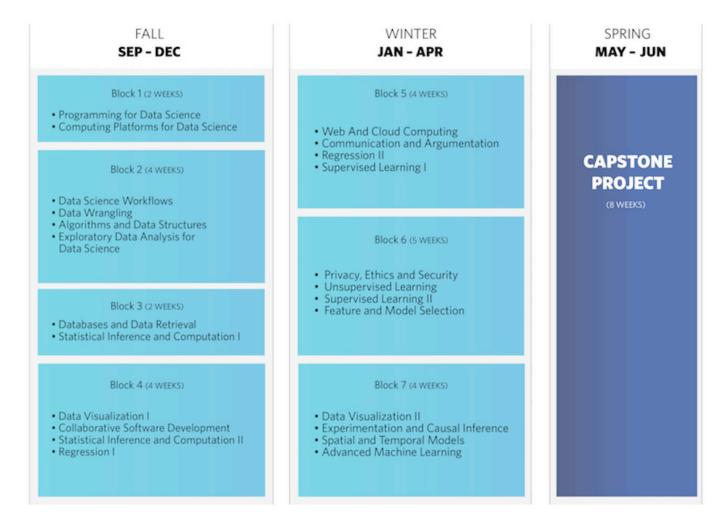
Sample lesson:

Simple linear regression models in R

Tiffany Timbers, Ph.D. June 6, 2017

Lesson context

UBC MDS Curriculum



source: UBC MDS blog

UBC MDS Curriculum



source: UBC MDS blog

DSCI 561 Regression I

(taken from public description of UBC MDS course DSCI 561)

Course Learning Outcomes

By the end of the course, students are expected to be able to:

- · Fit and interpret a linear regression model.
- · Identify whether a linear regression model is appropriate for a given dataset.
- · Critique a specific regression model applied to a given dataset on the basis of both diagnostic plots and hypothesis tests.
- · Specify and interpret interaction terms and nonlinear terms.

DSCI 561 Regression I

(adapted from public description of UBC MDS course DSCI 561)

Reference Materials

- · Faraway, Julian J. Linear Models with R, 2nd Edition. Chapman and Hall, 2014.
- · broom package vignette in R

Sample lesson: Simple linear regression models in R

1/4 of the way into the course. Before this lesson, students will have learned the following:

- · model notation in R
- · one-way ANOVA (theory & how to do in R)
- · linear regression via ordinary least squares (theory)

Sample lesson: Fitting and interpreting linear regression models in R

20 minute lesson learning objectives:

By the end of this lesson students are expected to be able to:

- · fit a simple linear model in R
- · interpret the output of the simple linear model object in R
- · use three functions from the broom package extract simple linear model object output

Lesson Motivation

Sample Lesson

The Data:

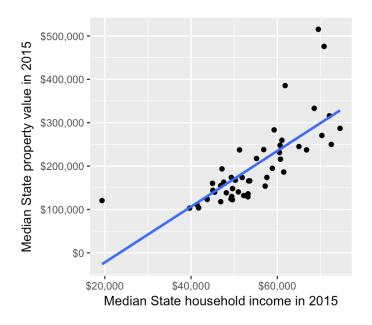
US property data from 2015 extracted from the Data USA API using Python https://datausa.io/

display_name	income	mean_commute_minutes	median_property_value	non_eng_speakers_pct	owner_occupied_housing_units	pop
Texas	53207	24.5090	136000	0.3503480	0.622325	26538614
Pennsylvania	53599	25.2695	166000	0.1064820	0.692052	12779559
South Carolina	45483	23.0552	139900	0.0686766	0.685914	4777576
New Hampshire	66779	25.2973	237300	0.0786821	0.709609	1324201
Kansas	52205	18.2779	132000	0.1130530	0.666891	2892987
Hawaii	69515	25.5813	515300	0.2521790	0.569030	1406299

^{## [1] 52 7}

Simple linear regression:

US State property value as a function of income



Y =State median property value $X_1 =$ income

State median property value = $\beta_0 + \beta_1$ income + ε

Model notation for linear regression in R

Simple linear regression:

Mathematical formula model formula in R

 $Y = \beta_0 + \beta_1 X_1 + \varepsilon$ Y ~ X1

More complex linear regression:

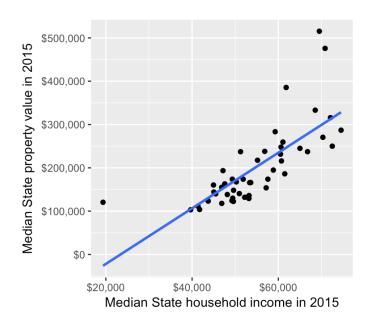
Mathematical formula model formula in R

 $Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3 + \varepsilon$ Y ~ X1 + X2 + X3

Cheatsheet for model notation in R:

http://faculty.chicagobooth.edu/richard.hahn/teaching/formulanotation.pdf

Syntax for linear regression in R



State median property value = $\beta_0 + \beta_1$ income + ε

prop_model <- lm(median_property_value ~ income, data = prop_data)</pre>

Check-in question:

https://b.socrative.com/login/student/

room number: F321E8CC

Syntax for simple linear regression

create linear model object and view output in base R:

```
prop model <- lm(median property value ~ income, data = prop data)</pre>
summary(prop model)
## Call:
## lm(formula = median_property_value ~ income, data = prop_data)
## Residuals:
     Min 1Q Median 3Q
## -65249 -36542 -6990 8003 219312
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.503e+05 4.393e+04 -3.422 0.00125 **
## income
            6.420e+00 7.999e-01 8.026 1.52e-10 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 58860 on 50 degrees of freedom
## Multiple R-squared: 0.563, Adjusted R-squared: 0.5542
## F-statistic: 64.41 on 1 and 50 DF, p-value: 1.517e-10
```

