



Internet of Things

Senior Design Project Course

Signals and Systems

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Signals And Systems



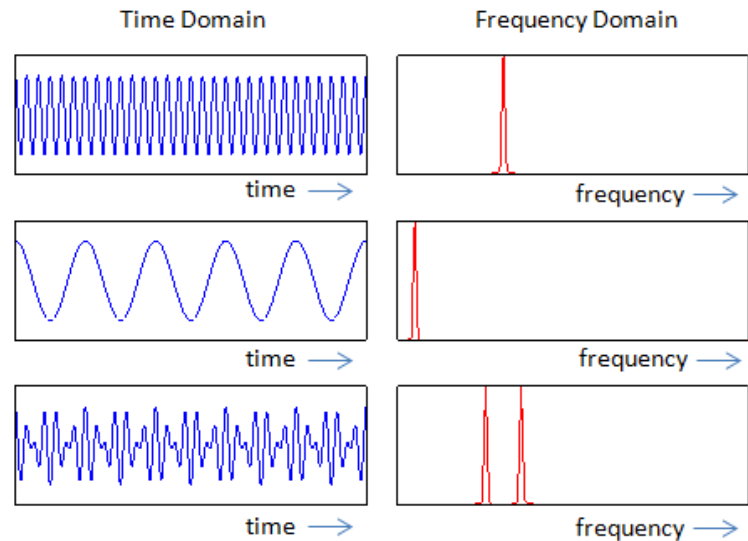
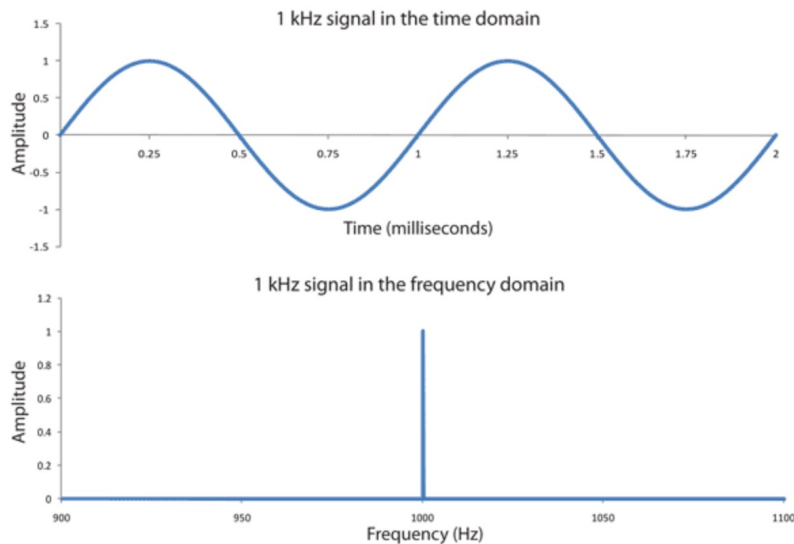
Signals and Systems

- In this part of lecture, we learn the following
 - ❑ Spectrum
 - ❑ Analog vs Digital
 - ❑ Time sampling
 - ❑ Quantization
 - ❑ Pulse Width Modulation

- How is it related to IoT?
 - ❑ Physical world events are continuous, while MCU operate on digital signals.
 - ❑ For reading and interpreting continuous input data from sensors
 - ❑ For generating continuous output data for actuators

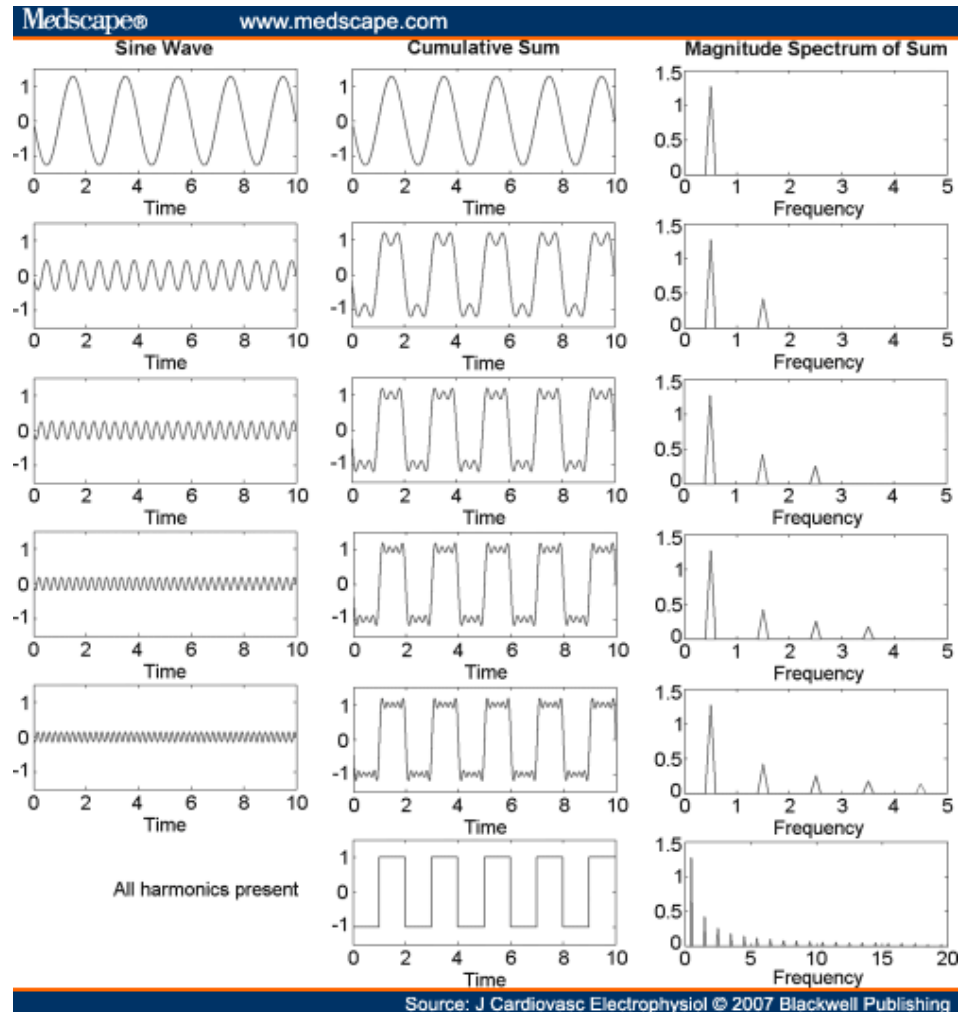
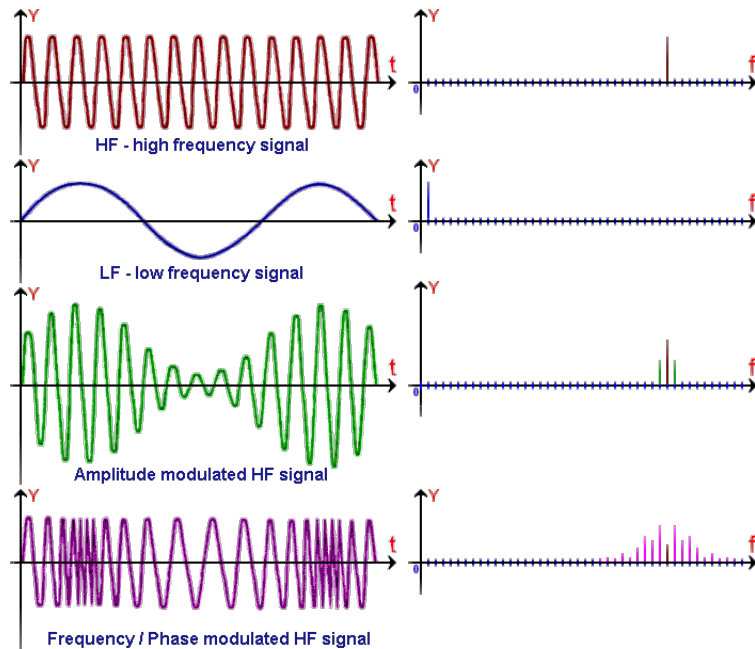
What Is a Signal

