## Sample lesson:

# Simple linear regression models in R

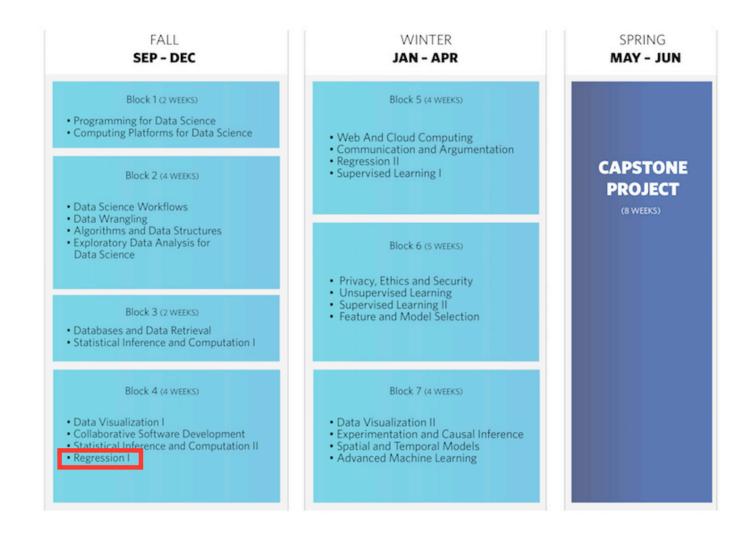
Tiffany Timbers, Ph.D. June 6, 2017

## Lesson context

#### **UBC MDS Curriculum**

#### WINTER SPRING FALL SEP - DEC JAN - APR MAY - JUN Block 1 (2 WEEKS) Block 5 (4 WEEKS) • Programming for Data Science Computing Platforms for Data Science · Web And Cloud Computing Communication and Argumentation · Regression II CAPSTONE Supervised Learning I Block 2 (4 WEEKS) **PROJECT** Data Science Workflows (8 WEEKS) Data Wrangling Algorithms and Data Structures · Exploratory Data Analysis for Block 6 (5 WEEKS) Data Science · Privacy, Ethics and Security Unsupervised Learning Supervised Learning II Block 3 (2 WEEKS) Feature and Model Selection · Databases and Data Retrieval Statistical Inference and Computation I Block 4 (4 WEEKS) Block 7 (4 WEEKS) Data Visualization I • Data Visualization II Experimentation and Causal Inference Spatial and Temporal Models Collaborative Software Development Statistical Inference and Computation II · Regression I Advanced Machine Learning

#### **UBC MDS Curriculum**



## **DSCI 561 Regression I**

#### Course Learning Outcomes

By the end of the course, students are expected to be able to:

- Fit and interpret a linear regression model.
- · Identify whether a linear regression model is appropriate for a given dataset.
- Critique a specific regression model applied to a given dataset on the basis of both diagnostic plots and hypothesis tests.
- · Specify and interpret interaction terms and nonlinear terms.

## Sample lesson: Simple linear regression models in R

1/4 of the way into the course. Before this lesson, students will have learned the following:

- · model notation in R
- · one-way & two-way ANOVA
  - theory
  - how to do in R with aov()
  - how to do in R with lm() (including reference-treatment parameterization)
  - interaction effects
- · linear regression via ordinary least squares (theory)

## Sample lesson: Simple linear regression models in R

#### learning objectives:

By the end of this lesson students are expected to be able to:

- · fit a simple linear model in R
- · interpret the output of the simple linear model object in R
- · use three functions from the broom package extract simple linear model object output

## **Lesson Motivation**

slides and code available at: https://github.com/ttimbers/UBC-stat-sample-lesson

## Sample Lesson

### The Data:

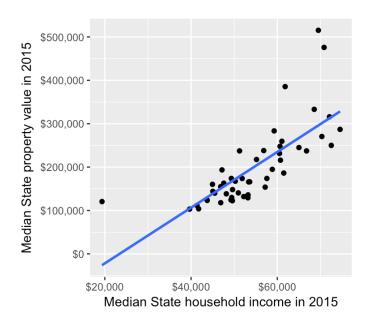
US property data from 2015 extracted from the Data USA API using Python <a href="https://datausa.io/">https://datausa.io/</a>

display_name	income	mean_commute_minutes	median_property_value	non_eng_speakers_pct	owner_occupied_housing_units	pop
Texas	53207	24.5090	136000	0.3503480	0.622325	26538614
Pennsylvania	53599	25.2695	166000	0.1064820	0.692052	12779559
South Carolina	45483	23.0552	139900	0.0686766	0.685914	4777576
New Hampshire	66779	25.2973	237300	0.0786821	0.709609	1324201
Kansas	52205	18.2779	132000	0.1130530	0.666891	2892987
Hawaii	69515	25.5813	515300	0.2521790	0.569030	1406299

<sup>## [1] 52 7</sup> 

## Simple linear regression:

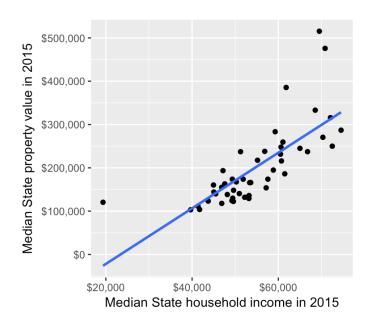
US State property value as a function of income



