

FD-LCS Algorithm 說明

- 1 - FD-LCS Algorithm

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1. FD_LCS( G, L )
2.   for all vertex v in G
3.     find "top", "oper", and "bottom" vertexes;
4.     Ru[v] = its resource-used;
5.   Initialization( top, bottom, A, R, S )
6.   if ( there is no feasible solution )
7.     return "No Feasible";
8.   do
9.     calculate_distribution( oper, A, R, Ru, p, q )
10.    calculate_total_force( G, tF );
11.    find the smallest tF[v, l];
12.    A[v] = l;
13.    R[v] = l;
14.    S[v] = 0;
15.  while ( there are vertexes not yet scheduled )
16.    return outcome;

```

Definition

G : graph

L : latency constraint

top : vertexes in G with in-degree of 0

oper : vertexes in G with in-degree > 0

bottom : vertexes in G with out-degree of 0

Ru[v] : resource used by vertex v in G, including { *, +, ' }

A[v] : arrive time of vertex v in G

R[v] : require time of vertex v in G

S[v] : slack of vertex v in G

p[v, l] : probability density of vertex v in G on cycle l

q[r, l] : distribution of resource r on cycle l

tF[r, l] : total force of resource r on cycle l

We obtain a graph G by parsing a BLIF file illustrated in figure 1. There are vertexes a, b, c, d, ..., p, q in graph G.

Firstly, find those vertexes belong to "top", "oper", "bottom" by traversing all vertexes in G. Then, initializing Ru[v] to the resource used by v, which can be obtained from the logic function of each vertexes.

A table is illustrated in figure 2. This table suggests several informations that this algorithm keeps. Firstly, p[v, l] is a two dimension array with the first dimension indexed by v, which is a vertex in G, and with the second dimension indexed by l, which is a # ranged from 1 to L, where L is the latency constraint. The value of p[v, l] stands for according probability density of vertex v over the cycles l. The color suggests the resource a vertex v used recorded in Ru[v]. The colored marks within each rows indicated arrive time, require time, and slack of the according vertex.

To obtain informations in the table, we initialize arrive time by traversing vertexes starting form "top" in breathe-first-search order; then, we initialize require time and slack by traversing vertexes starting form "bottom" in breathe-first-search order. The details are showed in algorithm: Initialization(top, bottom, A, R, S).

After initialize A, R, S, we can check whether there are some $S[v] < 0$, where v is a vertex in oper. Some $S[v] < 0$ suggests it is not feasible.

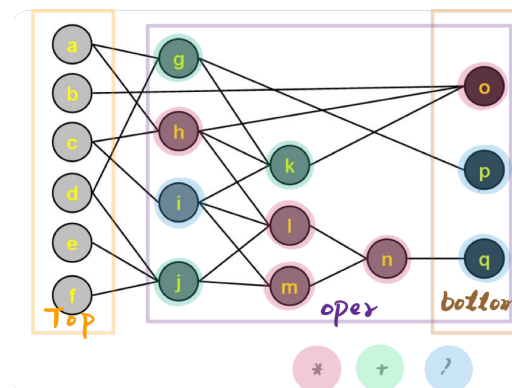


Figure 1. G is a directed graph obtained by parsing a BLIF file. Vertexes using resource "*" are colored in red. Vertexes using resource "+" are colored in green. Vertexes using resource "!" are colored in blue.

P	1	2	3	4	5
g	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$		
h	$\frac{1}{2}$	$\frac{1}{2}$			
i	$\frac{1}{2}$	$\frac{1}{2}$			
j	$\frac{1}{2}$	$\frac{1}{2}$			
k		$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	
l		$\frac{1}{2}$	$\frac{1}{2}$		
m		$\frac{1}{2}$	$\frac{1}{2}$		
n			$\frac{1}{2}$	$\frac{1}{2}$	
o			$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
p			$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$
q				$\frac{1}{2}$	$\frac{1}{2}$

Figure 2. This table suggests informations such as arrive-time, require-time, slack, resource-used of a vertex, probability density. For example, a vertex "g" uses a resource "+", finding an arrive time on cycle 1, a require time on cycle 3, thus, a vertex G accounts for $\frac{1}{3}$ probability density on cycle 1, 2, 3, and likewise are the other vertexes.

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1. Initialization( top, bottom, A, R, S )
2.   push all nodes in "top" paired up with -1 into Q;
3.   while ( Q is not empty )
4.     pop element ( v, c ) from Q;
5.     if c > A[v]
6.       A[v] = c;
7.       for all successors s of v
8.         push ( v, c + 1 ) into Q;
9.   push all nodes in "bottom" paired up with L - 1 into Q;
10.  while ( Q is not empty )
11.    pop element ( v, c ) from Q;
12.    if c < R[v]
13.      R[v] = c;
14.      S[v] = R[v] - A[v]
15.      for all predecessors p of v
16.        push ( v, c - 1 ) into Q;

