

# Program Structures & Algorithms

Spring 2022

## Assignment No. 3

Name: Yuan Huang

(NUID): 002117054

- **Task**

Step 1:

(a) Implement height-weighted Quick Union with Path Compression. For this, you will flesh out the class UF\_HWQUPC. All you have to do is to fill in the sections marked with `// TO BE IMPLEMENTED ... // ...END IMPLEMENTATION`.

(b) Check that the unit tests for this class all work. You must show "green" test results in your submission (screenshot is OK).

Step 2:

Using your implementation of UF\_HWQUPC, develop a UF ("union-find") client that takes an integer value  $n$  from the command line to determine the number of "sites." Then generates random pairs of integers between 0 and  $n-1$ , calling `connected()` to determine if they are connected and `union()` if not. Loop until all sites are connected then print the number of connections generated. Package your program as a static method `count()` that takes  $n$  as the argument and returns the number of connections; and a `main()` that takes  $n$  from the command line, calls `count()` and prints the returned value. If you prefer, you can create a main program that doesn't require any input and runs the experiment for a fixed set of  $n$  values. Show evidence of your run(s).

Step 3:

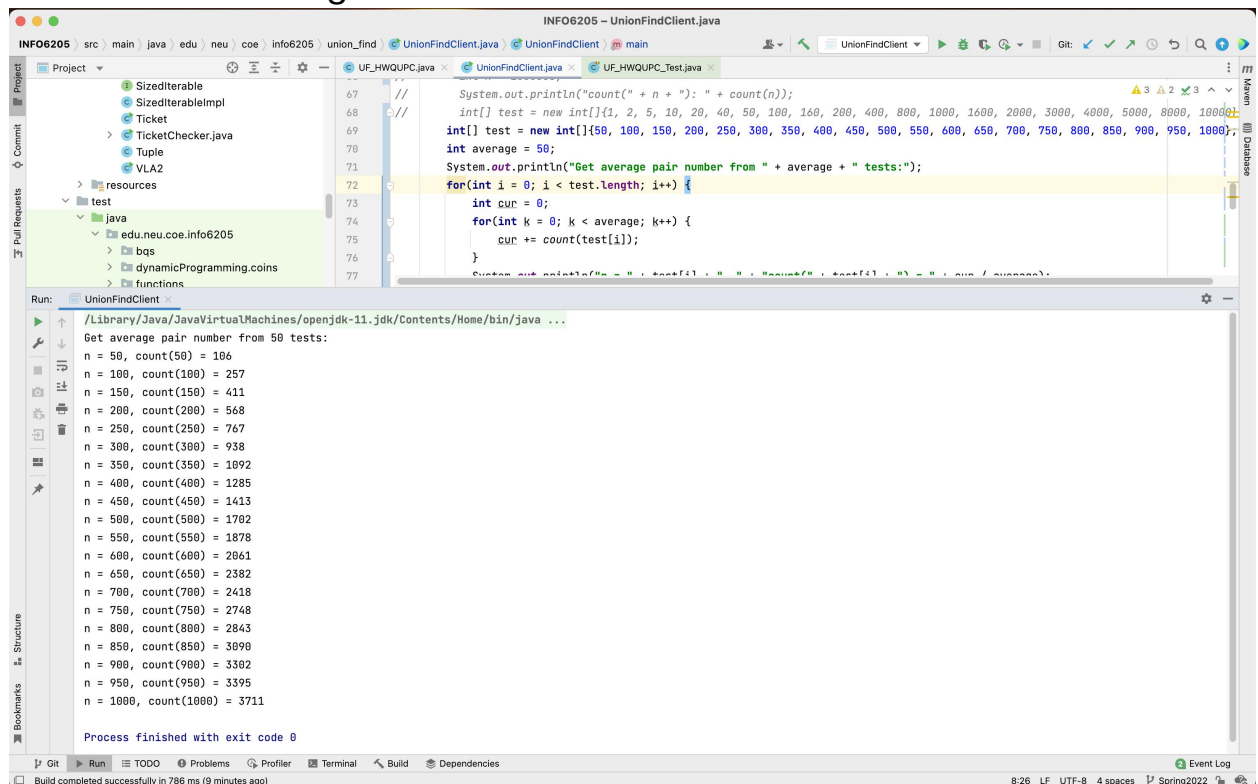
Determine the relationship between the number of objects ( $n$ ) and the number of pairs ( $m$ ) generated to accomplish this (i.e. to reduce the number of components from  $n$  to 1). Justify your conclusion in terms of your observations and what you think might be going on.

NOTE: although I'm not going to tell you in advance what the relationship is, I can assure you that it is a simple relationship.

Part2 output:

I created a UnionFindClient class for part 2 & 3. It has a static function called count(), which is used for “ $m = \text{count}(n)$ ”. Input number of objects n, and output the number of pairs m generated to union all of n objects to only one component. In the main function it is the testing process. There is a predefined array named test[], which contains a list of different input n range from 50 to 1000.

Each m is an average result of 50 times tests.



