

EEC133 Midterm Formula Sheet

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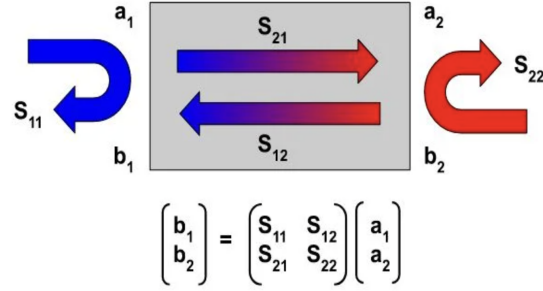


Figure 1: S Parameter

db to dbm

$$P(\text{dBm}) = 10 \times \log(P(w)) + 30$$

Steradian:

$$A = r^2 \Omega$$

where A is the surface area patch, r is the radius, and Ω is the solid angle.

Half Power Beamwidth:

$$\theta_2 - \theta_1$$

where θ_2, θ_1 are the angles where the normalized radiation intensity is $\frac{1}{2}$.

Directivity:

$$D_0 = \frac{4\pi}{\Omega_p} = \frac{4\pi}{\int_{\text{sphere}} F(\theta, \phi) d\Omega}$$

where Ω_p is the pattern solid angle.

$$\frac{A_e}{D_0} = \frac{\lambda^2}{4\pi}$$

where A_e is the effective area of the antenna, D_0 is the directivity of the antenna, and λ is the wavelength of the wave transmitted by the antenna.

Gain

$$G_0 = e \times D_0$$

where e is the efficiency of the antenna.

Poynting Vector

$$\vec{S}_{av} = \hat{z} \frac{|\tilde{E}|^2}{2\eta}$$

Power Radiated from the Antenna

$$|\vec{S}_{avg}| = \frac{e_t P_t}{4\pi r^2} D_t$$

Friss Transmission Equation:

$$\begin{aligned}
\frac{P_{rec}}{P_t} &= e_t e_r \left(\frac{\lambda}{4\pi R} \right)^2 D_t D_r \\
&= \left(\frac{\lambda}{4\pi R} \right)^2 G_t G_r \\
&= \frac{e_r e_t A_t A_r}{\lambda^2 R^2}
\end{aligned}$$

where subscript t denotes the transmitter's parameter, r denotes the receiver's parameter, and R is the distance between two antennas.

Vector Potential

$$\vec{H} = \frac{1}{\mu_0} \nabla \times \vec{A}$$

Retarded Potential

$$\tilde{A}(\vec{r}) = \int \frac{\mu_0 \tilde{J}(\vec{r}') e^{-jkR}}{4\pi R} dV'$$

Hertzian Dipole Antenna: $l < \frac{\lambda}{50}$
Far Field ($r \gg \lambda$)

$$\begin{aligned}
\tilde{E}_{ff,\theta} &= j\eta_0 \frac{Ikl}{4\pi r} e^{-jkr} \sin(\theta) \\
\tilde{H}_{ff,\phi} &= \frac{\tilde{E}_{ff,\theta}}{\eta_0} \\
D(\theta, \phi) &= 1.5 \sin^2(\theta) \\
F(\theta, \phi) &= \sin^2(\theta) \\
P_{rad} &= 40\pi^2 I_0^2 \left(\frac{l}{\lambda} \right)^2 \\
R_{rad} &= 80\pi^2 \left(\frac{l}{\lambda} \right)^2
\end{aligned}$$

Small dipole Antenna: $l < \frac{\lambda}{10}$
Fields are 1/2 those from the Hertzian Dipole.

$$\begin{aligned}
P_{rad} &= 10\pi^2 I_0^2 \left(\frac{l}{\lambda} \right)^2 \\
R_{rad} &= 20\pi^2 \left(\frac{l}{\lambda} \right)^2
\end{aligned}$$

Small Loop Antenna: $a \ll \frac{\lambda}{2\pi}$
Far Fields ($r \gg \lambda$)

$$\begin{aligned}
\tilde{H}_{ff,\theta} &= \frac{Ik^2(\pi a^2)}{4\pi r} e^{-jkr} \sin(\theta) \\
\tilde{E}_{ff,\phi} &= -\tilde{H}_\theta \eta_0 \\
D(\theta, \phi) &= 1.5 \sin^2(\theta) \\
R_{rad} &= 320\pi^6 \left(\frac{a}{\lambda} \right)^4 N^2
\end{aligned}$$

Choosing Capacitor to be in parallel with loop antenna to cancel antenna's input reactance

$$j\omega C - j \frac{X_A}{R_A^2 + X_A^2} = 0$$

where X_A is the input reactance and R_A is the input resistance of the antenna