- A function that carries information in **Time** and **Frequency**



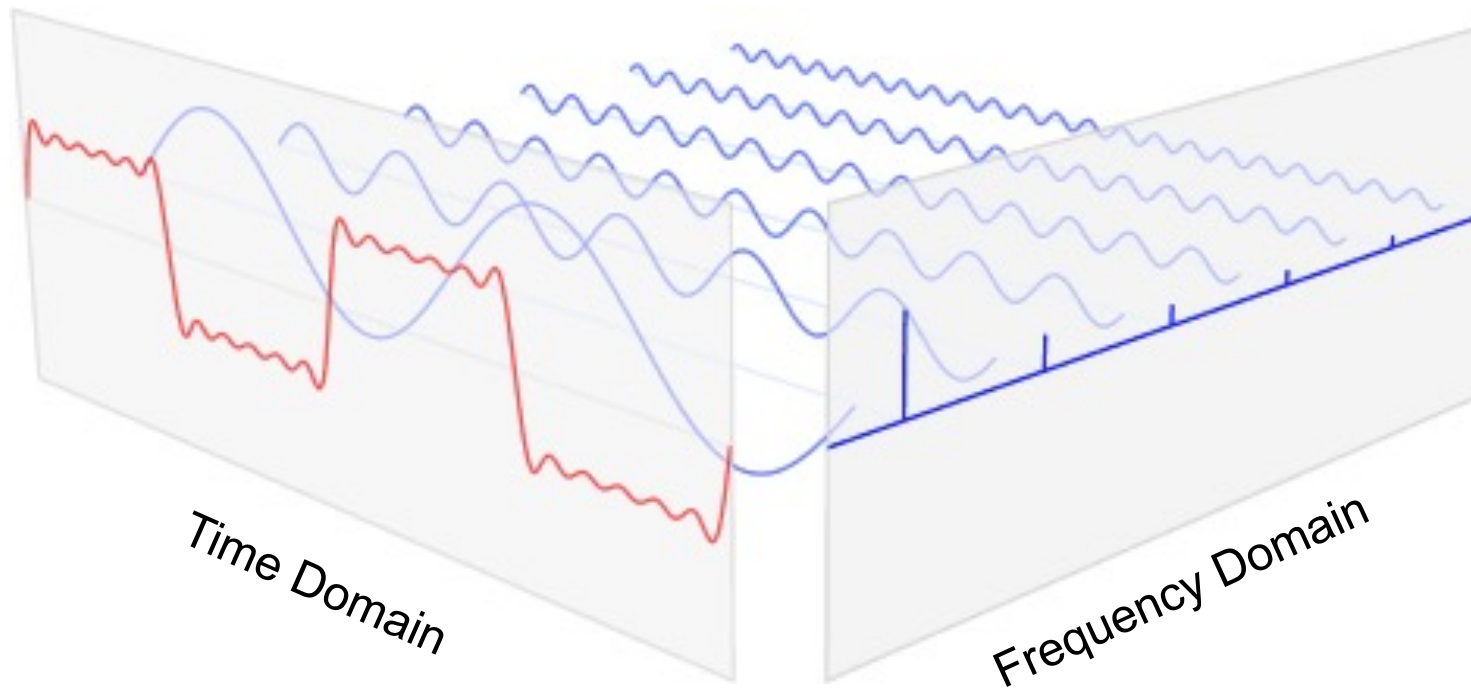
What Is a Spectrum?

- Spectrum is the **representation of a signal in frequency domain**.



Visualizing The Spectrum!

- Visualizing the relationship between time and frequency domain.



