easier to smooth over time but harder to smooth across states using bank loans—but also indirectly makes it cheaper to borrow payday loans as they can be discharged with formal default as well. Besides, the partial insurance role of payday loans across states are untouched. All lead to welfare gains for both types.

As for the rising filing cost for payday default, the payday default rate drops mechanically associated with a lower average payday loan interest rate. All bank-related variables remain roughly the same except the fraction of bank loan users decreases slightly. Surprisingly, the fraction of payday loan users drops. This in fact echos the way of household using both loans in the benchmark economy—bank loans for smoothing over time and payday loans for smoothing across states. A higher payday default cost makes it harder to smooth across states with payday loans, thus diminishing the major benefit of households from taking up payday loans. Higher payday default costs thus give rise to overall welfare-reducing outcomes.

 $<sup>^{56}\</sup>kappa_{PD} = 0.002 < \kappa_{FD} = 0.02.$ 

<sup>&</sup>lt;sup>57</sup>This argument is also valid across types. As shown in Table 4, the average payday interest rates are far higher than the ones for bank loans for both types.

# 8 Conclusion

One puzzle in the consumer finance literature is the so-called "Payday Loan Puzzle": households use expensive payday loans even when they still have cheaper available alternatives, like their credit cards. One proposed explanation for this behavior is that these households use payday loans in order to protect their credit scores. To investigate this hypothesis, we build a two-asset Huggett-type model with two types of consumer default as well as asymmetric information and hidden actions. Households can be of one of two types: patient or impatient. This household type is unobservable to lenders. Lenders compute a individual-specific type score in order to form an expectation of a household's type. In addition, a household's payday loan choice is also not observable to banks. This then endogenously creates an incentive for households to use payday loans instead of cheaper bank loans in order to protect their type scores.

Our model can successfully replicate the payday loan puzzle observed in the empirical literature and match both the fraction of households that show behavior consistent with the payday loan puzzle as well as the magnitude of the monetary costs. We also illustrate how the reputation protection channel can lead to the emergence of the payday loan puzzle in our model. Furthermore, we conduct a series of policy experiments. We show that restricting the size of payday loans could lead to heterogeneous welfare conclusions while a full ban on payday loans is welfare decreasing for both impatient and patient households. In addition, we also show that increasing the costs of defaulting on payday loans is welfare decreasing whereas increasing the costs of formal default is beneficial in terms of welfare. This implies that current regulatory efforts in the U.S. to curtail or even ban the payday loan sectors may potentially be harmful to households.

In the future, estimating the model with systematic procedures (e.g., SMM) could be desirable. As a result, the policy conclusion could be more robust. However, such an estimation is often constrained by the availability of payday loan data at the individual level. In addition, we are planning to consider a case where banks can observe payday loan usage (as if payday lenders become required to report). This would allow us to more cleanly separate the effect on policy outcomes of pooling across types versus pooling across payday loan users, thus guiding the regulation of payday lending industry.

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# A Theoretical Appendix

## A.1 Additional Type Score Updating Details

As the updated type score  $\psi$  may not lie on the original type score grid, it is randomly assigned to one of the two nearest grid points  $s_i'(\beta')$  and  $s_j'(\beta')$  for all  $\beta'$  with  $s_i'(\beta') \leq \psi_{\beta_H'}^{(\tilde{d},b')} \leq s_j'(\beta')$ , and assign probability  $\chi(\beta'|\psi)$  to  $s_i'(\beta')$  and  $1 - \chi(\beta'|\psi)$  to  $s_j'(\beta')$ , where

$$\chi(\beta'|\psi) = \frac{s_j'(\beta') - \psi_{\beta_H'}^{(\tilde{d},b')}(\omega_b)}{s_j'(\beta') - s_i'(\beta')}, \quad \forall \beta'.$$
(25)

For all s' such that  $s'(\beta') \in \{s'_i(\beta'), s'_j(\beta')\}$  for all  $\beta'$ , the probability of receiving score s' in the next period is thus equal to

$$Q^{s}(s'|\psi) = \prod_{s'(\beta') = s'_{i}(\beta')} \chi(\beta'|\psi) \cdot \prod_{s'(\beta') = s'_{j}(\beta')} (1 - \chi(\beta'|\psi)).$$
 (26)

For all other s',  $Q^s(s'|\psi) = 0$ .