```

Definition

Q : a FIFO queue whose elements are pairs of a vertex and an int
A[v] : arrive time of vertex v in G
R[v] : require time of vertex v in G
S[v] : slack of vertex v in G

Now it is feasible for sure.

We calculate each resource's distribution on each cycles. For example, a vertex g has a probability density of 1/3 scheduled on cycle 1, and a vertex j has a probability density of 1/2 scheduled on cycle 1 as well. Both of which use resource "+"; thus, there is a 1/3 + 1/2 distribution density of resource "+" on cycle 1. Likewise are other vertexes.

As an analogy to the physical formula: Force = constant * displacement, the mechanism for calculating "total force" is illustrated as follows.

Firstly, $q[r, l]$, where r is a resource, l ranges from 1 to L, is viewed as the constant and $p[v, l]$, where v is a vertex, l ranges from 1 to L, is viewed as the displacement. We define:

$$\begin{aligned}
 selfF[v, l] &= \sum_{l \in \{A[v], A[v]+1, \dots, R[v]\}} q[Ru[v], l] * p[v, l] \\
 &= q[Ru[v], l] - p[v, l] * \sum_{l \in \{A[v], A[v]+1, R[v]\}} q[R[v], l] \\
 &= q[Ru[v], l] - BaseF[v]
 \end{aligned}$$

And the calculation is demonstrated in figure 4. Furthermore, we define $aF[v, l]$, for all v is a vertex in G, and for all l ranges A[v] to R[v], as the force generated by moving R[v] forward to l; likewise, we define $dF[v, l]$, for all v is a vertex in G, and for all l ranges A[v] to R[v], as the force generated by postponing A[v] to l.

$$\begin{aligned}
 aF[v, l] &= \frac{\sum_{i \in \{A[v], \dots, l\}} q[Ru[v], i]}{l - A[v] + 1} - baseF[v] \\
 dF[v, l] &= \frac{\sum_{i \in \{l, \dots, R[v]\}} q[Ru[v], i]}{R[v] - l + 1} - baseF[v]
 \end{aligned}$$

```

1. calculate_distribution( oper, A, R, Ru, p, q )
2.   for all vertex v in oper
3.     for i = A[v] to R[v]
4.       q[Ru[v]] += p[v, i];

```

Definition

oper : vertexes in G with in-degree > 0
A[v] : arrive time of vertex v in G
R[v] : require time of vertex v in G
Ru[v] : resource used by vertex v in G, including { *, +, ' }
p[v, l] : probability density of vertex v in G on cycle l
q[r, l] : distribution of resource r on cycle l

$q(r, l)$	1	2	3	4	5
*	0.5	1.5	1.83	0.83	0.33
+	0.83	1.17	0.67	0.33	0.00
'	0.5	0.75	0.25	0.75	0.75

Figure 3. $q[r, l]$ is a two dimension array with the first dimension indexed by r, a resource-used by vertexes, and with the second dimension indexed by l, a cycle ranged from 1 to L. Suggested in this figure, the resource "*" has distributions of 0.5, 1.5, 1.83, 0.83, 0.33 over cycle 1 to 5, respectively; the resource "+" has distributions of 0.83, 1.17, 0.67, 0.33, 0.00 over cycle 1 to 5, respectively; the resource "'" has distributions of 0.5, 0.75, 0.25, 0.75, 0.75

