frivol

Generated by Doxygen 1.8.1.2

Thu May 23 2013 22:48:12

Contents

1	Clas	s Index		1
	1.1	Class I	Hierarchy	1
2	Clas	s Index		3
	2.1	Class I	ist	3
3	Clas	s Docu	mentation	5
	3.1	frivol::fe	ortune::Algorithm< PolicyT > Class Template Reference	5
		3.1.1	Detailed Description	5
		3.1.2	Constructor & Destructor Documentation	5
			3.1.2.1 Algorithm	6
		3.1.3	Member Function Documentation	6
			3.1.3.1 getSweeplineY	6
	3.2	frivol::fe	ortune::Arc Struct Reference	6
	3.3	frivol::c	containers::Array< T > Class Template Reference	6
		3.3.1	Detailed Description	7
		3.3.2	Constructor & Destructor Documentation	7
			3.3.2.1 Array	7
		3.3.3	Member Function Documentation	7
			3.3.3.1 operator[]	7
			3.3.3.2 operator[]	7
			3.3.3.3 resize	7
	3.4	frivol::fe	ortune::BeachLine< PolicyT > Class Template Reference	8
		3.4.1	Detailed Description	8
		3.4.2	Constructor & Destructor Documentation	8
			3.4.2.1 BeachLine	8
		3.4.3	Member Function Documentation	9
			3.4.3.1 getLeftArc	9
			3.4.3.2 getMaxArcCount	9
			3.4.3.3 getOriginSite	9
			3.4.3.4 getRightArc	9
			3 4 3 5 insertArc	q

ii CONTENTS

	3.4.3.6 removeArc	10
3.5	$frivol::containers::priority_queues::DummyPriorityQueue < PriorityT > Class\ Template\ Reference .$	10
3.6	$frivol::containers::search_trees::DummySearchTree < ElementT > Class\ Template\ Reference \ .\ .\ .$	10
3.7	$\label{thm:condt} \textit{frivol} :: \textit{GeometryTraits} < \textit{CoordT} > \textit{Struct Template Reference} \ . \ . \ . \ . \ . \ . \ . \ . \ . \ $	11
	3.7.1 Detailed Description	11
3.8	$\label{eq:frivol::GeometryTraits} \textit{Couble} > \textit{Struct Template Reference} \qquad \dots \qquad \dots \qquad \dots \\$	11
3.9	$\label{eq:fivol::GeometryTraits} \textit{Float} > \textit{Struct Template Reference} \; . \; . \; . \; . \; . \; . \; . \; . \; . \; $	11
3.10	frivol :: GeometryTraitsFloat < CoordT > Struct Template Reference 	12
	3.10.1 Detailed Description	12
3.11	$\textit{frivol} :: \textit{GeometryTraitsImplementedConcept} < \textit{CoordT} > \textit{Class Template Reference} \ . \ . \ . \ . \ . \ . \ . \ . \ . \ $	12
	3.11.1 Detailed Description	12
3.12	$\label{eq:condt} \textit{frivol} :: \textit{Point} < \textit{CoordT} > \textit{Struct Template Reference} $	13
	3.12.1 Detailed Description	13
	3.12.2 Constructor & Destructor Documentation	13
	3.12.2.1 Point	14
3.13	$frivol:: Policy < CoordT, \ EventPriorityQueueT, \ BeachLineSearchTreeT > Struct \ Template \ Reference$	14
	3.13.1 Detailed Description	14
3.14	$frivol::containers::Priority Queue Concept < X, \ Priority T > Class \ Template \ Reference \ \dots \dots \dots$	14
	3.14.1 Detailed Description	14
3.15	$frivol::containers::Search Tree Concept < X, Element T > Class Template Reference \dots \dots \dots$	15
	3.15.1 Detailed Description	15
3.16	$frivol::containers::Stack < T > Class \ Template \ Reference \\ \ \ldots \\ \ \ldots \\ \ \ldots \\ \ \ldots$	16
	3.16.1 Detailed Description	16
	3.16.2 Member Function Documentation	16
	3.16.2.1 push	16
	3.16.2.2 top	16