# **B** Computation

# **B.1** Grid Specifications

Variable	Symbol	# Grid points	Range
Danielant armina		2	(0.57.1.00.1.74)
Persistent earnings	e	3	$\{0.57, 1.00, 1.74\}$
Transitory earnings	z	3	$\{0.78, 1.00, 1.29\}$
Bank assets	b	201	[-0.40, 15.00]
Payday loans	p	16	[-0.15, 0.00]
Type scores	S	8	[0.013, 0.989]

Table 8: Grids used in model computation

# **B.2** One-Loop Algorithm

1. Set parameters and tolerances for convergence.

- 2. Create grids for  $(\beta, z, \omega_b, p)$  with lengths  $(n_\beta, n_z, n_\omega, n_p)$  where  $n_\omega = n_e \times n_b \times n_s$ .
- 3. Initialize algorithm with starting guesses:
  - (a)  $W(:,:,:,s,:) = W^{FI}$  for all s where  $W^{FI}$  denotes the unconditional value function under full information.

$$\text{(b)} \ \ \psi_{\beta'_{H}}^{(\tilde{d},b')}(\omega_{b}) = s \cdot Q^{\beta}(\beta_{H}|\beta_{H}) + (1-s) \cdot Q^{\beta}(\beta_{H}|\beta_{L}) \ \text{for all } \omega_{b} \ \text{and } (\tilde{d},b').$$
 
$$\text{i.} \ \ s'_{i} = \max \left\{ s \in \mathcal{S} | s \leq \psi_{\beta'_{H}}^{(\tilde{d},b')}(\omega_{b}) \right\} \ \text{and} \ \ s'_{j} = \min \left\{ s \in \mathcal{S} | s \geq \psi_{\beta'_{H}}^{(\tilde{d},b')}(\omega_{b}) \right\}.$$
 
$$\text{ii.} \ \ Q^{s}\left( s'_{i}(\beta_{H}) | \psi_{\beta'_{H}}^{(\tilde{d},b')}(\omega_{b}) \right) = \frac{s'_{j} - \psi_{\beta'_{H}}^{(\tilde{d},b')}(\omega_{b})}{s'_{i} - s'_{i}} \ \text{and} \ \ Q^{s}\left( s'_{j}(\beta_{H}) | \psi_{\beta'_{H}}^{(\tilde{d},b')}(\omega_{b}) \right) = \frac{\psi_{\beta'_{H}}^{(\tilde{d},b')}(\omega_{b}) - s'_{i}}{s'_{i} - s'_{i}}.$$

- (c)  $q_b^{(NFD,b')}(:,b,s)=q_b^{FI}$  for all b,s where  $q_b^{FI}$  denotes the bank loan price function under full information.
- (d)  $q_p^{(R,b',p')}(:,b,s) = q_p^{FI}$  for all b, s where  $q_p^{FI}$  denotes the payday loan price function under full information.
- (e)  $\mu(:,:,:,s,:) = \frac{1}{n_s} \times \mu^{FI}$  for all s where  $\mu^{FI}$  denotes the cross-sectional distribution of households under full information.

#### 4. Begin the one-loop algorithm:

- (a) Solve for new  $W_1$  taking as given  $W_0$ .
  - i. Find set of feasible actions (d, b', p') using (4).
  - ii. For each  $(\beta, z, \omega_b, p)$ , compute the value  $v^{(d,b',p')}(\beta, z, \omega_b, p)$  for each feasible action (d,b',p') according to (3).
  - iii. Compute new  $W_1$  using (7).
- (b) Compute  $\sigma^{(d,b',p')}(\beta,z,\omega_b,p)$  according to (6).
- (c) Compute new equilibrium functions.
  - i. On bank side:
    - A. Compute  $\tilde{\sigma}_b^{(\tilde{d},b')}(\beta,z,\omega_b)$  using (10) and (11).
    - B. Then  $\psi_{\beta'_H}^{(\tilde{d},b')}(\omega_b)$  using (13).
    - C. Then  $\chi(\beta'|\psi)$  using (25) for all  $\psi$  from previous step.
    - D. Then  $Q^s(s'|\psi)$  using (26) for all  $\psi$  from previously.
    - E. Then  $\mathbb{P}_b^{(NFD,b')}(\omega_b)$  using (14).
    - F. Finally  $q_b^{(NFD,b')}(\omega_b)$  using (9).

- ii. On payday lender side:
  - A. Compute  $\mathbb{P}_p^{(R,b',p')}(\omega_b)$  using (17).
  - B. Then  $q_p^{(R,b',p')}(\omega_b)$  using (18).
- (d) Compute stationary distribution  $\mu_1$  using (20).
- (e) Assess convergence of W,  $\psi$ ,  $q_b$ ,  $q_p$ , and  $\mu$ .
  - i. If achieved, continue to the next step.
  - ii. Otherwise, update the initialization of the targeted objects with relaxation and return to step (a).
- 5. Compute moments.

