Visualization.R

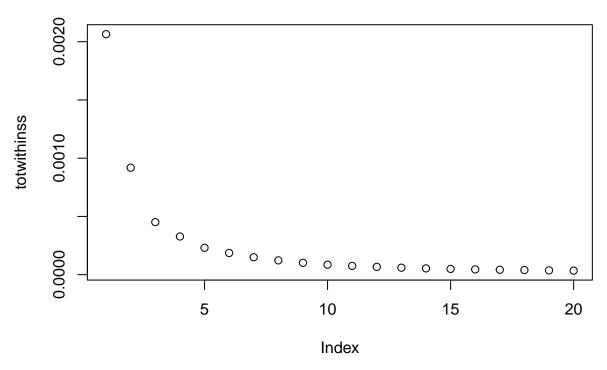
mpereda

Thu Jul 21 20:01:59 2016

```
#3D graphs in R with OpenGL
#Required libraries
rm(list=ls(all=TRUE))
library(igraph)
##
## Attaching package: 'igraph'
## The following objects are masked from 'package:stats':
##
##
       decompose, spectrum
## The following object is masked from 'package:base':
##
##
       union
library(rgl)
library(xlsx)
## Loading required package: rJava
## Loading required package: xlsxjars
# Seed for random numbers generation
set.seed(1)
#Working directory
myWD <- "/Users/mpereda/Dropbox/work-Other projects/Estrada/ejemplos/WorldTrade_Dichot_SymA"
setwd(myWD)
#Load files
myNet <- read.table("WorldTrade_Dichot_SymA.txt", header = FALSE, sep = "")</pre>
coordsAndsc <- read.table("WorldTrade_Dichot_SymA-metricsstress-coords-sc.txt", header = FALSE, sep = "</pre>
coords <- coordsAndsc[,1:3]</pre>
sc<-coordsAndsc[,4]</pre>
anglesAndGpq <-read.table("WorldTrade_Dichot_SymA-angles-Gpq.txt", header = FALSE, sep = ",")</pre>
angles <- anglesAndGpq[,1]</pre>
Gpq <- anglesAndGpq[,2]</pre>
An <- read.table("WorldTrade_Dichot_SymA-anglesFull.txt", header = FALSE, sep = ",")
names <- read.table("WorldTrade_Names.txt", header = FALSE, sep = "", stringsAsFactors=FALSE)</pre>
#Creation of the network
g <- graph_from_adjacency_matrix(as.matrix(myNet), mode=c("undirected"))</pre>
```

```
degrees<- as.matrix(degree(g))</pre>
g <- set.vertex.attribute(g, "sc", value=sc)</pre>
g <- set.vertex.attribute(g, "degree", value=degree(g))</pre>
g <- set.edge.attribute(g, "communicability_angle", value=angles)</pre>
g <- set.edge.attribute(g, "Gpq", value=Gpq)
rbPal <- colorRampPalette(c('paleturquoise1','black'))</pre>
Col <- rbPal(10)[as.numeric(cut(E(g)$Gpq,breaks = 10))] #Colors for edges</pre>
g <- set.edge.attribute(g, "color", value=Col)</pre>
g <- set.vertex.attribute(g, "names", value=names[,2])
lec <- cluster_leading_eigen(g)</pre>
clusters<-cluster_infomap(g, nb.trials = 100)</pre>
g <- set.vertex.attribute(g, "group", value=membership(clusters))</pre>
if (length(clusters)!=1){
ColNode <- rainbow(length(clusters))[as.numeric(cut(V(g)$group,breaks = length(clusters)))]</pre>
}else{ColNode=rep("#666666",length(sc))}
g <- set.vertex.attribute(g, "color", value=ColNode)</pre>
\# Para cada cluster, calculo el centroide, la distancia al centroide de cada nodo, y luego el radio med
n_elements <-rep(0, length(clusters))</pre>
centroid <-list()</pre>
rads <- list()
Avg_radius <-rep(0, length(clusters))</pre>
pack_index <-rep(0, length(clusters)) #Pack_index: Compacticidad Avg_radius/n_elements
