

My Simulator - Step Exaplination

October 27, 2021

Introduction

To get the plot data, we need to calculate the probability based on the randomly generating number. So we need to assign these numbers to corresponding interval. At first, I sort the array and iterate over the array to assign these numbers. I tried another method that does not require sorting. The performance does not improve a lot. Through time analysis, I found the main cost was from the iteration. So reducing the number of cycles is critical to performance. Based on the character of sorting, I tried to increase index more than 1 in each cycle. Fortunately, it worked. I tried to analyze how many steps we need to increase every cycle through probability.

Probabilty

Uniform Distribution

Suppose we have 10,000 data and 100 bins. For uniform distribution, in ideal state, each bin has 100 data. However, there exists bias. Suppose the step is x . The bias can be $1, 2, \dots, x-1$. Each has $\frac{1}{x}$ probability. The total cycles for one bin can be calculated by

$$\frac{100}{x} + \frac{x * (x - 1)}{2 * x} = \frac{100}{x} + \frac{x - 1}{2} \quad (1)$$

To minimize the formula, we should choose $x = \sqrt{200} = 14$. I used program to verify the idea. The result is same.

```

1  for step in range(1,40):
2      total_time = 0
3      total_cycle = 0
4      for i in range(0,100):
5          mu, sigma = 3,7
6          x,y,t,cycle = Uniform(mu, sigma,step)
7          total_time += t
8          total_cycle += cycle
9      print(step,total_time/100,total_cycle/100)

```

1	0.01186688899938964	10000.0
2	0.006400179862976074	5075.23
3	0.0046367192268371585	3466.82
4	0.0038373327255249025	2687.62
5	0.0034091639518737792	2240.8
6	0.003099534511566162	1958.0
7	0.0028620505332946776	1770.4
8	0.0027508282661437987	1644.8
9	0.0026365232467651365	1556.48
10	0.0025994491577148436	1497.61
11	0.0025410032272338867	1448.4
12	0.0025718331336975096	1426.71
13	0.0025388026237487793	1419.64
14	0.0025403165817260744	<u>1413.24</u>
15	0.0025771522521972658	1418.56
16	0.002607076168060303	1415.95
17	0.0026194000244140624	1441.28
18	0.002629528045654297	1451.21
19	0.002665207386016846	1469.08
20	0.0027320218086242676	1505.67
21	0.002742805480957031	1535.6
22	0.0027956008911132813	1550.02
23	0.0028055286407470703	1568.06
24	0.0028483033180236816	1606.15
25	0.0029718780517578123	1665.04
26	0.003029818534851074	1737.25
27	0.0030639100074768065	1757.48
28	0.0030347156524658204	1756.63
29	0.0030283665657043456	1752.04
30	0.0030641245841979982	1730.94
31	0.0030532956123352053	1756.6
32	0.0031549382209777833	1834.6
33	0.003326010704040527	1946.24

Figure 1: Uniform Distribution Step

Normal Distribution

For normal distribution, I calculate the number of data in each bin in ideal state and change the step based on it. Though the total cycle decrease, the extra calculation costs more time. I decided to estimate one value for step. Suppose the total interval length is 8σ . So every 2σ contains 25 bins. Based on the character of Normal Distribution and the assumption that the bias has uniform distribution, we can get our round estimation.

$$\frac{6820}{25 * x} + \frac{x - 1}{2} + \frac{2720}{25 * x} + \frac{x - 1}{2} + \frac{420}{25 * x} = \frac{9960}{25 * x} + \frac{3 * x}{2} - \frac{3}{2} \quad (2)$$

The best step is about 16. And the program shows similar result.

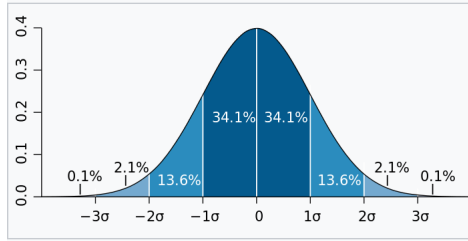


Figure 2: Normal Distribution. Source: Wikipedia

```

1  for step in range(1,40):
2      total_time = 0
3      total_cycle = 0
4      for i in range(0,100):
5          mu, sigma = 3,7
6          x,y,t,cycle = normB(mu, sigma,step)
7          total_time += t
8          total_cycle += cycle
9      print(step,total_time/100,total_cycle/100)