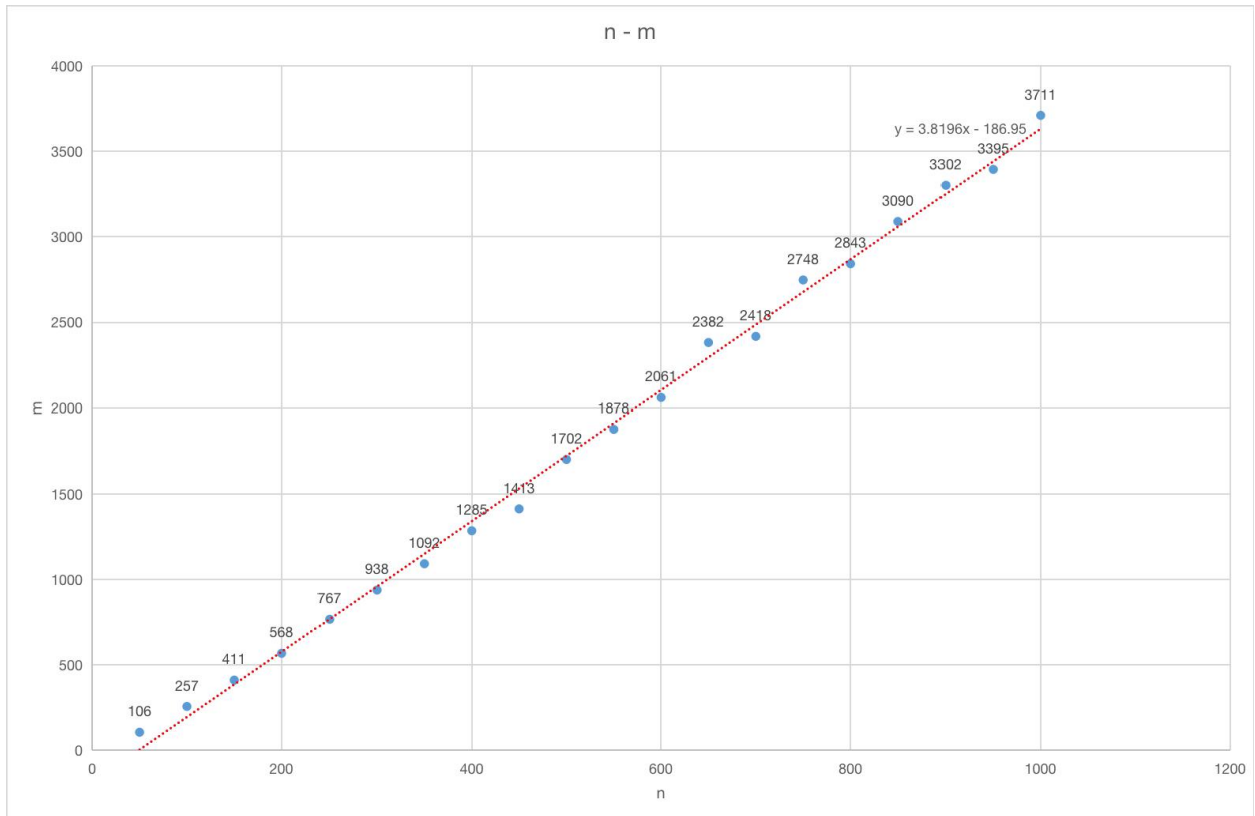
- **Relationship Conclusion**

$$m = 3.8196 * n - 186.95$$

- Evidence / Graph

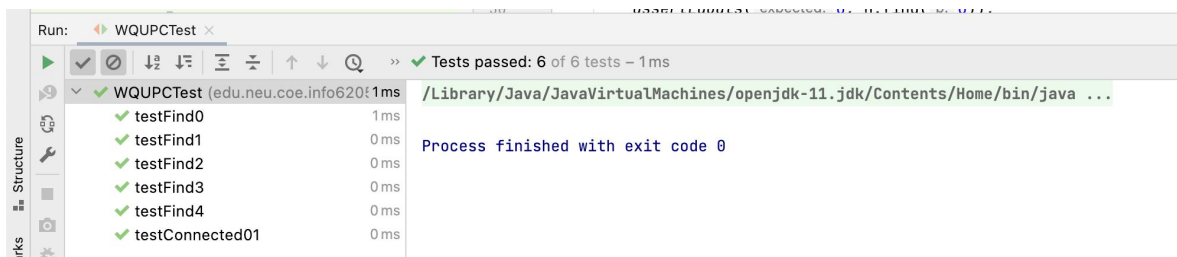
The blue dots are test result.

The red line is the relationship conclusion.



- Unit tests result

Test result:



Run: UF\_HWQUPC\_Test

✓ Tests passed: 13 of 13 tests – 4 ms

UF\_HWQUPC\_Test (edu.neu.coe.ir 4 ms)

testIsConnected012 ms

testIsConnected020 ms

testIsConnected031 ms

testFind00 ms

testFind10 ms

testFind20 ms

testFind30 ms

testFind41 ms

testFind50 ms

testToString0 ms

testConnect010 ms

testConnect020 ms

testConnected010 ms

/Library/Java/JavaVirtualMachines/openjdk-11.jdk/Contents/Home/bin/java ...

Process finished with exit code 0

Git

Run

TODO

Problems

Profiler

Terminal

Build

Dependencies

Tests passed: 13 (moments ago)