Decoding R's output from summary():

```
Call:
lm(formula = median_property_value ~ income, data = prop_data)
Residuals:
   Min
          10 Median
                        3Q
                              Max
-65249 -36542 -6990
                      8003 219312
                                                         p-value for H_0: \beta_0 = 0
Coefficients:
                                                         p-value for H_0: \beta_1 = 0
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.503e+05 4.393e+04 -3.422 0.00125 **
            6.420e+00 7.999e-01 8.026 1.52e-10****
income
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1
Residual standard error: 58860 on 50 degrees of freedom
Multiple R-squared: 0.563, ← Adjusted R-squared: 0.5542
F-statistic: 64.41 on 1 and 50 DF, p-value: 1.517e-10
```

Extracting output from model object in base R:

model output	code
parameter/coefficient estimates (e.g., β_0 & β_1)	model_object\$coefficients
residuals	model_object\$residuals
predicted/fitted values	model_object\$fitted.values
p-values for coefficients	<pre>summary(model_object)\$coefficients[,4]</pre>
σ estimate	<pre>summary(model_object)\$sigma</pre>
R^2	<pre>summary(model_object)\$r.squared</pre>

Working with model output in base R,



the good, the bad and the ugly...

The good...

- · all the information you want is viewable
- this has been used for many many years and thus should be familiar to most Data Scientists and Statisticians

The bad...

- · inconsistent syntax to extract model output
- · model output is returned in a variety of forms, and is not tidy data

The ugly...

- bizarre symbols in some column names (e.g., summary(model_object)\$coefficient)
- · F-statistic p-value is never stored in memory and thus must be calculated by hand

broom:



A better way for working with model output in R

broom for working with model output in R:

The good...

- \cdot all the information you want is stored in memory, and easy to access
- consistent syntax
- · no weird column names

The bad...

· it's new, so not everyone is familiar with it

The ugly...

· ???

broom for working with model output in R:

broom function	model output
tidy(model_object)	model parameters (e.g., coefficients and p-values)
<pre>augment(model_object)</pre>	model data (e.g., residuals and predicted values)
<pre>glance(model_object)</pre>	model quality, complexity and summaries (e.g., σ estimate and R^2)

Example output from tidy()

Example output from augment()

augment(prop_model)

##		median_property_value	income	.fitted	.se.fit	.resid	.hat
##	1	136000	53207	191289.28	8184.217	-55289.283	0.01933481
##	2	166000	53599	193805.96	8167.204	-27805.963	0.01925451
##	3	139900	45483	141700.42	10610.207	-1800.420	0.03249626
##	4	237300	66779	278422.90	13107.757	-41122.898	0.04959552
##	5	132000	52205	184856.34	8281.684	-52856.341	0.01979808
##	6	515300	69515	295988.30	14882.799	219311.705	0.06393739
##	7	162900	47583	155182.63	9624.070	7717.367	0.02673642
##	8	193500	47169	152524.71	9803.561	40975.289	0.02774300
##	9	160300	44963	138361.97	10880.682	21938.033	0.03417416
##	10	283400	59269	230207.94	9201.822	53192.063	0.02444181
##	11	153800	57181	216802.77	8559.790	-63002.765	0.02115007
##	12	237300	51243	178680.20	8446.070	58619.796	0.02059184
##	13	129200	53183	191135.20	8185.648	-61935.200	0.01934157
##	14	122400	49576	167977.89	8882.875	-45577.895	0.02277680
##	15	129900	49429	167034.14	8929.926	-37134.140	0.02301873
##	16	148100	49620	168260.38	8869.046	-20160.379	0.02270594
##	17	247800	60629	238939.27	9752.014	8860.725	0.02745202
##	18	159000	47507	154694.71	9656.419	4305.295	0.02691646
##	19	286900	74551	328319.93	18384.621	-41419.925	0.09756522
##	20	217500	55176	203930.46	8220.159	13569.538	0.01950501
##	21	259500	61062	241719.18	9945.789	17780.821	0.02855382
##	22	167500	50255	172337.14	8682.917	-4837.144	0.02176291
##	23	124200	49255	165917.04	8987.290	-41717.042	0.02331542
##	24	123200	43740	130510.18	11550.947	-7310.184	0.03851420
##	25	144100	45047	138901.26	10836.365	5198.744	0.03389635
##	26	173800	49331	166404.97	8962.014	7395.030	0.02318445
##	27	186200	61492	244479.82	10146.265	-58279.822	0.02971653
##	28	138400	48173	158970.49	9382.549	-20570.493	0.02541133
##	29	133200	52997	189941.06	8198.252	-56741.062	0.01940118

Example output from glance()

```
## r.squared adj.r.squared sigma statistic p.value df logLik
## 1 0.5629882     0.554248 58858.23 64.41339 1.517389e-10 2 -643.8752
## AIC BIC deviance df.residual
## 1 1293.75 1299.604 173214534971     50
```

Group challenge question:

https://tinyurl.com/stat-group-challenge

What did we learn today?

Where do we go from here?

- fitting and interpreting more complex linear models
 - theory
 - how to in R
- model diagnostics
- \cdot dealing with nonlinear terms

Questions/Discussion