```

```

1 0.011763937473297119 10000.0
2 0.006432297229766845 5067.34
3 0.004783821105957031 3451.78
4 0.004012978076934815 2664.04
5 0.0034560465812683103 2209.56
6 0.003127739429473877 1914.9
7 0.003084707260131836 1721.32
8 0.0029529190063476564 1582.29
9 0.0029254841804504396 1481.84
10 0.002750706672668457 1402.03
11 0.002683298587799072 1355.7
12 0.0025928497314453127 1321.33
13 0.0025288748741149904 1285.72
14 0.002563655376434326 1271.02
15 0.002576150894165039 1269.32
16 0.0025766658782958984 1254.1
17 0.002517256736755371 1257.92
18 0.002516908645629883 1251.12
19 0.00254561185836792 1272.7
20 0.0026000094413757323 1277.67
21 0.0025832962989807127 1297.6
22 0.0025513625144958497 1287.1
23 0.002620418071746826 1304.5
24 0.002950873374938965 1324.17
25 0.0026840567588806152 1339.84
26 0.0027476143836975097 1375.5
27 0.0027990031242370607 1384.12
28 0.002798354625701904 1393.48
29 0.002850031852722168 1416.04
30 0.002904794216156006 1440.36

```

Figure 3: Normal Distribution Step

Gamma Distribution

It is hard to analyze the Gamma Distribution. But based on python program, for most cases (except shape is close to 0), 17 is a good choice.

```

1  for step in range(1,40):
2      total_time = 0
3      total_cycle = 0
4      for i in range(0,100):
5          shape,scale = 3,7
6          x,y,t,cycle = Gamma(shape,scale,step)
7          total_time += t
8          total_cycle += cycle
9      print(step,total_time/100,total_cycle/100)

```

1	0.012365310192108155	10000.0
2	0.006805665493011474	5060.8
3	0.004944388866424561	3439.54
4	0.0041567254066467284	2645.44
5	0.0036684346199035646	2186.08
6	0.0033307695388793946	1888.25
7	0.003173038959503174	1687.36
8	0.003015613555908203	1544.35
9	0.0028899645805358885	1444.4
10	0.002818622589111328	1361.08
11	0.002792818546295166	1303.9
12	0.0027403974533081053	1256.21
13	0.002704651355743408	1235.32
14	0.002694427967071533	1209.14
15	0.002689361572265625	1191.06
16	0.002694599628448486	1176.85
17	0.0026636862754821776	1166.88
18	0.0027050137519836425	1174.11
19	0.002679414749145508	1176.04
20	0.0027202415466308595	1183.43
21	0.0026968717575073242	1186.4
22	0.0027088451385498045	1193.86
23	0.0028308129310607912	1198.02
24	0.002881004810333252	1211.24
25	0.0028670930862426756	1212.16
26	0.0028252005577087402	1239.25
27	0.00287893533706665	1265.82
28	0.00287663459777832	1268.74
29	0.00296755522918701	1288.08
30	0.002857973575592041	1286.66

Figure 4: Normal Distribution Step

Finally, I decrease the Simulation time to less than 3ms.