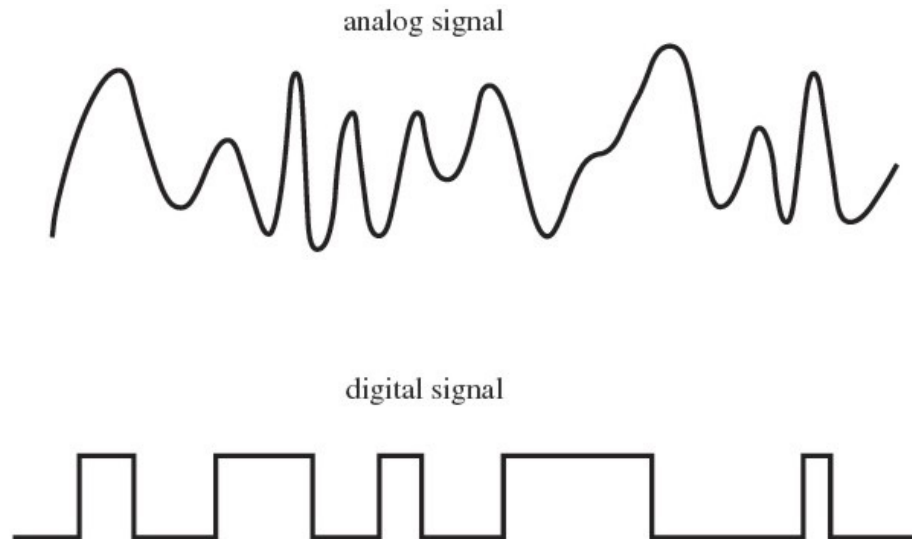
Analog vs Digital Signals

■ Analog

- Continuous
- Usually output of sensors
- ADC → analog to digital converter

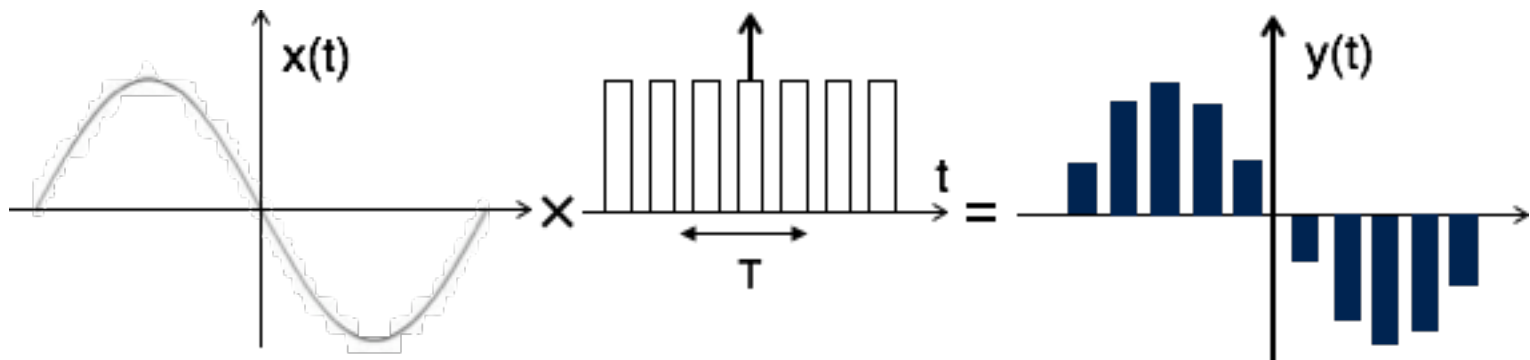
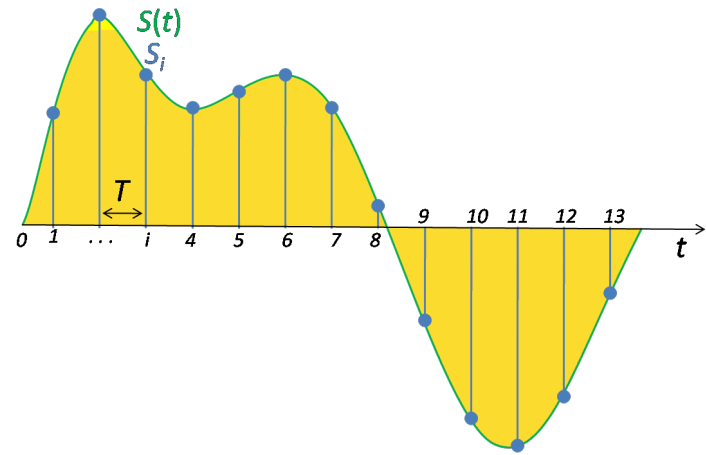
■ Digital

- Discrete/sampled
- Ones and zeros
- What we process
- DAC → digital to analog converter



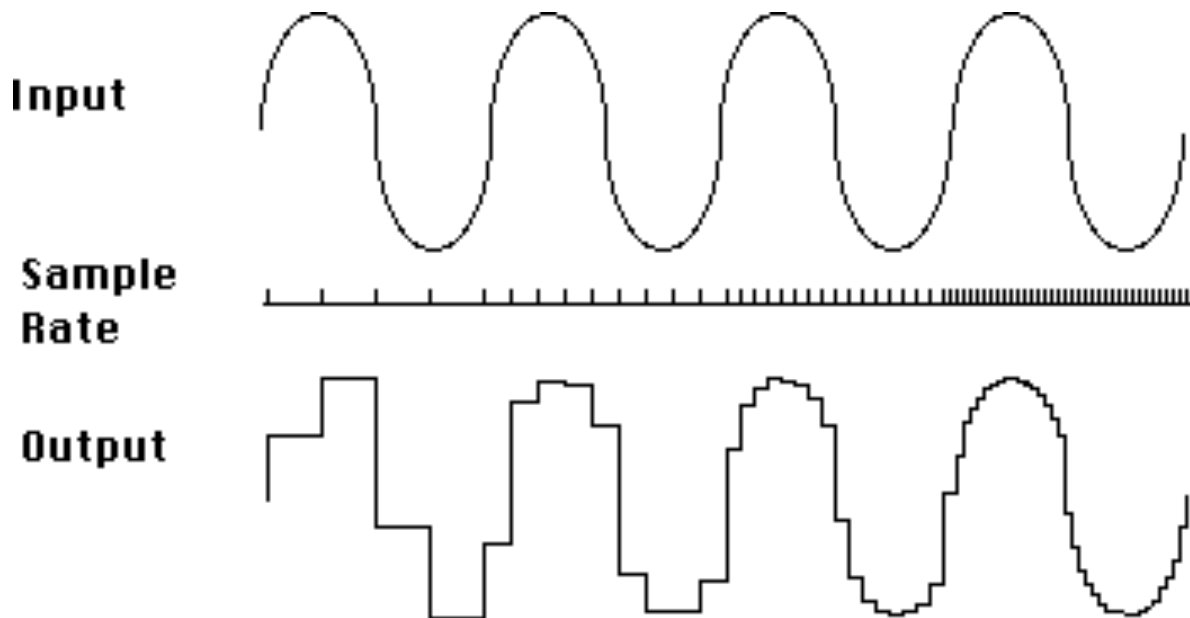
Time Sampling (discrete-time signals)