max_radius <-rep(0, length(clusters))</pre>
for (i in 1:length(clusters)){
  centroid[[i]] <- colMeans(coords[V(g)$group==i,])</pre>
  rads[[i]] <- sqrt(rowSums((coords[V(g)$group==i,]-centroid[[i]])^2))</pre>
  Avg_radius[i] <- mean(rads[[i]])</pre>
  n_elements[i] <- nrow(coords[V(g)$group==i,])</pre>
  pack_index[i] <- Avg_radius[i] / n_elements[i]</pre>
  max_radius[i] <- max(rads[[i]])</pre>
# Plot
#Node sizes
mns <- 5 #Min node size for plotting
Mns <- 20 #Max node size for plotting
a \leftarrow (Mns-mns)/(max(sc)-min(sc))
y0 \leftarrow Mns - ((Mns-mns)*max(sc))/(max(sc)-min(sc))
#edge sizes
mes <- 1 #Min edge size for plotting
Mes <- 10 #Max edge size for plotting
ae <- (Mes-mes)/(max(Gpq)-min(Gpq))</pre>
y0e <- Mes - ((Mes-mes)*max(Gpq))/(max(Gpq)-min(Gpq))
```

```
rgl.open()# Open a new RGL device
par3d("windowRect"= c(0,0,1300,1300))
rgl.bg(color = "white") # Setup the background color
rglplot(g, layout=as.matrix(coords), vertex.color=V(g)$color, vertex.size= y0 + a*V(g)$sc, vertex.label =
                   vertex.label.color="black", vertex.label.dist=1, edge.width= y0e + ae*E(g)$Gpq, edge.color=E(g)
#legend3d("top", legend ="Infomap communities", cex=1, bty = "n")
rgl.viewpoint( zoom = .8 )
#Axis en 0,0
rgl.lines(c(-1, 1), c(0, 0), c(0, 0), color = "green")
rgl.lines(c(0, 0), c(-1,1), c(0, 0), color = "green")
rgl.lines(c(0, 0), c(0, 0), c(-1,1), color = "green")
#Export to pnq
rgl.snapshot( 'infomap_clusters.png', fmt = "png", top = TRUE )
# # # # # # Detecting communicability communities in the reduced communicability space # # # # # #
#Select the number of clusters
nclu <- 20
n_k <- 1000 #times to train a nclu-cluster training
totwithinss <- rep(0,nclu)</pre>
tol <- 0.05 #minimum improvement in totwithinss (% of no clusters situation) required for selecting the
for (i in 1:nclu){ #1 to nclu clusters to try
    totwithinss1 <- rep(0,n_k)
    for (j in 1:n_k){
         communities <- kmeans(coords,i)</pre>
         totwithinss1[j]<-communities$tot.withinss</pre>
    }
    totwithinss[i] <- mean(totwithinss1)</pre>
#Vectors of reduction of totwithinss respect to no clusters situation
reduction <- rep(0,nclu)</pre>
for (i in 2:(nclu)){
     (totwithinss[1]-totwithinss[i])/totwithinss[1]
    reduction [i] <- (totwithinss[1] - totwithinss[i]) / totwithinss[1] - (totwithinss[1] - totwithinss[i-1]) / totwithinss[i] - (totwithinss[i] - totwithinss[i-1]) / totwithinss[i] - (totwithinss[i] - totwithinss[i] - totwithins
}
plot(totwithinss)
```



```
#Number of clusters obtained
num_clusters2 <- which(reduction==reduction[reduction<tol & reduction>0][1])
num_clusters2
```