# C Data Moment Details

**TBC** 

# **D** Model Moment Definitions

The fraction of households choosing to default on payday loans  $\mu(d = PD)$  is defined as:

$$\mu(d = PD) \equiv \sum_{\beta, z, e, b, s, p} \sum_{b'} \sigma^{(PD, b', 0)}(\beta, z, e, b, s, p) \cdot \mu(\beta, z, e, b, s, p). \tag{27}$$

The fraction of households choosing to formally default on both bank and payday loans  $\mu(d=FD)$  is defined as:

$$\mu(d = FD) \equiv \sum_{\beta, z, e, b, s, p} \sigma^{(FD, 0, 0)}(\beta, z, e, b, s, p) \cdot \mu(\beta, z, e, b, s, p). \tag{28}$$

The fraction of bank loan users among all households  $\mu(b < 0)$  is defined as:

$$\mu(b < 0) \equiv \sum_{\beta, z, e, b < 0, s, p} \mu(\beta, z, e, b, s, p).$$
 (29)

The fraction of payday loan users among all households  $\mu(p < 0)$  is defined as:

$$\mu(p<0) \equiv \sum_{\beta,z,e,b,s,p<0} \mu(\beta,z,e,b,s,p). \tag{30}$$

The fraction of bank or payday loan users  $\mu(b < 0 \lor p < 0)$  is defined as:

$$\mu(b < 0 \lor p < 0) \equiv \sum_{\beta, z, e, b < 0, s, p < 0} \mu(\beta, z, e, b, s, p).$$
(31)

The fraction of both loan users  $\mu(b < 0 \land p < 0)$  is defined as:

$$\mu(b < 0 \land p < 0) \equiv \sum_{\beta, z, e, b < 0, s, p < 0} \mu(\beta, z, e, b, s, p). \tag{32}$$

The debt-to-income ratio for banks loans  $DI_b$  is defined as:

$$DI_{b} \equiv \sum_{\beta,e,b<0,s,p} \left(\frac{|b|}{e}\right) \cdot \frac{\mu(\beta,e,b,s,p)}{\sum_{\hat{\beta},\hat{e},\hat{b}<0,\hat{s},\hat{p}} \mu(\hat{\beta},\hat{e},\hat{b},\hat{s},\hat{p})}.$$
 (33)

The debt-to-income ratio for payday loans  $DI_p$  is defined as:

$$DI_{p} \equiv \sum_{\beta,e,b,s,p<0} \left(\frac{|p|}{e}\right) \cdot \frac{\mu(\beta,e,b,s,p)}{\sum_{\hat{\beta},\hat{e},\hat{b},\hat{s},\hat{p}<0} \mu(\hat{\beta},\hat{e},\hat{b},\hat{s},\hat{p})}.$$
 (34)

The total-debt-to-income ratio *DI* is defined as:

$$DI = \sum_{\beta, e, b < 0, s, p < 0} \left( \frac{|b+p|}{e} \right) \cdot \frac{\mu(\beta, e, b, s, p)}{\sum_{\hat{\beta}, \hat{e}, \hat{b} < 0, \hat{s}, \hat{p} < 0} \mu(\hat{\beta}, \hat{e}, \hat{b}, \hat{s}, \hat{p})}.$$
 (35)

The average interest rate for bank loans  $i_b$  is defined as:

$$i_b \equiv \sum_{\beta,\omega_b,p} \sum_{d \in \{R,PD\},b' < 0,p'} \left( \frac{1}{q_b^{(NFD,b')}(\omega_b)} - 1 \right) \cdot \widehat{\sigma \mu}^{(d,b',p')}(\beta,\omega_b,p), \tag{36}$$

where recall that  $\omega_b=(e,b,s)$  and the relative share is defined as:

$$\widehat{\sigma\mu}^{(d,b',p')}(\beta,\omega_b,p) \equiv \frac{\sigma^{(d,b',p')}(\beta,\omega_b,p) \cdot \mu(\beta,\omega_b,p)}{\sum_{\hat{\beta},\hat{\omega}_b,\hat{p}} \sum_{\hat{d}\in\{R,PD\},\hat{b}'<0,\hat{p}'} \sigma^{(\hat{d},\hat{b}',\hat{p}')}(\hat{\beta},\hat{\omega}_b,\hat{p}) \cdot \mu(\hat{\beta},\hat{\omega}_b,\hat{p})}.$$
(37)