Chapter 1

Class Index

1.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

frivol::fortune::Algorithm< PolicyT >
frivol::fortune::Arc
$frivol::containers::Array < T > \dots $
$frivol:: for tune :: Beach Line < Policy T > \dots \\ $
$frivol::containers::priority_queues::DummyPriorityQueue < PriorityT> \ \dots \ $
$frivol::containers::search_trees::DummySearchTree < ElementT > \dots $
$\label{eq:frivol::GeometryTraits} frivol:: Geometry Traits < Coord T > \ \dots \$
$frivol:: Geometry Traits Float < Coord T > \dots \dots$
$frivol:: Geometry Traits Float < double > \dots $
$frivol:: Geometry Traits < double > \dots $
$\textit{frivol}:: \textit{GeometryTraitsFloat} < \textit{float} > \dots $
$frivol:: Geometry Traits < float > \dots $
$frivol:: Geometry Traits Implemented Concept < CoordT > \dots $
$ frivol:: Point < CoordT > \dots $
$frivol:: Policy < CoordT, \ EventPriority QueueT, \ BeachLineSearch TreeT > $
$frivol::containers::Priority Queue Concept < X, \ Priority T > \dots \dots$
$frivol::containers::Search Tree Concept < X, \ Element T > \dots \dots$
frivol::containers::Stack < T >

2 Class Index

Chapter 2

Class Index

2.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

frivol::fortune::Algorithm< PolicyT >	5
frivol::fortune::Arc	
Information of an arc in BeachLine	6
frivol::containers::Array< T >	6
frivol::fortune::BeachLine < PolicyT >	8
frivol::containers::priority_queues::DummyPriorityQueue< PriorityT >	
Simple implementation of PriorityQueueConcept	10
frivol::containers::search_trees::DummySearchTree< ElementT >	
Simple implementation of SearchTreeConcept (a wrapper around std::list)	10
frivol::GeometryTraits < CoordT >	11
frivol::GeometryTraits< double >	11
frivol::GeometryTraits< float >	11
frivol::GeometryTraitsFloat < CoordT >	12
frivol::GeometryTraitsImplementedConcept< CoordT >	12
frivol::Point < CoordT >	13
frivol::Policy< CoordT, EventPriorityQueueT, BeachLineSearchTreeT >	14
frivol::containers::PriorityQueueConcept< X, PriorityT >	14
frivol::containers::SearchTreeConcept< X, ElementT >	15
frivol::containers::Stack< T >	16

Class Index

Chapter 3

Class Documentation

3.1 frivol::fortune::Algorithm < PolicyT > Class Template Reference

```
#include <fortune.hpp>
```

Public Types

- typedef PolicyT::Coord CoordT
- typedef Point < CoordT > PointT

Public Member Functions

- Algorithm (const containers::Array< PointT > &sites)
- void step ()

Runs the algorithm one event handling forward.

- CoordT getSweeplineY () const
- bool isFinished ()

Returns true if the algorithm has finished.

void finish ()

Steps the algorithm until the end.

• int getVoronoiVertexCount () const

Returns the number of Voronoi vertices met in the algorithm.

3.1.1 Detailed Description

template < typename PolicyT = DefaultPolicy > class frivol::fortune::Algorithm < PolicyT >

State of Fortune's algorithm.

Template Parameters

PolicyT The algorithm policy to use, instance of Policy template.

3.1.2 Constructor & Destructor Documentation

3.1.2.1 template<typename PolicyT > frivol::fortune::Algorithm< PolicyT >::Algorithm (const containers::Array< PointT > & sites)

Constructs algorithm state.

Parameters

points Reference to the input set of sites. The object must exist throughout the existence of the Algorithm.

3.1.3 Member Function Documentation

3.1.3.1 template < typename PolicyT > PolicyT::Coord frivol::fortune::Algorithm < PolicyT >::getSweeplineY () const

Returns the sweepline Y coordinate of last step(). Undefined return value if step() has not been called yet.

The documentation for this class was generated from the following files:

- /home/topi/unison/Asiakirjat/frivol/frivol/fortune/fortune.hpp
- /home/topi/unison/Asiakirjat/frivol/frivol/fortune/fortune_impl.hpp

3.2 frivol::fortune::Arc Struct Reference

Information of an arc in BeachLine.

```
#include <beach_line.hpp>
```

Public Attributes

Idx site

The index of the site from which the arc originates.

• Idx arc_id

The ID of the arc.