[1] 5

```
n_times <- 10000
solutions<-list()
totwithinss_solutions <- rep(0,n_times)

for (n_t in 1:n_times){
   communities <- kmeans(coords,num_clusters2)
   solutions[[n_t]]<-communities
   totwithinss_solutions[n_t]<-communities$tot.withinss
}

summary(totwithinss_solutions)</pre>
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max. ## 0.0002128 0.0002171 0.0002369 0.0002310 0.0002369 0.0003008
```

```
best<-which(totwithinss_solutions==min(totwithinss_solutions))
#Store the set of best solutions (with the lowest totwithinss)
my_solutions<-list()

for (i in 1:length(best)){
   my_solutions[[i]]<-solutions[[best[i]]]
}</pre>
```

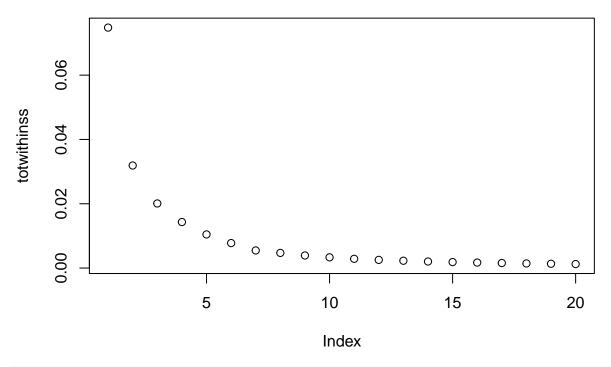
```
#Do the clusters in all the best solutions have the same size?
num_elements_solutions<-sapply(my_solutions, function(x) sort(x$size))</pre>
summary(t(num_elements_solutions)) # veo si todos tienen los mismos elementos
                      V2
                                                              V5
##
          V1
                                    V3
                                                 V4
## Min.
          :7
               Min.
                       :12
                             Min.
                                    :13
                                                  :19
                                                               :29
                                          Min.
                                                        Min.
## 1st Qu.:7
                1st Qu.:12
                             1st Qu.:13
                                           1st Qu.:19
                                                        1st Qu.:29
## Median :7
                Median :12
                             Median :13
                                          Median :19
                                                        Median:29
## Mean
          :7
                Mean
                      :12
                             Mean :13
                                           Mean :19
                                                        Mean
                                                               :29
## 3rd Qu.:7
                3rd Qu.:12
                             3rd Qu.:13
                                           3rd Qu.:19
                                                        3rd Qu.:29
## Max.
           :7
                Max.
                       :12
                             Max. :13
                                           Max.
                                                  :19
                                                        Max.
                                                               :29
SDs<- apply(t(num_elements_solutions), 2, sd)</pre>
## [1] 0 0 0 0 0
#Since all the solutions have the same totwithinss, I pick one randomly
my_solution<-sample(my_solutions, 1)</pre>
#Plot the solution
g <- set.vertex.attribute(g, "group", value=my_solution[[1]]$cluster)</pre>
if (length(my_solution[[1]]$size)!=1){
  ColNode <- rainbow(length( my_solution[[1]]$size))[as.numeric(cut(V(g)$group,breaks = length( my_solu
}else{ColNode=rep("#666666",length(sc))}
g <- set.vertex.attribute(g, "color", value=ColNode)</pre>
#Node sizes
mns <- 5 #Min node size for plotting
Mns <- 20 #Max node size for plotting
a <- (Mns-mns)/(max(sc)-min(sc))
y0 \leftarrow Mns - ((Mns-mns)*max(sc))/(max(sc)-min(sc))
#edge sizes
mes <- 1 #Min edge size for plotting
Mes <- 10 #Max edge size for plotting
ae <- (Mes-mes)/(max(Gpq)-min(Gpq))</pre>
y0e <- Mes - ((Mes-mes)*max(Gpq))/(max(Gpq)-min(Gpq))
rgl.open()# Open a new RGL device
par3d("windowRect"= c(0,0,1300,1300))
rgl.bg(color = "white") # Setup the background color
rglplot(g, layout=as.matrix(coords), vertex.color=V(g)$color, vertex.size= y0 + a*V(g)$sc, vertex.label =
        vertex.label.color="black", vertex.label.dist=1, edge.width= y0e + ae*E(g)$Gpq, edge.color=E(g)
#legend3d("top", legend ="Communicability (reduced) communities", cex=1, bty = "n")
rgl.viewpoint( zoom = .8)
#Ejes en 0,0
rgl.lines(c(-1, 1), c(0, 0), c(0, 0), color = "green")
rgl.lines(c(0, 0), c(-1,1), c(0, 0), color = "green")
```

```
rgl.lines(c(0, 0), c(0, 0), c(-1,1), color = "green")
#Export to pnq
rgl.snapshot( 'communicability_reduced.png', fmt = "png", top = TRUE )
my_clusters <- data.frame(names=names[,2],my_solution[[1]]$cluster)</pre>
my_clusters <- my_clusters[order(my_clusters[2]),]</pre>
#Uncoment for saving clusters to Excel file
write.xlsx(my_clusters, paste(myWD,"/my_clusters.xlsx",sep=""))
# Para cada cluster, calculo el centroide, la distancia al centroide de cada nodo, y luego el radio med
n_elements2 <-rep(0, num_clusters2)</pre>
centroid2 <-list()</pre>
rads2 <- list()
Avg_radius2 <-rep(0, num_clusters2)</pre>
pack_index2 <-rep(0, num_clusters2) #Pack_index: Compacticidad Avg_radius/n_elements
max_radius2 <-rep(0, num_clusters2)</pre>
for (i in 1:num_clusters2){
  centroid2[[i]] <- colMeans(coords[V(g)$group==i,])</pre>
  rads2[[i]] <- sqrt(rowSums((coords[V(g)$group==i,]-centroid2[[i]])^2))</pre>
  Avg_radius2[i] <- mean(rads2[[i]])</pre>
 n_elements2[i] <- nrow(coords[V(g)$group==i,])</pre>
 pack_index2[i] <- Avg_radius2[i] / n_elements2[i]</pre>
 max_radius2[i] <- max(rads2[[i]])</pre>
}
# # # # # # Detecting communicability communities in the full communicability space # # # # # # # # #
#Select the number of clusters
nclu <- 20
n_k <- 1000 #times to train a nclu-cluster training
totwithinss <- rep(0,nclu)
tol <- 0.05 #minimum improvement in totwithinss required
for (i in 1:nclu){ #1 to nclu clusters to try
 totwithinss1 <- rep(0,n_k)</pre>
 for (j in 1:n_k){
    communities <- kmeans(An,i)
    totwithinss1[j] <- communities $tot. withinss
 totwithinss[i] <- mean(totwithinss1)</pre>
#Vectors of reduction of totwithinss respect to no clusters situation
reduction <- rep(0,nclu)
for (i in 2:(nclu)){
  (totwithinss[1]-totwithinss[i])/totwithinss[1]
  reduction[i] <- (totwithinss[1]-totwithinss[i])/totwithinss[1] - (totwithinss[1]-totwithinss[i-1])/to
}
```

```
#Number of clusters obtained
num_clusters3 <- which(reduction==reduction[reduction<tol & reduction>0][1])
num_clusters3
```