The debt-weighted interest rate for bank loans is similarly defined as:

$$i_{b,weighted} \equiv \sum_{\beta,\omega_b,p} \sum_{d \in \{R,PD\},b' < 0,p'} \left( \frac{1}{q_b^{(NFD,b')}(\omega_b)} - 1 \right) \cdot \widehat{\sigma \mu}_{weighted}^{(d,b',p')}(\beta,\omega_b,p), \tag{38}$$

where the relative share is defined as:

$$\widehat{\sigma\mu}_{weighted}^{(d,b',p')}(\beta,\omega_b,p) \equiv \frac{\sigma^{(d,b',p')}(\beta,\omega_b,p) \cdot \mu(\beta,\omega_b,p) \cdot |b'|}{\sum_{\hat{\beta},\hat{\omega}_b,\hat{p}} \sum_{\hat{d} \in \{R,PD\},\hat{b}' < 0,\hat{p}'} \sigma^{(\hat{d},\hat{b}',\hat{p}')}(\hat{\beta},\hat{\omega}_b,\hat{p}) \cdot \mu(\hat{\beta},\hat{\omega}_b,\hat{p}) \cdot |b'|}.$$
(39)

The average interest rate for payday loans  $i_p$  is defined as:

$$i_p \equiv \sum_{\beta,\omega_b,p} \sum_{b',p'<0} \left( \frac{1}{q_p^{(R,p')}(\beta,\omega_b)} - 1 \right) \cdot \widehat{\sigma \mu}^{(R,b',p')}(\beta,\omega_b,p), \tag{40}$$

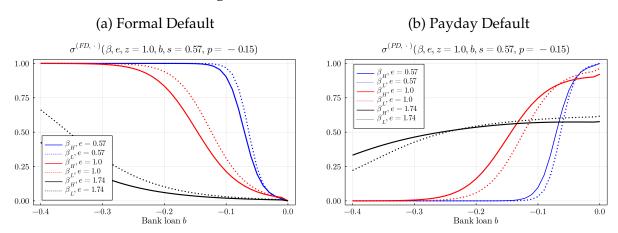
where the relative share is defined as:

$$\widehat{\sigma\mu}^{(R,b',p')}(\beta,\omega_b,p) \equiv \frac{\sigma^{(R,b',p')}(\beta,\omega_b,p) \cdot \mu(\beta,\omega_b,p)}{\sum_{\hat{\beta},\hat{\omega}_b,\hat{p}} \sum_{\hat{b}',\hat{p}'<0} \sigma^{(R,\hat{b}',\hat{p}')}(\hat{\beta},\hat{\omega}_b,\hat{p}) \cdot \mu(\hat{\beta},\hat{\omega}_b,\hat{p})}.$$
(41)

# **E** General Results

Figure 13 depicts how default probabilities vary across (persistent) earnings e and types  $\beta$ . The left-hand side shows how the probability of a household choosing formal default increases as its debt burden grows (b becomes more negative). Households with lower earnings start to formally default at lower debt burdens compared to households with higher earnings. Furthermore, more impatient households ( $\beta_L$ ) also start to formally default at smaller debt levels. In contrast, as can be seen on the right-hand side the probability of payday default decreases as the debt burden grows. This is due to the switching from payday to formal default: As bank loans increase households switch from payday defaulting on their payday loans only to formally defaulting on all debt in order to discharge their larger bank loans. We can see in Figure 13b that this switching starts earlier at lower debt levels for households with less income (black line starts dropping at lower b) and for households that are more impatient (dashed lines drop more quickly than solid lines). This happens because low types are less concerned about the long-term reputational damage from formal default.

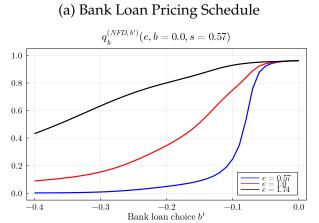
Figure 13: Default Probabilities



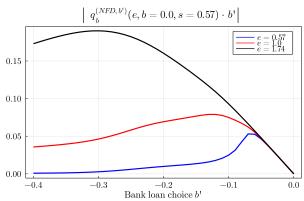
The pricing schedules and the risky borrowing limits of bank and payday loans across earnings in the model are depicted in Figure 14. These results are quite standard in consumer default models. The intuition is clear: On the one hand, borrowing more this period will lead to a higher default probability next period c.p. as the gain from defaulting is larger. As a result we can see in Figure 14a that borrowing more (more negative b') leads to lower prices/higher interest rates. Furthermore, an individual with lower persistent earnings e will face lower prices compared to one with higher e c.p. due to the difference in default probability in the following period. Similarly, the payday loan pricing schedules and the risky borrowing limits across earnings in the model are in the bottom panel. These results are similar to those of bank loans. The significant disparity in levels across bank and payday loans results from the fact that payday lenders have higher operating costs than banks (i,e, higher lending costs).