The documentation for this struct was generated from the following file:

• /home/topi/unison/Asiakirjat/frivol/frivol/fortune/beach_line.hpp

3.3 frivol::containers::Array < T > Class Template Reference

```
#include <array.hpp>
```

Public Member Functions

- Array (Idx size)
- Idx getSize () const

Returns the size of the array.

- void resize (ldx size)
- const T & operator[] (Idx index) const
- T & operator[] (ldx index)

3.3.1 Detailed Description

template<typename T>class frivol::containers::Array<T>

Simple fixed-size array.

Template Parameters

The type of stored elements. Should be default constructible.

3.3.2 Constructor & Destructor Documentation

3.3.2.1 template<typename T > frivol::containers::Array < T >::Array (ldx size)

Creates an array with all elements default-constructed.

Parameters

size The size of the array.

3.3.3 Member Function Documentation

3.3.3.1 template < typename T > const T & frivol::containers::Array < T >::operator[] (ldx index) const

Returns reference to an element in the array.

Parameters

index	The zero-based index of the element.
IIIGCX	The Zero based mack of the cichient.

Exceptions

std::out of range | if FRIVOL ARRAY BOUNDS CHECKING is defined and 'index' overflows.

3.3.3.2 template < typename T > T & frivol::containers::Array < T >::operator[] (ldx index)

Returns reference to an element in the array.

Parameters

index	The zero-based index of the element.
-------	--------------------------------------

Exceptions

std::out_of_range if FRIVOL_ARRAY_BOUNDS_CHECKING is defined and 'index' overflows.

3.3.3.3 template < typename T > void frivol::containers::Array < T >::resize (ldx size)

Resizes the array to size. If size decreases the extra elements are removed. If size increases, the new elements are default-constructed. The operation may assign the current elements to a new place, and therefore pointers to the array may be invalidated.

Parameters

size	The new size.

The documentation for this class was generated from the following files:

- /home/topi/unison/Asiakirjat/frivol/frivol/containers/array.hpp
- /home/topi/unison/Asiakirjat/frivol/frivol/containers/array_impl.hpp

3.4 frivol::fortune::BeachLine < PolicyT > Class Template Reference

```
#include <beach_line.hpp>
```

Public Types

- typedef PolicyT::Coord CoordT
- typedef Point < CoordT > PointT

Public Member Functions

- BeachLine (const containers::Array< PointT > &sites, Idx max_arcs)
- Idx getMaxArcCount () const
- std::pair< ldx, ldx > insertArc (ldx site, const CoordT &sweepline_y)
- void removeArc (ldx arc_id)
- Idx getLeftArc (Idx arc_id) const
- Idx getRightArc (Idx arc_id) const
- Idx getOriginSite (Idx arc_id) const

3.4.1 Detailed Description

 $template < typename\ PolicyT > class\ frivol::fortune::BeachLine <\ PolicyT >$

The advancing sweepline of Fortune's algorithm. Consists of parabolic arcs that are defined to be the curves that have equal distances from an input site and from the sweepline. Adjacent arcs are separated by their intersection points called breakpoints.

The arcs of the beach line are identified by numerical arc IDs. The maximum number of arcs in the beach line must be specified in advance.

Template Parameters

PolicyT	The algorithm policy to use, instance of Policy template.
FUILCY I	The algorithm policy to use, instance of Folicy template.

3.4.2 Constructor & Destructor Documentation

3.4.2.1 template<typename PolicyT > frivol::fortune::BeachLine< PolicyT >::BeachLine (const containers::Array< PointT > & sites, Idx max_arcs)

Constructs BeachLine.

Parameters

sites	The input sites for the algorithm.
max_arcs	The number of arcs the beach line must be able to contain.

3.4.3 Member Function Documentation

3.4.3.1 template < typename PolicyT > Idx frivol::fortune::BeachLine < PolicyT >::getLeftArc (Idx arc_id) const Returns the ID of the arc left from given arc.

Parameters

arc_id ID of the arc.

Returns

arc ID of the arc to the left from arc_id, or nil_idx if arc_id is the leftmost arc.

 $3.4.3.2 \quad template < typename \ PolicyT > ldx \ frivol:: for tune :: Beach Line < PolicyT > :: getMaxArcCount (\ \) \ const$

Gets the maximum number of arcs there can be in the beach line. The arc IDs are in 0, ..., getMaxArcCount()-1.