- F = frequency of sampling
- T = sampling period
- $F = 1/T$



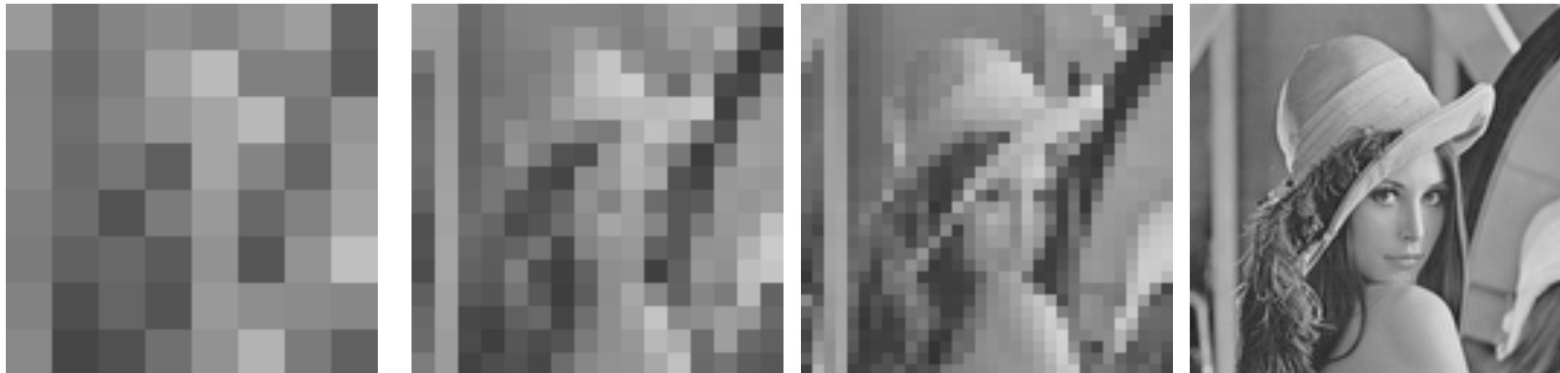
Discrete Time Signals

- Higher sampling rate
 - (+) Higher accuracy
 - (-) Higher power consumption



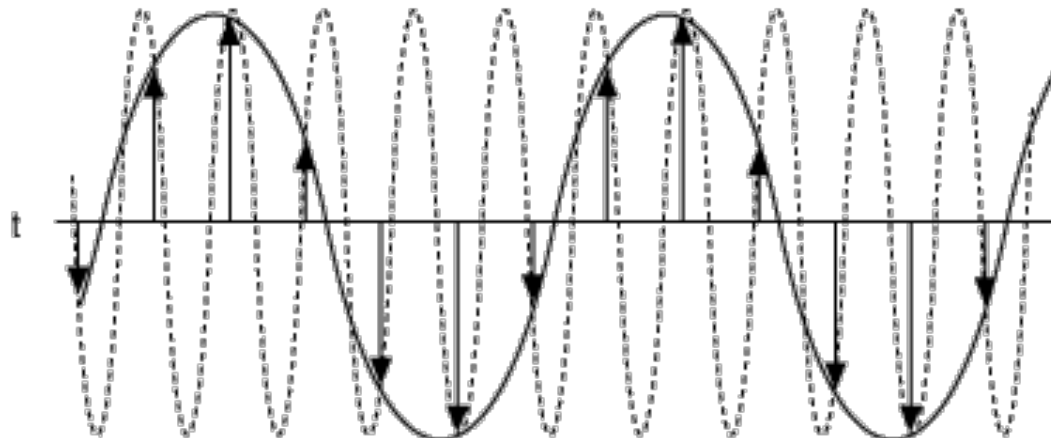
Sampling Two Dimensional Signals

- Pictures are two-dimensional spatial signals
- Videos are three-dimensional spatio-temporal signals
- Below sampling of picture Lena with different spatial sampling rates
 - 8×8 , 16×16 , 32×32 , and 128×128 samples (from left to right)
 - Each sample is represented with $n = 8$ bits
 - Each square represents average of luminance values it covers



Nyquist-Shannon Theorem

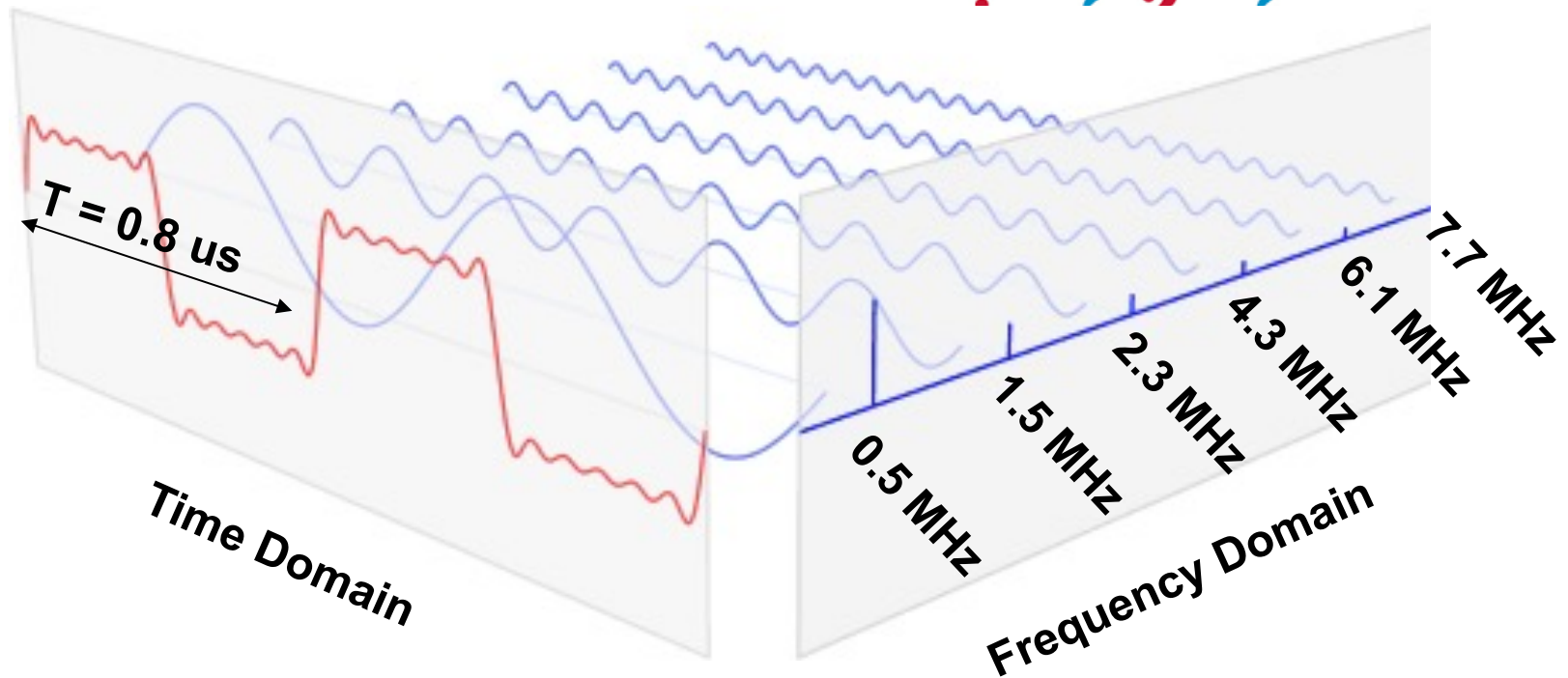
- If a function $x(t)$ contains no frequencies higher than B Hertz, it is completely determined by giving its ordinates at a series of points spaced $1/(2B)$ seconds apart.
- If the sampling frequency is less than $1/(2B)$ a wrong wave form could be sampled (An example is shown below)
- **Rule:**
 - The sampling frequency F_s should be equal or greater than $2B$
 - **$F_s \geq 2B$**