Figure 15 illustrates what kind of household in our economy saves or borrows. On the left, Figure 15a shows the distribution of savers and borrowers across *persistent* income. Unsurprisingly, savers in our economy tend to have higher (persistent) income compared to borrowers. We can also see that households who use bank loans (either only bank loans or together with payday loans) are overwhelmingly poor (the red bars). Perhaps more interestingly, payday loan users, while still being poor compared to savers, tend to have higher persistent income than bank loan users. On the right, Figure 15b shows the distribution of households across *transitory* income. Compared to Figure 15a it can be seen that payday loan users tend to have lower transitory income than bank loan users. These two figures suggest that the two types of loans are used to smooth different types of income shocks in our model: households use bank loans to smooth persistent income

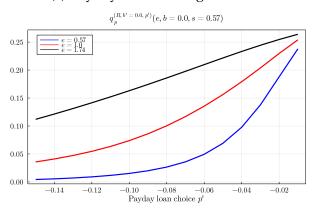
Figure 14: Pricing Schedule and Risky Borrowing Limit Across Persistent Earnings



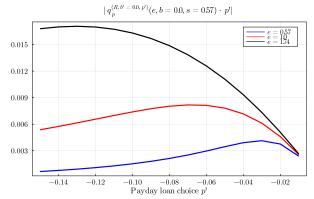
### (b) Bank Loan Risky Borrowing Limit



#### (c) Payday Loan Pricing Schedule



#### (d) Payday Loan Risky Borrowing Limit



shocks whereas payday loans are used to smooth transitory shocks. This makes sense: Payday loans are more expensive than bank loans and are much more costly to smooth a persistent negative income shock. On the other hand, using payday loans does not (directly) affect your type score. As a result, it can make sense to smooth transitory income shocks using payday loans in order avoid long-term reputational damage to a household.

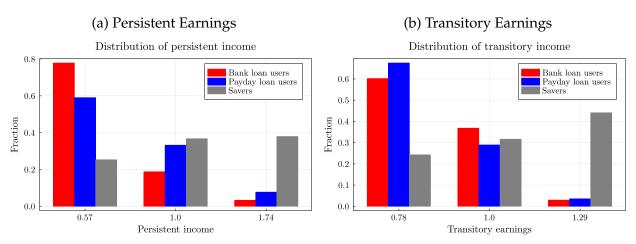


Figure 15: Earnings Distribution among Borrowers/Savers

Figure 16 shows how savers in our economy tend to have higher type scores (more likely to be the patient type from the viewpoint of the bank) compared to borrowers. Interestingly, payday loan users tend to have slightly worse type scores compared to bank loan users.

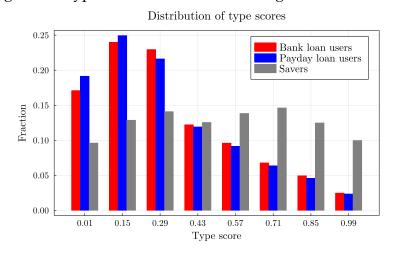


Figure 16: Type Score Distribution among Borrowers/Savers

In addition, puzzle users tend to have lower prior type scores in contrast to non-puzzle users. This is shown in Figure 17 which depicts the type score distribution of puzzle vs. non-puzzle users. We can see that the distribution of prior type scores among different

kinds of borrowers is all skewed to the right. This is because the reputation gain/interest costs for puzzle users are higher/lower for low type score households (see Figure 9).

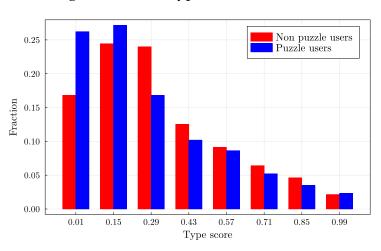


Figure 17: Prior Type Score Distribution

Figure 18 plots the percentage variation in updated type scores relative to priors conditionally for puzzle users (solid line) and if they were to borrow the same amount using instead only bank loans (dotted line). The borrowing portfolio of only banks loans results in overall lower posterior type scores across all priors, compared to using some payday loans.

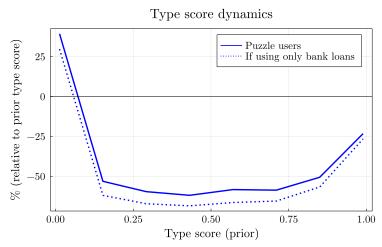


Figure 18: Prior Type Score Distribution