

Assignment 1 Bonus - DD2424 - One Layer Network

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Exercise 2 - Optional for Bonus Points

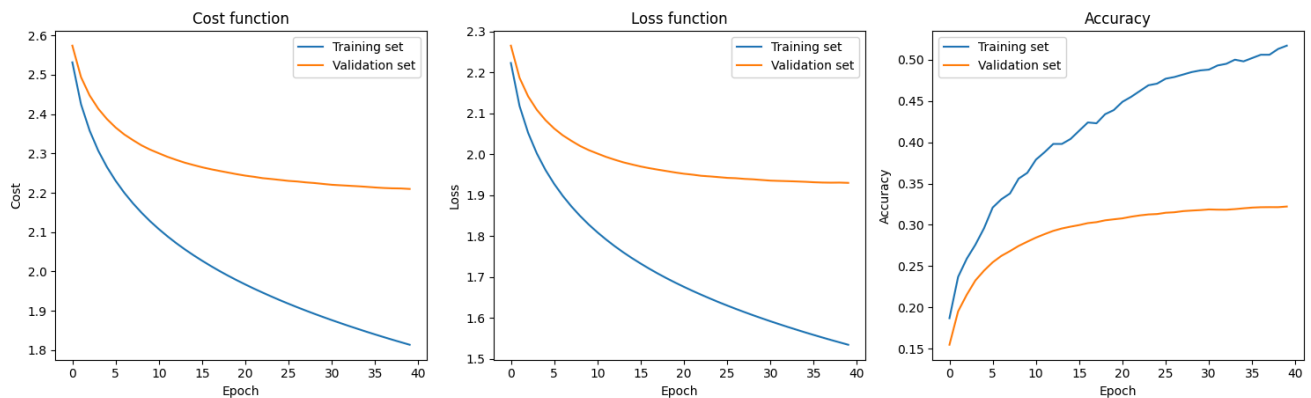
Improve performance of the network

The goal now is to improve the model by adding some techniques.

At first, I retrieve all the data and I normalize it after that I split it into a training, validation and test set. I also implement a grid search to see which parameters are the best for the model. This is the best result I obtained:

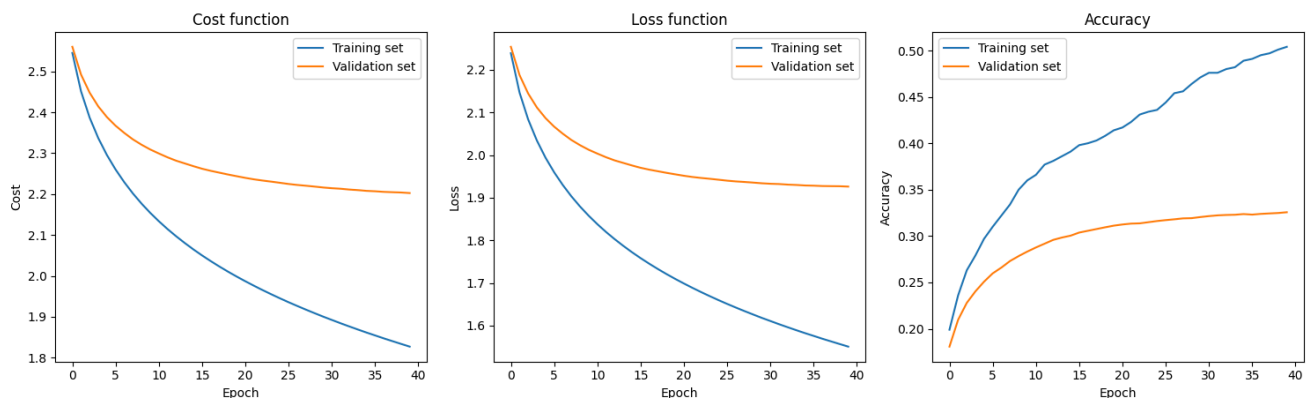
- With old hyperparameters: `lambda=0.1, n_epochs=40, n_batch=100, eta=.001`