 $3.4.3.3 \quad template < typename \ PolicyT > ldx \ frivol:: fortune:: BeachLine < PolicyT > :: getOriginSite (\ ldx \ arc_id) \ construction | ldx \ arc_id) \ construction | ldx \ arc_id | ldx \ arc_$

Returns the index of the origin site of given arc.

Parameters

arc_id	O of the arc.

3.4.3.4 template < typename PolicyT > Idx frivol::fortune::BeachLine < PolicyT >::getRightArc (Idx arc_id) const Returns the ID of the arc right from given arc.

Parameters

arc_id	ID of the arc.

Returns

arc ID of the arc to the right from arc_id, or nil_idx if arc_id is the rightmost arc.

3.4.3.5 template<typename PolicyT > std::pair< ldx, ldx > frivol::fortune::BeachLine< PolicyT >::insertArc (ldx site, const CoordT & sweepline_y)

Adds arc to the right place in the beach line. The arc ending up under the new arc is split in two.

Parameters

site	The origin site of the arc.
sweepline_y	The Y-coordinate of the sweep line that defines the parabolas.

Returns

pair consisting of the ID of the new arc and the ID of the arc on which it was placed and that was split in two, or nil_idx if the beach line was empty.

Exceptions

std::logic_error | if the maximum number of arcs (getMaxArcCount()) are already in use.

3.4.3.6 template<typename PolicyT > void frivol::fortune::BeachLine< PolicyT >::removeArc (ldx arc_id)

Removes arc from the beach line.

Parameters

```
arc_id | The ID of the arc to remove.
```

The documentation for this class was generated from the following files:

- /home/topi/unison/Asiakirjat/frivol/frivol/fortune/beach line.hpp
- /home/topi/unison/Asiakirjat/frivol/frivol/fortune/beach_line_impl.hpp

3.5 frivol::containers::priority_queues::DummyPriorityQueue< PriorityT > Class Template Reference

Simple implementation of PriorityQueueConcept.

```
#include <dummy_priority_queue.hpp>
```

Public Member Functions

- DummyPriorityQueue (Idx size)
- std::pair< ldx, PriorityT > pop ()
- bool empty () const
- void setPriority (Idx key, PriorityT priority)
- void setPriorityNIL (ldx key)

The documentation for this class was generated from the following files:

- /home/topi/unison/Asiakirjat/frivol/frivol/containers/priority queues/dummy priority queue.hpp
- /home/topi/unison/Asiakirjat/frivol/frivol/containers/priority_queues/dummy_priority_queue_impl.hpp

3.6 frivol::containers::search_trees::DummySearchTree< ElementT > Class Template Reference

Simple implementation of SearchTreeConcept (a wrapper around std::list).

```
#include <dummy_search_tree.hpp>
```

Public Types

typedef std::list< ElementT > ::iterator Iterator

Public Member Functions

template<typename FuncT >
 Iterator search (FuncT func)

The documentation for this class was generated from the following file:

/home/topi/unison/Asiakirjat/frivol/frivol/containers/search_trees/dummy_search_tree.hpp

3.7 frivol::GeometryTraits < CoordT > Struct Template Reference

#include <geometry_traits.hpp>

3.7.1 Detailed Description

template<typename CoordT>struct frivol::GeometryTraits< CoordT>

Traits class that gives needed geometry operations for the algorithm. Implemented traits are required by Policy.

Template Parameters

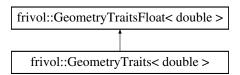
CoordT The coordinate type to use.

The documentation for this struct was generated from the following file:

/home/topi/unison/Asiakirjat/frivol/frivol/geometry_traits.hpp

3.8 frivol::GeometryTraits < double > Struct Template Reference

Inheritance diagram for frivol::GeometryTraits < double >:



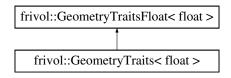
Additional Inherited Members

The documentation for this struct was generated from the following file:

/home/topi/unison/Asiakirjat/frivol/frivol/geometry_traits.hpp

3.9 frivol::GeometryTraits < float > Struct Template Reference

Inheritance diagram for frivol::GeometryTraits < float >:



Additional Inherited Members

The documentation for this struct was generated from the following file:

/home/topi/unison/Asiakirjat/frivol/frivol/geometry_traits.hpp

3.10 frivol::GeometryTraitsFloat < CoordT > Struct Template Reference

```
#include <geometry_traits.hpp>
```

Static Public Member Functions

- static CoordT getBreakpointX (const Point< CoordT > &a, const Point< CoordT > &b, CoordT topy, bool positive_big)
- static CoordT getCircumcircleTopY (const Point < CoordT > &a, const Point < CoordT > &b, const Point < CoordT > &c)
- static bool **isCCW** (const Point < CoordT > &a, const Point < CoordT > &b, const Point < CoordT > &c)

Static Public Attributes

• static constexpr CoordT epsilon = 1e-30

3.10.1 Detailed Description

 $template < typename\ CoordT > struct\ frivol:: Geometry Traits Float < \ CoordT >$

Implementation of GeometryTraits for floating point coordinate types (float and double).

The documentation for this struct was generated from the following files:

- /home/topi/unison/Asiakirjat/frivol/frivol/geometry_traits.hpp
- /home/topi/unison/Asiakirjat/frivol/frivol/geometry_traits_impl.hpp

3.11 frivol::GeometryTraitsImplementedConcept CoordT > Class Template Reference

```
#include <geometry_traits.hpp>
```

3.11.1 Detailed Description

template<typename CoordT>class frivol::GeometryTraitsImplementedConcept< CoordT>

Concept for checking that all required GeometryTraits are implemented for given coordinate type. Required operations are:

- CoordT getBreakpointX(Point<CoordT> a, Point<CoordT> b, CoordT topy, bool positive_big) returns the X coordinate of intersection of the two parabolas defined by (x-a.x)^2 + (y-a.y)^2 = (y-topy)^2 = (x-b.x)^2 + (y-b.y)^2 The function may assume that a.x <= b.x, a.y <= topy and b.y <= topy. The function should choose the solution where the parabola around a goes under the parabola around b. In cases where this does not happen, the result should be very big number, positive if positive_big, otherwise negative.
- CoordT getCircumcircleTopY(Point<CoordT> a, Point<CoordT> b, Point<CoordT> c) returns the Y coordinate of the top point (i.e. highest Y coordinate) of the circumscribed circle around triangle 'abc'. In case of (almost) collinear points, the result should be very big or very small compared to site coordinates.
- bool isCCW(Point<CoordT> a, Point<CoordT> b, Point<CoordT> c) returns true if triangle 'abc' is oriented counterclockwise.

Template Parameters

CoordT	The coordinate type.

The documentation for this class was generated from the following file:

/home/topi/unison/Asiakirjat/frivol/frivol/geometry_traits.hpp

3.12 frivol::Point < CoordT > Struct Template Reference

```
#include <point.hpp>
```

Public Member Functions

- Point (CoordT x, CoordT y)
- Point ()

Constructs point with undefined values as coordinates.

Public Attributes

CoordT x

The X coordinate of the point.

CoordT y

The Y coordinate of the point.

3.12.1 Detailed Description

template<typename CoordT = double>struct frivol::Point< CoordT >

Two-dimensional point.

Template Parameters

CoordT	The coordinate type to use. Should be default constructible. Defaults to double, which is
	the coordinate type of DefaultPolicy.

3.12.2 Constructor & Destructor Documentation

3.12.2.1 template<typename CoordT = double> frivol::Point< CoordT >::Point(CoordT x, CoordT y) [inline]

Constructs point with given coordinates.

Parameters

X	The X coordinate.
У	The Y coordinate.

The documentation for this struct was generated from the following file:

· /home/topi/unison/Asiakirjat/frivol/frivol/point.hpp

3.13 frivol::Policy < CoordT, EventPriorityQueueT, BeachLineSearchTreeT > Struct Template Reference

#include <policy.hpp>

Public Types

• typedef CoordT Coord

3.13.1 Detailed Description

 $template < typename\ CoordT, template < typename\ PriorityT > class\ EventPriorityQueueT, template < typename\ ElementT > class\ BeachLineSearchTreeT > struct\ frivol::Policy < CoordT,\ EventPriorityQueueT,\ BeachLineSearchTreeT >$

Policy class for the Fortune's algorithm, specifying data types and data structures to use.