Quiz:

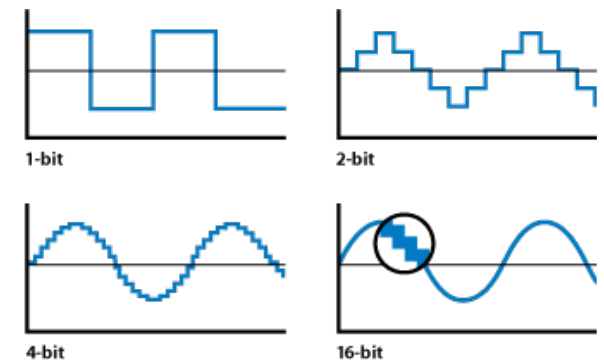
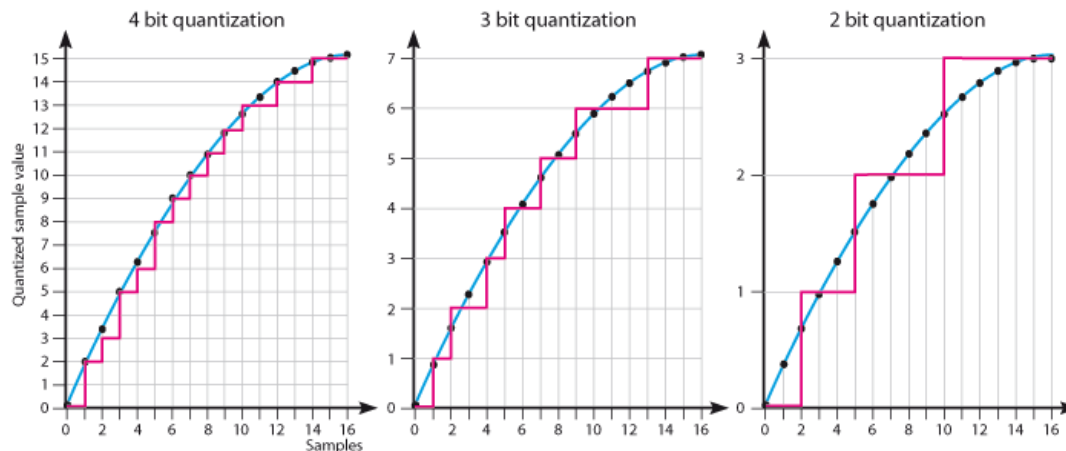
- What should our sampling Period (T) be?

? ? ? ?
quiz
? ? ? ?



Signal Quantization

- **Quantization** is the process of constraining an input from a continuous or otherwise-large set of values (such as the real numbers) to a discrete set.
- Number of quantization bits defines the accuracy of signal estimation.
 - More quantization bits \rightarrow (+) higher accuracy \rightarrow (-) but more data to process and communicate
 - Less quantization bits \rightarrow (-) less accuracy \rightarrow (-) but less data to process and communicate
 - E.g. representing a gray color with 8 bit \rightarrow 256 shades of gray (high quality image)
representing a gray color with 4 bits \rightarrow 16 shades of gray (low quality image)



Two Dimensional Signal Quantization

- Below quantization of picture Lena with different bits/sample
 - $k = 1, 2, 4,$ and 8 bits/sample (from left to right)
 - The spatial sampling rate is fixed to 128×128



Signal Quantization

- A parrot image quantized
 - **W** = width of image in pixels (lets consider
 - **H** = height of image in pixels
 - **3** channels of Red, Green and Blue (RGB) are needed.
 - Lets consider $W \times H = 544 \times 372$ (WebTV image size)
- Size of image
 - 3-bit RGB = $W \times H \times 3 \times 1 = 544 \times 372 \times 3 \times 1 = 607104 \approx 75.8 \text{ KBytes}$
 - 6-bit RGB = $W \times H \times 3 \times 2 = 544 \times 372 \times 3 \times 2 = 1214208 \approx 151.8 \text{ KBytes}$
 - 24bit RGB = $W \times H \times 3 \times 8 = 544 \times 372 \times 3 \times 8 = 4856832 \approx 607.1 \text{ Kbytes}$

3-bit RGB
 $2^{1 \times 3}$ colors



6-bit RGB
 $2^{2 \times 3}$ colors



9-bit RGB
 $2^{3 \times 3}$ colors



12-bit RGB
 $2^{4 \times 3}$ colors



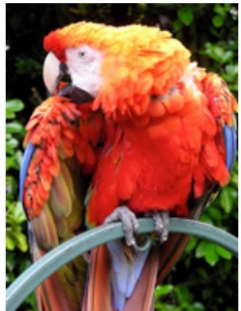
15-bit RGB
 $2^{5 \times 3}$ colors



18-bit RGB
 $2^{6 \times 3}$ colors



24-bit RGB
 $2^{8 \times 3}$ colors



Signal Quantization

- Lets consider we can communicate 1MByte/S and for each MByte/S we consume 1mW.
 - 3-bit RGB $\rightarrow \sim 75.8\text{ms}$ to transfer, $75.8\mu\text{W}$ to communicate \rightarrow consume low power.
 - 6-bit RGB $\rightarrow \sim 151.8\text{ms}$ to transfer, $151.8\mu\text{W}$ to communicate \rightarrow consume twice the power.
 - 24bit RGB $\rightarrow \sim 607.1\text{ms}$ to transfer, $607.1\mu\text{W}$ to communicate \rightarrow consume 8 times the power.