My Simulator

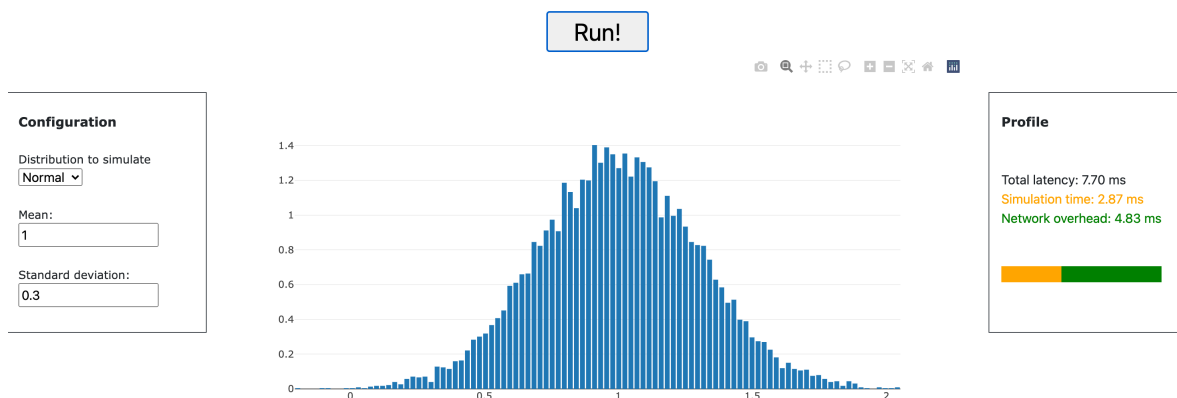


Figure 5: Normal Distribution Simulator

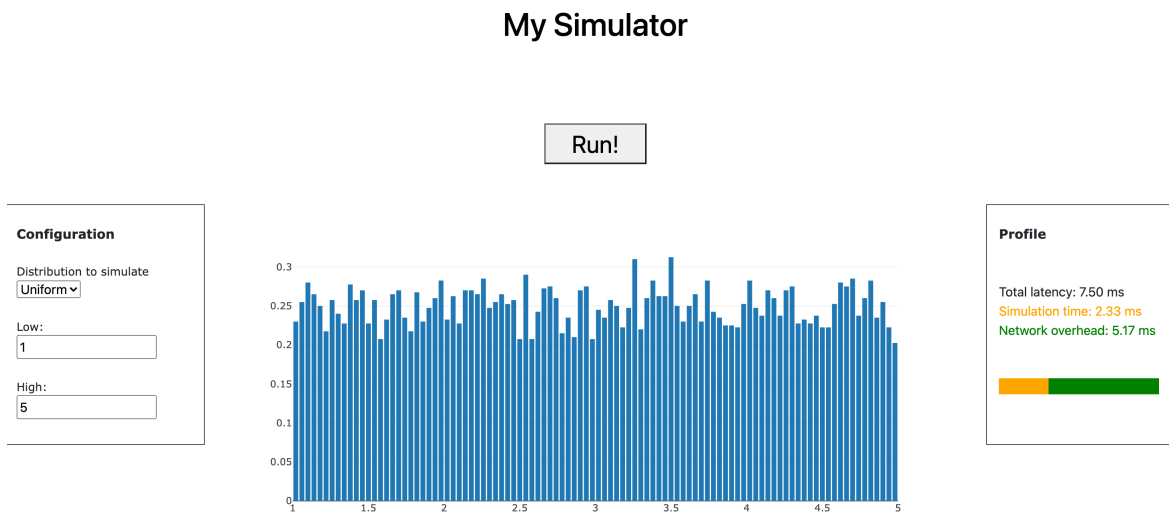


Figure 6: Uniform Distribution Simulator

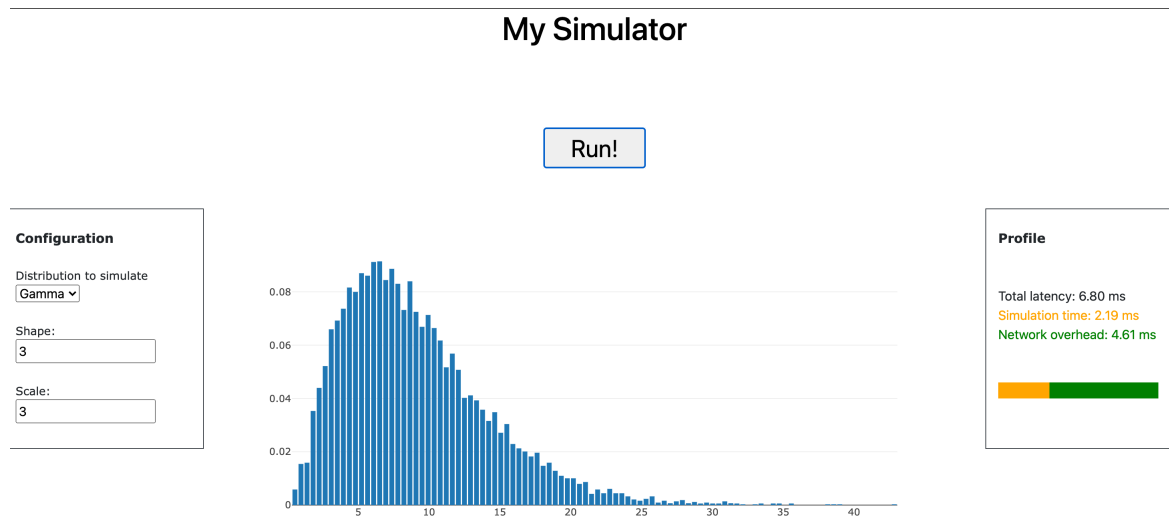


Figure 7: Gamma Distribution Simulator

All the data is got from test on Macbook Pro 2016, 2.7 GHz Quad-Core Intel Core i7.