

描述



CS101@ShanghaiTech

Programming assignment 4

Interval of interest

Motivation

A sequence of intergers are given: $i_1, i_2, ..., i_n$. Define the interval of interest(IOI) with respect to x , parameterized by $[l, r]$ subjected to: $\gcd(i_l, i_{l+1}, ..., i_r)=x$, where $1 \leq l \leq r \leq n$.

Gcd here means the greatest common divisor.

Goal

Count all possible intervals with respect to $x=x_1, x_2, ..., x_q$ for the given sequence $i_1, i_2, .., i_n$.

Interval of interest w.r.t 4						
	$l=2, r=4$		$x=4$	✓		
	15,	12, 24, 64,	12			
	i_1	i_2	i_3		i_4	i_5
	$l=2, r=5$		$x=4$			
	15,	12, 24, 64,			12	
	$l=3, r=5$		$x=4$			
	15, 12	24, 64,			12	
	$l=4, r=5$		$x=4$			
	15, 12, 24,	64,			12	
	$l=2, r=3$		$x=12$	✗		
	15,	12, 24,	64, 12			
				$\Sigma=4$ w.r.t. $x=4$		

输入

1. The first line: an integer n , ($1 \leq n \leq 10^5$), indicating the length of the given sequence.
2. Next line: n integers separated by space: $i_1, i_2, ..., i_n$ ($1 \leq i_{\{ \}} \leq 10^9$).
3. The third line: an integer q , ($1 \leq q \leq 3 \cdot 10^5$), indicating the number of x s
4. The forth line: q integers separated by space: $x_1, x_2, ..., x_q$, ($1 \leq x_{\{ \}} \leq 10^9$).

输出

For each x , output the number of possible IOIs with respect to $x_1, x_2, ...$

输入样例 1

5

15 12 24 64 12

2

4 12

输出样例 1

4 3

提示

- Observation1:** $\gcd(a, b, c) = \gcd(\gcd(a, b), c)$
- Observation2:** for the sequence $i_1, ..., i_n$, define the sequence $k_1=i_1, k_j=\gcd(k_{\{j-1\}}, i_{\{j\}})$ for $2 \leq j \leq n$. The number of distinct values in k sequence is no more than $1+\log_2\{i_1\}$.
- Hint1:** Divide & conquer may be useful:

1. count IOIs at left half(by recursion)

2. count IOIs at right half(by recursion)

3. merge and conut intervals that start from the left half and end at right half(how to count efficiently?, hint: observation 2)
- Hint2:** try to set a AVL tree / hash, count gcd for all x in one time.
- Hint3:** the solution of $n\log n$ is possible