3-bit RGB
 $2^{1 \times 3}$ colors



6-bit RGB
 $2^{2 \times 3}$ colors



9-bit RGB
 $2^{3 \times 3}$ colors



12-bit RGB
 $2^{4 \times 3}$ colors



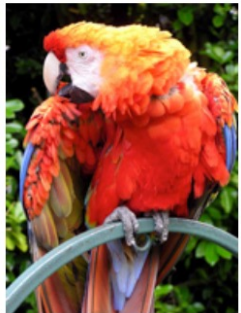
15-bit RGB
 $2^{5 \times 3}$ colors



18-bit RGB
 $2^{6 \times 3}$ colors



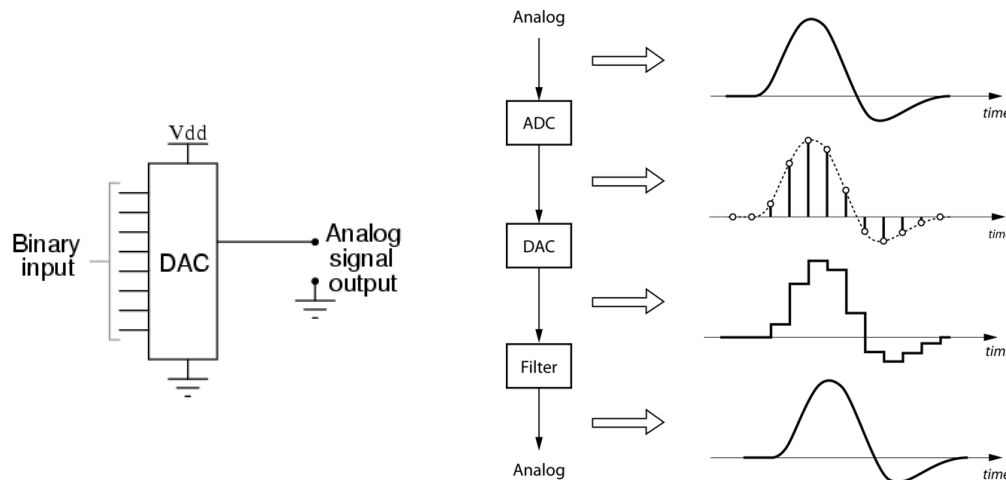
24-bit RGB
 $2^{8 \times 3}$ colors



Signal Conversation

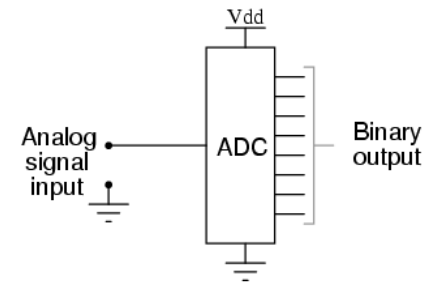
■ Digital to Analog converter

- ❑ **DAC, D/A, D-A, D2A, or D-to-A**
- ❑ A device that converts a digital signal into an analog signal

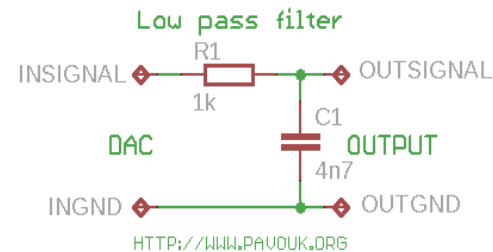


■ Analog to Digital converter

- ❑ **ADC, A/D, A-D, A2D, or A-to-D**
- ❑ A device that converts an analog signal into a digital signal



Generating an analog signal from a discrete signal require a reconstruction *filter* to **smooth** the discrete steps.

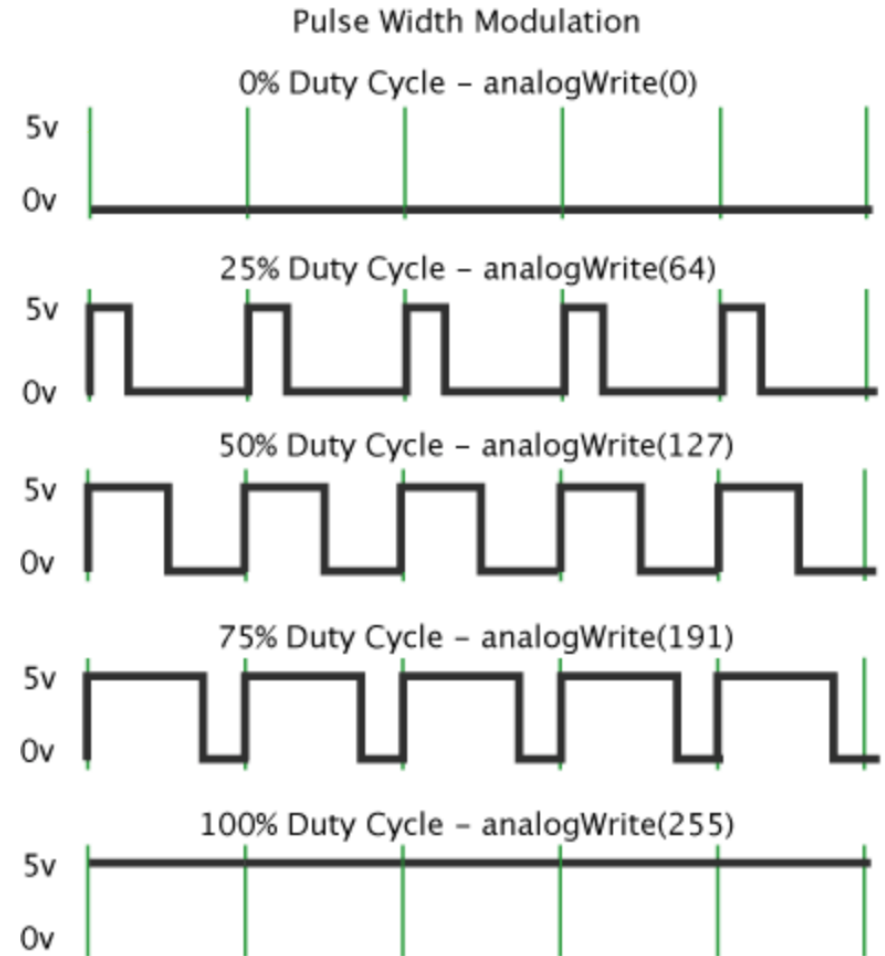


Your Assignment for the next class

- **Can we sample a signal by lower sampling frequency as determined by Nyquist-Shannon Theorem?**
 - Hint: Maybe by using compress sensing?
- **Your assignment:** Research, Read online articles, and write a 1-page report on how compress sensing is works and what are its limitations!
 - **Due date: Nov 11th (upload to canvas)!**

