Lesson Objectives

- 1. Solve a linear equation graphically.
 - a. by hand
 - b. with graphing calculator
- 2. Determine if an ordered pair is a solution to a system of linear equations.
- 3. Solve a linear system of equations graphically.
- 4. Classify a system of equations:
 - a. consistent-independent (one solution)
 - b. consistent-dependent (infinite solutions)
 - c. inconsistent (no solutions)

A. Solve a Linear Equation Graphically

- 1. Solve f(x) = c (c is some number)
- **EXAMPLE:** Use the graph of y = f(x) shown to the right to solve each equation. [2.2.55]

(a)
$$f(x) = -1$$

(b)
$$f(x) = 0$$

(c)
$$f(x) = 2$$

(a) f(x) = -1 means that ___ = -1.

In the graph when y = -1, x =

That's the point: (3, -1).

The solution to f(x) = -1 is x =____.

(b) f(x) = 0 means that ___ = 0.

In the graph when y = 0, x =

That's the point: (4,0).

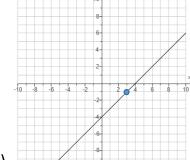
The solution to f(x) = 0 is x =____.

(c) f(x) = 2 means that ___ = 2.

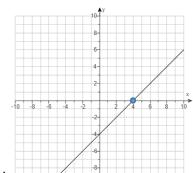
In the graph when y = 2, x =___

That's the point: (6,2).

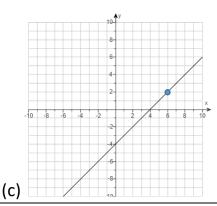
The solution to f(x) = 0 is x =____.



(a)



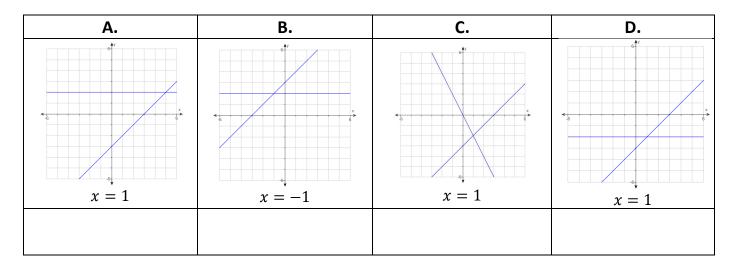
(b)



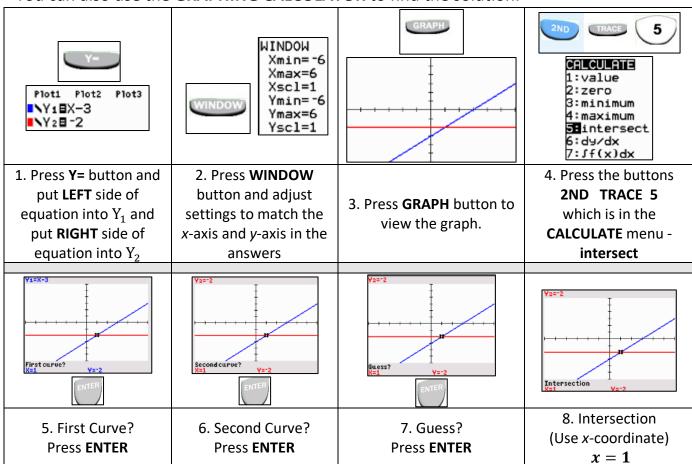
2. Solve equation graphically

• **EXAMPLE:** Let y_1 equal the left side and let y_2 equal the right side of the given equation. Graph y_1 and y_2 and use the graph to solve the equation x - 3 = -2 [2.2-19]

 $y_2 = \underline{\hspace{1cm}}$ y-intercept: $(0,\underline{\hspace{1cm}})$, slope $m = \underline{\hspace{1cm}}$ ($\underline{\hspace{1cm}}$ line through y-axis at -2)



You can also use the **GRAPHING CALCULATOR** to find the solution.



