

## Worksheet 2 (due Sunday June 19, 11:59 pm)

Course 01435: Practical Cryptanalysis  
June 2016

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### Introductory Remarks

All comments from worksheet 0 apply.

### Meet-In-The-Middle Attacks

#### Recommended Reading

R.C. Merkle and M.E. Hellman. On the Security of Multiple Encryption, 1981.

P.C. van Oorschot and M.J. Wiener. A know-Plaintext Attack on Two-Key Triple Encryption, 1990.

#### Exercises

**Exercise 12 (P):** DES is only using a key size of 56 bits which makes it vulnerable to brute-force attacks. It was suggested to use two 56 bits keys and double encryption to increase the key-space and increase the resistance against those attacks, called *2DES*. The encryption is done in the following way

$$c = E_{k_2}(E_{k_1}(m))$$

- Give the complexity for an exhaustive key search.
- Can you apply a meet-in-the-middle attack to reduce the complexity?
- Would the system be more secure when using  $c = E_{k_2}(E_{k_1}(E_{k_1}(m)))$ .
- Would the system be more secure when using  $c = E_{k_1}(E_{k_2}(E_{k_1}(m)))$ .

**Exercise 13:** DES has a blocksize of 64 bits. When using 2DES with two 56-bit keys:

- What is the expected number of key pairs  $k_1, k_2$  such that  $E_{k_1}(m_1) = D_{k_2}(c_1)$ ?
- What is the expected number of key pairs  $k_1, k_2$  such that  $E_{k_1}(m_1) = D_{k_2}(c_1)$  and  $E_{k_1}(m_2) = D_{k_2}(c_2)$ ?

**Exercise 14:** Another mode 3DES which is still used in practice works uses three 56-bit keys and encrypts a message in the following way

$$c = E_{k_3}(D_{k_2}(E_{k_1}(m)))$$

- Give the complexity for an exhaustive key search.
- Can you still apply a meet-in-the-middle attack?

**Exercise 15 (P):** In this exercise you should implement a meet-in-the-middle attack on a simple block cipher. The block cipher operates on 16-bit blocks and is based on the Feistel structure (see Figure 1). It uses 8-bit independent round keys  $k_i$  and S is the 8-bit AES S-Box. See the C code (`mitm.c`) on CampusNet.

- Implement a meet-in-the-middle attack on this cipher and recover the key.
- Given the following plaintext/ciphertext pairs:

Rounds	Plaintext	Ciphertext
4	0000	4748
	1234	3cf6

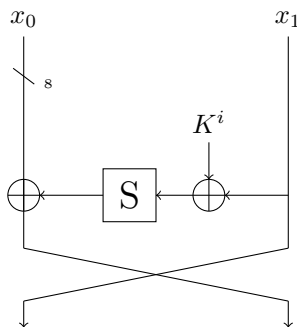


Figure 1: One round of the feistel cipher used in this exercise, where S is the AES S-Box.