Array	baseF	selfF(v, l)	1	2	3	4	5
g	$\frac{0.83 + 1.17 + 0.67}{3}$	g	-0.06	0.28	-0.22		
h	$\frac{0.5 + 1.5}{2}$	h	-0.5	0.5			
i	$\frac{0.5 + 1.5}{2}$	i	-0.12	0.12			
j	$\frac{0.83 + 1.17}{2}$	j	-0.17	0.17			
k	$\frac{1.17 + 0.67 + 0.33}{3}$	k		0.44	-0.06	-0.39	
l	$\frac{1.5 + 1.83}{2}$	l		-0.17	0.17		
m	$\frac{1.5 + 1.83}{2}$	m		-0.17	0.17		
n	$\frac{1.83 + 0.83}{2}$	n			0.5	-0.5	
o	$\frac{1.83 + 0.83 + 0.33}{3}$	o			0.33	-0.17	-0.67
p	$\frac{0.75 + 0.25 + 0.75 + 0.75}{4}$	p			0.12	-0.38	0.12
q	$\frac{0.75 + 0.75}{2}$	q				0.00	0.00

Figure 4. $baseF[g] = (0.83 + 1.17 + 0.67) / 3$; $selfF[g, 1] = 0.83 - baseF[g] = -0.06$; $selfF[g, 2] = 1.17 - baseF[g] = 0.28$; $selfF[g, 3] = 0.67 - baseF[g] = -0.22$, and so on. The greater negativity of $selfF[v, l]$ suggests that v scheduled on cycle l is more desirable since it lower the distribution of the resource over that cycle.

Then, we define $pF[v, l]$, for all v is a vertex in G , and for all l ranges $A[v]$ to $R[v]$, as the sum of $aF[p, k]$, where p belongs to ancestors of v , and where k is the new $R[p]$ after scheduling v on cycle l . Again, we define $sF[v, l]$, for all v is a vertex in G , and for all l ranges $A[v]$ to $R[v]$, as the sum of $dF[s, k]$, where s belongs to descendants of v , and where k is the new $A[s]$ after scheduling v on cycle l . Now we define $tF[v, l] = self[v, l] + pF[v, l] + sF[v, l]$, for all vertex v in G , for all l ranges from 1 to L .

$$pF[v, l] = \sum_{p \in \text{ancestors of } v} aF[p, k], \text{ where } k \text{ is the new } R[p] \text{ after scheduling } v \text{ on cycle } l$$

$$sF[v, l] = \sum_{s \in \text{descendants of } v} dF[s, k], \text{ where } k \text{ is the new } A[s] \text{ after scheduling } v \text{ on cycle } l$$

$$tF[v, l] = self[v, l] + pF[v, l] + sF[v, l]$$

```

1. calculate_total_force( oper, A, R, aF, dF, pF, sF, selfF, tF )
2.   for all vertex v in oper
3.     for i = A[v] to R[v]
4.       baseF[ v ] += distribution[ Ru[v] ][ i ];
5.     baseF[v] /= S[v] + 1;
6.   for all vertex v in oper
7.     selfF[v, A[v]] = aF[v, A[v]] = q[Ru[v], A[v]] - baseF[v];
8.     selfF[v, R[v]] = dF[v, R[v]] = q[Ru[v], R[v]] - baseF[v];
9.     for i = A[v] + 1 to R[v] - 1
10.      selfF[v][i] = q[Ru[v], i] - baseF[v];
11.      for j = A[v] to i
12.        aF[v, i] += q[Ru[v], j];
13.        aF[v, i] = aF[v, i] / ( i - A[v] + 1 ) - baseF[v];
14.        for j = i to R[v]
15.          dF[v, i] += q[Ru[v], j];
16.          dF[v, i] = dF[v, i] / ( R[v] - i + 1 ) - baseF[v];
17.   for all vertex v in oper
18.     for l = A[v] to R[v]
19.       for all predecessor p of v
20.         k = R[p] that changed when v scheduled on cycle l;
21.         pF[v, l] += aF[ p, k];
22.       for all descendant s of v
23.         k = A[s] that changed when v scheduled on cycle l;
24.         sF[v, l] += dF[ s, k];
25.   for all vertex v in oper
26.     for l = A[v] to R[v]
27.       tF[v, l] = self[v, l] + pF[v, l] + sF[v, l]
```