Template Parameters

•	
CoordT	The coordinate type to use. Should be ordered and default constructible to undefined
	value. Should have specialization of GeometryTraits.
EventQueueT	The priority queue type for events. Must conform to PriorityQueueConcept.
BeachLineT	The search tree to use for the "beach line" of arcs. Must conform to SearchTreeConcept.

The documentation for this struct was generated from the following file:

/home/topi/unison/Asiakirjat/frivol/frivol/policy.hpp

3.14 frivol::containers::PriorityQueueConcept < X, PriorityT > Class Template Reference

#include <priority_queue_concept.hpp>

3.14.1 Detailed Description

 $template < typename\ X,\ typename\ Priority T > class\ frivol::containers::Priority Queue Concept < X,\ Priority T > template < typename\ X,\ Priority T > template\ X,\ Priority T > te$

Concept checking class for priority queues X with priority values of type PriorityT (or NIL). Priority queues are initialized with given size, and contain priority values for keys 0, 1, ..., size-1. Initially, all priority values are NIL. X must support the following operations:

- <construct>(ldx size) creates priority queue for keys 0, 1, ..., size-1.
- · bool empty() const returns true if all keys have NIL priority.
- std::pair<Idx, PriorityT> pop() returns pair of a key with lowest non-NIL priority and its priority and sets the priority to NIL.
- void setPriority(Idx key, PriorityT priority) sets the priority value of 'key' to non-NIL value 'priority'.
- void setPriorityNIL(ldx key) sets the priority value of key 'key' to NIL.

X may assume that PriorityT is ordered with <-operator. X may have undefined behavior if supplied keys are out of range or if pop() is called when empty() returns true.

The documentation for this class was generated from the following file:

· /home/topi/unison/Asiakirjat/frivol/frivol/containers/priority_queue_concept.hpp

3.15 frivol::containers::SearchTreeConcept < X, ElementT > Class Template Reference

```
#include <search_tree_concept.hpp>
```

Public Types

• typedef X::Iterator IteratorT

3.15.1 Detailed Description

template < typename X, typename ElementT > class frivol::containers::SearchTreeConcept < X, ElementT >

Concept checking class for search trees X for elements of type ElementT. Search trees are sequence containers, the elements of which are iterated using iterator objects of type X::Iterator. The iterator must be a standard bidirectional iterator. X must support the following operations:

- <construct>() creates empty search tree.
- · bool empty() const retuns true if the search tree is empty.
- Iterator begin() returns the iterator of the first element (or past-the-end if empty).
- Iterator end() returns the iterator past the last element.
- template<typename FuncT> Iterator search(FuncT func) searches the sequence using the supplied int(lterator)-function that for given iterator iter returns negative if the searched element is before iter, positive if it is after iter, and 0 if iter is the right element. If an element such that func returns 0 is found, it is returned, otherwise end() is returned.
- void erase(Iterator iter) removes element at iter. Other iterators should not be invalidated.
- Iterators insert(Iterator iter, const ElementT& elem) inserts elem before iter and returns the iterator of the new element. Does not invalidate any iterators.

X may assume that ElementT is copy constructible.

The documentation for this class was generated from the following file:

/home/topi/unison/Asiakirjat/frivol/frivol/containers/search tree concept.hpp

3.16 frivol::containers::Stack < T > Class Template Reference

```
#include <stack.hpp>
```

Public Member Functions

• Stack ()

Constructs empty stack.

• bool empty () const

Returns true if the stack is empty.

- T & top ()
- void pop ()

Removes the top element of the stack. Call only if empty() is false.

void push (const T &element)

3.16.1 Detailed Description

template<typename T>class frivol::containers::Stack< T>

Stack of elements.

Template Parameters

The type of stored elements. Should be default constructible.

3.16.2 Member Function Documentation

3.16.2.1 template < typename T > void frivol::containers::Stack < T >::push (const T & element)

Pushes element to the top of the stack.

Parameters

element | The element to push.

3.16.2.2 template<typename T > T & frivol::containers::Stack< T >::top ()

Returns reference to the top element of the stack. Call only if empty() is false.

The documentation for this class was generated from the following files:

- /home/topi/unison/Asiakirjat/frivol/frivol/containers/stack.hpp
- /home/topi/unison/Asiakirjat/frivol/frivol/containers/stack_impl.hpp