B. Systems of Linear Equations

_____ of linear equations – involves two or more linear equations at the same time.

_____ to a linear system – values of the variables that make _____

the equations in the system _____

- 1. Determine if an ordered pair is a solution
- **EXAMPLE:** Decide whether the ordered pair (2, -5) is a solution to the given system.

$$\begin{cases} 2x + y = 9 \\ 3x + 2y = 16 \end{cases}$$
 [6.1-15]

Given (2, -5) means (x = 2, y = -5). ______ these into each equation:

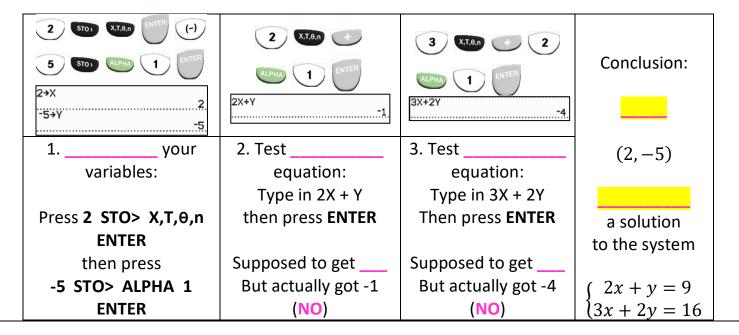
$$\begin{cases} 2(_) + (_) \stackrel{?}{=} 9 \\ 3(_) + 2(_) \stackrel{?}{=} 16 \end{cases} \begin{cases} - + (-5) \stackrel{?}{=} 9 \\ - + (-10) \stackrel{?}{=} 16 \end{cases} \begin{cases} -1 \stackrel{?}{=} 9 \\ -4 \stackrel{?}{=} 16 \end{cases}$$
Conclusion:
$$(2, -5)$$
a solution

NOTE: You must get YES for ______ equation in the system for the point to be a solution!

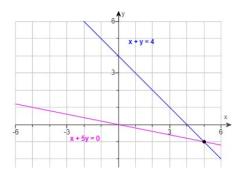
You can also use the _____ method on the graphing calculator.

• **EXAMPLE:** Decide whether the ordered pair (2, -5) is a solution to the given system.

$$\begin{cases} 2x + y = 9 \\ 3x + 2y = 16 \end{cases}$$
 (2, - 5) means $(x = 2, y = -5)$



- 2. Solve a System of Linear Equations Graphically
- **EXAMPLE:** Use the graph of the system to determine the solution.

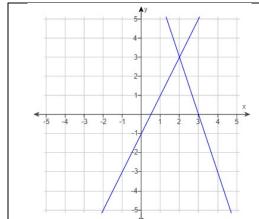


$$\begin{cases} x + y = 4 \\ x + 5y = 0 \end{cases}$$

[6.1.25]

The **solution** to the system is where the lines ______:

• **EXAMPLE:** A system of two linear equations has been solved graphically. Use the graph to find any solutions. [6.1-17]



- **A.** There is an infinite number of solutions.
- **B.** (3,2)
- **C.** (2,3)
- **D.** There are no solutions.

Has no solutions

3. Three Types of Linear Systems

Types of Linear Systems with Two Variables

Consistent system:

Has either one solution (independent equations) or infinitely many solutions (dependent equations)

Inconsistent system:

One Solution

, x

Consistent System Independent Equations Infinitely Many Solutions

x

Consistent System
Dependent Equations

No Solutions

Inconsistent System

• **EXAMPLE:** Graph the system of equations and find any solutions. Check the answers. Identify the system as consistent or inconsistent. If the system is consistent, state whether the equations are dependent or independent. [6.1.35-Setup & Solve]

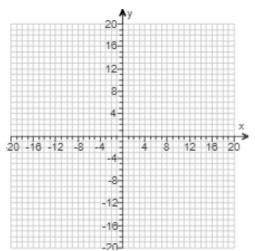
$$\begin{cases} 4x + y = 8 \\ -4x - y = 16 \end{cases}$$

Solve each equation for y so that you can graph. (show your work below)

$$4x + y = 8$$

$$-4x - y = 16$$





What is the solution of the system? There is _____.

y =

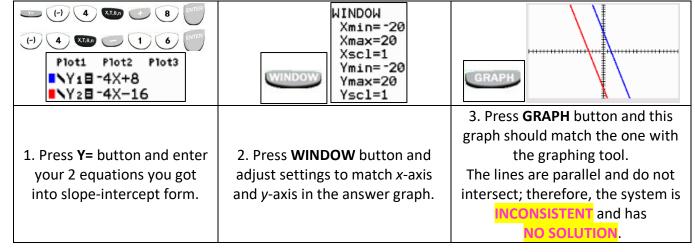
Use the graphing tool to graph the system.

Equation	<i>y</i> -intercept	Slope	rise run
$y_1 = -4x + 8$	(0,)		
$y_2 = -4x - 16$	(0,)		

Identify the system as consistent or inconsistent. If the system is consistent, state whether the equations are dependent or independent.