[1] 6

plot(totwithinss)



```
n_times <- 10000
solutions<-list()
totwithinss_solutions <- rep(0,n_times)

for (n_t in 1:n_times){
   communities <- kmeans(coords,num_clusters3)
   solutions[[n_t]]<-communities
   totwithinss_solutions[n_t]<-communities$tot.withinss
}

summary(totwithinss_solutions)</pre>
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.0001588 0.0001597 0.0001997 0.0001862 0.0002118 0.0002445

best<-which(totwithinss_solutions==min(totwithinss_solutions))

my_solutions<-list()

for (i in 1:length(best)){
    my_solutions[[i]]<-solutions[[best[i]]]</pre>
```

```
}
#Do the clusters in all the best solutions have the same size?
num_elements_solutions<-sapply(my_solutions, function(x) sort(x$size))
summary(t(num_elements_solutions)) # veo si todos tienen los mismos elementos
                      ٧2
                                   VЗ
                                                ۷4
                                                              ۷5
##
          V1
                       :12
                                    :12
                                                 :13
                                                               :14
## Min.
           :6
               Min.
                             Min.
                                          Min.
                                                       Min.
               1st Qu.:12
  1st Qu.:6
                             1st Qu.:12
                                          1st Qu.:13
                                                        1st Qu.:14
## Median:6
              Median :12
                            Median :12
                                          Median:13
                                                       Median:14
## Mean :6
               Mean :12
                            Mean :12
                                          Mean
                                                 :13
                                                       Mean
                                                              :14
## 3rd Qu.:6
                3rd Qu.:12
                             3rd Qu.:12
                                          3rd Qu.:13
                                                        3rd Qu.:14
## Max.
          :6
               Max. :12 Max.
                                    :12
                                          Max.
                                                 :13
                                                       Max.
                                                              :14
          ۷6
##
## Min.
           :23
## 1st Qu.:23
## Median :23
## Mean
         :23
## 3rd Qu.:23
## Max.
          :23
SDs<- apply(t(num_elements_solutions), 2, sd)</pre>
SDs
## [1] 0 0 0 0 0 0
#Since all the solutions have the same totwithinss, I pick one randomly
my_solution<-sample(my_solutions, 1)</pre>
#Plot the solution
g <- set.vertex.attribute(g, "group", value=my_solution[[1]]$cluster)
if (length(my_solution[[1]]$size)!=1){
  ColNode <- rainbow(length( my_solution[[1]]$size))[as.numeric(cut(V(g)$group,breaks = length( my_solution[[1]]$)
}else{ColNode=rep("#666666",length(sc))}
g <- set.vertex.attribute(g, "color", value=ColNode)
#Node sizes
mns <- 5 #Min node size for plotting
Mns <- 20 #Max node size for plotting
a <- (Mns-mns)/(max(sc)-min(sc))
y0 \leftarrow Mns - ((Mns-mns)*max(sc))/(max(sc)-min(sc))
#edge sizes
mes <- 1 #Min edge size for plotting
Mes <- 10 #Max edge size for plotting
ae <- (Mes-mes)/(max(Gpq)-min(Gpq))</pre>
y0e <- Mes - ((Mes-mes)*max(Gpq))/(max(Gpq)-min(Gpq))
```

```
rgl.open()# Open a new RGL device
par3d("windowRect"= c(0,0,1300,1300))
rgl.bg(color = "white") # Setup the background color
rglplot(g, layout=as.matrix(coords), vertex.color=V(g)$color, vertex.size= y0 + a*V(g)$sc, vertex.label =
        vertex.label.color="black", vertex.label.dist=1, edge.width= y0e + ae*E(g)$Gpq, edge.color=E(g)
#legend3d("top", legend ="Communicability (full) communities", cex=1, bty = "n")
rgl.viewpoint( zoom = .8 )
#Ejes en 0,0
rgl.lines(c(-1, 1), c(0, 0), c(0, 0), color = "green")
rgl.lines(c(0, 0), c(-1,1), c(0, 0), color = "green")
rgl.lines(c(0, 0), c(0, 0), c(-1,1), color = "green")
#Export to pnq
rgl.snapshot( 'communicability_full.png', fmt = "png", top = TRUE )
my_clusters <- data.frame(names=names[,2],my_solution[[1]]$cluster)</pre>
my_clusters <- my_clusters[order(my_clusters[2]),]</pre>
write.xlsx(my_clusters, paste(myWD,"/my_clusters_full.xlsx",sep=""))
# Para cada cluster, calculo el centroide, la distancia al centroide de cada nodo, y luego el radio med
n_elements3 <-rep(0, num_clusters3)</pre>
centroid3 <-list()</pre>
rads3 <- list()
Avg_radius3 <-rep(0, num_clusters3)</pre>
pack_index3 <-rep(0, num_clusters3) #Pack_index: Compacticidad Avg_radius/n_elements</pre>
max_radius3 <-rep(0, num_clusters3)</pre>
for (i in 1:num_clusters3){
  centroid3[[i]] <- colMeans(coords[V(g)$group==i,])</pre>
  rads3[[i]] <- sqrt(rowSums((coords[V(g)$group==i,]-centroid3[[i]])^2))</pre>
  Avg_radius3[i] <- mean(rads3[[i]])</pre>
  n_elements3[i] <- nrow(coords[V(g)$group==i,])</pre>
 pack_index3[i] <- Avg_radius3[i] / n_elements3[i]</pre>
 max_radius3[i] <- max(rads3[[i]])</pre>
#Infomap
length(clusters)
## [1] 1
Avg_radius
```