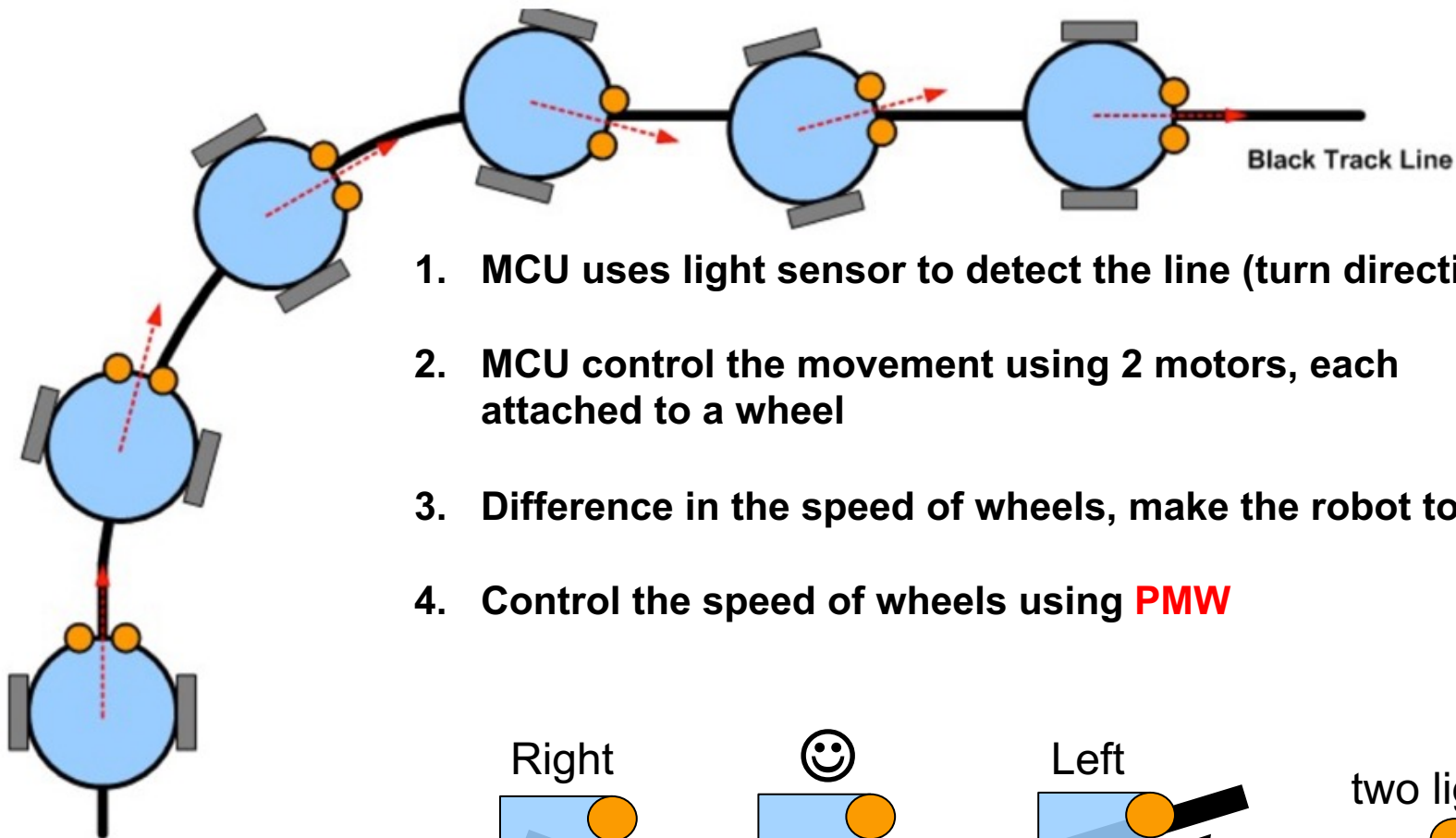
Pulse Width Modulation (PWM)

- A technique for getting analog results with digital means
- **Pulse Width:** The duration of "on time"
- **PWM:** The duration of High (1) and Low (0) Voltage is controlled.
- If you repeat this on-off pattern fast enough the result is as if the signal is a steady voltage between 0 and 5v.
 - With an LED, for example, you can control the brightness of the LED
 - With a motor, you can control the speed of motor.



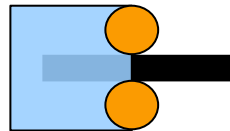
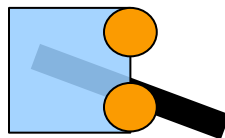
A Cute Example!

Line Tracking Navigation of The Line Follower Robot (LFR)

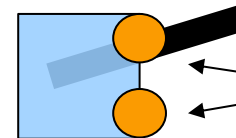


1. MCU uses light sensor to detect the line (turn directions)
2. MCU control the movement using 2 motors, each attached to a wheel
3. Difference in the speed of wheels, make the robot to turn
4. Control the speed of wheels using **PMW**

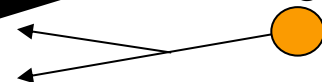
Right



Left



two light sensor



What If MCU doesn't have a DAC!!!!!!

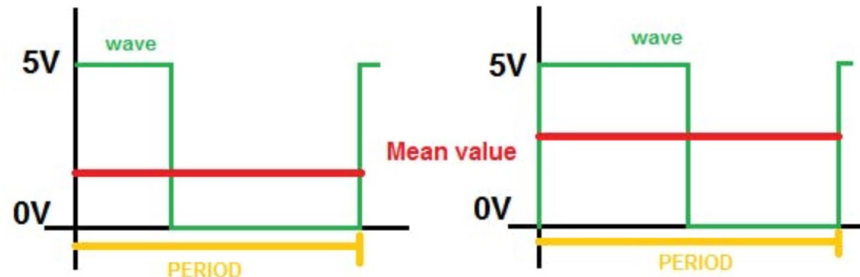
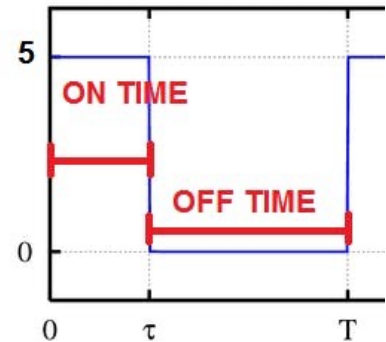
- Use an external DAC!



- Can we build a simple one? 😊
- **Our Goal:** To translate numeric values into analog signals using a MCU (Arduino in our case!)
 - ❑ have output voltages variable from 0 to 5V by setting only a variable.
- What do you need:
 - ❑ Operational Amplifier (you can use almost every operational amplifier, just remember to check that is rail-to-rail).
 - ❑ 22uF capacitor
 - ❑ 3.3kOhm resistor.