Y =State median property value  $X_1 =$ income

State median property value =  $\beta_0 + \beta_1$  income +  $\varepsilon$ 

## Syntax for linear regression in R



State median property value =  $\beta_0 + \beta_1$  income +  $\varepsilon$ 

prop\_model <- lm(median\_property\_value ~ income, data = prop\_data)</pre>

## Syntax for simple linear regression

create linear model object and view output in base R:

```
prop model <- lm(median property value ~ income, data = prop data)</pre>
summary(prop model)
## Call:
## lm(formula = median_property_value ~ income, data = prop_data)
## Residuals:
     Min 10 Median 30
## -65249 -36542 -6990 8003 219312
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.503e+05 4.393e+04 -3.422 0.00125 **
## income
            6.420e+00 7.999e-01 8.026 1.52e-10 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 58860 on 50 degrees of freedom
## Multiple R-squared: 0.563, Adjusted R-squared: 0.5542
## F-statistic: 64.41 on 1 and 50 DF, p-value: 1.517e-10
```

## Decoding R's output from summary():

```
Call:
lm(formula = median_property_value ~ income, data = prop_data)
Residuals:
   Min
          10 Median
                        3Q
                              Max
-65249 -36542 -6990
                      8003 219312
                                                         p-value for H_0: \beta_0 = 0
Coefficients:
                                                         p-value for H_0: \beta_1 = 0
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.503e+05 4.393e+04 -3.422 0.00125 **
            6.420e+00 7.999e-01 8.026 1.52e-10****
income
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1
Residual standard error: 58860 on 50 degrees of freedom
Multiple R-squared: 0.563, ← Adjusted R-squared: 0.5542
F-statistic: 64.41 on 1 and 50 DF, p-value: 1.517e-10
```

## Extracting output from model object in base R:

model output	code		
parameter/coefficient estimates ( $eta_0 \& eta_1$ )	model_object\$coefficients		
residuals	model_object\$residuals		
predicted/fitted values	model_object\$fitted.values		
p-values for coefficients	<pre>summary(model_object)\$coefficients[,4]</pre>		
$\sigma$ estimate	<pre>summary(model_object)\$sigma</pre>		
$R^2$	<pre>summary(model_object)\$r.squared</pre>		

#### Working with model output in base R,



the good, the bad and the ugly...

#### The good...

- · all the information you want is viewable
- this has been used for many many years and thus should be familiar to most Data Scientists and Statisticians

#### The bad...

- inconsistent syntax to extract model output
- · model output is returned in a variety of forms, and is not tidy data

#### The ugly...

- bizarre symbols in some column names ( summary(model\_object)\$coefficient)
- · F-statistic p-value is never stored in memory and thus must be calculated by hand

#### broom:



A better way for working with model output in R

## **broom** for working with model output in R:

#### The good...

- · all the information you want is stored in memory, and easy to access
- · consistent syntax
- · no weird column names
- · output is returned as data frames in tidy data format

#### The bad...

· it's new, so not everyone is familiar with it

#### The ugly...

· ???

## **broom** for working with model output in R:

broom function	model output		
tidy(model_object)	model parameters ( coefficients and p-values)		
<pre>augment(model_object)</pre>	model data ( residuals and predicted values)		
<pre>glance(model_object)</pre>	model quality, complexity and summaries ( $\sigma$ estimate and $\mathit{R}^2$ )		

## Example output from tidy()

## Example output from augment()

augment(prop\_model)

##		median_property_value	ingomo	fittod	co fit	.resid	.hat
##	1	136000				-55289.283	
##		166000				-27805 <b>.</b> 963	
##		139900				-1800.420	
##		237300				-41122.898	
##		132000	52205			-41122.090 -52856.341	
##		515300				219311.705	
##		162900		155182.63		7717.367	
##		193500				40975.289	
##		160300				21938.033	
##		283400				53192.063	
##		153800				-63002.765	
##	12	237300	51243	178680.20	8446.070	58619.796	0.02059184
##	13	129200	53183	191135.20	8185.648	-61935.200	0.01934157
##	14	122400	49576	167977.89	8882.875	-45577.895	0.02277680
##	15	129900	49429	167034.14	8929.926	-37134.140	0.02301873
##	16	148100	49620	168260.38	8869.046	-20160.379	0.02270594
##	17	247800	60629	238939.27	9752.014	8860.725	0.02745202
##	18	159000	47507	154694.71	9656.419	4305.295	0.02691646
##	19	286900	74551	328319.93	18384.621	-41419.925	0.09756522
##	20	217500	55176	203930.46	8220.159	13569.538	0.01950501
##	21	259500	61062	241719.18	9945.789	17780.821	0.02855382
##	22	167500	50255	172337.14	8682.917	-4837.144	0.02176291
##	23	124200	49255	165917.04	8987.290	-41717.042	0.02331542
##	24	123200	43740	130510.18	11550.947	-7310.184	0.03851420
##	25	144100	45047	138901.26	10836.365	5198.744	0.03389635
##	26	173800	49331	166404.97	8962.014	7395.030	0.02318445
##	27	186200	61492	244479.82	10146.265	-58279.822	0.02971653
	28	138400				-20570.493	
##		133200				-56741.062	

## Example output from glance()

```
## r.squared adj.r.squared sigma statistic p.value df logLik
## 1 0.5629882     0.554248 58858.23 64.41339 1.517389e-10 2 -643.8752
## AIC BIC deviance df.residual
## 1 1293.75 1299.604 173214534971     50
```

## Group challenge question:

https://tinyurl.com/UBC-stat-group-challenge

What did we learn today?

## Where do we go from here?

- · finish simple linear regression
  - predicted values and confidence intervals
- · more complex linear regression models (multiple regression)
  - theory (least squares)
  - how to in R (revisit reference-treatment parameterization)
  - interaction effects in linear regression
- model diagnostics
- · dealing with nonlinear terms

## Questions/Discussion