Definition

$oper$: vertexes in G with in-degree > 0
 $A[v]$: arrive time of vertex v
 $R[v]$: require time of vertex v
 $S[v]$: slack of vertex v
 $tF[r, l]$: total force of resource r on cycle l
 $pF[r, l]$: predecessor force of resource r on cycle l
 $sF[r, l]$: successor force of resource r on cycle l
 $selfF[r, L]$: self force of resource r on cycle l

- 2 - Experimental result

Comparing several benchmarks, starting from using the minimum latency constraints and incrementing it by 20 for each test. As the result suggests, MR-LCS uses less gates as the latency constraint given become larger; and thus, using larger latency constraint improves the result. However, FD-LCS uses less gates only when the latency constraint given is tight; and uses more gates when latency constraint become greater. FD-LCS has a better result when the latency constraint given is tight but has a worse result when the latency constraint given is large.

To conclude, when using tight latency is needed, it is best to use FD-LCS; However, it suggests that using MR-LCS is a better choice when latency constraint given is large.

aoi_9symml.blif					aoi_cht.blif					aoi_t481.blif				
11	MR	32	15	3	7	MR	68	35	1	9	MR	219	17	13
	FD	17	9	6		FD	18	14	3		FD	153	16	15
31	MR	18	12	1	27	MR	52	15	1	29	MR	120	11	1
	FD	7	6	5		FD	18	8	1		FD	59	13	13
51	MR	38	1	1	47	MR	32	29	1	49	MR	100	10	1
	FD	17	9	6		FD	18	8	1		FD	153	16	15
71	MR	18	1	1	67	MR	12	9	1	69	MR	80	6	1
	FD	17	9	6		FD	18	8	1		FD	153	16	15
91	MR	17	1	1	87	MR	26	1	1	89	MR	60	1	1
	FD	17	9	6		FD	18	8	1		FD	153	16	15
aoi_alu4.blif					aoi_cm138a.blif					aoi_x2.blif				
37	MR	13	15	5	3	MR	1	8	3	5	MR	7	6	9
	FD	7	11	7		FD	1	8	2		FD	5	5	7
57	MR	4	10	2	23	MR	1	1	1	25	MR	1	1	1
	FD	7	8	4		FD	1	1	1		FD	4	3	3
77	MR	3	11	7	43	MR	1	1	1	45	MR	1	1	1
	FD	7	9	5		FD	1	1	1		FD	4	3	3
97	MR	13	5	6	63	MR	1	1	1	65	MR	1	1	1
	FD	7	10	8		FD	1	1	1		FD	4	3	3
117	MR	7	6	1	83	MR	1	1	1	85	MR	1	1	1
	FD	7	10	8		FD	1	1	1		FD	4	3	3
aoi_big1.blif					aoi_des.blif					aoi_z4ml.blif				
20	MR	427	403	39	19	MR	90	239	36	8	MR	7	5	5
	FD	212	292	113		FD	140	128	44		FD	6	4	4
40	MR	342	330	20	39	MR	220	101	26	28	MR	2	1	1
	FD	133	133	78		FD	140	128	32		FD	4	4	2
60	MR	297	210	27	59	MR	30	35	22	48	MR	1	1	1
	FD	124	132	73		FD	140	128	32		FD	4	4	2
80	MR	83	326	21	79	MR	184	44	12	68	MR	1	1	1
	FD	124	132	73		FD	140	128	32		FD	4	4	2
100	MR	39	350	7	99	MR	20	23	8	88	MR	1	1	1
	FD	124	132	73		FD	140	128	32		FD	4	4	2

aoi_C6288.blif					aoi_i2.blif				
		AND	OR	NOT			AND	OR	NOT
179	MR	11	12	8	6	MR	7	11	1
	FD	7	12	9		FD	5	9	1
199	MR	8	10	7	26	MR	1	4	1
	FD	6	14	9		FD	5	9	1
219	MR	8	10	8	46	MR	1	1	1
	FD	6	11	8		FD	5	9	1
239	MR	11	9	10	66	MR	1	1	1
	FD	6	11	8		FD	5	9	1
259	MR	6	16	4	86	MR	1	1	1
	FD	8	11	8		FD	5	9	1