Cost, loss and accuracy, final accuracy test: 32.37%



- With best hyperparameters: `lambda=0.5, n_epochs=80, n_batch=100, eta=.001`

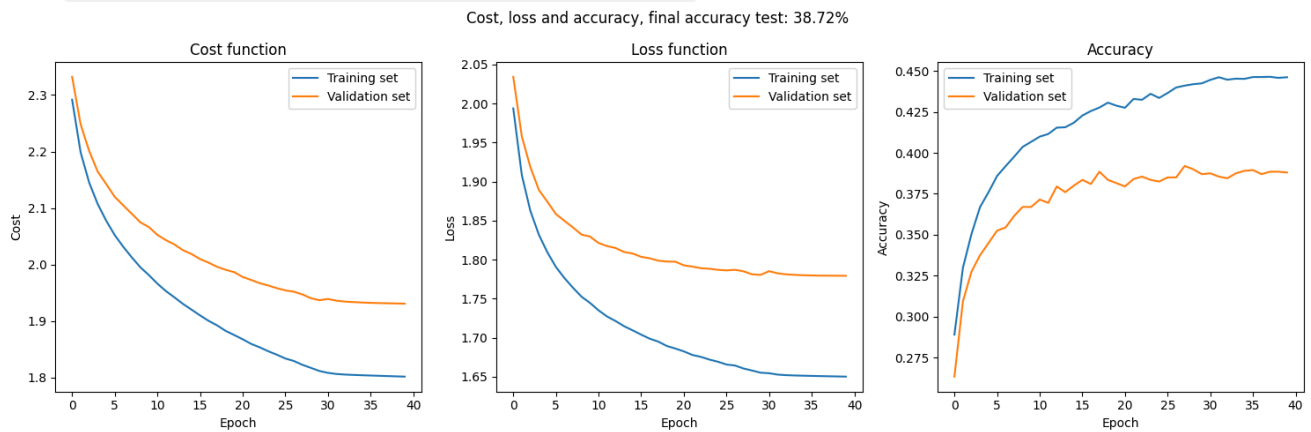
Cost, loss and accuracy, final accuracy test: 32.32%



Unfortunately, we see here not much improvement by selecting all the data! Indeed, it's important to have in mind that we try to classify RGB images with a single layer network ! The capacity to memorize and well classify images for a single layer neural network is not enough. A more complex model is needed to have better results, like a convolutional neural network. However, the grid search is a good way to find the best hyperparameters for the model, it's just a bit long to compute.

After that, I implement the **step decay** and I only used the one batch that we used before. I re used the best parameters but with more epochs to see if the step decay is helping. I obtained the following results:

- With `lambda=0.1, n_epochs=1000, n_batch=100, eta=.1`



Unfortunately, the step decay is not helping, the cost is not decreasing and the accuracy is not increasing compared to the best previous model.

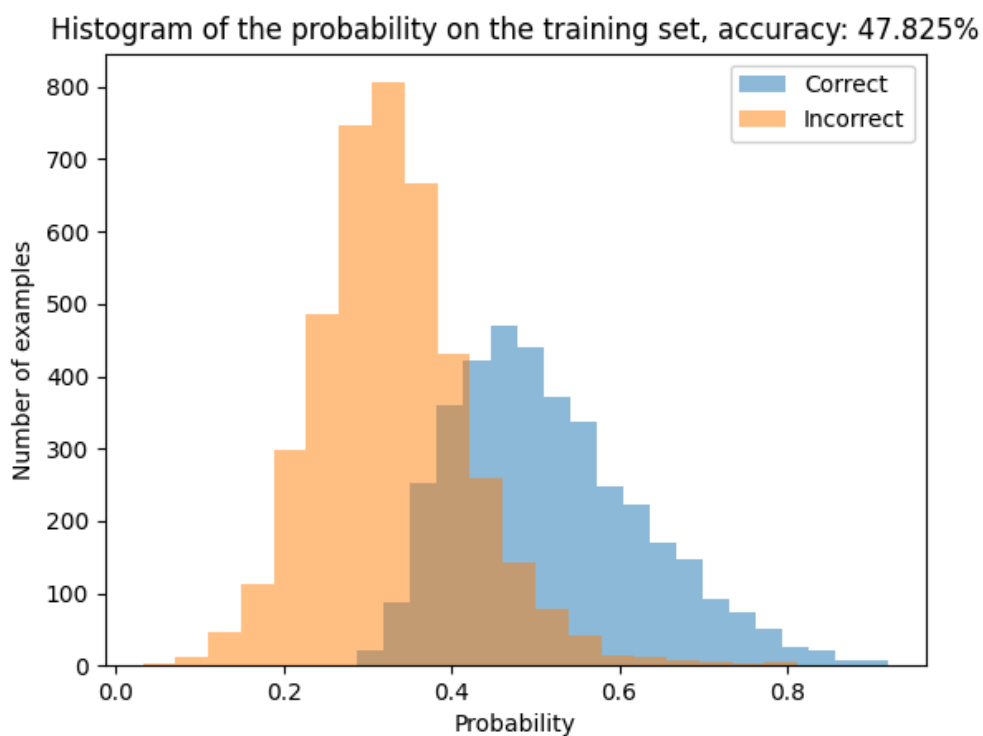
Train network - multiple binary cross-entropy losses

After that, I implement the **multiple binary cross-entropy losses** with **sigmoid** activation function.