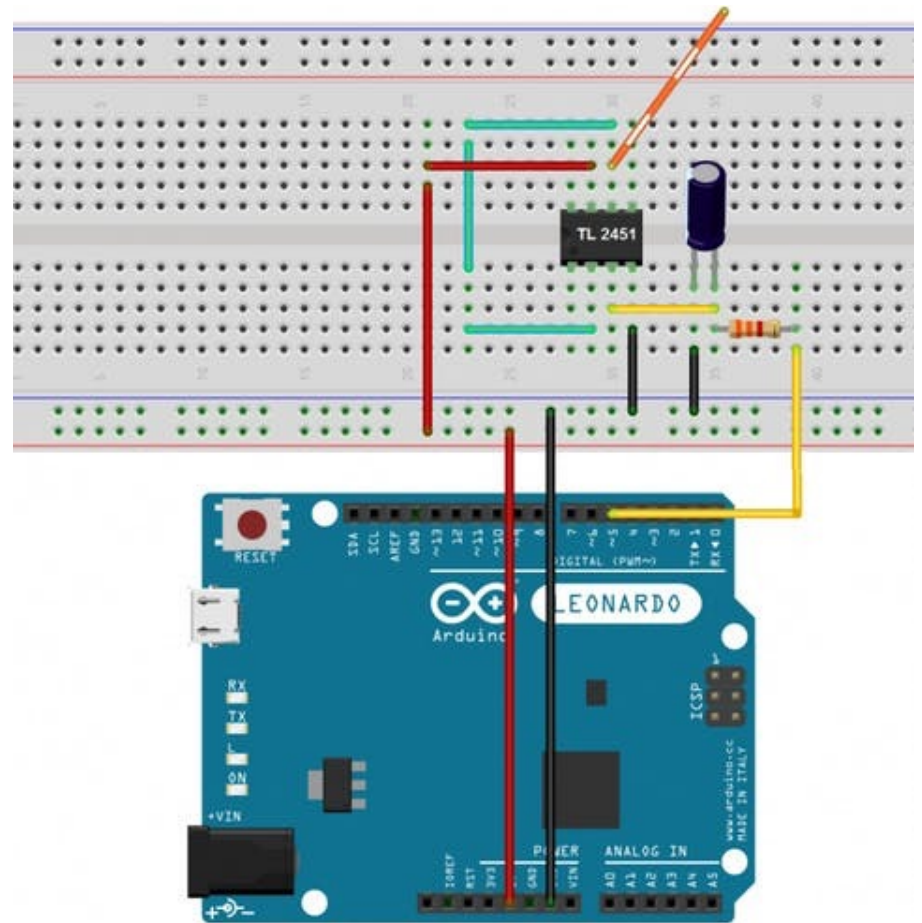
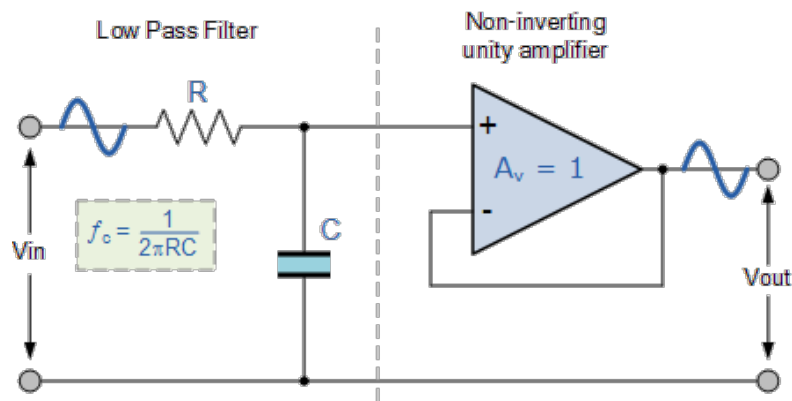
Using PWM and Duty Cycle

- **analogWrite()** function allow you to set the output duty cycle
 - vary between 0% and 100% by choosing values with the second parameter you pass to the function (0 - 255)
 - ☺ This means Analog pin has built in PWM
 - `analogWrite(pin,127)` is 50% duty cycle (default).
- **Mean or DC** = $\text{ON TIME} / (\text{OFF TIME} + \text{ON TIME})$



- You can extract the DC value of the signal by using a **low-pass filter** that allows only the DC signal to pass and blocks nearly all others signals.

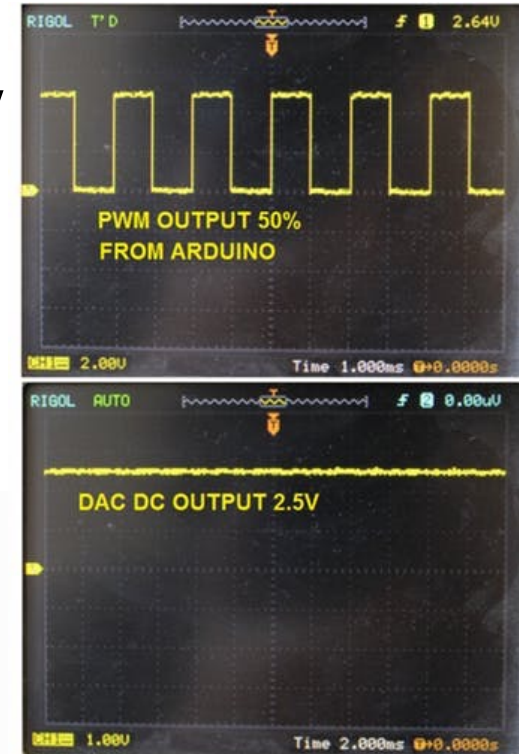
Build Your Filter Circuit



Using the Circuit

- **analogWrite(5,127)** is 50% duty cycle on pin 5.
- The DC voltage is then **50%** of supply voltage (5V in this case!) which is 2.5V

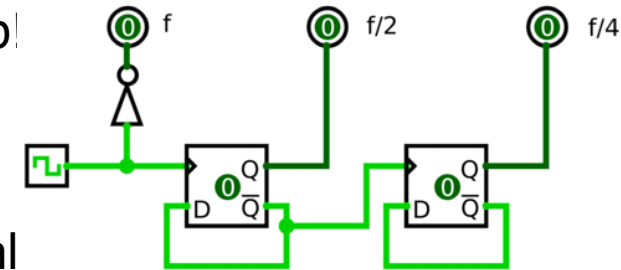
```
void setup() {  
    // initialize the digital pin as an output.  
    pinMode(5, OUTPUT);  
}  
void loop() {  
    analogWrite(5,127); //Set the PWM at 50 % on digital pin 5  
}
```



Know Your MCU DAC and ADC

- The conversion of A2D and D2A takes time.
 - Depending on the type of ADC or DAC converter used, you have a cap on how fast you can convert!
 - Depending on frequency of MCU clock you have a cap!
 - Depending on clock **divider used**, you have a cap!

- Example:



- If **analogRead()** in Arduino takes 100us for signal conversion → 10,000 samples per second.
 - Can you sample a sound signals 1KHz, 4KHz, 10KHz, 14KHz?
- If you need higher sampling rate in Arduino, there are ways (**out of scope of this class**)
 - Such as playing with clock divider variable (prescale)
 - Using ADC free running code which is based on Interrupts
 - If interested to know more [click here!](#)