[1] 0.004392951

```
mean(Avg_radius)
## [1] 0.004392951
n_{elements}
## [1] 80
pack_index #Pack_index: Avg_radius/n_elements
## [1] 5.491189e-05
mean(pack_index)
## [1] 5.491189e-05
max_radius
## [1] 0.01211865
{\it \#Communicability reduced}
num_clusters2
## [1] 5
Avg_radius2
## [1] 0.005128112 0.003594130 0.009721367 0.006439820 0.002391861
mean(Avg_radius2)
## [1] 0.005455058
n_{elements2}
## [1] 13 19 7 12 29
pack_index2 #Pack_index: Compacticidad Avg_radius/n_elements
## [1] 3.944701e-04 1.891648e-04 1.388767e-03 5.366517e-04 8.247795e-05
mean(pack_index2)
```

[1] 0.0005183062

```
{\tt max\_radius2}
## [1] 0.008689813 0.006152763 0.017174269 0.008216948 0.004045419
#Communicability full
num_clusters3
## [1] 6
Avg_radius3
## [1] 0.002612369 0.006294708 0.004609075 0.001651044 0.007072672 0.013078445
mean(Avg_radius3)
## [1] 0.005886386
n_{elements3}
## [1] 23 12 14 13 12 6
pack_index3 #Pack_index: Compacticidad Avg_radius/n_elements
## [1] 0.0001135813 0.0005245590 0.0003292197 0.0001270034 0.0005893893
## [6] 0.0021797409
mean(pack_index3)
## [1] 0.0006439156
max_radius3
```

[1] 0.004531512 0.008452125 0.006520937 0.003180517 0.009447945 0.016672674