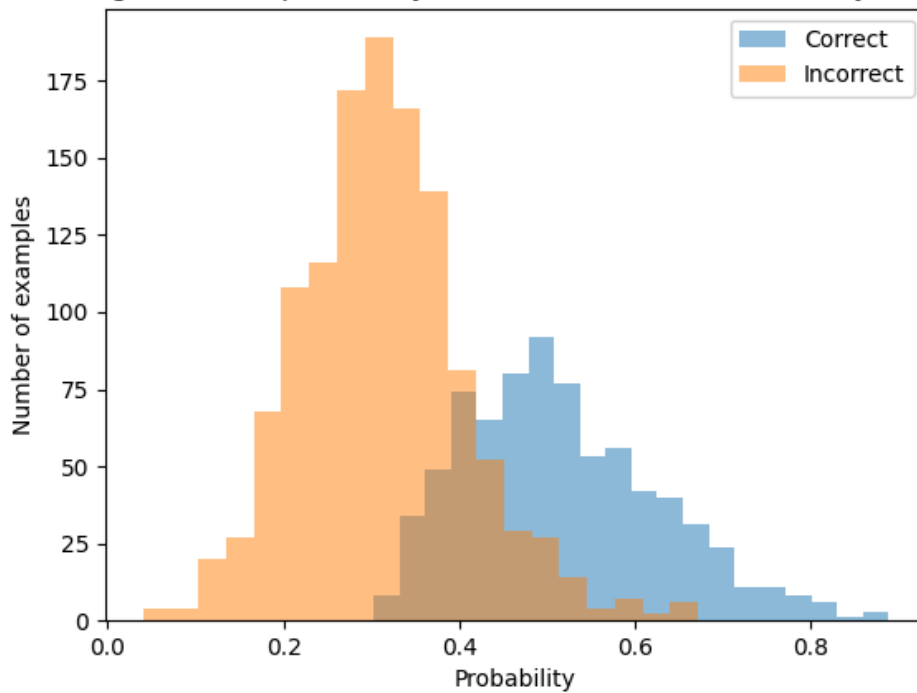
$$\sigma(s) = \frac{1}{1 + e^{-s}} l_{multiple\ bce} = -\frac{1}{K} \sum_{i=1}^K y_i \log(\hat{y}_i) + (1 - y_i) \log(1 - \hat{y}_i) z = Wx + b\hat{y} = \sigma(z)$$

$$\frac{\partial l_{multiple\ bce}}{\partial W} = \frac{\partial l_{bce}}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial z} \frac{\partial z}{\partial W} \frac{\partial l_{multiple\ bce}}{\partial W} = \left(\frac{\hat{y} - y}{\hat{y}(1 - \hat{y})} \right) (\hat{y}(1 - \hat{y}))x = (\hat{y} - y)x \frac{\partial l_{multiple\ bce}}{\partial b} = \frac{1}{K} \sum_{i=1}^K (\hat{y}_i$$

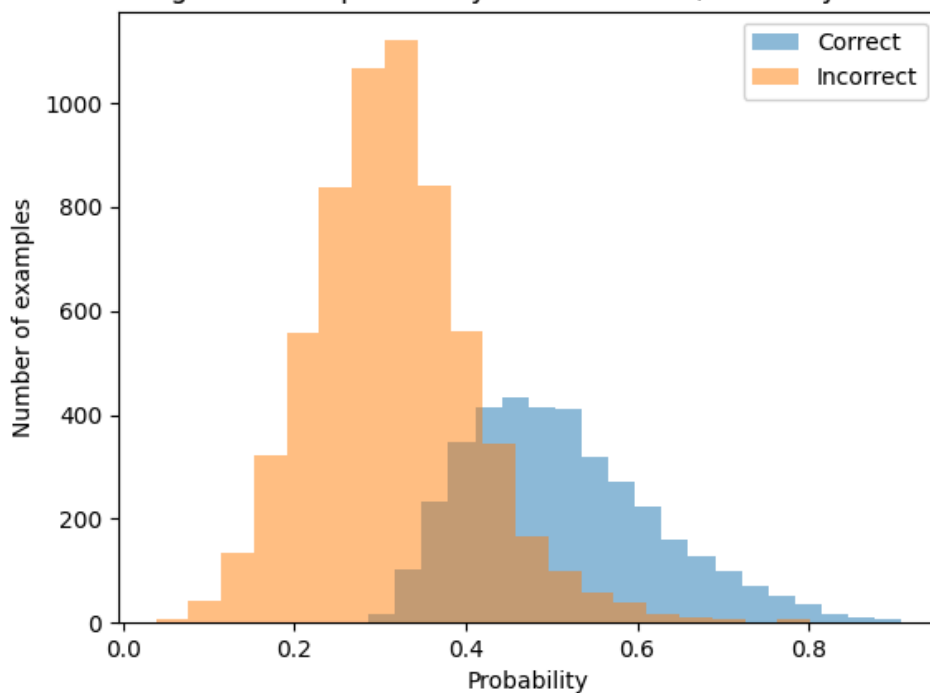
And this is the result I obtained with the hyperparameters: `lambda=0.1, n_epochs=50, n_batch=100, eta=.0001`:



Histogram of the probability for the validation set, accuracy: 38.25%



Histogram of the probability on the test set, accuracy: 37.64%



Here we have not a huge improvement on the accuracy compared to the previous model. The model is not overfitting but we could have a better accuracy by using a more complex model, more adapted to the problem.