The system is:

Once you have your equations in slope-intercept form (y = mx + b), you can also verify you have the correct lines using your graphing calculator – assuming you made no errors.



• **EXAMPLE:** Graph the system of equations and find any solutions. Check the answers. Identify the system as consistent or inconsistent. If the system is consistent, state whether the equations are dependent or independent. [6.1.39]

$$\begin{cases} x - 2y = -6 \\ -2x + y = 6 \end{cases}$$

Solve each equation for **y** so that you can graph. (show your work below)

$$1x - 2y = -6$$

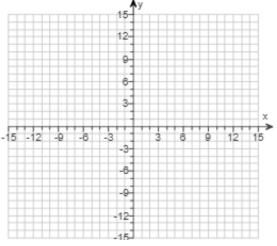
$$-2x + y = 6$$

y =



Use the graphing tool to graph the system.

Equation	<i>y</i> -intercept	Slope	rise run
$y_1 = \frac{1}{2}x + 3$	(0,)		
$y_2 = 2x + 6$	(0,)		



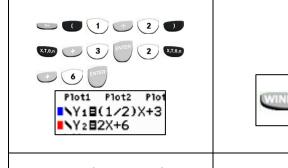
What is the solution of the system? (Type an ordered pair.)

The solution is

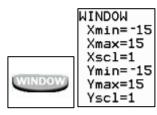
Identify the system as consistent or inconsistent. If the system is consistent, state whether the equations are dependent or independent.

The system is: _____ and the equations are _____.

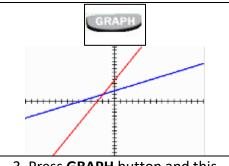
Once you have your equations in slope-intercept form (y = mx + b), you can also verify you have the correct lines using your graphing calculator – assuming you made no errors.



 Press Y= button and enter your 2 equations you got into slope-intercept form.

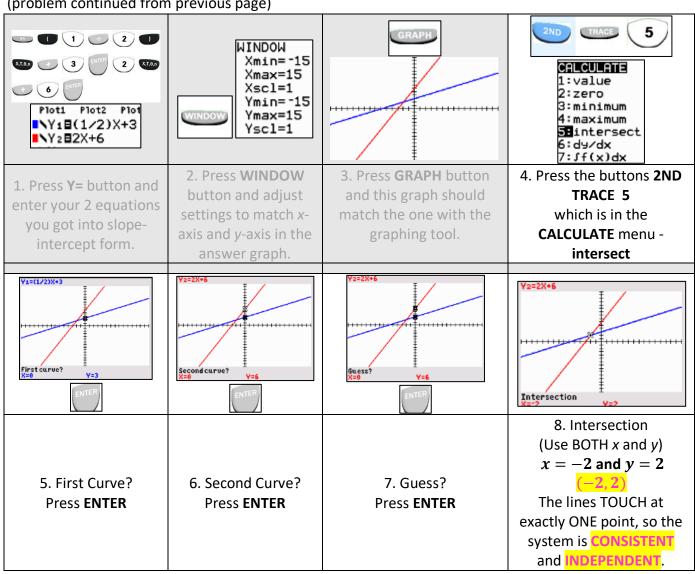


2. Press **WINDOW** button and adjust settings to match *x*-axis and *y*-axis in the answer graph.



3. Press **GRAPH** button and this graph should match the one with the graphing tool.

(problem continued from previous page)



EXAMPLE: Solve the system of equations by graphing. Then classify the system.

$$\begin{cases} x + y = 2 \\ 8x + 8y = 16 \end{cases}$$
 [6.1.41]

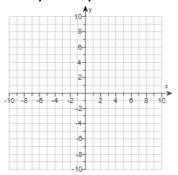
Solve each equation for y so that you can graph. (show your work below)

$$x + y = 2$$

$$8x + 8\mathbf{y} = 16$$



These equations are the _____ line! Since they TOUCH on top of each other, it's and



<i>y</i> -intercept	Slope	rise run
(0,)		

There are solutions.

Sources used:

- 1. Pearson MyLab Math College Algebra with Modeling and Visualization, 6th Edition, Rockswold
- 2. Wabbitemu calculator emulator version 1.9.5.21 by Revolution Software, BootFree ©2006-2014 Ben Moody, Rom8x ©2005-2014 Andree Chea. Website https://archive.codeplex.com/?p=wabbit